

A
Compleat Body
OF
SURVEYING:

Formerly Publish'd by *Vincent Wing*, Math.

NOW

Much Augmented and Improv'd; with an APPENDIX thereunto
subjoin'd, shewing the whole ART of SURVEYING, by a New
Instrument,

CALLED

The EMPERIAL TABLE;

Performing exactly in all Respects, and in all Cases that can possibly
happen in the Practical Part of SURVEYING, the Work of the
Theodolite, Circumferentor, Semi-Circle, Chord and Needle.

WITH THE

DESCRIPTION and USE

OF A

New QUADRANT.

To which is added, by Way of SUPPLEMENT,

SCIENTIA STELLARUM:

Containing New and Accurate Tables of the Planetary Motions,
whereby the Planets Places both in Longitude and Latitude, the
Places of the fix'd Stars, with the Eclipses of the Luminaries, are
more easily attain'd than by any yet Extant.

By JOHN WING, *Math. Philosopher*

L O N D O N:

Printed for A C. and Sold by W. TAYLOR at the Ship in Pater-
Noster-Row.

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THE END

TO THE
HONOURABLE
JOHN NOEL Esq;

Son to the Right Honourable the LORD
CAMPDEN, and Brother to the late
Earl of GAINSBOROUGH.

Right Honourable,

THE Arts and Sciences Mathematical have in former Ages not only Received the Applause and Approbation of the Learned, but the Professors thereof have been also more favourably and gratefully admitted into the Society of the Noblest Persons, and it would be Weakness in me to tell your Honour of the Worth and Excellency of that, which all Great Men do approve and admire. That worthy Syracusean ARCHIMEDES, has left us such Excellent Helps and Devices Mathematical, that all the World since hath been beholden to his Pains and Industry; and should I enumerate the continual advantages and benefits we daily receive from the Mathematical Sciences (especially to your Honour) it would be like reading a Military Lecture before the Illustrious Hanibal; who in his Time, was the greatest Master of the Art of War: I must therefore only beg your Honour's favourable Acceptance of this my Performance. And
as

DEDICATION.

as the Grand Cyrus graciously accepted a Cup of Water from poor Sineætes, so let me be allowed Your Honour's kind Reception; And I hope it will not detract from Your Honour to Patronize my Slender Labours; which will not only encourage me to make a further Progress in this Sublime Study, but confirm me in what I have already done, and oblige me to a Dependence upon the Rays of Your known Humanity, by encouraging me to Study what may be further serviceable to the Publick: In the interim, committing YOU, Right Honourable, and Your Noble Family, to the great Architect of Heaven and Earth, I cease to trouble Your Honour further at this time, ever remaining,

A Real Honourer of YOU

and

Your Noble Family,

JOHN WING.

THE

T O T H E R E A D E R.

Courteous Reader,

AS I have been this Twenty Six Years last past, imploy'd in matters of great concernment, in the Practice of Surveying: I may (I hope) contend for some Experience, (if not Judgment) in this Noble Science, and my frequent experience discovered to me, the great want of such an Instrument, as might be truly subservient in all Cases that may happen in this excellent Art of Surveying: Upon which, I betook my self to the contriving and perfecting such an Instrument as is Describ'd, Illustrated, and Exemplified in the *Appendix* to the Fourth Book; truly and exactly performing, (and that most Naturally) all the Cases that can possibly happen in the Practical part of Surveying; and having communicated my Conceptions upon this Subject to several Ingenious Artists, who not only approving the matter, but earnestly importun'd me to publish it: Accordingly, I did then design to make a Compleat body of this most Useful Art in *Folio* by it self; but others at the same time desiring me to Revive my Deceased Uncle, Mr. *Vincent Wing's* Book of Surveying, which was almost lost to the World, as being out of Print: I did then in Compliance to all, Revive this Deceased Author's Book, *viz.* the Essential part thereof, that of little Use being left out, and having made such large Additions, and and that wholly New, as are not only Useful but truly Serviceable to a Work of this Nature, and tho' several able Artists have already handled this Subject with good Success, that may give some occasion to Object that my undertaking is Superfluous, I therefore think my self obliged to inform my Reader

A

that

P R E F A C E.

that here are several advances made in this Tract towards the bringing this Noble Science to greater perfection, and may lead the Young Reader through the Study and Practice thereof with more ease, Expedition, and Satisfaction, than any that has hitherto appeared in our Language, as may in some measure appear from this short Specimen of the whole Work, which is divided into Seven Books; as follows,

I. The first Book contains *Arithmetic* in whole Numbers, Vulgar Fractions, and Decimals, after a Plain and Practicable manner.

II. The Second Book consists of *Geometry*, being divided into four Parts. The first part treats of the Description and Inscription of all Geometrical Figures. The second part contains the Mensuration of all Superficial Figures, demonstrated in Problems, Theorems, Definitions; and *Arithmetically Solv'd*. The third part directs the parting or cutting any Geometrical Figure into equal or unequal parts, as the matter is required. The fourth part teacheth how to Reduce one Figure into another, still keeping the same proportion.

III. The third Book consists of *Plain Trigonometry* or the *Solution* of all Plain-Triangles, both Right and Oblique, with a Canon of Sines and Tangents to every 10 Minutes, with a Table of Logarithms to 1000.

IV. The fourth Book shews by the *Plain-Table* how to take the Plot of all manner of Grounds several ways, and how to cast up the just quantity thereof in Acres, Roods, and Perches, and also how to inclose a Lord-ship that Lieth in common, or open Fields, and to draw a perfect Mapp thereof. To which Book is Subjoyn'd an *APPENDIX*, wherein is the Description and Use of a New Instrument call'd *EMPERIAL TABLE*, with a New Scale and Chain fitted thereto, performing exactly and in all Respects the work of the *Plain-Table*, *Circumferenter*, *Semicircle*, *Peractör*, *Chard* and *Needle*, all fully compleated

P R E F A C E.

completed thereon, without the least confusion of Lines or Parts; and from this Instrument by each several way, both Separately and Conjunctively, is demonstrated all Practicable Cases that may possibly happen in the Art of Surveying, either in Kingdoms, Provinces, or private Estates.

V. The Fifth Book shews *Arithmetically* how to measure all manner of Work and Materials belonging to *Buildings*, to which is added, the Rates, and Prices both of Work and Materials; by which any Gentleman may know, what his Building shall cost him before he begins the Work.

VI. The Sixth Book contains the Description and Use of a *New Quadrant*, plainly resolving the *Hour* and *Azimuth*, the *Right Ascension*, *Declination*, *Oblique Ascension* and *Decension* in time, of all points of the *Ecliptic* with *Latitude*, and thereby the *Rising*, *Setting*, and *setting* of the *Planets* and *Fixed Stars*; also the *Sun's Rising* and *Setting*, with the *Increase* and *Decrease* of the *Days* to a *Minute*; and on the back-side of the *Quadrant*, are *Lines* inserted for the erecting a *Scheme* of the *Heavens*, for any time, and also *Lines* shewing the *Diameter*, *Circumference*, *Area*, and *Square* equal of a *Circle*; with an *Useful Almanack*, and other *Quadrantal* performances.

VII. The Seventh Book consists of several *Problems* in *Geography*, and *Spherical Trigonometry*, whereby the Reader may be inform'd how to find the *Scituation* of any place upon the *Terrestrial Globe*; and thence transferr it into a *Map*. To which end are annexed the most necessary *Problems* in *Astronomy*, and a *Practical Tract* of the *Art of Dialling*, with which all *Surveyors* ought to be acquainted; that they may give directions for *Ornamental* ones, upon such *Mansion-Houses* as belong to the *Manor* or *Land* which they *Survey*.

To these is added *SCIENTIA STELLARUM*, consisting of *New Astronomical Tables* Exposed, with their *Uses* in the *Calculation* of the *Planets*

P R E F A C E.

nets Places, both in Longitude and Latitude, as also the Doctrine of the Eclipses, with the places of the Fixed Stars, &c.

Now the Utility of the Mathematick Sciences, being so well known, that for me to commend them, would be like speaking before *Apollo*, and therefore needless: But as to what oversights and omissions have escaped, I submit to the Censure of all Impartial Artists, knowing tis an easy matter (where Prejudice doth not stop the way) for the Reader to distinguish between the Author's, and Printer's faults, but having the Advantage of a *Good Printer*, and a *Careful and Ingenious Corrector*, who have so excellently behaved themselves herein, that very little of an *Errata* appears, to what I have seen in most works of this Nature. Thus wishing all Ingenious, Impartial, and Unprejudiced Artists a happy Progress in all their Just endeavours, I remain

From my House at
Pickworth in the
County of *Rut-*
land, November
27th, 1699.

Your Mathematical Friend,

J O H N W I N G.

I

THE ART OF SURVEYING.

Common Arithmetick. BOOK I.

CHAP. I.

Of Notation, or Numeration.

I. **A**RITHMETICK is the Art of Numbering, or Accounting by Numbers.

II. *Arithmetick* is either Single, or Compound.

III. Single, is that which is performed by single Numbers alone, and consists of two Parts, *viz.* Notation, and Numeration.

IV. Notation is only the Noting, or Writing down any Summ, or Number that is to be pronounced, or its Value expressed or determined.

V. Numeration is the Reading, or Expressing any Number given, or propounded; or the exact pronouncing its true Value, according to the Number of Figures proposed, or noted down.

VI. The Notes, or Characters, are Nine, and a Cypher (o), by which Numbers are usually expressed, and are as followeth; 1, one; 2, two; 3, three; 4, four; 5, five; 6, six; 7, seven; 8, eight; 9, nine; o, Cypher.

VII. Tho' the Cypher signifie nothing of it self, yet it being post-poned, or placed behind any of the rest, it doth increase the Value of the Number, as hereafter will appear.

VIII. The Figures are to be numbred, and the Order of Places to be observed from the Right-hand to the Left.

IX. The first Figure of any given Number to be read, or pronounced, toward the Right-hand, is said to stand in the First place, or place of Units; the Figure standing in the Second place, is called the place of Tens; the Third, the place of Hundreds; the Fourth, the place of Thousands; the Fifth, the place of Tens of Thousands; the Sixth, the place of Hundreds of Thousands; the Seventh, the place of Millions; the Eighth, the place of Tens of Millions; the Ninth, the place of Hundreds of Millions; and the rest as the Table of Numeration here expresses.

X. The first three Figures towards the Right-hand, possess the place of Hundreds, the three next on the Left-hand them, stand in the place of Thousands, the three next in the place of Millions; and so on, as the following Table of Numeration directs.

XI. The aforesaid, or foregoing Rules being understood, 'tis easie to express, or read, the Value of any Number propounded; hence then let it be required to read, or pronounce, this Number, 987,654,321. First, distinguish by a Point, or Comma, every three places, which unburthens the Memory, and makes the Work the easier: The reading, or pronouncing, is thus; Nine hundred eighty seven Millions, Six hundred fifty four Thousand, Three hundred twenty one.

The Table of Notation, in Figures and Letters.

Units.	1	First	place.	1 I	18 XVIII	200	CC
Tens.	12	Second		2 II	19 XIX	300	CCC
Hundreds.	123	Third		3 III	20 XX	400	CD
Thousands.	1234	Fourth		4 IIII	21 XXI	500	D
X. Thous.	12345	Fifth		5 V	30 XXX	600	DC
C. Thous.	123456	Sixth		6 VI	40 XL	700	DCC
Millions.	1234567	Seven.		7 VII	49 XLIX	800	DCCC
X. Million	12345678	Eight.		8 VIII	50 L	900	DCCCC
C. Million	123456789	Ninth		9 IX	59 LIX	1000	M
Thou. Mil.	1234567891	Tenth		10 X	60 LX	10000	CIO
X Th. Mil.	12345678912	Eleven.		11 XI	89 LXXXIX	50000	ICD
C. Th. Mil.	123456789123	Twelfth.		12 XII	100 C	100000	CM

CHAP. II.

Addition of Whole Numbers.

ADDITION is that by which many Numbers are gathered, or added together, that in the end their Summ, Aggregate, or Total, may be found. In *Addition*, place the Numbers given one above another; that is, Units above Units, Tens above Tens, Hundreds

Hundreds above Hundreds, and so on, according to the Number of Places given.

Addition of one Denomination.

Let us suppose these two Numbers 5127, and 2561, be given to be added together; set them one under another, as you see in the Margin, and draw a Line under them, as you see; then begin with the Units, and say, 7 and 1 makes 8, which place under 1 and 7; then to the next, being the place of Tens, and say, 6 and 2 makes 8; then to the next place, being the place of Hundreds, and say, 5 and 1 makes 6; then to the last place, or place of Thousands, and say, 2 and 5 is 7, all which subscribe orderly under the Line, as you see: So is the Work finished, whose Summ amounteth to 7688, as appears by the Work in the Margin.

But these three Numbers be given to be added together, viz. 9532, and 7069, and 557; place them down as before is taught, and if any of the Ranks exceed Ten, write down the Excess, and for the odd Ten keep 1 in your Mind; so 7, 9, and 2, makes 18; so is the Excess above 10, 8, so I write down 8, and the 1 that I have in my mind I carry to the next Rank; so 1 that I keep in my mind, and 5, 6, and 3, makes 15; so 5 being the Excess above 10, I write it down under the same Rank, and for the 10, I carry 1 in my mind, as before; then again, 1, and 5, and 5, makes 11; so 1, being the Excess above 10, I write down 1, and carry 1 for the 10, as I said before; so 1, 7, and 9, makes 17, it being the last Number, I write it down orderly under the Line: So doth the whole Summ amount to 17158.

And if any Number be given, that the first Rank exceeds 10, 20, 30, 40, 50, 60, or any other Number of Tens, write down the Excess above, or more than the Tens; and for so many Tens as there is in number above the Excess, so many Units carry in your Mind to the next Rank of Figures; and so may you proceed from one Rank to another, till you have compleated your whole Work, as each particular Example following directs.

E X A M P L E S.

90527	277853	7590324	7538216
18631	799472	7654031	1978194
25978	972934	9561987	8657327
863	879915	9819751	1472961
<hr/>	<hr/>	<hr/>	<hr/>
135999	2930174	34626093	19646698

Thus far of Addition of Numbers of one Denomination: In the next place, I shall briefly shew, how Numbers of divers Denominations may be added together; as Pounds, Shillings, Pence,

and Farthings ; Years, Months, Days, and Hours ; and Signs, Degrees, Minutes, and Seconds : In all which observe ; First, To write down the Numbers given, orderly one under another ; Secondly, In all which begin with the Lesser Denomination, as in Pounds, Shillings, Pence and Farthings, which is Farthings, four whereof makes one Penny ; so that what that Rank exceeds in Farthings above the Number of Pence, write down the Excess, or Farthings over and above, and carry the Number of Pence to the next Rank ; then 12 Pence makes one Shilling, what that Rank exceeds the Number of Shillings, write down the Excess in Pence, and carry the Shillings to the next Rank, *viz.* the Rank of Shillings ; so what that Rank exceeds in Shillings above the Number of Pounds therein contained, place under the same Denomination, and carry the Pounds to the last Rank, which being added thereto, and because it being the last Rank, place its Result under its own Denomination accordingly, which concludeth the whole Work. So likewise in Addition of Signs, Degrees, Minutes, and Seconds, begin with the least Denomination, which is Seconds, 60 whereof makes one Minute, and 60 Minutes one Degree, and 30 Degrees one Sign, and 12 Signs one Great Circle. Again, in adding Years, Months, Days, and Hours, whose lesser Denomination is Hours, 24 making one Day Natural, 28 Days one Month, and 12 Months one Year. Examples of all which follow.

E X A M P L E S.

Addition of divers Denominations.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>f.</i>	<i>y.</i>	<i>m.</i>	<i>d.</i>	<i>h.</i>	<i>f.</i>	<i>d.</i>	<i>m.</i>	<i>s.</i>
20	15	06	03	15	11	20	16	11	20	42	31
7	12	10	00	50	09	13	10	9	11	15	51
19	07	01	01	75	10	18	08	10	09	56	41
37	19	11	02	10	05	07	19	5	29	10	02
<hr/>				<hr/>				<hr/>			
85	15	05	02	153	01	04	05	01	11	05	05
<hr/>				<hr/>				<hr/>			

So likewise in Weights and Measures, observe the particular Denominations, and you cannot err, if what before is treated of be rightly understood.

C H A P. III.

Subtraction of Whole Numbers.

SUBTRACTION of Numbers is, that one Number being taken out of another, to the end that a Remainder, or Difference may be known. That Number the Subtraction must be made from, is to be greater than your other Number; and for placing the Numbers in *Subtraction*, it is the same as is before taught in *Addition*.

Subtraction of one Denomination.

Let this Number 87562, be given to be Subtracted from 198765, place them one above another, as you are before directed, placing your greatest Number uppermost, otherways your Subtraction cannot be made; then begin your Subtraction, and say, 2 from 5, and there remains 3, which write down under the Line in the same Rank; then to the second Rank, and say, 6 from 6, and there remains nothing, so place 0 under the Line in the same Rank; then proceed to the next, and say, 5 from 7, and there remains 2, which place under the Line, as before; Then proceed to the fourth place, and say, 7 from 8, and there remains 1, which place orderly under the Line; then to the fifth place, and say, 8 from 9, and there remains 1, which subscribe orderly under the Line; then in the last place, subscribe 1 under the Line, because there is no Figure under it, to take from it; and so is the Work finished, whose Remainder, or Difference is found 111203.

$$\begin{array}{r} 198765 \\ 87562 \\ \hline 111203 \end{array}$$

Again, let it be required to Subtract one Number out of another; when the Figures of the under Numbers are greater than those placed over them, in such a case you must borrow 10 of the next Rank towards the Left-hand, and add it to the Figure above, which makes the Figure more by 10 than it is of it self; and for the 10 that you borrowed, keep 1 in your Mind, which add to the next Number given to be Subtracted, and Subtract all out of the Numbers above, till the Work be finished.

TABLE

C

EXAMPLE.

EXAMPLE.

It is required to Subtract 6792, from 35671; begin then with the place of Units, and say, 2 from 1, which cannot be, wherefore borrow 10 of the next Rank, and add it to 1, which makes it 11; then say, 2 from 11, and there remains 9, which note down under the same Line; and for the 10 which I borrowed, I carry an Unit (or one) in my Mind, and add it to the next Figure, namely 9, then 9 and 1 is 10; then say, 10 from 7, that I cannot have, then I must borrow 10 of the next Rank, as before, and add it to 7, which makes 17, then take 10 from 17, and there remains 7; then again, 1 that I have in my Mind, add to the next Figure 7, which makes 8; then say, 8 from 6, which cannot be, borrow 10 as before, and add it to 6, which maketh 16; then say, 8 from 16, there remains 8; then for the 1 I have in my Mind, I add it to 6, which makes it 7; then say, 7 from 5, which I cannot have, then borrow 10 as before, and add to it, which makes it 15; then say, 7 from 15, and there remains 8; then for the 1 I have in my Mind, having no Figure to add it to, I Subtract it from the next Figure 3, and the Remainder is 2: Thus the Work being finished, the Remainder, Difference, or Number sought, is found to be 28879.

$$\begin{array}{r} 35671 \\ 6792 \\ \hline 28879 \end{array}$$

I have here added three Examples answerable to those three in *Addition*, which is sufficient to inform, or instruct any truly Ingenious in this matter,

EXAMPLES.

Subtraction of divers Denominations.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>f.</i>	<i>y.</i>	<i>m.</i>	<i>d.</i>	<i>h.</i>	<i>f.</i>	<i>d.</i>	<i>m.</i>	<i>f.</i>
79	17	10	02	97	02	15	20	9	21	50	23
51	18	11	03	15	10	16	23	7	23	51	30
<hr/>				<hr/>				<hr/>			
27	18	10	03	81	03	26	21	1	27	58	53
<hr/>				<hr/>				<hr/>			

So likewise in Weights and Measures observe the particular Denominations, and you cannot err, if the former part of the Chapter be rightly understood.

C H A P. IV.

Multiplication of Whole Numbers.

MULTIPLICATION is that which teacheth us by having two Numbers given, to find a third. Of the 2 Numbers given in *Multiplication*, the greater ought to be placed uppermost, and is call'd the *Multiplicand*, and the Number placed under the *Multiplicand*, is call'd the *Multiplicator*, the Number produced by these two, is call'd the *Product*.

Multiplication of one Figure.

Let it be required to multiply 324 by 2; the same order is to be observed in placing your Numbers as in *Addition*; which done, with a Line under them, proceed to your Multiplication, and say, 2 times 4 makes 8, which place under the Line in the same Rank; this done, say again, 2 times 2 makes 4, which place or-

324 *Multiplicand.*
2 *Multiplicator.*
—
648 *Product.*

derly under the Line; then again, two times 3 is 6, which place under the Line as before, so the Product of this Multiplication is found to be 648; and here you must understand, that if your Multiplicator had consisted of more Figures than one, you should have wrought after the same manner, placing them orderly under the same Rank, and so on to the Left-hand till the Work be finished; but if your Number given to be multiplied, when the Product of each particular Figure exceed 10, keep 1 in your Mind; or if the Excess be above 20, write it down, and keep 2 in your Mind, if above 30, keep 3 in your Mind, &c. which is to be added to the next Rank.

E X A M P L E.

Multiplication of divers Figures.

Let it be required to multiply 5762 by 45, place them as before, and as in this Example, and begin with the first Figure towards the Right-hand, viz. 5, saying, 5 times 2 makes 10; now because the Excess above 10 is nothing, I write a Cypher 0 under the Line in the same Rank, and for the 10 keep 1 in your Mind; then say again, 5 times 6 makes 30, to which if I add 1 that I kept in my Mind, it makes 31, so 1 being the Excess above 30, I write down 1 under the Line in the same Rank, and for the three Tens keep 3 in Mind; again, say 5 times 7 is 35, to which I add 3, which I

5762
45
—
28810
23048
—
259290 *Product.*

C 2

kept

kept in my Mind, the whole is 38, so 8 being the Excess above 3 Tens, which I put orderly under the Line, and keep 3 Tens in Mind; then again, say 5 times 5 is 25, to which if I add the 3 I kept in my Mind, the Number is 28; and because it is the last, I write down the whole Sum of 28 under the Line, so the single Product arising from 5, is 28810: Then begin with the next Figure of your Multiplier, viz. 4, and proceed to multiply as before, saying, 4 times 2 makes 8, which place under the Line, and under 4 being the same Rank; then again say, 4 times 6 is 24, so 4 being the Excess above 2 Tens, I put down 4 under the Line, and keep 2 in my Mind for the 2 Tens; again 4 times 7 is 28, to which add 2 I kept in Mind, and it makes 30, the Excess being nothing, I write 0 under the Line, and for the 3 Tens keep 3 in Mind; then say, 4 times 5 is 20, to which add 3 I kept in Mind, the Sum is 23, it being the last of my *Multiplication*, I write it down under the Line towards the Left-hand, which Product is 23048, which two Sums added together, produceth the mean Product 259290: And thus may you multiply by as many Figures as Necessity requires.

C H A P. V.

Division of Whole Numbers.

DI V I S I O N teacheth to find out how many times one Number, or Sum, is contain'd in another, or to divide any Number into as many equal parts as shall be required.

There are three remarkable Numbers in *Division*, viz. the *Dividend*, the *Divisor*, and the *Quotient*; the *Dividend* is that Number which is given to be divided, the *Divisor* is the Number by which the *Dividend* is to be divided, the *Quotient* is the Number that ariseth from the *Division*.

Division by Single Figures.

Let us for the first *Example* divide 576 by 4, write down your Numbers as in the Margin, and ask how often you can have the Divisor. 4 in 5, which is the first Figure of your Dividend, which can be had but once, which place behind the crooked Line for the first Figure in the Quotient, then multiply the Divisor by the Figure placed in the Quotient, and write the Product under the Dividend, from which it must be Subtracted; so 4 multiplied by 1 is 4, which Subtract from 5, the Remainder is 1; draw a Line under your

576	Dividend.
4	Divisor.
<div style="display: flex; justify-content: space-between; align-items: flex-start;"> 17 (144 Quot. </div> <div style="display: flex; justify-content: space-between; align-items: flex-start;"> 4 16 </div> <div style="display: flex; justify-content: space-between; align-items: flex-start;"> 16 4 </div> <div style="display: flex; justify-content: space-between; align-items: flex-start;"> 16 00 </div>	
<div style="display: flex; justify-content: space-between; align-items: flex-start;"> 00 Remainder. </div>	

Divisor,

Divisor, and place your Remainder 1 orderly under the Line, then transcribe the next Figure of your Dividend, which is 7, and place your Divisor orderly under it; then ask how often your Divisor 4 is contain'd in your new Dividend 17, which being 4 times, which 4 place behind 1 in the Quotient, then multiply your Divisor 4 by 4, the last Figure placed in the Quotient, and the Product is 16, which Subtract from 17, the Remainder is 1, which place under the Line as in the Example; then transcribe 6, the last Figure of your Dividend, so have you another new Dividend, to which bring down 4 your Divisor, and ask how often it is contained in 16 your new Dividend, which is 4 times, which four place in the Quotient, and multiply it by your Divisor 4, and the Product is 16, which Subtracted from your new Dividend 16, and the Remainder is 0, thus the whole Work is finished, and the Quotient found to be 144; see the whole Operation in the Margin: And this is call'd single Division, because the Divisor is but one Figure, but when the Divisor consists of more Figures than one, the Work is more difficult than the former, but being well instructed in the former, the following will be more readily apprehended.

Division by Several Figures.

Let us suppose this Number 52063 to be given to be divided by 232; in placing your Numbers you are to observe, that if your Divisor be greater than the same number of Figures of the Dividend above it, then remove your Divisor one Figure towards the Right-hand, and then the Work will be the same with the following: Your Numbers being placed as before directed, make a Crooked Line on the Right-hand of your Dividend, to place your Quotient in, then proceed to your Work, and ask how often 232 may be taken out of 520, or ask how often 2, the first Figure of your Divisor, may be taken out of 5, the first Figure of your Dividend, which in this *Example* is found twice, which 2 place behind the Crooked Line, for the first Figure in the Quotient; then Multiply 232 the Divisor, by the Figure placed in the Quotient, and the Product of that Multiplication will be 464, which place under the Divisor, and draw a Line under them; then Subtract 464 from 520, (the three first Figures of your Dividend) the Remainder is 56, which place orderly under the Line: This done, the next Figure of your Dividend, is to be placed on the Right-hand 56, so will your Number be 566, for a new Dividend: Then place down your Divisor under 566, your new Dividend, and Work as before, asking how often 232, may be taken out of 566, or rather, 23 out of 56, or 2 out of 5, which in this *Example* can only be taken twice: Place 2 in

$$\begin{array}{r}
 52063 \\
 232 \\
 \hline
 464 \\
 \hline
 566 \\
 232 \quad (224 \frac{23}{232}) \\
 \hline
 1023 \\
 232 \\
 \hline
 928 \\
 \hline
 95
 \end{array}$$

D

the

the Quotient, then as before, Multiply the Divisor by the Figure last placed in the Quotient, and the Product is 464, which Subtract from 566 (your Dividend) and the Remainder is 102; then bring down 3, the last Figure of your first Dividend, to the Remainder 102, so will the Number be 1023 for another new Dividend; then as before, place down your Divisor orderly under the new Dividend: Now because the new Dividend consists of one place more than is in the Divisor, it must be asked, How often the first Figure of your Divisor, is contain'd in the two first Figures of the new Dividend 10, which may be had five times; but because the next Figure of your Divisor cannot be taken so many times out of the Figure above it, I must take a less Number, which let be 4, which write in the Quotient: Then again Multiply your Divisor by 4, and the Product is 928, which is to be Subtracted from 1023, and the Remainder is found 95, which is so many parts of the Divisor: The whole Operation being finished, the Quotient sought, is found $224\frac{2}{3}\frac{1}{2}$.

Division and Multiplication do always prove one another: In *Division* Multiply the Divisor by the Quotient, and add the Remainder to the Product, the Sum will be the same with the Dividend.

To prove *Multiplication*, divide your Product by your Multiplier, and the Quotient produceth the Multiplicand.

C H A P. VI.

The Rule of Three Direct.

The Single Rule of Three Direct.

THE Rule of Three, which for its Excellency, is term'd the Golden-Number, and by many (and that properly) call'd, the Rule of Proportion; for having Three Numbers given that are known, it teacheth to find out a Number unknown in proportion to them; and this Rule is performed by *Multiplication* and *Division*: For by Multiplying the second Number into the third, or third into the second, which is all one, the Number thence arising divide by the first Number, so is the Quotient the fourth Number required: So if 6 Foot of Board cost 12 d. what shall 9 Foot cost? In this *Rule of Three Direct*, the fourth Number that is sought, is to have such Proportion to the second, as the third hath to the first, in the former Question; the fourth Number is to have such Proportion to 12, as 9 hath to 6. Hence, by

f.	d.	f.	d.
6	: 12	::	9 : 18
			9
			108 Product.
			6 Divisor.
			48
			6 (18 Quotient
			48
			00 Remainder.

this

this Analogy, we say, as 6 is to 12, so is 9 to the fourth Number required. In the placing of your Numbers, you are to observe to place them as they are propounded; then Multiply the second Term by the third, *viz.* 12 by 9, and the Product is 108, which divide by 6, the first Term, and the Quotient is 18, the fourth Number found as was required: See the Work in the Margin, and this is the *Rule of Three Single*.

The Rule of Three Compound.

The *Rule of Three Compound*, is when any of the Numbers propounded are of several Denominations, as Acres, Roods, and Perches; Pounds, Shillings, and Pence; or Days, Hours, and Minutes; or Yards, Feet and Inches: If they be of two or three Denominations, they must first be reduced to the least Denomination propounded.

EXAMPLE.

If 5 Yards 8 Foot of Painting cost 8 Shillings, what shall 4 Yards cost? Here the first Term is of two Denominations, *viz.* Yards and Feet, it must therefore be reduced to the least Denomination, because they express things of different Names, *viz.* Shillings into Pence, and Yards into Feet: The first Number given is 5 Yards 8 Feet, which according to the Rules of *Reduction*, will be reduced into 53 Feet, so accordingly will 8 Shillings be reduced into 96 Pence; so likewise will the third Term, 4 Yards, be reduced into 36 Feet; these three Numbers being thus reduced to the least Denominations, the Working it will be the same with the former, and the Numbers are to be placed as in the former Example; which done, proceed to the Work, Multiplying 96 by 36, the Product is found 3456. which divide by 53, the first Term, and the Quotient is 65 Pence, and somewhat more, but it being less than a Farthing, we omitted it as useless.

$$\begin{array}{r}
 53 : 96 :: 36 : 65 \\
 \hline
 36 \\
 \hline
 576 \\
 288 \\
 \hline
 3456 \text{ Product.} \\
 53 \text{ Divisor.} \\
 \hline
 318 \\
 \hline
 276 \text{ (65 Quot.} \\
 53 \\
 \hline
 265 \\
 \hline
 11 \text{ Remainder}
 \end{array}$$

The Rule proved.

The Proof of this Rule: Multiply the fourth Term by the first, and if the Product be equal to the Product of the second and third Term Multiplied, the Work is right, otherways not; and if there happen to be any thing remain after the Work is finished, it is to be added to the Product of the first and fourth Terms Multiplied, and that Sum will be equal with the Product of the second and third Term.

C H A P. III.

The Rule of Inverse.

IT will not be amiss first to shew the Difference betwixt this and the former Rule, and when this, and when the former are properly to be used: Hence observe, if more require more, or less require less, then the former *Rule of Three Direct* is to be used; but if more require less, or less require more, then use this Reverse Rule.

This Reverse Rule is wrought contrary to the former; for in this Multiply the first Term by the second, and divide the Product by the third, so is the Quotient the desired Number: I shall instance only in one Example, as followeth.

If 20 Masons perform a certain Piece of Walling in 12 Days, how many Workmen shall do the same in 4 Days? Place your Numbers as here in the Margin, then Multiply the first Term by the second, or second by the first, which is all one, viz. 20 by 12, the Product is 240, which divide by 4, the Quotient is 60, the Number required.

Days	Men	Days	Men
12	: 20	: 4	: 60
	12		
	40		
	20		
	240		
	4		
	24		
	00		

Product.

(60 Quotient.

I shall not add any more Examples, since this is only the Converse of the former; for it will be easie (if what before is said be rightly understood) to any truly Ingenious, to consider the State of the Question, and consequently by which of the foregoing Rules it is to be solved by.

To prove this Inverse Rule, Multiply the third Term by the fourth, which shall be equal to the first and second Term Multiplied.

C H A P. VIII.

The Extraction of the Square-Root.

THE Extraction of the *Square-Root* is by having a Number given, by which we may find the Number sought, by Multiplying the given Number in it self.

Let it be required to Extract the *Square-Root* out of 1296; to prepare your Number for Extraction, set over the Figure 6 a Prick, and upon the third next to it another Prick thus, 1296; and if the Number

Number had consisted of more Places, it is but placing over every third Figure, a Prick, or Dot, to the end of your Number, always leaving one Figure betwixt two Pricks; and as many Pricks as there is put over the Figures, so many Figures must there be in the Quotient; then proceed and take out the Root of 12, which is 3, and place it in the Quotient; then subscribe the Square of the Figure placed in the Quotient under the first Square of the Number given, viz. 9 under 12, from which it is to be Subtracted, and place the Remainder 3 orderly under the Line; then to the said Remainder bring down 96, so this Square 96 being placed next to the Remainder, the Sum will be 396, which we call the Resolvend; then double the Root, and place it before a Crooked Line on the Left-hand the Resolvend, which is to be a Divisor; the double of the Root is 6, then must the Resolvend be a Dividend, all but the first Figure towards the Right-hand, to wit, the place of Units: Then ask how often 6, your Divisor, may be taken out of 39 the Dividend, which may be had 6 times, which place in the Quotient, and also betwixt the Divisor and the Crooked Line: This done, Multiply all the Number on the Left the Resolvend, by the Figure last placed in the Quotient, and place the Product orderly under the Resolvend; so 66 Multiplied by 6, the Product is 396, which Subtract from the Resolvend, the Remainder is nothing: And thus is the Work finished, the Root being found just 36.

$$\begin{array}{r}
 1296 \\
 9 \overline{) 1296} \\
 \underline{9} \\
 396 \text{ Resolvend.} \\
 66 \overline{) 396} \text{ (36 Root.} \\
 \underline{396} \\
 000 \text{ Remainder.}
 \end{array}$$

If after the Work is done, any Fraction remain, you may add (either at first, viz. to the Number given, or to the Remainder) a convenient Number of Pairs of Cyphers, and then Work according to the former Directions; and so many Points as was placed over the whole Number, so many whole Numbers will be in the Root, the rest towards the Right-hand will be the Numerator of a Decimal Fraction, which will consist of as many Places as there were Pricks over the Cyphers, which Numerator will be so many parts of 10, 100, 1000, 10000, &c. which is easily discovered thus: If the Numerator of the Decimal Fraction be but one Figure, it is so many parts of 10, if two, it is so many parts of 100, &c.

C H A P. IX.

The Extraction of the Cube-Root.

THE Extraction of the *Cube-Root*, is, that by having a Number given, and another Number is found, which being Multiplied in it self, and then by the Product that ariseth, produceth the Number required.

Let it be required to Extract the *Cube-Root* out of 17576: Set a Point upon the first Figure towards the Right-hand, *viz.* upon 6, then another Prick upon the fourth Figure 7, and to the end of the Sum, always leaving betwixt every two Pricks, two Figures; and as many Pricks as there are so made, so many Figures must be in the Quotient: Then begin and find the *Cube-Root* of 17, which is 2, for 2 times 2 is 4, and 2 times 4 is 8; if I had taken 3 it had been too much; for 3 times 3 is 9, and 3 times 9 is 27, which exceeds the first Cube 17; therefore take always the next lesser Number: But to our present Example, draw a Crooked Line on the Right-hand the Number propounded, and place the Root of 17, which is 2 behind the said Crooked Line; then subscribe the Cube of the Root placed in the Quotient, which was found 8, under 17, the Cube-Number given; the Numbers thus placed with a Line under them, Subtract 8 from 17, and the Remainder is 9, which place orderly under the Line; then to the said Remainder 9, bring down the next Cube of the Number given, which is 576, which makes 9576, which call a Resolvend; next the Root in the Quotient is to be Squared, that is, Multiplied in it self, which makes 4, the Triple whereof is 12, which is to be subscribed under the Resolvend, in such manner that the first Figure of the Triple Square, *viz.* the place of Units, is to be placed under the Hundreds in the Resolvend; then triple the Root in the Quotient, and place the Triple thereof under the Resolvend, in such manner as the place of Units may stand under the place of Tens in the Resolvend; then place the Triple of the Root 2, which is 6, under 7, the place of Tens in the Resolvend; which done, draw a Line under them, and add them together in such order as they are placed, which makes 126, which Number is to be a Divisor; then let the Resolvend only, the first Figure towards the Right-hand, be a Dividend, (*viz.* the place of Units;) then ask how often the Figures of your Divisor may be taken out of the Figures of the Dividend, and place the Answer in the Quotient: Thus by the

$$\begin{array}{r}
 \begin{array}{r}
 \cdot \quad \cdot \\
 17576 \\
 \underline{8} \\
 9576 \quad \text{Resolvend.} \\
 \underline{12} \\
 6 \\
 \underline{126} \quad (26 \text{ Quotient.}) \\
 72 \\
 216 \\
 \underline{216} \\
 9576 \\
 \underline{0000} \quad \text{Remainder.}
 \end{array}
 \end{array}$$

Rules

Rules of *Division*, 126 the Divisor, may be taken out of 957, the Dividend, 6 times; so I place 6 in the Quotient, and draw a Line under the Divisor: Then Multiply 12, the Triple Square, by 6, the last Figure placed in the Quotient, and place the Product 72, under 12, the Triple Square: Then Multiply the Figure last placed in the Quotient, first by it self, and then by the Triple Number before subscribed, placing this Product under the Triple Number; so 6 Multiplied first in it self, produces 36, which Multiplied by the Triple Number 6, the Product is 126, which place under the Triple Number, (*viz.* Units under Units, Tens under Tens;) this done, Cube the Figure last placed in the Quotient, and subscribe the Cube under the Resolvend in such manner, that the first place of the Cube, *viz.* the place of Units, may stand under the place of Units in the Resolvend; so the Cube of 6, is 216, which place under the Resolvend as I said before: These three, *viz.* 72, 216, 216, thus placed, draw a Line under them, and add them together as they are placed, which Sum amounteth to 9576, which Subtracted from the Resolvend, the Remainder is 0. The whole Work being finished, the *Cube-Root* of 17576, is found to be 26.

If any Fraction at any time remain after the Work is done, annex a convenient Number of Ternaries of Cyphers to the first Number given, then esteeming it one intire Number, the Work is to be performed according to the preceding Rules; and so many Points as were placed over the Whole Number given, so many Whole Numbers will be in the Root: The rest towards the Right-hand will be a Fraction, as I have shewed in the Extraction of the *Square-Root*.

CHAP. X.

Reduction of Fractions.

RULE I. *To find the Common Measure.*

TO find the Common Measure of two given Fractions, Divide the greater by the lesser, and the Divisor by the Remainder; so do continually till nothing remains, so is the last Divisor the Common Measure sought: See the Example in the Margin, *viz.* 66 and 18 being the Numbers given, to find the greatest Common Measure belonging to them, which according to the former Directions, is found to be 3, as the Example plainly demonstrates in the Margin.

$$\begin{array}{r}
 18) : 66 : (3 \\
 \underline{54} \\
 12) 18 (1 \\
 \underline{12} \\
 6) 18 (3 \\
 \underline{18} \\
 0
 \end{array}$$

RULE II. To Reduce Fractions to their least Terms.

Let us suppose the aforefaid Numbers, 66 and 18, were given to be reduced to leffer Terms: Divide 66 and 18 by 3, (the Common Measure to both Numbers found by the former Rule) and the Quotients are 22 and 6, so that $\frac{66}{18}$ is Reduced to $\frac{11}{3}$.

Again: Suppose $\frac{240}{55}$, were given to be Reduced to their least Terms, still keeping the same Proportion, whose Common Measure, by the first Rule, is found to be 11; by which dividing 240, the Denominator given, and it gives a new Denominator 22: So likewise divide the Numerator 55 by 11, the Quotient is 5 for a new Numerator; so is $\frac{240}{55}$ Reduced to $\frac{24}{11}$, but where both the given Fractions end with 5 or 0, or one with 5, the other with a Cypher, then 'tis but dividing either Number by 5. As if 240 be divided by 5, the Quote is 48, and the Quotient of 55, divided by 5, is 11, so $\frac{240}{55}$ is in Proportion to $\frac{48}{11}$, or $\frac{24}{5.5}$.

RULE III. To Reduce Vulgar Fractions to Decimals.

To Reduce Vulgar Fractions to Decimals. Multiply the Numerator given, by the Denominator required, and divide the Product by the Denominator given.

Let it be required to Reduce $\frac{5}{8}$ of a Pound, Perch, Yard, Foot, &c. to Decimals whose Denominator is 1000: Multiply 5, the Numerator given by 1000, the Product is 5000, which divide by the Denominator 8, the Quotient is $\frac{625}{1000}$, the Decimal required: See the Example in the Margin.

Again: Suppose $\frac{1}{3}$ of a Perch, Yard, &c. were given to be Reduced to the known parts of a Decimal, whose Denominator is 100, which Multiply and Divide according to the former Directions, so will the Vulgar Fraction of $\frac{1}{3}$, be Reduced to the Decimal of $\frac{33}{100}$.

	1000
	5
	—
	5000
Divis. 18)	48
	—
	20 (625 Q.
	16
	—
	40
	40
	—
	00

RULE IV. Reduction of Compound Fractions.

Compound Fractions, or Fractions of Fractions, before they can be worked up, must be Reduced into Single Fractions: As suppose these Fractions $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{5}{8}$ were given to be Multiplied, or Divided by $\frac{2}{3}$ of $\frac{3}{4}$, which must first be Reduced to a Single Fraction thus: Multiply all the Numerators continually for a new Numerator; and Multiply all the Denominators continually for a new Denominator, thus; 2 times 3 is 6, and 6 times 5 is 30, for a new Numerator; then 3 Multiplied by 5, makes 15, which 15 Multiplied by 8, makes 120, for a new Denominator; so are these Fractions

Fractions Reduced to $1\frac{3}{20}$, and by the same Rule the other Fractions will be Reduced to $2\frac{4}{4}$, which are thus fitted either for *Addition, Subtraction, Multiplication, or Division.*

RULE V. *Reduction of Improper Fractions to Proper, with Whole, or Mixt Numbers.*

To bring an Improper Fraction into its Equivalent, either Whole, or Mixt Numbers, do thus: Divide the Numerator by the Denominator, so will the Quotient give the Whole, or Mixt Number sought.

E X A M P L E.

Let this Improper Fraction $\frac{51}{14}$, be given to be Reduced into this Mixt Number $3\frac{2}{4}$; for if 51 be divided by 14, the Quotient is $3\frac{2}{4}$, the thing required. Likewise this Improper Fraction $\frac{12}{8}$, will be Reduced to $6\frac{2}{8}$.

RULE VI. *Reduction of Fractions to a Common Denominator.*

If Fractions have unequal Denominators, they must be reduced to Fractions, which shall have equal Denominators, which is thus performed, *viz.* Multiply the Numerator of the first Fraction, by the Denominator of the second; so will the Product be a new Numerator of that first Fraction; then Multiply the Numerator of the second Fraction, by the Denominator of the first, so the Product is a new Numerator of the second Fraction; and lastly, Multiply the Denominators one by the other, and that Product is a common Denominator to both the Numerators.

E X A M P L E.

Suppose these Fractions $\frac{3}{4}$ and $\frac{4}{6}$, be the Fractions propounded; Multiply 3 by 6, the Product is 18, for a new Numerator common to 3; likewise Multiply 4 by 4, the Product is 16, for a new Numerator common to 4; then Multiply the Denominators together, *viz.* 4 by 6, the Product is 24, for a new Denominator common to both the New Denominators: Observe the Work in the Margin, which explains the whole Matter.

$$\begin{array}{r} 3 \quad 4 \\ \times \\ 4 \quad 6 \\ \hline 16 \quad 18 \\ \hline 24 \quad 24 \end{array}$$

RULE VII. *Reduction of Mixt Numbers to Improper Fractions.*

Multiply the Integer, or Integers in the Mixt Number, by the Denominator of the Fraction so joyned to the Integer; and to that Product add the Numerator of the same Fraction, and that Sum is the Numerator of an Improper Fraction, whose Denominator is the same it was without any alteration.

F

E X A M-

E X A M P L E.

Five $\frac{1}{3}$ will be Reduced to the Improper Fraction $\frac{16}{3}$; for if 15 the Denominator, be Multiplied by 5 the Integer, the Product is 75, to which add 13 the Numerator, the Sum is 88, which place over the Denominator 15. According to the former Method $20\frac{2}{3}$ will be Reduced to the Improper Fraction of $\frac{142}{3}$.

R U L E VIII. *To find the true Value of a Single Fraction.*

To find the true Value of a Single Fraction in its known Terms, or Parts of its Proper Integer, is only Multiplying the Numerator of the Fraction propounded, by the Denominator proposed, and Divide that Product by the Denominator given, and if a Fraction still remain, find the Value thereof in the next Inferiour Denomination.

E X A M P L E.

To find the Value of $\frac{1}{8}$ of a Pound Sterling: Multiply 8, the Numerator, by 20 the next Inferiour Denomination, and the Product is 160, which Divide by 16, the given Denominator, the Quotient is 10 Shillings.

Again: Suppose $\frac{1}{8}$ of a Pound were given, 9 Multiplied by 20, the Product is 180, which divided by 16, the Quotient is 11 $\frac{1}{2}$, which Remainder 4 Multiply by 12 Pence, the next Inferiour Denomination, the Product is 48, which divided by 16, gives 3 Pence in the Quotient; so that $\frac{1}{8}$ of a Pound is brought to its known parts, viz. 11 s. 3 d. Observe the same by Weights and Measures.

C H A P. XI.

Numeration of Vulgar Fractions.

A FRACTION, or Broken Number, is part of a Whole Number, or Integer, as may be thus expressed: If you measure the Length of any Superficies that contains three Fourths, or three Quarters of a Yard, you are to express it thus $\frac{3}{4}$, because a Yard is supposed to be divided into four equal Parts, also a Foot divided into 12 equal Parts, call'd Inches; write four Inches thus $\frac{4}{12}$, that is, four 12 Parts of a Foot; but if the Foot be divided into 100 equal Parts, the Fractional part may be thus expressed; $\frac{4}{100}$; that is, 36 parts of a Foot.

But here you are to take notice for the Terms of the Fractions; that which is placed above the Line, is call'd the Numerator, and

and the Number under the Line, is call'd the Denominator, as in the last Example, 36 being the Numerator, and 100 the Denominator.

C H A P. XII.

Addition of Vulgar Fractions, and Mixt Numbers.

R U L E I.

IF Single Fractions be given to be added, and have their Denominators all alike, or of one Denomination; then 'tis but adding all the Numerators together, which Sum is to be placed over the Common Denominator, and the Work is done: So if $\frac{2}{9}$, and $\frac{1}{9}$, and were given to be added, their Sum would be found $\frac{3}{9}$.

R U L E II.

If the Fractions given to be added, have unequal Denominators, then must they be Reduced to the same Value by the Sixth Rule of *Reduction*; then is the Addition the same with the former.

E X A M P L E.

Suppose $\frac{1}{3}$ and $\frac{2}{5}$ were given to be added, which by the Sixth Rule of *Reduction*, will be Reduced to $\frac{2}{15}$ and $\frac{4}{15}$, which is added, as in the First Rule, makes $\frac{6}{15}$; now because the Numerator is greater than the Denominator, it is an Improper Fraction, and to be Reduced by the Fifth Rule of *Reduction*, which brings it to this Mixt Number $1\frac{2}{5}$, the thing required.

R U L E III.

When Mixt Numbers are given to be added, first find the Sum of the Fractions, as is taught in the two former Rules; then add the Integers (if any be) in the Sum of the Fractions, to the Whole Numbers, and then add them as Whole Numbers.

E X A M P L E.

Suppose $4\frac{1}{3}$, and $5\frac{2}{3}$, be given to be added: First, by the Sixth Rule of *Reduction*, the Fractions are Reduced to one Common Denominator, and stand thus, $\frac{1}{3}$, $\frac{2}{3}$, which added, is $\frac{3}{3}$, being now an Improper Fraction, which by the Fifth Rule of *Reduction*, is

brought to $1\frac{2}{3}$; which added to 4 and 5, the Whole Numbers makes $10\frac{2}{3}$, the thing required.

Again, If $5\frac{3}{4}$, and $10\frac{1}{2}$; by the former Rules, will be found $15\frac{3}{4}$.

RULE IV.

If several Fractions be to be added, as $\frac{1}{3}$, $\frac{2}{5}$, $\frac{3}{7}$: First, Multiply continually the first Numerator into the second and third Denominators 5 and 7, saying, 3 times 5, is 15, and 7 times 15, is 105, for a new Numerator proper to 3. Secondly, Multiply continually the Numerator 2, into the first and third Denominator 8 and 7, saying, 2 times 8, is 16, and 7 times 16 is 112, being a Numerator proper to 2. Thirdly, Multiply continually the third Numerator 5, into the first and second Denominators 8 and 5, saying, 5 times 8 is 40, and 5 times 40, is 200, for a new Numerator instead of 5. Lastly, Multiply all the Denominators continually one into another, viz. 8 by 5, which makes 40, and 40 by 7, which makes 280, which is the Common Denominator, as followeth, viz. $\frac{1}{3}\frac{2}{5}\frac{3}{7}$, $\frac{112}{280}$, $\frac{200}{280}$. Hence always observe this General Rule in finding the new Numerators; Always miss the Denominator, in your Multiplication of its own Numerator, and then you cannot fail. See the Example.

$\begin{array}{r} 5 \\ \hline 3 \\ 15 \\ 7 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ 2 \\ \hline 16 \\ 7 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ 5 \\ \hline 40 \\ 5 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ 5 \\ \hline 40 \\ 7 \\ \hline \end{array}$
1st Numer. 105	2d Numer. 112	3d Numer. 200	Denomina. 280

Then the Numerators being all added, make 417, which place over 280, the Common Denominator, thus, $\frac{417}{280}$; which by the Fifth Rule of *Reduction*, is brought to this Mixt Number $1\frac{137}{280}$, the thing required.

C H A P. XIII.

Subtraction of Vulgar Fractions and Mixt Numbers.

RULE I.

IF the Fractions be both Single, Subtract the lesser Numerator from the greater, and place the Remainder of the Fraction over the Common Denominator.

E X A M-

EXAMPLE.

The Difference betwixt $1\frac{2}{4}$, and $1\frac{4}{4}$, is $1\frac{1}{4}$; also the Difference of $\frac{20}{33}$, and $\frac{11}{33}$, is $\frac{9}{33}$; and the Difference between $1\frac{46}{20}$, and $1\frac{20}{20}$, is $1\frac{61}{20}$.

RULE II.

But when the Numbers given are both Single Fractions, and have different Denominators, they are to be reduced to a Common Denominator by the Sixth Rule of *Reduction*, then the Work will be the same with the former.

RULE III.

When one of the Numbers given, happen to be a Whole, or Mixt Number, or when both of them are Mixt Numbers, Reduce them to an Improper Fraction by the Seventh Rule of *Reduction*, then is the Work to be performed according to this First Rule.

EXAMPLE.

If $8\frac{4}{6}$ be given to be Subtracted from 14, the Remainder will be found $5\frac{2}{3}$; for by the Seventh Rule of *Reduction*, $8\frac{4}{6}$, is Reduced to $\frac{52}{6}$, also 14 is Reduced to $\frac{84}{6}$; then by the Sixth Rule of *Reduction*, these Improper Fractions are Reduced to one Common Denominator of $\frac{52}{6}$, and $\frac{84}{6}$; which Subtracted, as in the First Rule, gives the Remainder $\frac{32}{6}$; which by the Fifth Rule of *Reduction*, is Reduced to its Proper Mixed Number $5\frac{2}{3}$.

Again, If $10\frac{1}{2}$, be given to be Subtracted from $20\frac{4}{5}$, the Remainder (according to the former Prescriptions) will be found $9\frac{11}{10}$. These are all the Cases that can happen in Subtraction of Vulgar Fractions, and Mixt Numbers.

CHAP. XIV.

Multiplication of Vulgar Fractions, and Mixt Numbers.

RULE I.

IF the Numbers given to be Multiplied, be both Single Fractions, Multiply the Numerators together, so is the Product a new Numerator: Likewise Multiply the Denominators together, which Product is the new Denominator sought. So if $1\frac{1}{6}$, and $\frac{1}{2}$,
G be

be given to be Multiplied, the Product will be found $1\frac{1}{2}$; for 5 Multiplied by 3, produceth 15, for the new Numerator; and 16 Multiplied by 7, gives 112, for the new Denominator: Also $\frac{1}{2}$, and $\frac{7}{9}$ Multiplied as before, the Product will be found $\frac{34}{18}$.

R U L E II.

But let it be required to Multiply Mixt Numbers, as $324\frac{1}{4}$, by $62\frac{1}{2}$: First Multiply the Whole Numbers, and place the Products orderly, as is taught, in whole Numbers; then Multiply the Fractions into the Whole Numbers cross ways, viz. $\frac{1}{2}$ of 324, is 162; and $\frac{1}{4}$ of 62, is $15\frac{1}{4}$, which place as you see; lastly, add them together, and annex the Fractional part $\frac{1}{8}$ to the Product; which

$$\begin{array}{r} 324\frac{1}{4} \\ 62\frac{1}{2} \\ \hline 648 \\ 1944 \\ 162 \\ 15 \\ \hline 20265\frac{1}{8} \end{array}$$

done, the Product sought, is $20265\frac{1}{8}$. But this way in all Cases of Mixt Numbers, is not so precisely true, as this which follows.

Let us suppose these following Numbers be given to be Multiplied, viz. $9\frac{2}{3}$, by 6, a Whole Number, the Product will be found $58\frac{2}{3}$; for $9\frac{2}{3}$ must be Reduced by the Seventh Rule of *Reduction*, to the Improper Fraction $\frac{29}{3}$, and 6 to $\frac{6}{1}$, whose Numerators 29 and 6, Multiplied together, makes 174, which place over 3 thus, $\frac{174}{3}$; then the Denominators 1 by 3, the Product is 3 for the Denominator: Hence $\frac{174}{3}$ Reduced to its Whole, or Mixt Number, by the Fifth Rule of *Reduction*, is brought to $58\frac{2}{3}$, the Product sought.

C H A P. XV.

Divisoon of Vulgar Fractions and Mixt Numbers.

R U L E I.

IF the Fractions given be both Single Fractions, Multiply the Denominator of the Divisor, by the Numerator of the Dividend, and that Product is a new Numerator; also Multiply the Numerator of the Divisor, by the Denominator of the Dividend, the Product is a new Denominator; which new Fraction is the Quotient sought.

E X A M-

EXAMPLE.

If $\frac{1}{8}$ be given to be divided by $\frac{1}{4}$, the Quotient will be found $\frac{20}{24}$; for 5 Multiplied by 4, is 20, for a new Numerator; and 3 Multiplied by 8, is 24 for the new Denominator.

Again, If $\frac{4}{9}$ be given to be divided by $\frac{2}{8}$, the Quotient will be found $\frac{24}{18}$, which is to be Reduced by the Fifth Rule of *Reduction*, into this Mixt Number $1\frac{4}{3}$, the Proper Quotient sought.

RULE II.

If any one of the Numbers is a Whole, or Mixt Number, or both happen to be Mixt Numbers, such Whole, or Mixt Numbers, are to be Reduced to an Improper Fraction by the Seventh Rule of *Reduction*, and then the Work will be the same as is taught in the last Rule.

EXAMPLE.

If 19 be Divided by $6\frac{1}{2}$, the Quotient will be found $2\frac{1}{3}$; for $6\frac{1}{2}$ will be Reduced to the Improper Fraction of $\frac{13}{2}$, and 19 to $\frac{19}{1}$, which Divide as in the First Rule, and the Quotient is $\frac{19}{13}$; which by the Fifth Rule of *Reduction*, is Reduced to the Mixt Number $2\frac{1}{3}$, the thing desired. If these Directions be rightly understood, it will be sufficient for all Cases in Fractions, and Mixt Numbers.

$$\begin{array}{r} 6\frac{1}{2}) \quad 19 \\ \underline{13} \\ 6 \\ \underline{13} \\ 2 \end{array} \quad \begin{array}{l} \frac{19}{1} \\ \frac{13}{13} \end{array} \quad \begin{array}{l} (\frac{19}{13}) \\ \text{Quote.} \end{array}$$

CHAP. XVI.

Numeration of Decimals.

WHEN a Single Fraction hath for its Denominator an Unite in the Place on the Left-hand, and if there be nothing but Cyphers towards the Right-hand, it may be termed a Decimal of these kind that follow, viz. $\frac{1}{10}$, $\frac{1}{100}$, $\frac{1}{1000}$, $\frac{1}{10000}$; if the Numerators and Denominators both end with Cyphers, it may be Reduced to a less Fraction; as $\frac{1000}{10000}$ is reduced to $\frac{1}{10}$, or $\frac{1}{10}$: the like is to be understood of the rest that have Cyphers at the ends of both Numbers.

C H A P. XVII.

Addition of Decimals.

GREAT care of placing Decimal Fractions to be added, is the greatest Work of this part, which is to place every Number under its proper Denominator; as Whole Numbers, under Whole Numbers, and Tenths under Tenths; adding them together as Whole Numbers, separating the Whole Numbers from the Fractions, as in the following

E X A M P L E S.

20.2376	70.104	50.016
15.541	11.9721	1.07
42.7631	56.2379	.8
88.5417	138.3140	51.886

C H A P. XVIII.

Subtraction of Decimals.

THE same Order is to be observed in placing the Numbers for *Subtraction*, as in *Addition*; and the Subtraction to be made as in Whole Numbers; the Distinction of Integers from the Fractional parts being observed as in *Addition*. See the following

E X A M P L E S.

.962	76.	87.0079	243.271	50.
.771	05.37	.6570	52.310	.760
.191	70.63	86.3509	190.961	49.240

C H A P.

C H A P. XIX.

Multiplication of Decimals.

IN *Multiplication of Decimals*, whether Fractions, or Mixt Numbers, they are to be Multiplied as Whole Numbers; observing so many Places of Fractions as are in both the Multipliers; for so many Figures is to be cut off in the Product towards the Right-hand, for the Fractional part, and those which are on the Left-hand, are Integers, or Whole Numbers; and if the Product do not consist of as many Places as there are Decimals in both Multipliers, then prepare so many Cyphers as shall make that Number up: This may only happen when the Product is a Fraction.

$\begin{array}{r} 20.15721 \\ 21.3 \\ \hline 429.38573 \end{array}$	$\begin{array}{r} .67 \\ .0132 \\ \hline .008844 \end{array}$	$\begin{array}{r} 412.32 \\ 51. \\ \hline 21028.32 \end{array}$
---	---	---

C H A P. XX.

Division of Decimals.

IN *Decimal-Division* the Dividend must sometimes have Cyphers *Post-poned*, that it may consist of more Decimals than the Divisor, which may be increased at pleasure; and if the Decimals in the Divisor and Quotient, do not amount to those of the Dividend, then *Post-pone* as many Cyphers, as may make them equal: Let the Dividend be 1725, and the Divisor 3.746; then, as I said before, *Post-pone* a convenient Number of Cyphers, that may make way for the Divisor, then the Work will stand thus:

$$3.746) 172.500000$$

Then perform the Division as in Whole Numbers, and it stands thus:

$$3.746) 172.500000 (46049$$

Now for to separate the Integers from the Decimal Parts, is the Key to unlock the whole Work, which is thus performed, viz.

H

Sepa-

Separate so many Figures from the Quotient towards the Right-Hand, as may make the Decimals in the Divisor, equal to those in the Dividend : Hence I find the Point of Separation falls betwixt 6 and 0 ; for the Dividend consisting of Six Places of Decimals, and the Divisor only Three, I must take Three Places from the Quotient towards the Right-hand, to add to the Decimals of the Divisor, which makes them equal to those in the Dividend ; so will the Work be as underneath expressed.

3.746) 172.500000 (46.049

The End of the First BOOK.

T H E

T H E
Art of Surveying,
The S E C O N D B O O K.

Containing the Effential Part of
G E O M E T R Y
In the Practice of
S U R V E Y I N G,
Divided into Four Parts, *Viz.*

- I. The First Part Contains the Description and Inscription of all *Geometrical Figures*.
- II. The Second Part Contains the Mensuration of all *Superficial Figures*; Demonstrated in Problems, Theorems, Definitions, and *Arithmetically Solved*.
- III. The Third Part Contains the Dividing, or Cutting of Figures *Geometrical*, into Parts, Equal, or Unequal, as shall be required.
- IV. The Fourth Part Teacheth how to Reduce one Figure into another, still keeping the same Proportion; and to Add and Subtract *Geometrically*, one Figure to, or from another, with their *Arithmetical Solutions* also to each Problem.

Comprized into a Plain and Practicable Method.

By J O H N W I N G, Math.

L O N D O N,
Printed for *Awnsham and John Churchill*, at the *Black-Swan*,
in *Pater-Noster-Row*, MDCXCIX.

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BOOK II.

Consisting of Definitions, and
Problems Geometrical.

PART I.

The DEFINITIONS.

A POINT is that small part which cannot
be divided, whose part is nothing, as A
in the Margin.

A (.)
A Point.

Euclid 2. 1.

A Line is a Length without Breadth or Thickness, of which
there are two sorts, *viz.* Straight and Crooked, which kind of
Magnitude is conceived in the Measuring of Roads, Inclosures,
or the Distance of one Place from another.

A Straight Line is the shortest Extension betwixt two Points, as the Line in the Margin A.

A Spherical, or Crooked Line, hath Compass, and so it differeth from a Right Line, and being Regular, is called, an Arch-Line; and Irregular, is called, a Curve Line, as in the Margin.

A Superficies hath only length and breadth, the Extrems whereof are Lines; and a Plain Superficies, is that which lieth equally betwixt his Lines, as the Figure C in the Margin.

A Solid is that which hath Length, Breadth, and Thickness, represented by D in the Margin.

An Angle is the meeting together of two Lines in one Point, so meeting, that they make not one Straight Line; and if the Lines that contain the Angle, be Right Lines, then is that Angle said to be a Right Lined Angle, as E in the Margin; if Circular, as the Figure F; then is that said to be a Spherical Angle.

Of Angles, there are 3 sorts, viz.
 1. Orthogonal.
 2. Obtuse, or Blunt.
 3. Acute, or Sharp.

Of the First; when one Line falleth down plumb upon another, it maketh 2 Right Angles, each containing 90 Degrees, as the Figure G.

Of the Second; an Obtuse, or Blunt Angle, is wider than a Right Angle, therefore always more than 90 Degrees, as the Figure H.

Of the Third; an Acute (or Sharp) Angle, is less than a Right, or Rectangle, therefore always lesser than 90 Degrees, as is demonstrated by the Letter I in the Margin.

A Circle is a Plain Figure contained under one Crooked-Line, called, his Circumference; in the Middle whereof, is a Point called, his Center; from whence all Lines drawn to the Circumference, are of equal Length, and are called Semidiameters: See the Figure K, Semicircle A, B, C.

A Portion, or Segment of a Circle, is contain'd under a Chord-Line, and part of a Circumference, A B being the Chord-Line.

A Sector of a Circle is contain'd upon the Ends of 2 Right-Lines, or Semidiameters, making an Angle in the Center, having any part of the Circumference for its Base, as C D.

A Straight Line.

An Arch or Spherical Line

A Curve Line.

Superficies.

D
Solid

A Plain Angle E

A Spherical Angle F

A Perpendicular
G
A Right Angle

An Obtuse Angle H

An Acute Angle I

B
Circumference
A Diameter
Center
K
C

A Segment of a Circle
A B

Base
A Sector of a Circle.
C D

A

A Quadrant is the fourth part of a Circle, and is made by letting two Lines concur of equal length, and making a Right Angle, and from that Angle describing an Arch to touch the other end of each Line, represented by the Figure L in the Margin.

Right Lin'd Figures are contain'd under Right Lines, whereof three sided Figures, are such as are contain'd under three Lines, and are call'd Triangles; whereof, in respect of their Sides, there are three sorts, viz. *Equilateral*, *Isofceles*, *Scalenum*. And in respect of their Angles, there are also three sorts, viz. *Oxigonium*, *Orthogonium*, *Ambligonium*.

The Exposition in respect of their Sides, viz. { A Triangle of three equal Sides, is called *Equilateral*; two equal Sides is called *Isofceles*; and a Triangle with one Blunt Angle, is call'd, *Scalenum*.

The Exposition in respect of their Angles, viz. { A Triangle of three Sharp Angles, is called, *Oxigonium*; with one Right Angle, *Orthogonium*; with one Blunt Angle, *Ambligonium*.

By which former Definition, it appeareth, That every Triangle hath a double Name; and so there are seven sorts of Plain Triangles.

1. An *Equilateral Oxigonium* Triangle, is contain'd under three equal Sides, and three Sharp Angles; as the Triangle A B C in the Margin.

2. A Right Angled *Isofceles*, hath one Right Angle, and two equal Sides; as the Angle D E F.

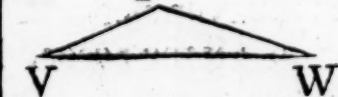
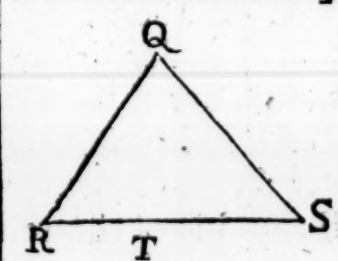
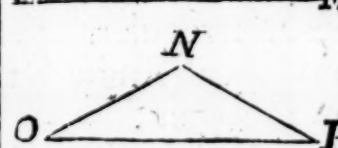
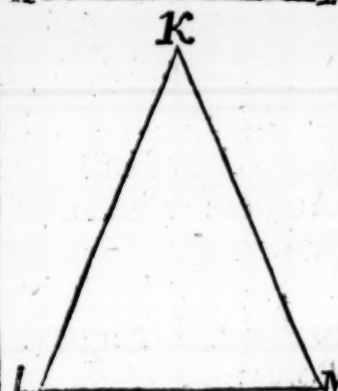
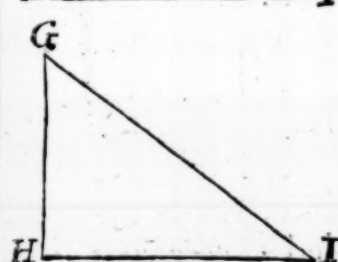
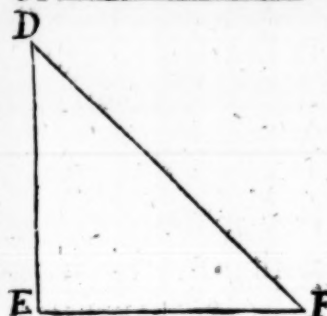
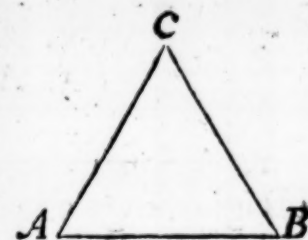
3. A Right Angled *Scalenum*, hath one Right Angle; as the Angle G H I.

4. An *Oxigonium Isofceles*, hath three sharp Angles, and two equal Sides; as the Angles K L M.

5. An *Isofceles Ambligonium*, hath two Sides equal, and one Blunt Angle; as the Angle N O P.

6. An *Oxigonium Scalenum*, hath three Sharp Angles, and three unequal Sides; as the Angle Q R S.

7. An *Ambligonium Scalenum*, hath one Obtuse, or Blunt Angle, and three unequal Sides; as the Angle T V W.



Four sided Figures are such as are contained under four Sides, or Lines, viz. under 4 Right Lines, whereof

There are five sorts, viz. $\left\{ \begin{array}{l} 1. \text{ A Square.} \\ 2. \text{ A Long Square, or Parallelogram.} \\ 3. \text{ A Rhombus.} \\ 4. \text{ A Rhomboides.} \\ 5. \text{ A Trapezium.} \end{array} \right.$

1. A Square is contain'd under 4 equal Sides, and 4 Right Angles, as A.

2. A Long Square, or Parallelogram, is contain'd under four Right Angles, but not equal Sides; yet the opposite Sides are equal, as the Figure B in the Margin.

3. A Rhombus is contained under 4 equal Sides, but not Right Angles, as the Figure C, yet the opposite Angles are all equal.

4. A Rhomboides is contain'd under 4 Lines, whose opposite Sides are equal, and opposite Angles equal; but yet not all equal Sides, nor any Right Angles, as the Figure D.

All other 4 sided Figures, and 4 Angles, which have neither equal Sides, nor equal Angles, are called *Trapeziums*, as the Figure E in the Margin.

Many sided Figures which consist of more than 4 Sides, are called, *Polygons*, and do every of them receive their Names according to the Number of their Angles; whereof there are two kinds, Regular and Irregular.

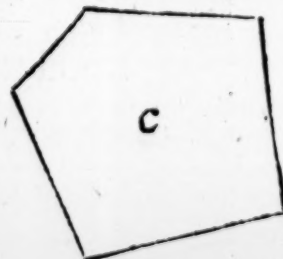
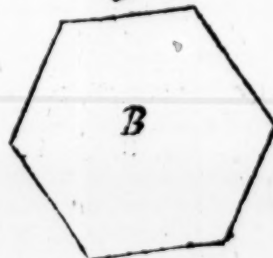
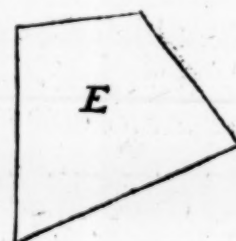
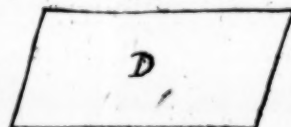
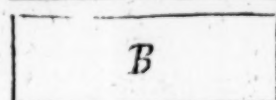
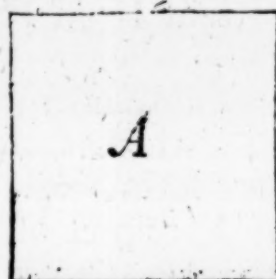
1. Regular Polygons, are such as have equal Sides, and equal Angles: Hence they are called, Regular Polygons.

2. Irregular, are such as have neither equal Sides, nor equal Angles; therefore called, Irregular Plots, or Polygons.

1. Of the First; A *Pentagon*, is a Polygon, contained under 5 equal Sides, and 5 equal Angles, as the Figure A.

An *Hexagon*, is a Figure, or Polygon, contained under 6 equal Sides, and 6 equal Angles, as the Figure B; and so of the rest, being denominated according to the Number of their Sides.

2. Of the Second kind of Polygons, called, Irregular Polygons, which have neither equal Sides, nor equal Angles, as the Figure C.



Paral-

Parallel-Lines, are Lines, or Lines drawn equidistant in all places one from another, of such there are two sorts, *viz.* The Right Lin'd Parallel, and the Circular.

1. Of the First; A Right Lin'd Parallel, is two Right Lines equidistant in all places one from another, which being drawn to an infinite Length, would never meet, as the 2 Right Lines at D.

2. Of the Second; A Circular Parallel, is a Circle, or part of a Circle, drawn within or without another Circle upon the same Center, as E, and F.

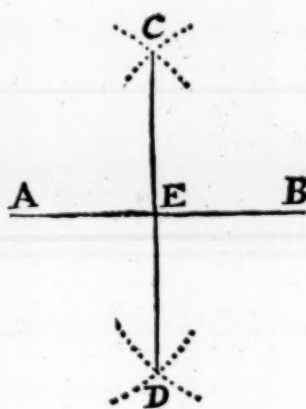


PROBLEM I.

To Divide a Line given, not being Infinite, into two Equal Parts, at Right Angles.

THEOREM.

OPEN your Compasses to a greater Distance than $\frac{1}{2}$ of the Line given; set one Foot in one end of the Line given, and with the other make an Arch above and below the Line given; then (the Compasses unaltered) set one Foot in the other end of the given Line, and cross the former Arches: Lastly, from those two Intersections, draw a Line, and it shall cut the Line given, into 2 Equal Parts at Right Angles.



EXAMPLE.

Let AB be a Line given, C, D the 2 Intersections found, by which the Line CD is drawn, which cutteth the Line AB, at E, into 2 equal parts, with Right Angles.

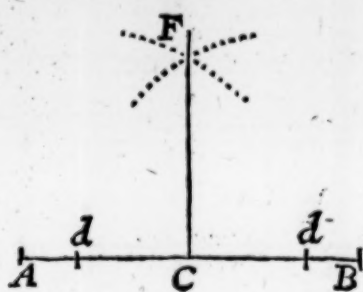
PROBLEM II.

From a Point in a Line given, to raise a Perpendicular.

THEOREM.

Set one Foot of the Compasses in the Point, and with the other make a Point on each side of the Point given in the Line, equidistant from the Point given; then open your Compasses to any wider Distance, and set one Foot of your Compasses in one of those made
K Points,

Points, and with the other make an Arch above the Line given, (the Compasses unstirred) set one Foot in the other made Point, and cross that former Arch; from the Interfection of these two Arches to the Point given, draw a Line, which shall be the Perpendicular required.



E X A M P L E.

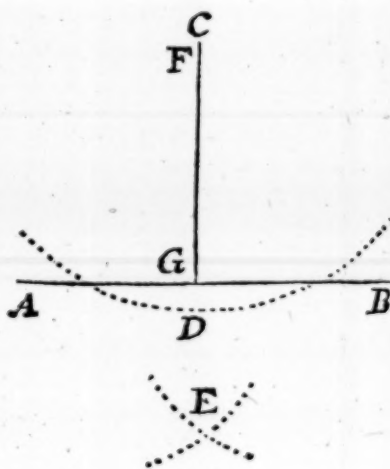
Let A B be the Line given, C the Point assigned, *dd* the two made Pricks, or Points, equidistant from C, F, the Point, or Interfection above, by which the Perpendicular F and C is drawn.

P R O B L E M III.

From a Point above, to let fall a Perpendicular on a Ground-Line.

T H E O R E M.

Set one Foot of the Compasses in the Point assigned, and with the other make an Arch below the Line given, so that it may touch the Line in two places; then set one Foot of the Compasses in one of those Points, where the Arch cutteth the Ground Line, and with the other make a Portion of an Arch below the Line given; then (the Compasses unstir'd) set one Foot in the other Point, and cross that Arch: Last-ly, lay your Ruler by the Point found, and the other Point assigned, and so draw the Perpendicular to the Line given.



E X A M P L E.

Let A B be the Line given, C the Point assigned, and D the Arch Line drawn, E the Point found, by which the Perpendicular F G is drawn.

P R O B L E M IV.

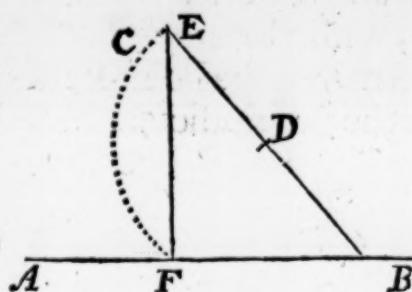
From a Point above to draw a Perpendicular, when there wanteth space below the Line.

T H E O R E M.

From the Point assigned, to any part of the Line given, draw a Slope-Line, which Divide into two equal parts; then set one Foot of

of

of the Compasses in that Point, opening the other to that half, letting one Foot stand open in that Point where the first half is found to be, and with the other strike an Arch from the Point assigned to the Ground Line, and the Intersection in the Ground Line, shall be the Perpendicular Point to the Point assigned.



EXAMPLE.

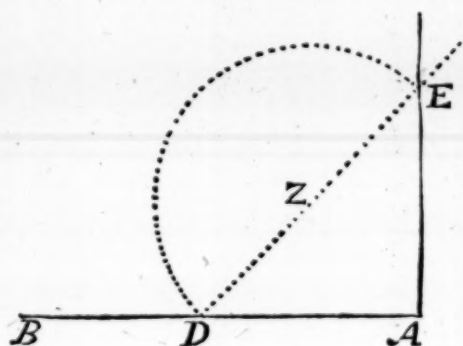
Let AB be the Line given, E the Point assigned, BC a Line drawn, D one half thereof, EF the Arch drawn; so is F the Point of the Perpendicular found to E: Lastly is the Line EF, the Perpendicular required.

PROBLEM V.

Upon the End of a Line given, to raise a Perpendicular.

EXAMPLE.

Let AB be the Line given, and let A, the end thereof, be the Point assigned; whereon to raise a Perpendicular Line, open the Compasses to any convenient Distance, and set one Foot in the Lines-end at A, and make a Point with the other above, as at Z; (the Compasses unstir'd) describe the Portion of the Circle DE, which cutteth the Ground Line in D, and the Point made above the Line at Z, and it will cut the Arch Line in E: Lastly, draw the Line AE the Perpendicular required.

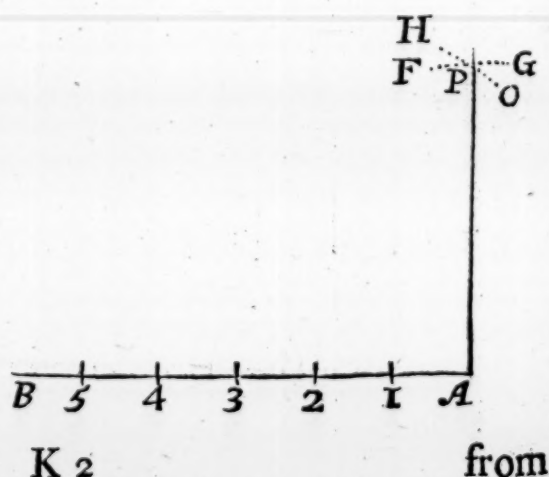


PROBLEM VI.

To raise a Perpendicular upon the End of a Line given, another Way.

EXAMPLE.

With your Compasses opened to any convenient Distance, prick off 5 small and equal Divisions from A towards B, upon that same Line AB; then take with your Compasses, the Distance from A, to 4 Divisions; and setting one Foot in A, describe with the other the Arch FG; then take the Distance



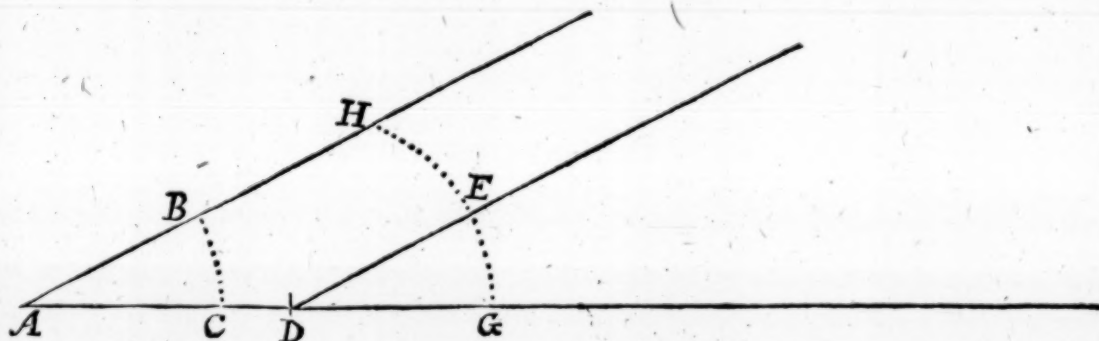
from A, to 5 Divisions, and placing one Foot of the Compasses in 3, with the other Foot, describe the Arch H O, intersecting the former in the Point P: Lastly, from P, draw the Line A P, which is the Perpendicular to the given Line A B required.

P R O B L E M VII.

An Angle being given, and a Point also given in one Side thereof, to draw a Line Parallel to the other by that Side assigned.

E X A M P L E.

From the Point assigned, make an Angle equal to the Angle given, by the Direction of the next Problem, so shall the Side produced, be Parallel to that Side of the Angle it cutteth not. As



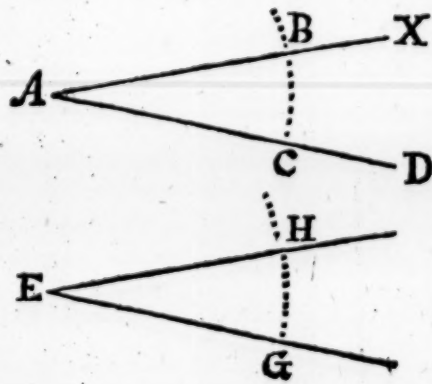
admit A B C be the Angle given, D the Point assigned, D E G the Angle made equal to A B C; so is the Line D E, found to be Parallel to A B.

P R O B L E M VIII.

To make one Angle equal to another Angle given.

E X A M P L E.

Let the Angle given be X A D, and it is required to make another Angle equal to the same: Open the Compasses to any convenient Distance, and setting one in A the given Angle, with the other describe the Arch B C; then with the same Extension set one Foot in E the Line assigned, and with the other describe the Arch H G; which done, take the Extent of the Arch Line B C, and setting one Foot of the Compasses in G, with the other mark the Point H: Lastly, with your Ruler draw the Line E H, which shall make the Angle H E G, equal to B A C required.



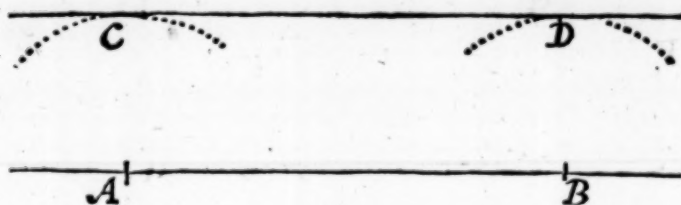
P R O-

PROBLEM IX.

Unto a Line given, to draw a Line Parallel to it, at any Distance given.

EXAMPLE.

Let the Right Line given be AB , unto which it is required to draw another Parallel Line: First open your Compasses to the Distance given, and setting one Foot in the Point A , with the other make an Arch on that side the Line whereon the Parallel Line is to be; then make the like Arch at the other end of the Line at B , as the Arch Lines C and D :



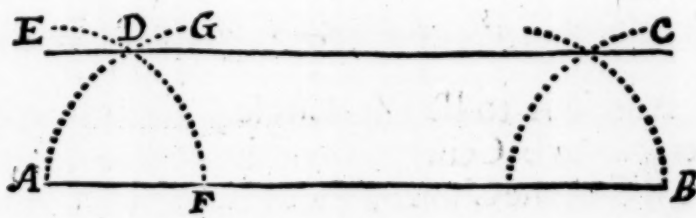
Lastly, lay your Ruler by the Convexity, or outside of those two Arches, and draw the Line CD , which shall be Parallel to the given Line AB , as was required.

PROBLEM X.

To draw a Parallel Line, without stirring the Compasses from the Distance given, a more Readier and Exacter Way.

EXAMPLE.

Let AB be the Line given, to which I would make another Parallel: I open my Compasses to the Distance required, and describe the Arch EDF , then the Foot remaining in F , describe the other Arch ADG ; then remove the Compasses to B , and do the like; then lay the Ruler that it may cut both the Intersections; then draw a Line from the Point of Intersection in the one end, till it touch the Point of Intersection in the other end, and so is EDC Parallel to AB , which was required.

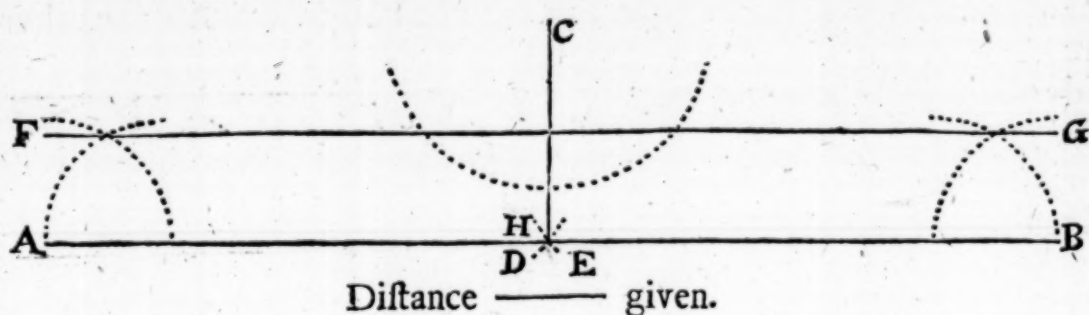


P R O B L E M X I.

From a Point assigned unto a Line given to draw a Perpendicular, without stirring the Compasses from the Distance given.

E X A M P L E.

Admit A B be the Line given, C, the Point assigned, and the Line D E, the Distance of the Compasses: First, draw the Parallel



Line F G, and A B, at that Distance; then by the *Third Problem*, let fall the Berpendicular C H, which is the thing required.

P R O B L E M XII.

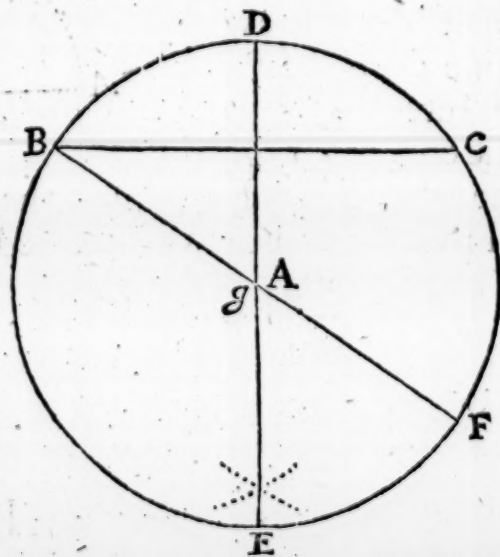
A Circle being given, to find the Center thereof.

T H E O R E M.

From any part of a Circumference given to another, draw a Chord-Line, which divide into two equal parts, at Right Angles, by the *First Problem*, letting that Line end in the Circumference of the Circle; so shall that Line be the Diameter of the Circle, and the Middle the Center.

E X A M P L E.

Admit A to be the Circle given, whose Center is required; let B C be the Chord-Line drawn, which is Divided into two equal parts at Right Angles, by the Diameter D E in the one half, is the Center, which may be found by setting the Distance of C D, from E to F, the Line B F drawn, cutteth the Line D in g, which Point (g) is the Center to the Circle A, which was required.



P R O-

PROBLEM XIII.

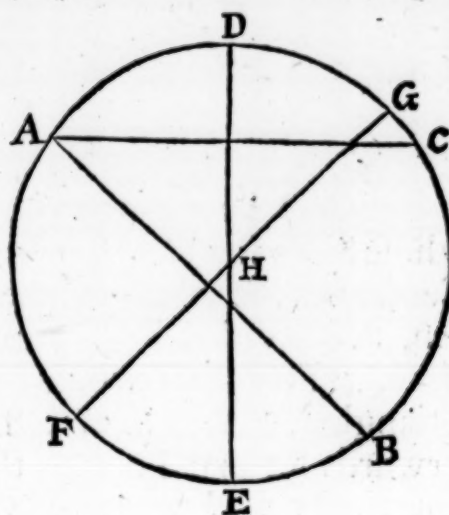
To bring three Pricks (not lying in a Straight Line) into a Circle.

THEOREM.

First draw three Points given, into an Angle, and divide each Side into 2 equal parts, at Right Angles; and where the 2 Perpendiculars cut one another, that Point shall be the Center required.

EXAMPLE.

Admit ABC , the three Points given; let the Line AB , and AC , be drawn; let AC be divided at Right Angles by FG ; now DE , and FG , cut one another in H ; which is the Center found, as was required.

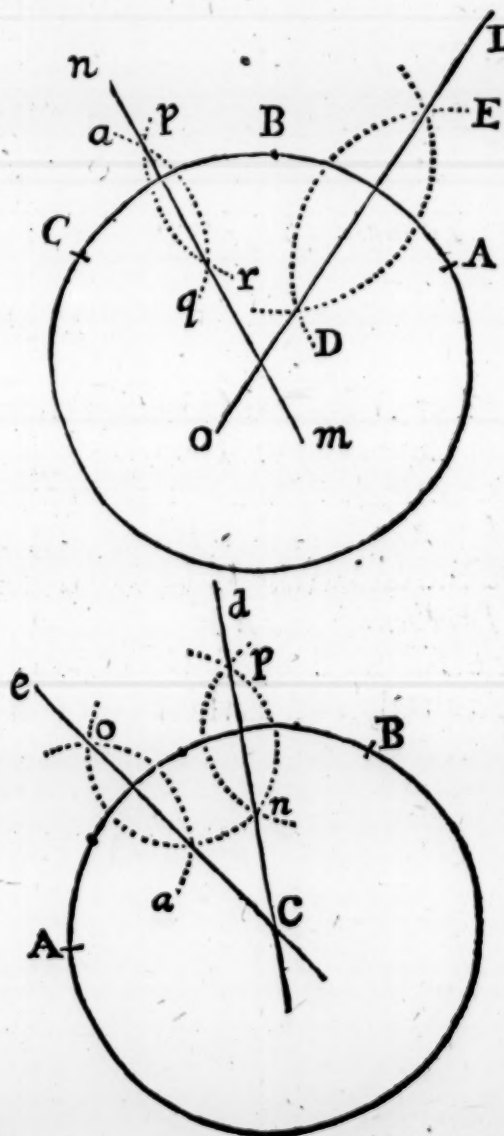


PROBLEM XIV.

To perform the former Work a nearer Way, and to find the Center to any Arch, or Portion of a Circle.

EXAMPLE.

Let A , B , and C , be the three Pricks to be brought into the Edge of a Circle, by finding a Center common to them all: First, open the Compasses to something more than half the Distance between two of the Pricks, (as are AB ;) then set one Foot in A , and describe the Arch DE ; likewise set one Foot in the Prick at B , crossing the former Arch DE : Then from these two Intersections, draw the Line $O I$; then taking something more of the Distance between the 2 Pricks C and B ; make the 2 Arches aq , and rp , and from their Intersection draw the Line nm ; and where these two Lines cut one another is the Center, that runneth upon the 3 given Pricks.



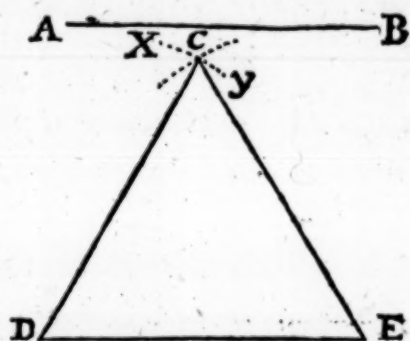
In like manner you may find the Center to any Arch, or Segment of a Circle, as may be seen in the Margin, marked with ABC, and *aodpn*; otherways, *vide* Path-way to Knowledge, the 26th Conclusion.

PROBLEM XV.

To make an Equi-angled Triangle, whose Sides are equal to a Line given.

EXAMPLE.

Let AB be a Line given, to make an Equi-angled Triangle, whose Sides shall be equal to the given Line AB; then open the Compasses the length of the Line given, and lay down the same in that place, where you would have the Triangle described, *viz.* DE; afterwards set one Foot of the Compasses in D, and with the same Extent make the Arch XY; then set one Foot of the Compasses in the other end of the Line, and cross the former Arch in C; then from C, to D and E, draw the Equi-angled, or Equilateral Triangle CDE, as was required.

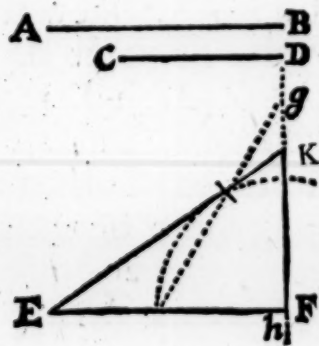


PROBLEM XVI.

To make a Right Angled Triangle, the two Sides being given.

EXAMPLE.

Let AB, and CD, be the two Lines given: First, lay down the Line AB, for the Base EF; then, by the *Fifth Problem*, raise the Perpendicular (*gh*); then take the Length of the other given Line CD, and set it up on the end of the Base, at F; then draw the *Hypotenuse* from E to K, which includeth the Right Angled Triangle EKF, as was required, and as the Figure in the Margin directs.



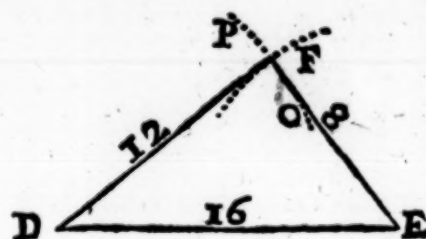
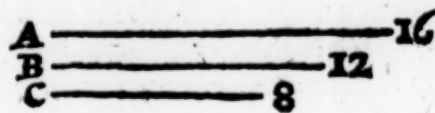
PRO-

PROBLEM XVII.

Three Lines of Unequal Lengths given to make a Triangle, if the Sum of the two shortest Sides be longer than the third.

EXAMPLE.

Let the three Lines given, be A, B, C, whereof a Triangle is to be made: First, place the longest Line A, from D, to E, for the Base; then take the Length of the second Line B, and set one Foot in the end of the Base at D, and make the Arch P O; then open your Compasses to the Length of the third Line C, and set one Foot in the other end of the Base at E, and cross the former Arch at F; from which Intersection draw the Lines F D, and F E, whose Sides are equal to the three Sides, or Lines given, A, B, and C.

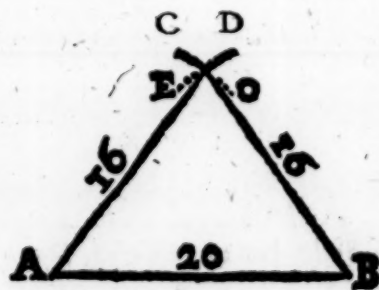


PROBLEM XVIII.

To make an Ifofceles Triangle, upon a Right Line given.

EXAMPLE.

Let the Right Line given, be A B, 20; whereon it is required to describe an *Ifofceles* Triangle, whose Sides shall be 16 a piece; open the Compasses upon the Scale to 16; and with one Foot in A, describe the Arch C O; and with the same Distance, place one Foot in B, and cross the former Arch as E D; and to that Intersection draw two Lines from A and B; which shall include the Triangle required.



PROBLEM XIX.

A Triangle being made, to find of what kind it is.

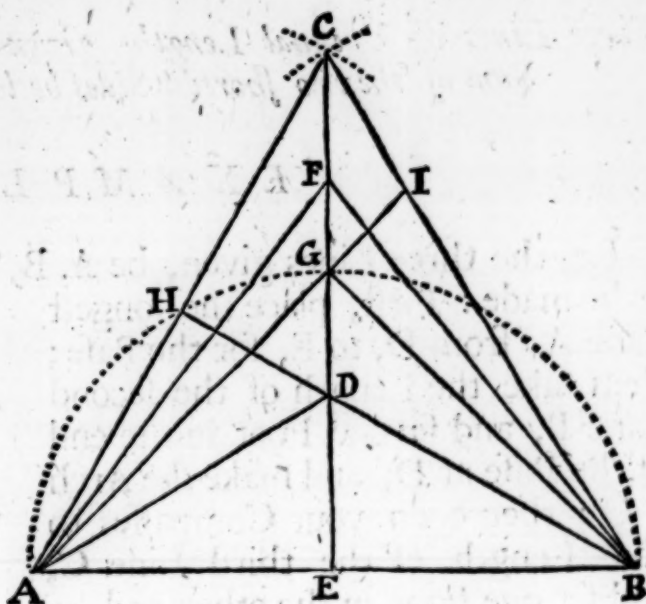
THEOREM.

Upon the Base Line of the Triangle, describe a Semicircle; and upon the Center thereof, raise a Perpendicular, in height equal, or higher than the third Angle; then if the Angle fall within the

M

Cir-

Circumference, that Triangle is *Ambligonium*; and if it fall upon the Circumference, it is *Orthogonium*; but if the third Angle fall without the Circumference, then is that Triangle *Oxigonium*; and if the third Angle fall upon the Perpendicular, it is either Equilateral, or *Isofceles*: It is *Equilateral*, when all the three Sides are equal, otherways it is *Isofceles*; but if the Angle do not fall upon the Perpendicular, then it is *Scalenum*.



EXAMPLE.

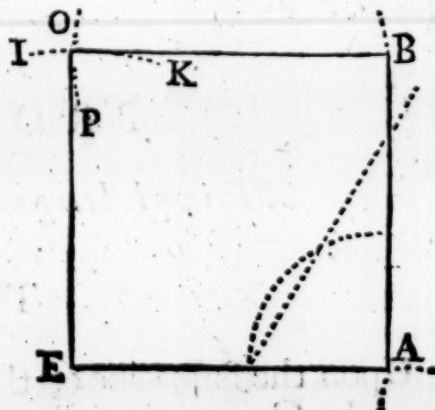
Admit ABC , be the Triangle; AGB half of the Circumference drawn upon the Center E ; and EF , a Perpendicular, raised upon the Center E ; now for that the Angle C falleth without the Circumference, therefore the Triangle ABC , is *Oxigonium Equilateral*; for that the Angle C , falleth upon the Perpendicular, therefore the Triangle ABG , is a Right Angled *Isofceles*; the Triangle ABH , is a Right Angled *Scalenum*; ABF , an *Oxigonium Isofceles*; ABD , an *Ambligonium Isofceles*; ABI , is a *Scalenum*.

PROBLEM XX.

To make a Square, whose Sides shall be equal to a Line given.

EXAMPLE.

Admit AE , be the Line given: First, make the pricked Right Angle by the Fifth Problem; then set the Side of the Square, on each side thereof, from the Angle at A ; then set one Foot in E , and describe the Arch IK ; and with the same Distance, set one Foot in B , and describe the Arch OP ; and from that Intersection draw the Lines OE , and IB ; so is the Square $IBAE$ made, whose Sides are equal in Length to the Line AE , required.

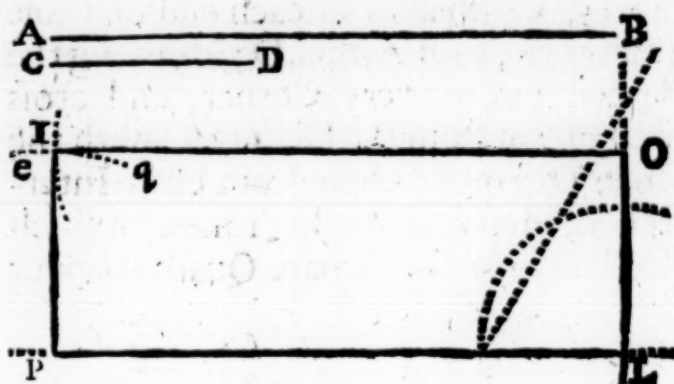


PROBLEM XXI.

To make a Long Square, or Parallelogram, equal to two given Lines.

EXAMPLE.

Admit AB , and CD , to be the two Lines given: First, by the *Fifth Problem*, make the prick't Right Angle OLP ; then set AB , for the Base from P to L ; next let the Line CD , be set from L to O ; then take with your Compasses, the Length of the Line CD , and set one Foot in P , and describe the Arch (eq); then take the Length of the Line AB , and set one Foot in O , and cross the former Arch; and from that Intersection, draw the Lines IP , and IO ; which include the Long Square $IOLP$.

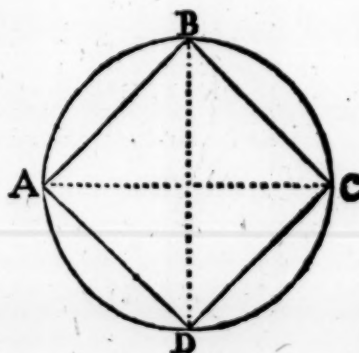


PROBLEM XXII.

To make a Square Quadrat in a Circle assigned.

EXAMPLE.

First, draw the Circle, and cross it with two Diameters, AC , and BD , represented by the two prick'd Lines; then make, or draw the other four Lines; as from A , to B ; from B , to C ; from C , to D ; and from D , to A ; which shall include a Square Quadrat in the Circle assigned: And this is also termed, The Inscribing of a Square within a Circle.

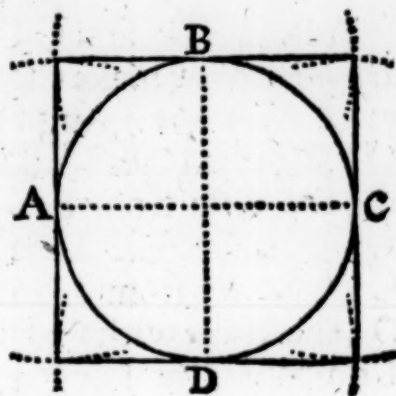


P R O B L E M XXIII.

To make a Square Quadrat about a Circle assigned.

E X A M P L E.

First, draw two Diameters a-cross-ways, so that they make four Right Angles in the Center; then with your Compasses take the Length of the half Diameter, and set one Foot of the Compasses in each end of those Diameters, as at A, B, C, D; drawing the Arch-Lines in every Corner, and cross each of 'em from the Diameters with the same Distance; then from each Intersection, draw 4 Right Lines, which shall include the Square Quadrat about the Circle assigned.



P R O B L E M XXIV.

To draw a Circle within a Triangle appointed.

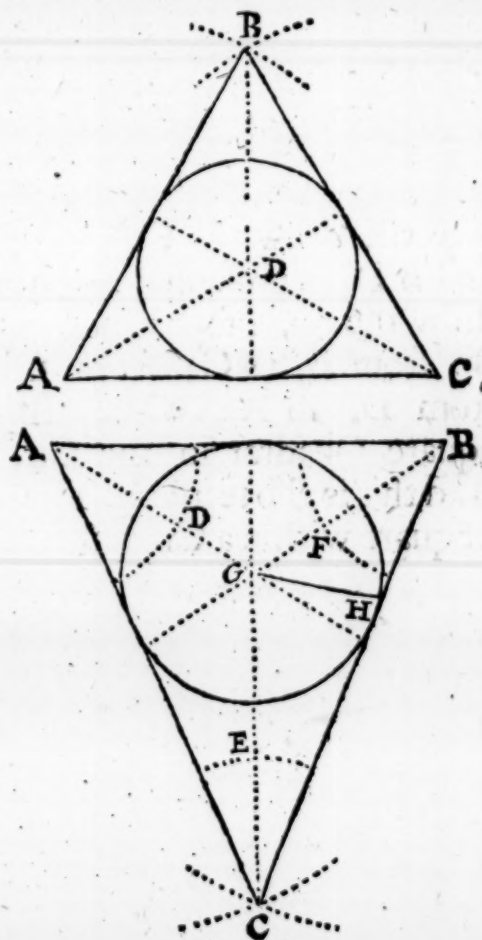
E X A M P L E I.

If the Triangle have all Sides equal, then take the Middle of every Side, and from the contrary Corner draw a Right Line unto that Point; and where those Lines do cross each other, there is the Center; in which set one Foot of the Compasses, and stretch out the other to the Middle Prick of any of those Sides, and so draw a Circle which shall touch every side of the Triangle, but shall not pass without any of them.

But to do this in all other kinds of Triangles, you must divide every Angle in the Middle, and so draw Lines from each Angle to their Middle Prick; and where those Lines do intersect one another, there is the Common Center.

E X A M P L E II.

Admit this Triangle ABC, which by the Eighth Problem, I di-



vide

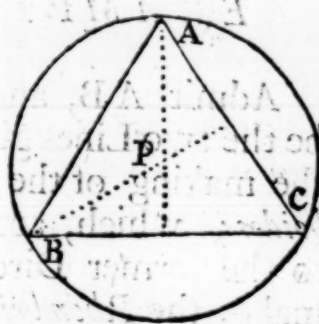
vide into two equal parts at D E F ; from whence are drawn the Prickt Lines of Division, A D, B F, and C E, which cross in G ; therefore shall G, be the Common Center ; then make one Perpendicular, viz. G H, and set one Foot of the Compasses in G, and extend the other to H, and so draw the Circle, which will justly answer to that Triangle.

PROBLEM XXV.

To draw a Circle about any Triangle assigned.

EXAMPLE.

First, Divide two Sides of the Triangle into equal parts, viz. in the half ; and from those two Pricks, raise two Perpendiculars ; and where they two cut one the other, there is the Center, upon which you may draw the Circle, which shall include the Triangle as was required.



This also may be performed by the Fourteenth Problem.

PROBLEM XXVI.

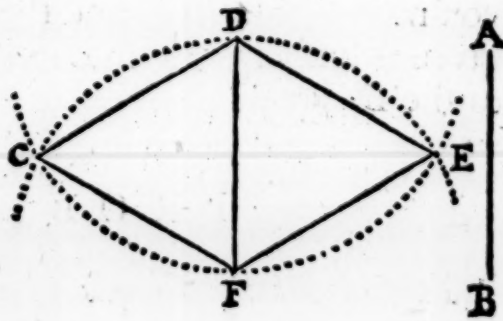
To make a Rhombus, whose Sides shall be equal to a Line given.

THEOREM.

A Rhombus may be described by the Fifteenth Problem, by joyn- ing two Equi-angled Triangles together, leaving out the Pricked Line in the Figure.

EXAMPLE.

Admit A B, to be the Line gi- ven ; then by working, as the Figure in the Margin directs, or according to the Fifteenth Pro- blem, either way will make the Rhombus C D E F, whose Sides are equal to the Line A B, as was required.



P R O B L E M XXVII.

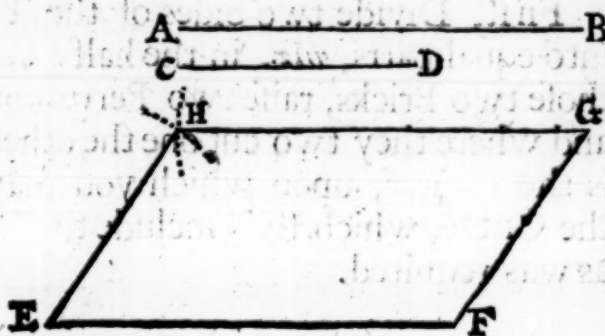
To make a Rhomboides, the two Sides being limited.

T H E O R E M.

First, lay down the longer of the two Sides given; then open your Compasses to the Length of the shorter Line, and draw another Line Parallel to that, and of the same Length; then by the end of those two Lines is included the *Rhomboides*.

E X A M P L E.

Admit AB, and CD, be the two Lines given for the making of the *Rhomboides*; which, according to the former Directions, makes the *Rhomboides*.



Of P O L Y G O N S.

The making of *Equi-angled*, or *Regular Polygons*.

TO make any *Regular*, or *Equi-angled Polygons*; you must first make a *Blind*, or *White Circle*; and then find out the Chord thereof according to the Side of the Polygon; which Chord-Line, or Distance, must be set so many times in the Circumference of that Circle; and Lines being drawn from Point to Point, will include the Polygon; therefore before you can make a Polygon, you must first learn to find the Chords in a Circle, according to a given Number; which is taught as followeth, from the *Trigone*, to the *Decagone*.

P R O B L E M XXVIII.

To find out the Chords in a Circle from the *Trigone*, to the *Decagone*.

T H E O R E M.

Which are performed, as in the Exposition of the Demonstration following.

E X A M-

EXAMPLE.

Admit $A B E F$, be the Circle given to find the Chords thereof.

First, draw the Diameter $A B$; then open your Compasses to the Semidiameter; set one Foot in A , and with the other Foot cross the Circumference at C , and D , and draw the Line $C D$, which will be the third Chord.

DEMONSTRATION.

4. This done, draw the Line $E F$, which divideth the Diameter $A B$, into two equal parts at Right Angles; then draw the Line $A E$, which shall be the fourth Chord-Line, or the Side of an inscribed Square.

5. To find the Fifth, set one Foot of your Compasses in H , and extend the other to E ; and with that Distance, cross the Diameter in I , and draw the Line $E I$, which shall be the Fifth Chord, or the Side of a *Pentagon*.

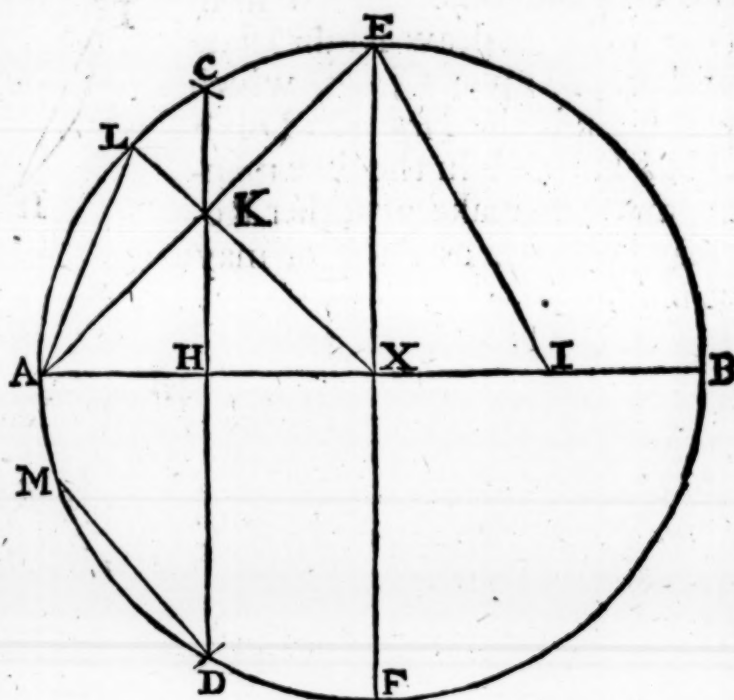
6. The Sixth is the Semidiameter, which is the Side of a *Hexagon*.

7. The Seventh is half the Third, as $C H$, or $H D$; which is the Side of an Inscribed *Heptagon*.

8. To find the Eighth, lay your Ruler upon the Center X , and the Intersection K , which will cut the *Periphery* in L ; then draw the Line $A L$, which is the Side of an Inscribed *Octagon*.

9. The Ninth is a third part of the Arch $C A D$, as $M D$.

10. The Tenth is the Line $X I$, which is the Side of an Inscribed *Decagon*.

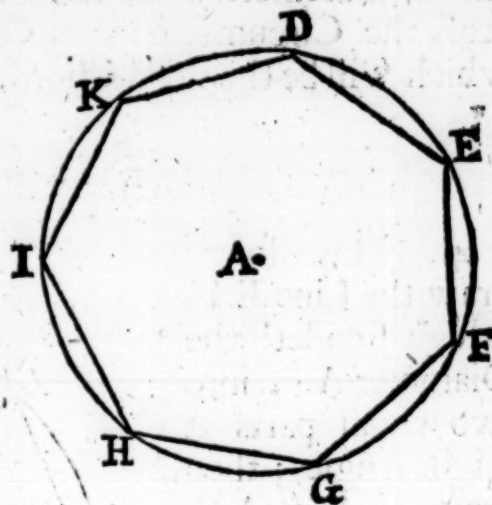


P R O B L E M XXIX.

To make a Heptagon, the Circle Inscribing it being given.

E X A M P L E.

Let A, be a Circle given, where-
in a *Heptagon* is to be Inscribed;
therefore by the last *Problem* find
out the Seventh Chord G H, or
H I, and place it Seven times in
the Circumference; then from
Point to Point, draw Right Lines
within the given Circle, which
will Include the *Heptagon* D E F
G H I K; and in the like man-
ner may you make any other Re-
gular Polygon, as shall, or may
be required.



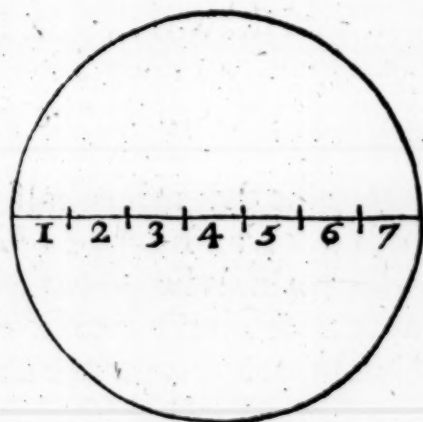
P R O B L E M XXX.

The Diameter of any Circle being given, to find a Right Line equal to
the Right Extension of the Circumference, according to Archi-
medes's Proportion.

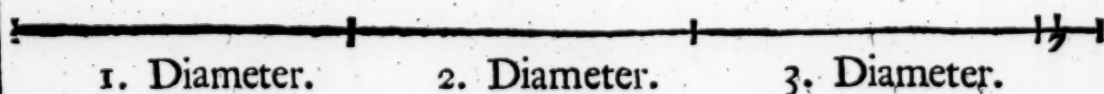
T H E O R E M.

True it is, there is no Agreement
betwixt Circular and Right Lines, to
a precise Quantity, as yet known;
the Old-retained Proportion 7 to 22,
is precise enough, and sufficiently
near enough the Truth, for any Busi-
ness.

Now the Diameter being given to
find the Circumference, take $\frac{1}{7}$ of the
Diameter, and add it to three Diame-
ters, so have you its Circumference
in a Straight Line.



E X A M P L E.



P R O.

P R O B L E M XXXI.

*The Length of the Diameter being given in Numeral Denomination,
to find the Circumference Arithmetically.*

R U L E.

Multiply the Diameter by $3\frac{1}{7}$, so have you the Circumference.

E X A M P L E.

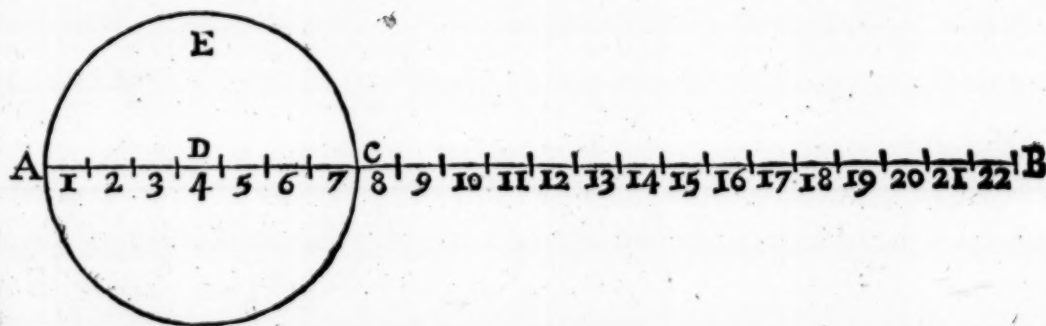
Admit the Diameter to be 21; which Multiplied by $3\frac{1}{7}$, produceth 66, for the Circumference.

P R O B L E M XXXII.

A Right Line being limited, to make a Circle, whose Circumference being extended, shall be equal thereunto.

T H E O R E M.

Of the Line given, take $\frac{2}{3}$, which part divide into two equal halves, and with that Distance make a Circle; and the Circumference thereof being extended, shall be equal to the Line given.



E X A M P L E.

Admit A B, be the Line limited; then let A C be found $\frac{2}{3}$, and let the Middle part thereof, be found at D; upon which Point describe the Circle E; the Extension of the Circumference thereof is equal to the Line A B, which was required.

P R O B L E M XXXIII.

The Extension of a Circumference being given in Numeral Denomination, to find the Length of a Diameter Arithmetically.

R U L E.

Multiply the Circumference given, by 7, and Divide that Product by 22; so have you the Length of the Diameter required.

E X A M P L E.

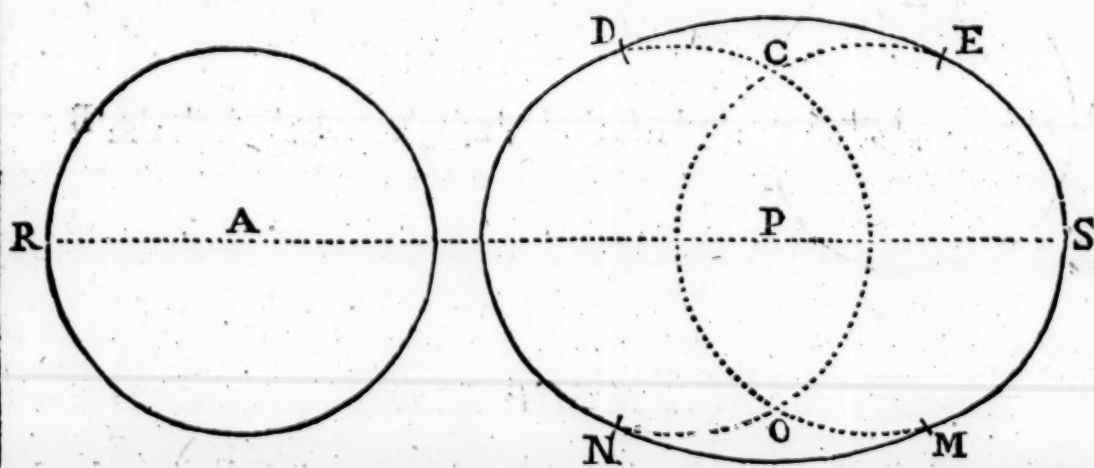
Admit the Circumference given, be 66; which Multiplied by 7, produceth 462; which Divide by 22, quotes 21, for the Diameter.

P R O B L E M XXXIV.

To describe a Geometrical Oval at any Circumference appointed.

E X A M P L E.

Let A be the Circumference appointed to describe an Oval of: First, draw a Blind, or White Line, as R S; upon which describe a White, or Blind Circle, equal to that of A; then set one Foot in the Edge of the Circle in the Right Line, and draw ano-



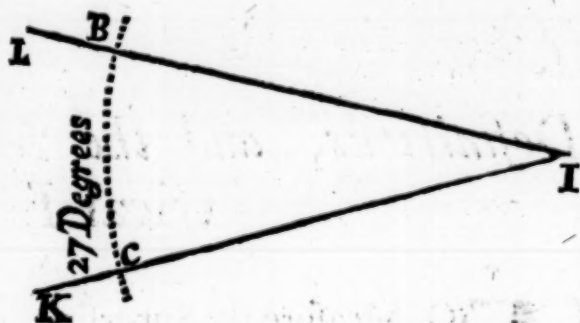
ther of the same Circumference; then open the Compasses to the Length of your Diameter, and set one Foot in O, and strike the Arch D E; with the same Distance set one Foot in C, and strike the Arch M N, which includeth the Oval P.

PROBLEM XXXV.

An Angle being given, to find the Quantity thereof.

EXAMPLE.

Suppose KIL were an Angle given, and that it were required to find the Quantity thereof: Open your Compasses from the beginning of a Line of Chords to 60 Degrees; then with that Extension place one Foot in I, and with the other describe the Arch CB; then take in your Compasses the Distance of CB, and applying that Distance to the Scale of Chords, which reacheth from the Beginning, to 27 Degrees, which is the Quantity of the Angle required.



Note. If any Angle given, shall contain above 90 Degrees, you must then protract it at twice, by taking first the whole Line, and then the Remainder, or dividing the Angle into any two parts equal unto it.

As if the Angle were 159 Degrees; take 80, and 79; or 90, and 69 Degrees, &c.

PROBLEM XXXVI.

A Portion, or Part of a Circumference being given to find the right Extension thereof.

EXAMPLE.

First, find out the Center to that Arch by the *Fourteenth Problem*, by which Point draw a Line by each end of the Arch, which will make an Angle, the Quantity whereof, find by the last Problem; and consequently the Circumference of the whole Circle, whereof that is a part; then say, (by the *Rule of Three*) as the Degrees of that Angle are in proportion to 360, so is that Arch to the whole Circumference.

The End of the First Part.

GEOMETRY.

PART II.

Definitions, and the Measuring of Geometrical Figures.

TO Measure the Superficies of any Figure, is to shew how many Squares are therein contained, according to a Scale assigned.

A Scale is any Right Line divided into any equal parts, by which equal parts may be represented; an Inch, a Foot, a Yard, a Pace, a Perch or Pole, a Mile, a League, a Degree, &c. according to the thing to be represented.

Now, notwithstanding that a Triangle is one of the Simplest Figures of all Superficies, yet for as much as the Ground and Measuring of a Triangle, and all other Figures, is Demonstrated out of the Square, and Long Square, I shall therefore begin with these two Figures.

PROBLEM I.

To Measure a Geometrical, or True Square.

THEOREM.

Every Square is a Rectangled Equilateral Parallelogram, whose Sides are all equal: Hence in all Right Angled Parallelograms, the Length Multiplied by the Breadth produceth the Area thereof.

E X A M-

self, produceth 400; the which being doubled, maketh 800 for the Area of the Square ACEF, whose Square Root is 28 $\frac{1}{2}$ for the Diagonal BD.

For Measuring a Right Angled Triangle.

THEOREM.

By the Ground of this Theorem, a Right Angled Triangle may be thus Measured, *viz.* Multiply the Diagonal in it self, and half of that Product sheweth the Area.

EXAMPLE.

Admit AEF, to be a Triangle, whose Diagonal AF is 40; which Multiplied by 40, produceth 1600; whose half is 800 for the Area.

Note, That if the Side of the Square be Rational; then is the Diagonal Irrational; but if the Diagonal be Rational, then is the Side Irrational.

PROBLEM III.

To Measure a Long Square, or Parallelogram.

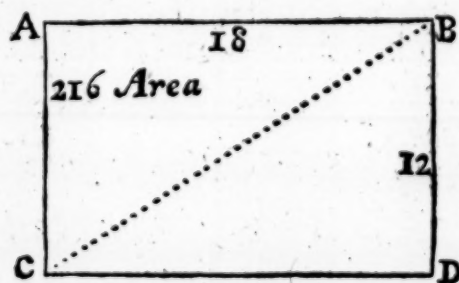
THEOREM.

Multiply the Length by the Breadth, the Product is the Area.

EXAMPLE.

Admit ABCD, to be an Ob-long to be Measured, whose Length is 18, and the Breadth 12; which being Multiplied together, produceth 216 for the Area thereof.

To find the Length of the Diagonal Line BC; Square AB 18, and AC 12, which Squares added together, the Square Root thereof will be the thing required.



PROBLEM IV.

To Measure a Rhombus,

THEOREM.

Every Rhombus is an Oblique-angled Parallelogram Equilateral, and is equal to that Long Square, whose Length is equal to one of the

the Sides, and Breadth is equal to the Parallel Distance thereof, and may be Measured several ways ; but the most Common way is this that follows.

To find the Perpendicular.

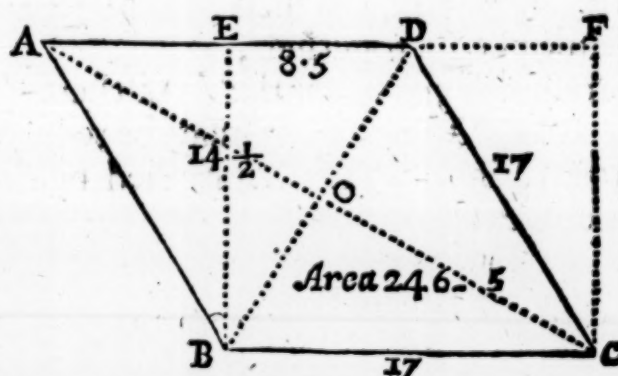
But first to find the Perpendicular EB or FC ; Square AE and AB , and Subtract the lesser Square from the greater ; the Square Root of the Remainder is the Length of the Perpendicular required.

R U L E.

Multiply the Length of the Perpendicular by one of the Sides, the Product is the Area.

E X A M P L E.

Admit $ABCD$, to be the *Rhombus* whose Side is 17 , and the Perpendicular $14\frac{1}{2}$; which Multiplied together produceth $246\frac{1}{2}$, for the Area thereof, and is thus further Demonstrated, viz.



D E M O N S T R A T I O N.

Make a Long Square, whose Length let be equal to the Side of the *Rhombus*, and the Breadth equal to the Perpendicular, as the Long Square $EBCF$; now the Triangle ABE , is equal to the Triangle CDF , so consequently $EBCF$ is equal to the *Rhombus* $ABCD$.

Note also *Arithmetically*, A Mean Proportion between EB , the Perpendicular, and BC the Side, is the Side of the Square equal to the *Rhombus*, or *Rhomboides*.

P R O B L E M V.

Given AB the Side of a *Rhombus* and one Diagonal, to find the other.

T H E O R E M.

Divide the Diagonal AC , and BD , into two equal parts, making Right Angles at the Center O ; then from the Square of AB , Subtract the Square of half the given Diagonal, the Square Root of the Remainder is half the other Diagonal.

P 2

P R O-

P R O B L E M VI.

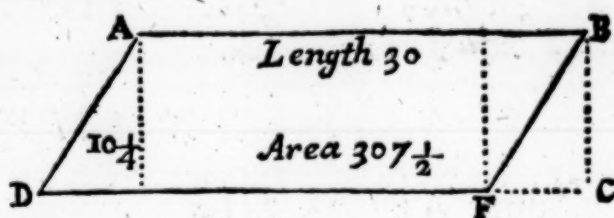
To Measure a Rhomboides.

T H E O R E M.

Every *Rhomboides* is equal to that Long Square, whose Length is equal to one of the Longest Sides, and the Breadth equal to the Parallel Distance.

E X A M P L E.

Admit *ABFD* to be a *Rhomboides*, whose Length is 30; the Perpendicular, or Parallel-Distance $10\frac{1}{4}$, which Multiplied together, produceth $307\frac{1}{2}$, for the Area thereof, as was required.



Note, Otherways it may be reduced into 2 Triangles by a Diagonal Line; which Multiplied by the Perpendicular, produceth the Area also.

P R O B L E M VII.

To Measure Right Angled Triangles.

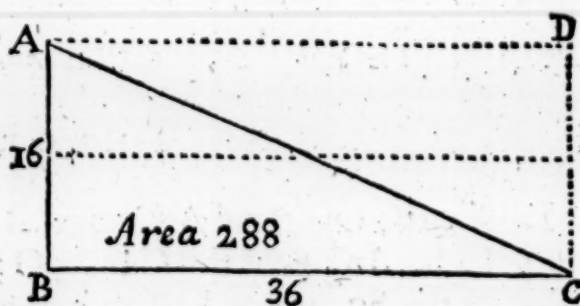
T H E O R E M.

Every Right Angled Triangle is half that Long Square, whose Length and Breadth are equal to the two containing Sides thereof.

Therefore Multiply the two containing Sides together, (*viz.* the Perpendicular and the Base) half the Product is the Area; or the Base by half the Perpendicular, or the Perpendicular by half the Base; either Product is the Area.

E X A M P L E.

Admit *ABC* to be a Right Angled Triangle to be Measured, whose Base *BC* is 36, and *AB* the Perpendicular 16, which Multiplied together, whose half Product 288 is the Area.



Otherwise 8 the half-Perpendicular, Multiplied by 36 the whole Base, the Product is 288 for the Area.

Or

Or 18, half the Base, being Multiplied by the whole Perpendicular 16, makes likewise 288 for the Area, as before.

P R O B L E M VIII.

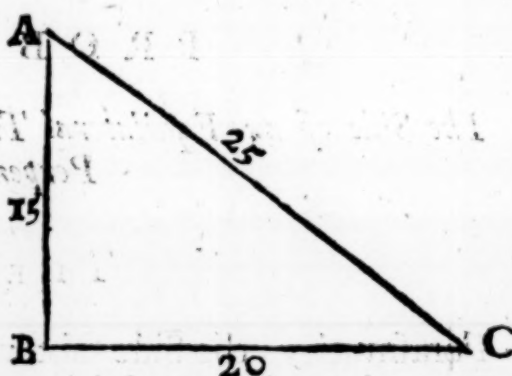
Having given in a Right Angled Triangle, the Perpendicular and Base; to find the Length of the Hypothenufe, &c.

T H E O R E M.

The Line that Subtendeth the Right Angle, viz. the Hypothenufe, is double (or equal) in power, to both the containing Sides thereof; viz. The Base, and the Perpendicular.

E X A M P L E.

Admit A B C, to be a Right Angled Triangle, whose Subtendent, or Hypothenufe A C, is required; now the Base, or Side B C is 20, and the Perpendicular, or Side A B, is 15: Therefore to find A C, Square A B, and B C, severally; and the Square Root of their Aggregate, is the Length of the Subtendent A C, which is found 25.



To find either of the other Sides.

Admit the Subtendent Line A C, to be given 25, and the Base B C 20: Hence by the foregoing Directions, Square the two Sides severally, and subtract the lesser from the greater, and the Square Root of the Remainder is 15 for the Length of the Perpendicular Line A B, as was required: Observe the same Method in finding the Length of the Base Line B C.

P R O B L E M IX.

How to Measure an Equiangled Triangle.

T H E O R E M.

Cube half one of the Sides, and Multiply that Number by half the Perimeter; of that Product, Extract the Square Root, which sheweth the Area of the Triangle.

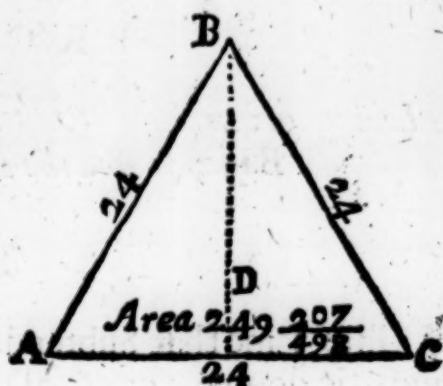
Q

E X A M.

EXAMPLE.

Admit ABC , to be an Equilateral Triangle to be Measured, whose Side is 24, whose half is 12, the Cube thereof is 1728; which Multiplied by 36, half the Perimeter, the Product is 62208; whose Square Root is $249\frac{49}{8}$, near Rational, for the Area.

Otherways, it may be Measured by letting fall a Perpendicular from either Angle, to the opposite Side; and then Multiplying the half of the one, by the whole of the other, the Product is the Area.



PROBLEM X.

The Side of an Equilateral Triangle being given, to find the Perpendicular.

THEOREM.

Forasmuch as the Side subtending the Right Angle, is equal in power to both the containing Sides thereof; Subtract the Square of half the Side, from the Square of the whole, and the Square Root of that Remainder is the Length of the Perpendicular.

EXAMPLE.

Admit the former Figure ABC , to be an Equilateral Triangle, whose Perpendicular is required; the Side of the Triangle is 24, whose Square is 576; and the half of 24 is 12, whose Square 144; which subtracted from 576, there remains 432; whose Square Root is 20.79, for the Length of BD , the Perpendicular required.

PROBLEM XI.

An Isosceles Triangle being given to find the Length of the Perpendicular, and also its Area.

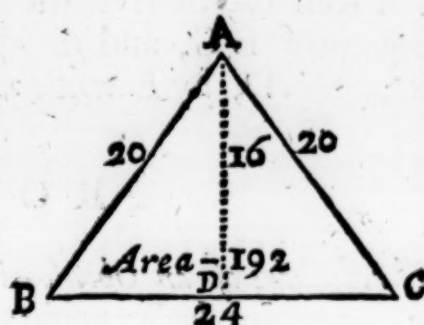
THEOREM.

By the Ground of the last Problem, subtract the Square of half the unequal Side, from the Square of one of the equal Sides; the Square Root of the Remainder, is the Length of the Perpendicular.

EXAMPLE.

EXAMPLE.

Admit one of the equal Sides, as A B, or A C, is 20, its Square 400; the half of the Unequal Side B C, is 12, and its Square 144; which subtracted from the Square of A B 400, leaveth 256; whose Square Root is 16, the Length of A D, the Perpendicular required.



For the Area.

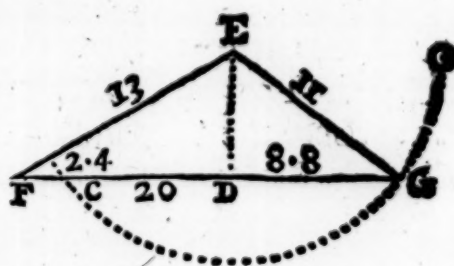
Multiply the Root 16, by $\frac{1}{2}$ B C 12, it produceth 192, for the true Area: Or, Multiply $\frac{1}{2}$ the Root 8, by B C 24, and it produceth 192, as before.

PROBLEM XII.

Three Sides of any Oblique Angled Triangle being given, to find where the Perpendicular shall fall.

THEOREM.

The greatest Side being put for the Base, upon which the Perpendicular shall fall, find both the Sum and Difference of the other two Sides, and then the Proportion will be as followeth. As the Base, or greater Side, is to the Sum of the other two Sides, so is the Difference of the same Sides to a fourth Number, which being subtracted out of the Base, the Perpendicular will fall in the middle of the Remainder.



EXAMPLE.

By this Operation 8.8. are the parts of the Base between C, and D, or between D and G. Therefore 8.8. is the Point D, where the Perpendicular ought to fall, and its length is found by Prob. 8.

E F	13	} Sub.	13	} Add.	} Analogy is this.
E G	11		11		
2 Rests. 24 Sum.				20 : 24 :: 2 : 2.4.	
				2.4 Sub.	
					17.6 Remains.
					8.8 the $\frac{1}{2}$ parts the Base.

Euclid 13. 2.

From the Sum of the Squares of E F, and F G, subtract the Square of E G, and divide half the Remainder by F G, the Quotient is F D, by Euclid 13. 2.

P R O B L E M XIII.

Three Sides of an Obtuse Angled Triangle being known, to find how far the Perpendicular falls without the Obtuse Angle.

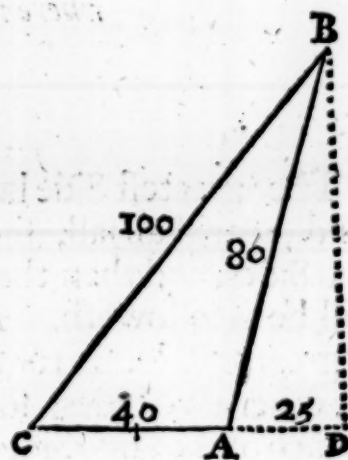
T H E O R E M.

From the Square of B C, subtract the Square of A B, and A C, and divide half the Remainder by A C, the Quotient is A D, by Euclid Prop. 12. 2.

E X A M P L E.

Thus the Square of A B 80, is 6400; and of A C 40 is 1600; the Sum of these two Squares is 8000; which subtracted from the Square of B C 100, viz. 10000, there remains 2000, the half of which is 1000; which divided by A C 40, the Quotient is A D 25 Parts; and by Prob. 8. the Length of the Perpendicular B D will be found.

Otherways, Divide the Side A C, into two equal parts; and one of these parts will be the Length of A D; and D is the Point where the Perpendicular B D must fall.



P R O B L E M XIV.

To Measure any manner of Triangle whatsoever.

T H E O R E M.

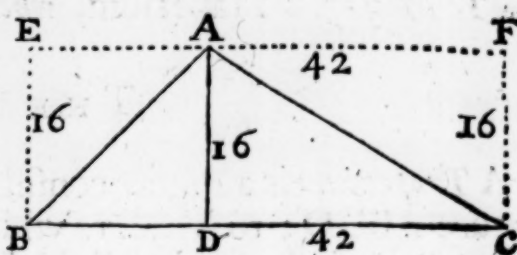
Every Triangle is half that Long Square, whose Length and Breadth is equal to the Perpendicular and Base, or Side cut by the Perpendicular thereof. Therefore from one of the greatest Angles, draw a Perpendicular, as A D; which Multiply in half the Base, or Side cut thereby, and the Product is the Area.

Or, Multiply the whole Base, by half the Perpendicular, and that Product is the Area.

E X A M-

EXAMPLE.

Admit ABC , be a Triangle to be Measured, whose Base BC , is 42 Perches, and the Perpendicular AD 16, as they are both taken from one Scale; now I Multiply the half Base 21, by the whole Perpendicular 16, and the Product is 336, for the Area of the Triangle ABC .



Or if you Multiply the whole Base 42, by 8 the half Perpendicular, the Product is 336, as before.

Or else Multiply the whole Base 42, by the whole Perpendicular 16, the Product will be the Content of the Long Square $EFCB$, which is 672, whose half is 336, the Area, as before.

PROBLEM XV.

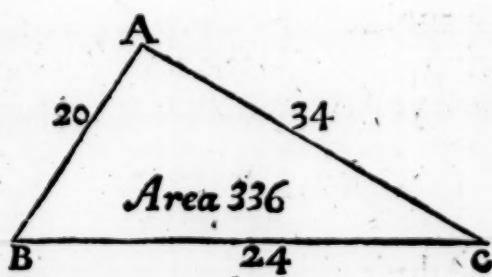
To Measure any manner of Triangle, the three Sides being given without finding the Perpendicular.

THEOREM.

Add together all the three Sides, and take half the Total, and from this half Subtract every Side, which call the three Differences; Multiply these three Differences, and the half Sum continually together, the Square Root of this last Product is the Area thereof.

EXAMPLE.

Admit the three Sides of the Triangle are 42, 34, 20, the Sum is 96, the half Sum is 48; from which Subtracting the several Sides, the Differences are 28, 14, 6: First then Multiply 48, by 28, and the Product is 1344; which Multiplied by 14, that Product is 18816; This Multiply by the last Difference 6, and the Product is 112896, whose Root 336, is the Area of the Triangle, agreeing with all the Operations in the last Problem.



PROBLEM XVI.

To Measure a Trapezium, when none of the Sides are Parallel.

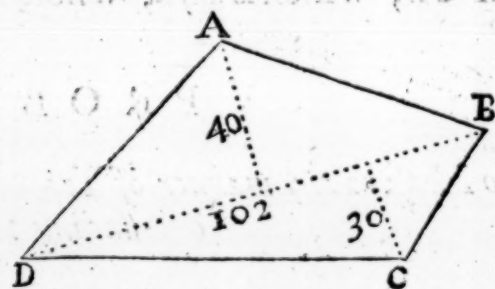
THEOREM.

A *Trapezium* is a Figure consisting of four unequal Sides, as the Figure ABCD; to Measure which *Trapezium*, draw the Diagonal DB; so is the Figure divided into two Triangles, which you may Measure according to the *Fourteenth Problem*, by letting Perpendiculars fall from the Angles A, and C, upon the Base Line DB.

But with more brevity, you may add the two Perpendiculars together, and Multiply the Sum of them by half the Base, and the Product will be the Area of the *Trapezium*, A B C D.

EXAMPLE.

The Sum of the two Perpendiculars is 70, and half the Base is 51; which Multiplied together, makes 3570, for the Area of the Trapezium ABCD.



PROBLEM XVII.

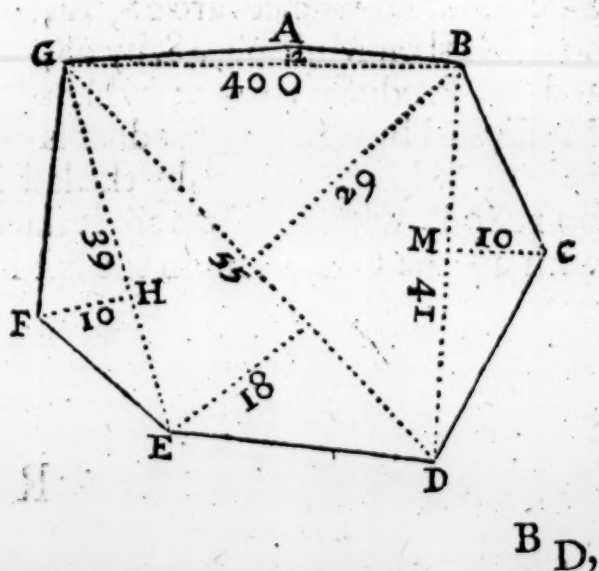
To Measure any Irregular Polygon, or Plot of Ground.

THEOREM.

First, Take care that the whole Plane be divided into *Trapeziums* and Triangles according to your own Fancy, and as the Nature of the Thing will bear; then Measure those *Trapeziums* and Triangles, as is directed in the 14th and 16th Problems before-going, and add the several Contents together; so will the Sum produce you the whole Content of that Irregular Figure.

E X A ' M P L E.

Admit this Figure noted with the Letters A B C D E F G, be the Irregular Plot given; and because it is not in any of the Shapes before given, therefore the best way is to reduce it into *Trapeziums* and Triangles, which is done by drawing the Lines D G,



BD, GB, and GE, so is the Figure divided into one *Trapezium*, and three *Triangles*, as the Figure directs.

Now to find the Content of this Figure, Measure the *Trapezium* and *Triangles* as before directed, and add them together as followeth.

<i>Trapezium</i>	EGBD	1292.50
<i>Triangles</i>	BDC	205.00
	EGF	195.00
	ABG	40.00

The Area of the Figure ABCDEFG 1732.50

PROBLEM XVIII.

To Measure any Regular Polygon.

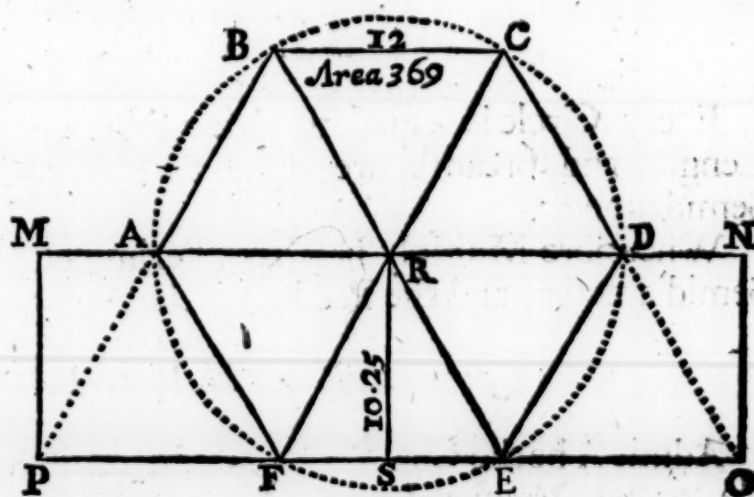
Every Polygon is equal to that Long Square, whose length is half the Perimeter, and Breadth equal to a Perpendicular drawn from the Center to the Middle of any one of the Sides thereof. Therefore,

THEOREM.

From the Center, to any of the Sides, by *Problem 3.* of the *First Part*, let fall a perpendicular or else find it *Arithmetically* by *Problem 11.* of this Part; by which Perpendicular, half the Perimeter being Multiplied, the Product sheweth the Area.

EXAMPLE.

Admit ABCDEF, to be a Hexagon to be Measured, whose Side is 12, and Perpendicular is 10.25, or $10\frac{1}{4}$; which Multiplied by 36, half the Perimeter, the Product is 369 for the Area of the whole Polygon.



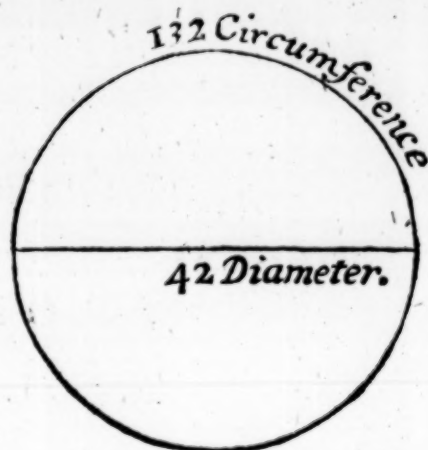
This Theorem is Demonstrated by the Long Square MNOP; for the whole Polygon being 6 Equilateral Triangles, the Long Square is also 5 such Triangles, and 2 Right Angled Triangles equal to another Equilateral Triangle; so that the Long Square is in all six Equilateral Triangles, equal to the whole Polygon.

PROBLEM XIX.

The Diameter of a Circle being given, to find the Circumference.

THEOREM.

Every Circumference is more than triple his Diameter; by such Proportion it is more than $\frac{7}{22}$, and less than $\frac{1}{3}$; but the nearest Rational Number, between the Diameter, and the Circumference is as 7 to 22. Therefore if you Multiply the Diameter by 22, and Divide the Product by 7, the Quotient will shew the Circumference.



EXAMPLE.

Diam. Circum. Diamet.
If 7, be 22: what is 42? (132. Circumference.)

Contrariwise; to find the Diameter: As 22 to 7, so is 132 to 42, for the Diameter: Therefore to find the Diameter, Multiply the given Circumference always by 7, and divide the Product by 22, and the Quotient sheweth the Diameter.

PROBLEM XX.

To Measure a Circle several ways.

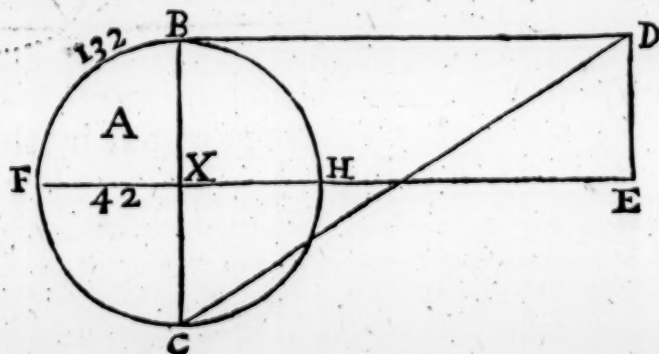
THEOREM.

Every Circle is equal to that Oblong or Long Square, whose Length and Breadth, are equal to half the Circumference and Semidiameter.

Wherefore Multiply half the Perimeter of the Circle, by its Semidiameter, and the Product is the Area thereof.

EXAMPLE.

Admit A be the Circle to be Measured, whose Diameter FH, or BC, is 42; and the Circumference BHCF, 132, by the last Problem; whose half 66 being Multiplied by



the

the Sernidiameter X B 21, it produceth 1386 for the Area of the Circle.

Note, Also every Circle is equal to that Right Angled Triangle, whose two containing Sides, one whereof is equal to half the Circumference, and the other to the Diameter.

Therefore if you Multiply the Diameter 42, by the fourth part of the Circumference 33, it produceth 1386, for the Area, as before.

By which you may see that the Oblong B D E X, is near equal to the Circle A, as likewise the Rectangled Triangle C B D.

Note, Also every Circle is $\frac{11}{14}$ of the Geometrical Square about it, which is made of the Diameter; therefore if you Multiply the Diameter by $\frac{11}{14}$ of the Diameter, the Product is the Area.

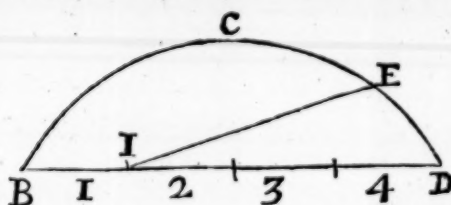
Note, Otherways Square the Diameter, and Multiply that by 11, and Divide that Product by 14, the Quotient is the Area.

P R O B L E M XXI.

To find the Length of an Arch-Line of a Circle, Geometrically.

T H E O R E M.

Let B C D be an Arch-Line given, whose Length is required: First, draw the Chord-Line B D, which must always be Divided into 4 equal parts, as you see Numbred with 1, 2, 3, 4: Then take one of those Parts, and set it from D to E, upon the Arch-Line: That done, draw a Line from the Point E, to the first Division, which shall be I E; this Line is half of the Arch-Line B C D, whose double shall be the Length of the Arch-Line required.

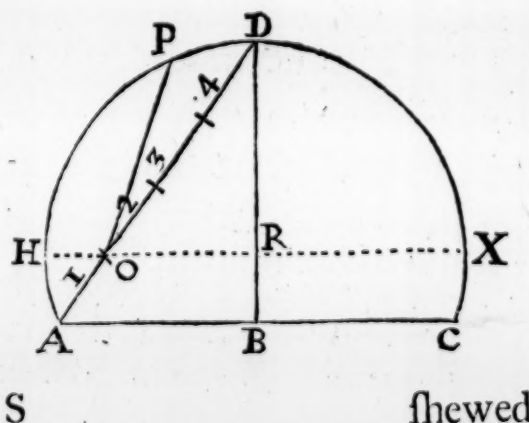


P R O B L E M XXII.

To find the Length of an Arch-Line greater than a Semicircle.

T H E O R E M.

When the Portion of the given Circle is greater than a Semicircle, whose Extent is desired: First, therefore divide the said Arch into two equal parts, as D B; then divide the Chord-Line A D, into four equal parts; by help whereof, draw the Line O P, as was



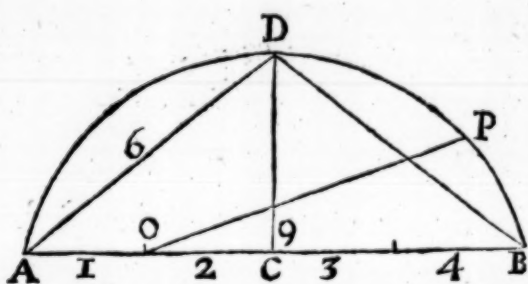
shewed in the last *Problem*, which Line is half the Arch AD , by consequence four times the Line OP , is equal to the Segment ADC .

PROBLEM XXIII.

To find the Length of the Arch of any Segment of a Circle, Arithmetically.

THEOREM.

First draw the Chord of the Arch-Line, as AB , which divide in half at C ; from which Point, raise the Perpendicular, or Versed Sine CD , which shall divide the Arch ADB , into two equal parts at D ; then from D to A , draw the half Chord AD of its Segment; as likewise from D , to B .



EXAMPLE.

Then upon a Scale of equal parts, take off the Length of the half Chord of the Arch AD , or BD , which let be 6; then take off the whole Chord-Line AB , which let be 9; then from eight times AD , or BD , the Chord of the half Segment; subduct AB , the Chord of the whole Segment, and divide the Remainder by 5, the Quotient is the Length of the Arch-Line ADB , which is 13.

For finding it another way *Arithmetically*, you may consult *Prob. 24. of Babington's Geometry*.

PROBLEM XXIV.

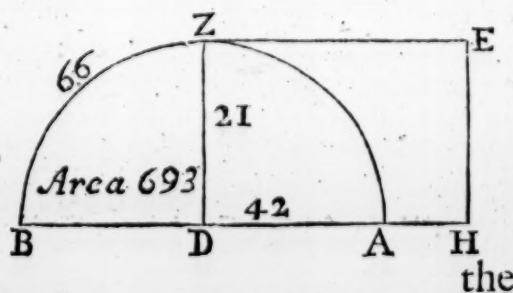
To Measure a Semicircle.

THEOREM.

Every Semicircle is near equal to that Long Square, whose length and breadth is equal to half the Arch-Line and the Semidiameter. Therefore Multiply half the Arch-Line by the Semidiameter, and the Product is the Area of the Semicircle.

EXAMPLE.

Suppose the half Circle AZB , is to be Measured, whose Arch-Line AZB , is found 66; now I Multiply the half thereof 33, by



the

the Semidiameter Z D 21, and it produceth 693 for the Area of the Semicircle, to which the Oblong Z E H D is near equal.

P R O B L E M XXV.

To Measure any Portion of a Circle.

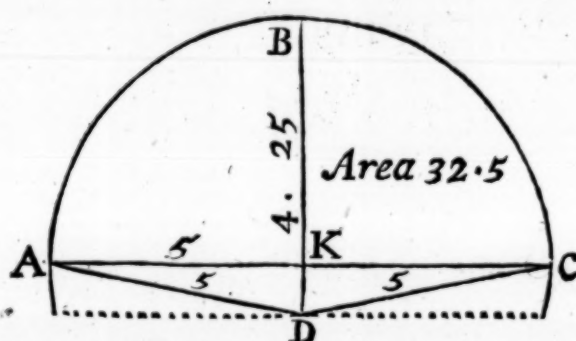
Note, That six sorts of Portions of Circles may be given to be Measured; the Reason whereof is grounded upon this Theorem following.

T H E O R E M.

Every portion of a Circle, which is contained under two Semidiameters, and one Arch-Line, is equal to that Long Square, whose length and breadth is equal to the Semidiameter, and one half of the Arch-Line.

Therefore in any such portion, first find out the Center of that Circle, whereof the Arch-Line is a part of the Periphery, by *Prob. 13. of Part I.*

Or else find the Diameter *Arithmetically* thus: Multiply half the Chord-Line, *viz.* A K 5 by it self, which makes 25; then divide that Product by 4.25, the Versed Sine K B, the Quotient whereof will be 5.882; then if you add 4.25 the Versed Sine to the Quotient 5.882, the Sum will be 10.132, for the Diameter of the Segment ABC; then Multiply half the Arch-Line by the Semidiameter, and the Product sheweth the Area.

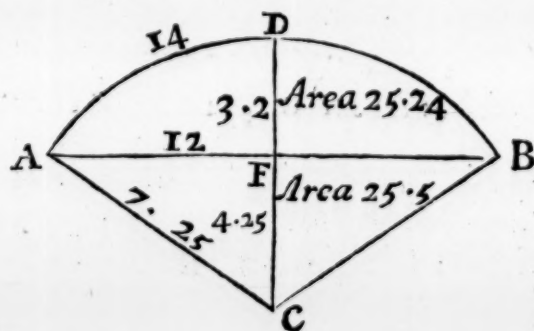


E X A M P L E of the First.

Let ABCD be a Portion, or Sector of a Circle to be measured, the Arch-Line ABC is found (by *Prob. 22. of this part*) 13; the half whereof being Multiplied by 5 the Semidiameter A D, or C D, produceth 32.5 for the Area of the Sector ABCD.

E X A M P L E of the Second.

Let A D B be the Segment of a Circle to be Measured: Now for that it is not at the first giving to be Measured, included with two Semidiameters, and an Arch-Line, you must therefore find the Center C, whereof the Arch-Line, or Segment A D B, is a part of the Periphery, by the last *Problem*; then draw the two Semidiameters



AC and BC; so shall you include the Triangle ABC, more than the Segment ADB: Now first Measure the whole Figure ACBD by the last *Proposition*; then Measure the *Isoceles* Triangle ACB, and from the Content of the whole Sector ACBD, subtract the Content of the Triangle ABC; and the Remainder is the Area of the Segment ADB.

The Operation.

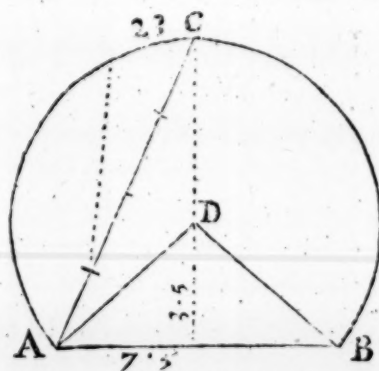
Take $\frac{1}{2}$ 14 the Arch-Line ADB	The Perpend. EC 4.25
7.25 the Semidiamet.	The Base AB 12
7 the $\frac{1}{2}$ of the Arch	
50.75 Area of the Sector	Take $\frac{1}{2}$ 51.00 Prod.
Substr. 25.5 Area of the Tria.	The $\frac{1}{2}$ of the Prod. 25.5 Is the
	Area of the Triangle ABC
Refts 25.25 the Area of the	required.
Segment ADB	

Otherwise, The Segment of a Circle may more readily be found very near the truth at once, without finding the Center of the Circle, or Content of the Sector as followeth.

By the last *Example*, draw the Chord-Line AB, and Measure the length thereof, which is 12; then Measure the Perpendicular DE, which is 3.2: Now if you Multiply the Perpendicular 3.2, by $\frac{2}{3}$ parts of the Chord-Line AB, which is 8; you shall have 25.6 for the Area of the Segment ADB, differing very little from the former.

E X A M P L E of the Third.

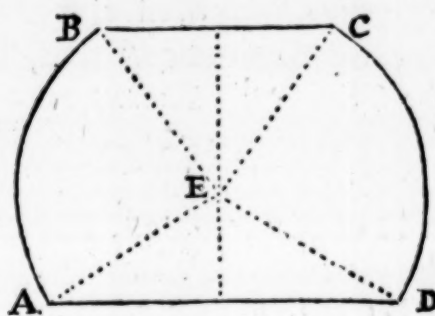
Let ABC be a portion of a Circle to be Measured: Now for that the whole consisteth of an Arch-Line, and a Chord-Line, therefore first find out the Center D; then draw the two Semidiameters AD, and BD, and find the Content of the Figure ABD and C, (omitting the Triangle ADB) by Multiplying $\frac{1}{2}$ of the Arch-Line ACB, which is 23, the $\frac{1}{2}$ of it is 11.5, which Multiplied by the Semidiameter 6.25, produceth 71.875, for the Area of ABD and C, to which the Content of the Triangle ABD being added, whose Area is 26.25, maketh in all 98.125, for the whole Area, or portion of the Circle ABC, as was required.



E X A M-

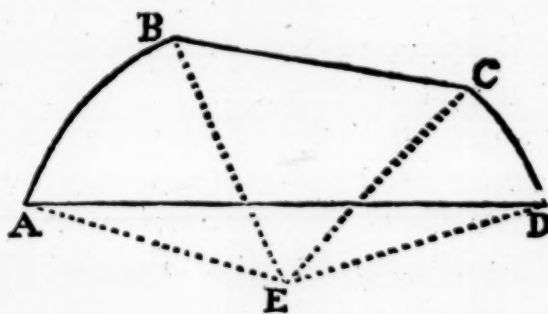
EXAMPLE of the Fourth.

Let $ABCD$ be a portion of a Circle to be Measured: Now for that the Perimeter thereof consisteth of two Arch-Lines, and two Chord-Lines, therefore first, the Center is to be found, which is E ; from which draw the four Semidiameters, as EB , EC , ED , & EA ; so shall you Reduce that Figure, or portion of a Circle, into the two Sectors ABE , and DCE , being both equal one to the other; therefore the one being Measured, *viz.* The Area thereof, is the Area also of the other; likewise it partakes of two Triangles, *viz.* BEC , and AED , which must both be Measured severally, because they are not equal; and these four Areas thus found, and added together, is the Area, or Content of the whole Figure $ABCD$; which was the thing required.



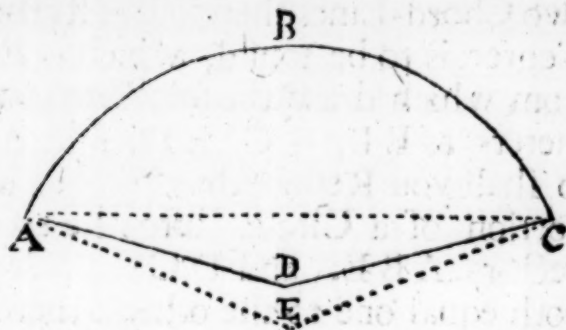
EXAMPLE of the Fifth.

Let $ABCD$ be a portion of a Circle to be Measured, being inclosed, in which are two Chord-Lines, and two Arch-Lines; but whereas in the last Example, the Center was within the Figure, and in this the Center is without; yet as in all the rest, so in this, the Center is first to be found, which let be E ; then draw the four Semidiameters, so shall you Reduce the Figure $ABCD$ and E , into three Figures, *viz.* two Sectors; namely, AEB , and ECD , as also the *Isoceles* Triangle $EB C$; all which are to be Measured, as hath been before taught; and from the Total Content of all the three, the Area or Content of the Triangle AED , is to be Subtracted, and the Remainder is the Area, or Content of the Figure $ABCD$, which was required.



EXAMPLE of the Sixth.

Let $ABCD$ be a Figure to be Measured: First, let the Center be found as before; then draw the Semidiameters AE and EC , so shall you include the Sector $ABCE$; that done, Measure the Content of the Con-
 tle, or Segment ABC , by the Second Example; to which Area, or Content, the Content of the Triangle ADC being added, maketh the Area of the whole Figure $ABCD$, as was required.

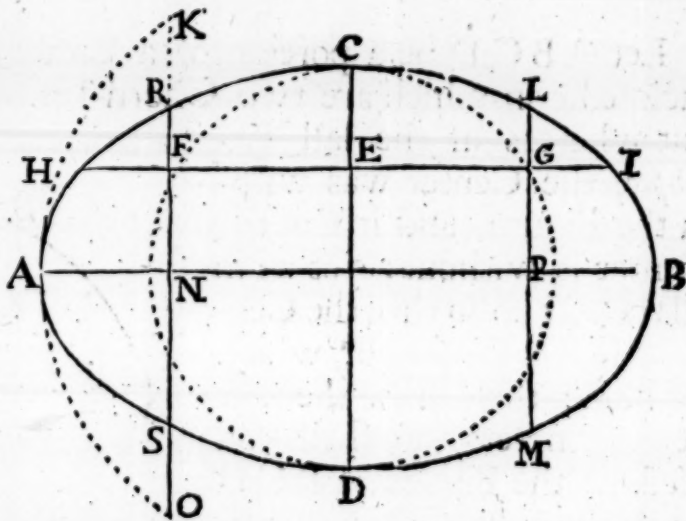


PROBLEM XXVI.

To Measure an Ellipsis, or Oval, and its Segments.

THEOREM.

For the Measuring of an *Ellipsis*, the best way is to Reduce it to a Circle, thus. Find a mean proportion between the greater and lesser Diameters of the *Ellipsis*, commonly called, the Transverse and Conjugate Diameters, and that mean proportion is the Diameter of a Circle, whose Area is equal to the Area of the *Ellipsis*; and how to Measure a Circle, is shewed in Problem 20, of this Part.



PROBLEM XXVII.

Given AB , and CD , the Diameters of an Ellipsis, and CE the Versed Sine; to find the Segment HCI .

THEOREM.

As $CD = NP$, the lesser Diameter, is to the Segment FCG ,
 So is AB , the greatest Diameter, to the Segment HCI .

$$\text{As } CD : FCG :: AB : HCI.$$

PRO-

PROBLEM XXVIII.

Given AB , and CD , the Diameters of an Ellipsis, and $AN=PB$, the Versed Sine, to find the Segment SAR .

THEOREM.

As AB , the Transverse Diameter, is to the Segment KAO , So is CD , the Conjugate Diameter to the Segment SAR .

As $AB : KAO :: CD : SAR$.

PROBLEM XXIX.

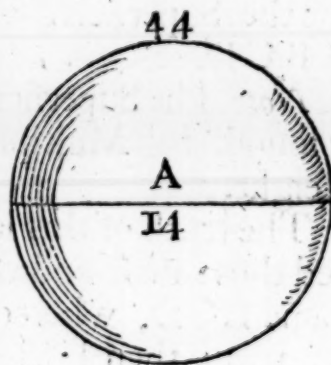
To Measure the Superficial Content of a Sphere, or Globe.

THEOREM.

Multiply the Diameter by the Circumference, the Product is the Superficial Content of the Globe, or Sphere.

EXAMPLE.

Admit A , be a Globe, or Sphere, whose Superficial Content, or Area of its Surface, is required; I Multiply the Circumference (which is gained by Problem 19.) or Periphery 44, by the Diameter 14, the Product is 616, for the Superficial Content of the Sphere required.



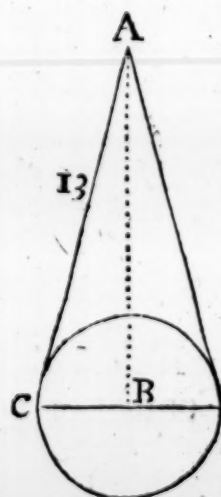
PROBLEM XXX.

How to Measure the Superficies of a Cone.

THEOREM.

Multiply the Slant height by half the Circumference at the Base, the Product is the Conical Surface; to which if you add the Area of the Circle underneath, you shall have the whole Surface Content.

Note, That the most exact way would be to find the Perpendicular's height AB , instead of the Slant height AC , and to Multiply it by half the Circumference as before; which Perpendicular may be found, making the Circumference the Base, and the Slant height the Sides of an Isosceles Triangle; then by Prob. 11. find the Perpendicular.



P R O B L E M XXXI.

How to Measure the Superficies of the Fruustum of a Cone.

T H E O R E M.

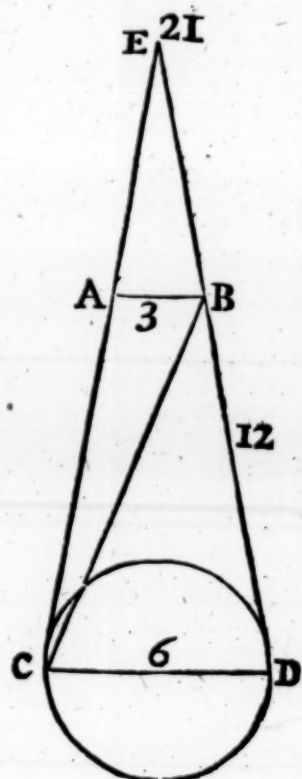
Add the greater and lesser Circumference of the Bases together, $\frac{1}{2}$ of the Sum is an *Arithmetical Mean*, which Reduces the Fruustum into a *Cylinder*; which half Sum, or Mean, Multiplied by its height, the Product is the Superficial Content of the Fruustum.

E X A M P L E.

Let ABCD be the Fruustum, or part of a Cone, whose Superficial Content is required, the Circumference of the greater and lesser Base being 6 and 3, which added is 9, the half is 4.5 for the *Arithmetical Mean*, for the Circumference of the Bases of a *Cylinder* at both ends; the which 4.5 Multiplied by 12, the height AC, the Product produces 54.0 for the Superficial Content of the Fruustum ABCD.

Note The Superficial Content of a *Cylinder* is found, by Multiplying the Girth by the Height.

The truth of this last *Problem* may be proved thus: First find the Length of the whole Cone ECD, whereof the Fruustum ABCD is a part; then having the whole height of the Cone, Measure first its Superficies by *Problem 30*; then Measure the Superficies of the top part, or lesser Cone, by the same *Problem*, and Subtract the Content of the lesser, from the Content of the greater Cone; and the Remainder shall be the Content of the Fruustum.



P R O B L E M XXXII.

To Measure the Superficies of any Angular Pyramid, with its Frustrums.

T H E O R E M.

If the Sides, or Angles at the Base be all equal Measure; the Content of one side by *Prob. 11*. then Multiply that Area by the Number of all its Sides, and the Product is the Area of the whole Pyramid. But if the Sides be unequal, Measure them severally as

as

as so many Triangles, and the Sum of their Contents is the Sum of the whole Pyramid.

But if you are to Measure the Fruustum of such a Pyramid, find an *Arithmetical* Mean, betwixt the broader and narrower end of one Side, or Square; and that Mean, Multiplied by its height, is the Content of one of the Sides, which being all equal, Multiply that Content by the Number of all the Sides, the Product is the Content of the whole Fruustum.

If the Sides be unequal, Measure them severally, and the Sum of all their Contents is the whole Area, or Content.

The End of the Second Part.

U

G E O.

GEOMETRY.

PART III.

CONTAINING

The Dividing (or Cutting off) both Right-Lined and Irregular Figures, into as many Parts, Equal or Unequal, as shall be required.

PROBLEM I.

To cut off from a Triangle any Parts, as $\frac{1}{2}$, $\frac{2}{3}$, $\frac{3}{4}$, &c. with a Line issuing from any Angle assigned.

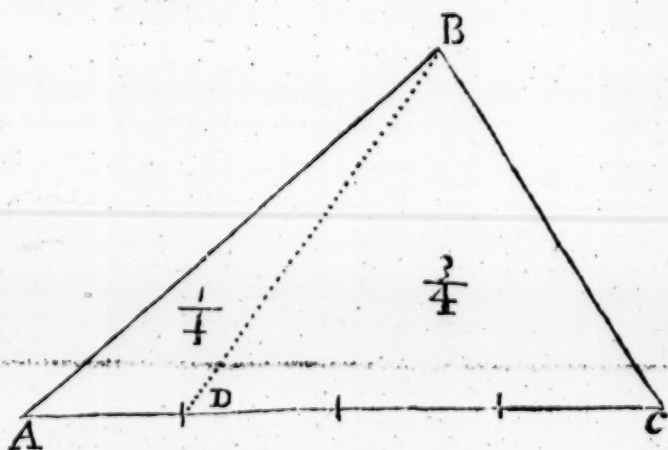
THEOREM.

Triangles, consisting of equal Bases, and in the same Parallel, are equal; Therefore take $\frac{1}{2}$, $\frac{2}{3}$, $\frac{3}{4}$, &c. of the Line opposite to the Angle; draw a Line, which shall include a Triangle to retain the Parts required.

EXAMPLE.

Admit ABC , to be a Triangle, whose $\frac{1}{4}$ part is required to be cut off, with a Line issuing from B , to cut the Line AC ; and that AB be one side of the new Triangle; Then let the $\frac{1}{4}$ part of the Line AC be taken, the which endeth in D , and let the

Line BD be drawn, which includeth the Triangle ABD , which is the $\frac{1}{4}$ part of the Triangle ABC ; and then consequently the Triangle BCD , is $\frac{3}{4}$ parts of the Triangle ABC , &c.



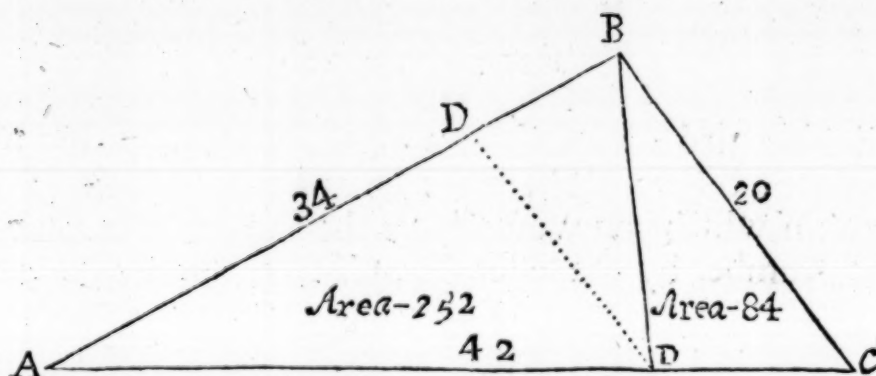
PRO-

PROBLEM II.

To cut off from a Triangle any number of Measures or Parts, as 4, 6, 8, 32, &c. with a Line issuing out of the Angle assigned.

THEOREM.

First, Measure the Area of the whole Triangle, then multiply the side opposite to the Angle assigned, by the parts to be cut off,



and divide the Product by the Area of the whole Triangle ; the Quotient sheweth how much you shall cut off, to make a new Triangle to retain the Parts required.

EXAMPLE.

Let ABC be a Triangle given, and let the Proposition be to cut off 84 parts, with a Line issuing from the Angle B, and falling on the Line AC, and making BC, one of the sides of the new Triangle ; first, the whole Content of the whole Triangle ABC, is found to be 336 : Having proceeded thus, let 84 be the Numerator, and 336 the Denominator, which being abbreviated thus, $3\frac{2}{3} \div 1\frac{4}{6} = \frac{2}{3}$, $\frac{1}{4}$ of the Content ; then proceed in all respects as you did in the last Problem ; and you shall find the Triangle BCD, to contain 84 parts of the Area of the Triangle ABC, which was required.

Arithmetically Performed.

First, The Content or Area of the Triangle ABC, being found to contain 336, and the Line AC is 42 ; then say by the Rule of Proportion, as the whole Area 336, is to 42 ; so is the lesser Area 84, to a fourth Number, which is found $10\frac{1}{2}$ in the same Parallel ; which set from C towards A, which falleth in D : Then draw the Line BD, which Triangle BCD, contain 84 parts, the thing required.

EXAMPLE II.

The foregoing Problem performed Geometrically.

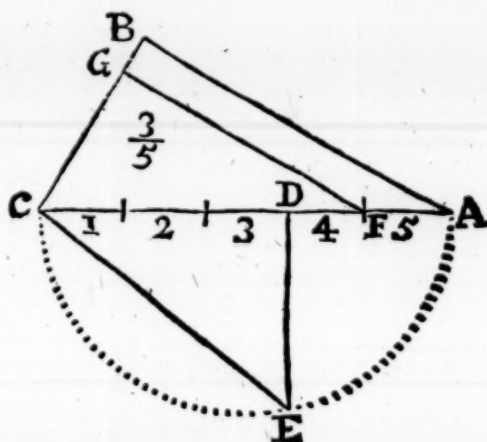
Admit ABC , in the foregoing Problem, to be a Triangle, from whence $\frac{1}{4}$ parts is to be cut off by a Line parallel to AC , in the same Order; first then, on the Line BC , describe a Semi-Circle, which Line BC divide into 4 equal parts: Note where 3 of them do end, in f ; on which point raise the Perpendicular fG , and from that point G , draw the Line GB , which set from B , towards C , which terminates in d , by which point draw a Line parallel to AC , as dE ; so is dEB , $\frac{1}{4}$ of the Triangle ABC required.

Note; After this manner you may reduce any Plot into any Proportion, either greater or lesser, as shall be required.

EXAMPLE III.

A Third Example of the former Problem, as followeth.

Admit ABC be a Triangle given, and it is required to cut off $\frac{3}{5}$, by a Line parallel to AB : First, on the Line AC describe, the Semi-Circle AEC ; then divide the Line CA , into 5 equal parts, and upon 3 of those parts erect the Perpendicular DE , which cutteth the Arch-Line in E ; then set the Line CE , from C to F ; and from thence draw the Line FG , parallel to AB ; so will the Triangle CGF contain $\frac{3}{5}$ of the Triangle ABC , as was before required.



PROBLEM IV.

To cut off any number of Parts, as 20, 40, 60, &c. in a Triangle, proportional to the Triangle given, with a Line parallel to any Side appointed.

THEOREM.

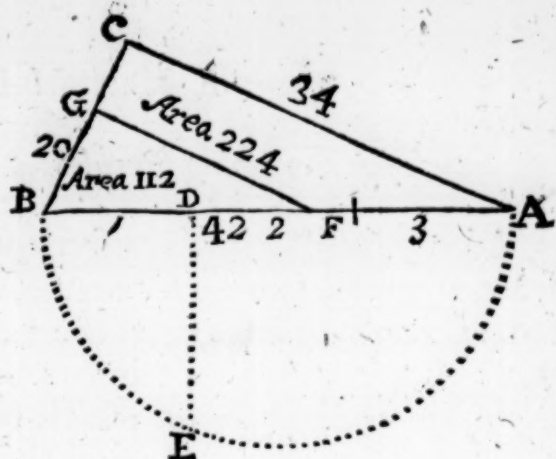
First, Measure the whole Triangle, then square any of the Sides, in which you would have the Parallel to cut; that Square Number multiply by the parts given to be cut off, and divide the Product by the Area of the whole Figure, out of which Quotient extract the Square-Root; and it sheweth how much you shall take

X

take of that Side the Triangle, to make a New Triangle; with which Measure found, work as in the last Proposition, by the first Example.

EXAMPLE.

Let ABC be a Triangle, from which 112 is to be cut off, with a Line parallel to the Line CA ; The Triangle being measured, and found to be 336, then put 112 over it, for the Numerator; and 336 under it, for the Denominator; and by abbreviating it you shall find the same to be $\frac{1}{3}$: then having described the Semi-Circle on the Line AB , divide the Line AB into 3 equal parts, and from one of them erect the Perpendicular DE ; then take the Distance from B to E , and set the same from B , towards A , which endeth in F ; by which point draw a Line parallel to AC : So the Triangle BGF doth contain 112, as was required.



Arithmetically Performed.

First, Square the Side BC 20, which makes 400; then say, as 336 is to 400, the Square of that Side, so is 112 to $133\frac{1}{3}$, whose Square-Root is $11\frac{1}{3}$, near rational; which is the Distance from B to G ; so if you draw from that point at G , a Line parallel to AC , you have the Triangle BFG , which containeth 112, as before.

PROBLEM V.

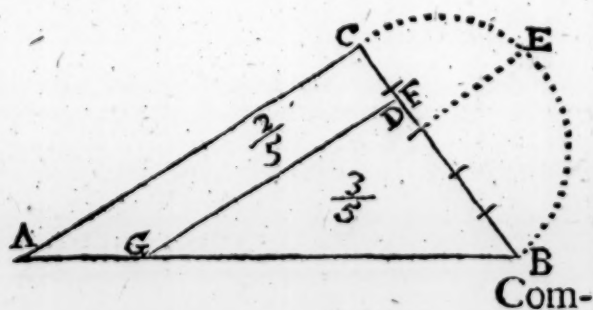
From a Triangle given, to lay the Parts cut off in a Trapezium; if there be a Proportion given between the Parts cut off, and the whole Figure.

THEOREM.

Subtract the lesser from the greater, then with the Remainder work as before is taught.

EXAMPLE.

Let the Triangle ABC be given, from whence $\frac{2}{3}$ is to be cut off in a Trapezium: First then, on the Line CB describe a Semi-Circle; then divide CB into 5 equal parts, and of 3 of them from B , erect the Perpendicular DE ; then, setting one Foot of your



Compasses in B, extend the other to E, which Distance set off from B towards C, which endeth in F; by which point draw a Line parallel to AC: So I include the Triangle GFB, to contain $\frac{2}{3}$ of the whole; and consequently the Trapezium ACFG, doth contain $\frac{1}{3}$ of the same, as was required.

Arithmetically Performed.

First, Take $\frac{1}{3}$ from the whole, the remainder will be $\frac{2}{3}$; then by the last Problem make the Triangle GFB to contain $\frac{2}{3}$, and then it will follow, that the Trapezium ACFG must contain $\frac{1}{3}$ of the whole Triangle, which was required.

PROBLEM VI.

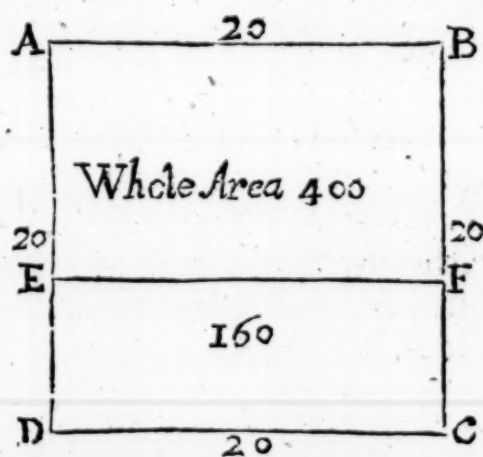
To cut off from a Square any Parts appointed in a Parallelogram.

THEOREM.

Divide the Parts to be cut off, by the side of the Square; the Quotient sheweth how much of the side you shall take, from the side of the Square for the Breadth of the Parallelogram; at which distance draw a Parallel Line; which shall include the Parallelogram required.

EXAMPLE I.

Admit ABCD to be a Square given, whose side is 20; from whence 160 parts is to be cut off with a Line Parallel to CD, so that CD makes one side of the Parallelogram; then work as is before taught, and draw the Line EF; which includeth the Parallelogram CDEF, and Contains 160, the parts required.

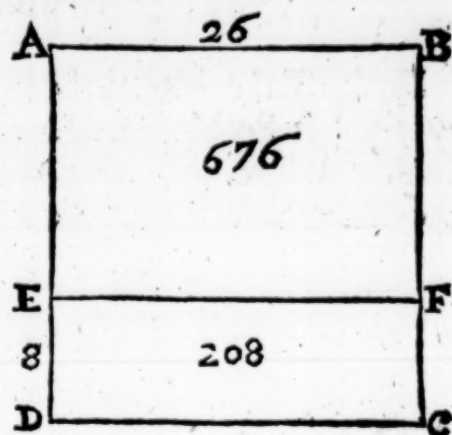


Note; And if you would have cut off $\frac{2}{3}$ $\frac{1}{3}$, &c. then you should have divided the Square side to be cut off into these proportional parts, and so by those parts draw a Parallel Line which would have included a Parallelogram to have contained the parts proportionable.

Another Example of this kind.

E X A M P L E. II.

Let the Square given be A B C D, containing 676 parts, and it is required to cut off 208 parts with a Line Parallel to C D, to be laid out next unto the same; first divide 208, by the side of the Square 26, and the Quotient is 8, which distance set from C to F, and from D to E; then draw the Line E F, which shall include the long Square or Parallelogram C D E F, to contain 208 parts, which is the thing inquired after.

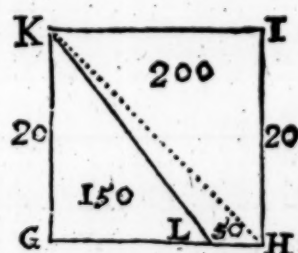
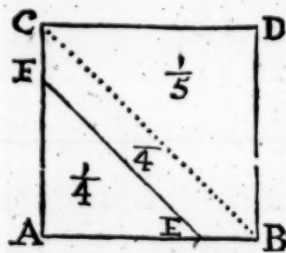


P R O B L E M VII.

To cut off from a Square any Parts assigned, and to make those Parts into a Triangle; wherein you must Note, that the Parts so cut off may not exceed $\frac{1}{2}$ of the Square, if they do, the Remainder will then be a Triangle.

T H E O R E M.

To work this, draw a Diagonal-Line to the Square; that being done, the Square is reduced into two Right-Angled Triangles; then may you from either of the Triangles which is assigned, cut off any Number of Parts therein, by the Rules concerning Triangles beforegoing; either by a Line issuing out of an Angle, or with a Line parallel to any one of the Sides.



E X A M P L E.

From the Square A B C D, let there be cut $\frac{1}{4}$ of the Area, with a Line parallel to the Diagonal B C; then Note, $\frac{1}{4}$ of the Whole, is $\frac{1}{2}$ of the Half; therefore the Proportion standeth thus: From the Triangle A B C, let there be cut $\frac{1}{2}$, with a Line parallel to B C, which is found by the third *Problem* of this Part; which will be the Triangle A E F, which is $\frac{1}{4}$ of the Square A B C D, the thing required.

E X A M-

EXAMPLE II.

Again; the Square $GHIK$, being found to be 400; I desire to cut off 150 parts, with a Line issuing out of the Angle K , and falling on GH , which is performed by the foregoing Directions, as in the Figure.

Note ; But if you were to cut any parts from a Square greater than the half, and to lay those Parts in a Trapezium ; you must substract the Parts to be cut off, from the Content of the whole Square, and cut off the Remainder in a Triangle, as before directed : So shall the Trapezium remaining contain the Parts required to be cut off.

PROBLEM VIII.

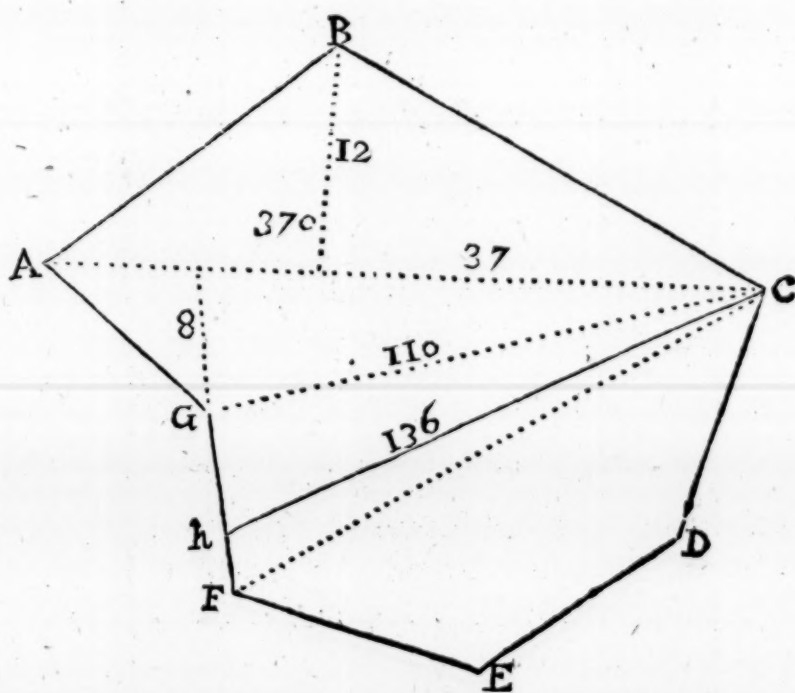
From an irregular Figure to cut off any Parts required.

THEOREM.

Measure so many Triangles lying next to the Side assigned, till you have something too much; then by the *first* and *second Problem* of this Part, cut off the Overplus from the last Triangle; So shall you have a Figure to contain the Parts required.

E X A M P L E.

Admit $ABCDEFG$ to be a Plot, from whence 480 parts are to be cut off, with a Line issuing from C , and to lie towards the Side AB : First, let the Trapezium $ABCG$, be measured,



whose Area is 370, which added to 136, the Area of the Triangle CFG , maketh 506, which is too much by 26, which 26 let be cut off from the Triangle CFG , by the Line Ch ; so doth the

the Figure $ABCbG$, contain 480, the Parts required to be cut off.

Note; This *Problem* is very material in the Practice of Surveying, in dividing and laying-out Grounds, whether into Parts equal or unequal; which every Surveyor ought well to acquaint himself with.

For the better understanding this Point, we will suppose a Point given in the Perimeter of the Plot, from which the said Plot is to be divided into as many equal parts as shall be required; First, Measure the Area of the whole Plot, then divide that Content by the Number of Parts, and the Quotient sheweth how many Measures each part shall contain; then cut off each part severally, as you are taught in the preceding Work.

PROBLEM IX.

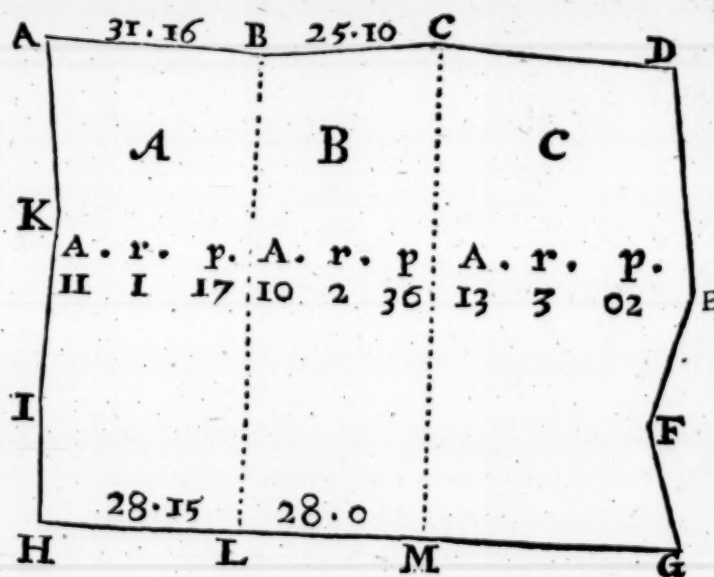
To divide a Common Field or Pasture, into as many Parts as shall be required; either according to the Number of Bease-Commons each Man possesseth, or according to each Person's Proportion of Rent.

EXAMPLE I.

Let this Figure noted with the Letters $ABCDEFGHIK$, be a Common Field or Pasture, in the Use and Occupation of 3 Men, viz. $A.B.C.$ and it is mutually agreed by them all, that each Man shall have his proportion of Ground laid out, according to his Quantity of Common in the same place.

First, Measure the whole Field, and it will be found to contain 35 a. 3 r. 15 p. or 5735 Perches; then consider how many Bease-Gates there are in the Pasture, and divide the Quantity of the Field accordingly by the *Rule of Proportion*,

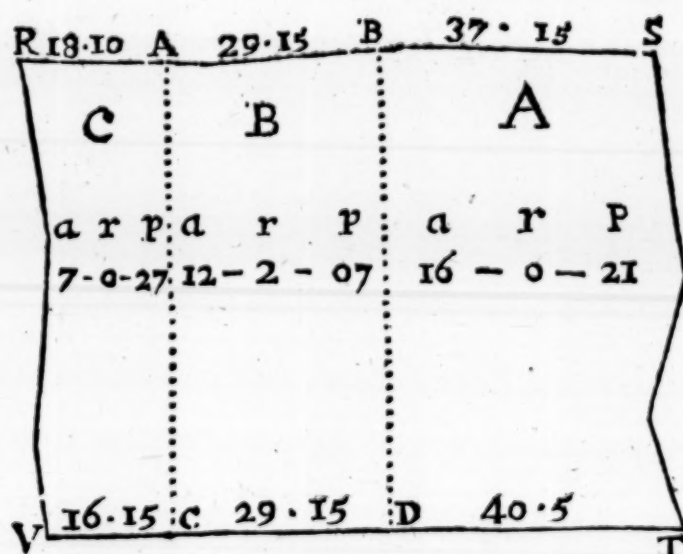
thus; saying, If the whole Number of Bease-Gates of $A.$ $B.$ and $C.$ give or belong to the whole Quantity of Perches in the Field 5735, what shall the Number of them belonging to $A.$ be? and the Answer will be his Part; and so work severally for each Man's Part: but we may suppose them thus; to $A.$ 1817 Perches, or 11 a. 1 r. 17 p. to $B.$ 1716 Perches, or 10 a. 2 r. 36 p. and to $C.$ 2202 Perches, or 13 a. 3 r. 02 p. Then to lay out every Man's Plot, I divide the Figure by the Direction aforegoing, by the Lines BL and CM , which to lay out upon the Ground, take from



from your Scale the Distance on the Plot, between the Net-Angle and that beginning of your first Line, as H L 28.15, then measure out the Distance on the Ground from the Angle H to L, also from the Angle A, measure upon the Ground 31.16 to B, then draw the Line B L, and make Dots or Marks; again, take from your Scale the Quantity of L M, 28.00, which measure on the Ground from L to M, and there set a Mark; and in like manner measure from B to C upon the Ground, 25.10, equal to B C upon the Plot, drawing the Line C M: So is your Plot divided according to every Man's just Quantity and Proportion, according to the Number of Bease-Gates.

EXAMPLE II.

But suppose it were required to divide this Field between 3 Persons, viz. A. B. and C. according to each Man's proportion of Rent: As suppose the whole Ground to be 20 pounds a Year; whereof A. pays 9 l. B. 7 l. and C. 4 l. the Question is, how many Acres, Roods, Perches belong to each Man, according to his Proportion of Rent? which by the Rule of Three argue thus; (first for A.) if 20 l. the whole Rent, give 5735 Perches (being the Content of the whole Field in Perches) what will 9 l. give? viz. 2581 Perches, or 16 a. or. 21 p. being the proportion



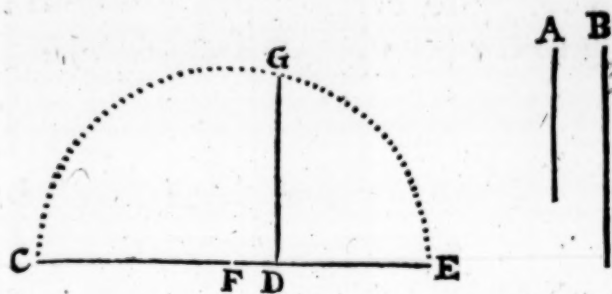
of Ground belonging to A. for his 9 l. Rent: In like manner, B. will have 12 a. 2 r. 07 p. being his quantity of Ground proportionably for his Rent of 7 l. and C. for his 4 l. Rent will have 7 a. or. 27 p. Then to lay out these parts upon the Ground, observe the Directions in the former Example, and as 'tis here explained by this Figure R A B S T V; Thus, 'tis easie to perceive how any thing in this kind may be effected.

P R O B L E M X.

To find a mean Proportion between any two Lines prescribed.

T H E O R E M.

Let A, B, the two Lines given, be so joined together, that they make both one straight Line, which let be the Line CDE; then divide the Line CE, into two equal parts, in the point F, and describe the Arch CGE, and raise the Perpendicular on the point D, where the two Lines are joined, till it come and join with the Arch in the point G; which done, you have the Line DG, which is a Mean Proportion between the Lines A and B required.



The End of the Third Part.

G E O-

GEOMETRY.

PART IV.

BEING

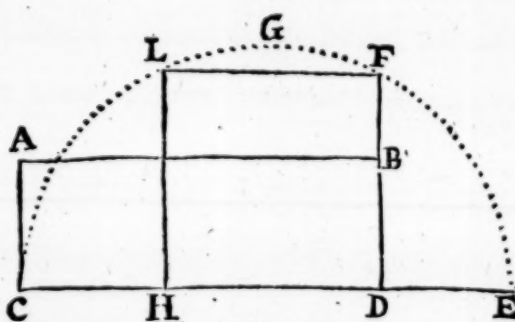
The Reduction of one Figure into another, keeping still the same Proportion.

PROBLEM I.

To Reduce a Long-Square into a Geometrical-Square, keeping the same Area or Proportion.

EXAMPLE.

LET the Long-Square $ABDC$, be given to be reduced into a Geometrical Square; First, therefore I add the Breadth to the Length, extending the Line to E , then describing the Arch CGE , erect the perpendicular at the joining of the Lines at D , which extended to the Circumference, cutteth the Arch in F ; So is the Perpendicular DF , the side of the Geometrical-Square $FDHL$; containing the Area of the long-Square $ABDC$, as was required.



Arithmetically Performed.

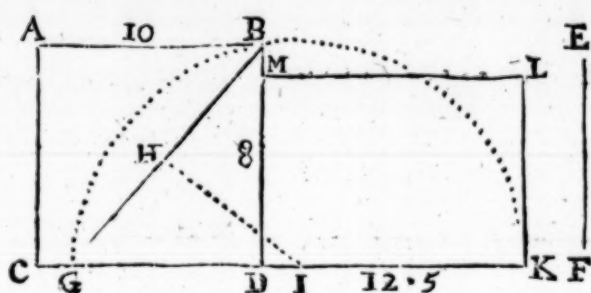
Multiply the Length by the Breadth of the long-Square, the Square-Root of that Product, is the side of the Geometrical-Square.

P R O B L E M II.

To Reduce a Geometrical-Square into a Long-Square, whose Breadth is limited by a Right Line given.

E X A M P L E.

Suppose $ABCD$ to be a Geometrical-Square, given to be reduc'd into a Long-Square, whose Breadth shall be equal to the Line EF : First, enlarge the side of the Square CD towards K ; then setting down the Breadth from D to G , draw the Line GB , which divide into 2 equal parts in the point H , and on that point erect the Perpendicular, extending it till it cut the Line CK , in the point I ; upon which describe the Arch GBK , and from D to K is the Length of the Long-Square, whose Breadth is equal to the Line EF : And so have you the Long-Square $KLM D$, equal to the Geometrical-Square $ABDC$, which was required to be done.



Arithmetically Performed.

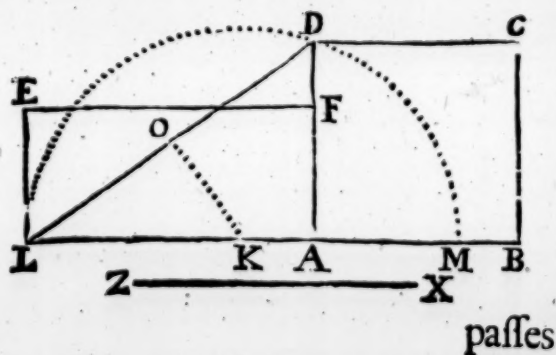
Square the Side AB , which is 10, which makes 100, and divide the Product by the Side $DM = KL$, the Breadth of the Long-Square 8, the Quotient is 12.5, for the Length of the Long-Square; whose Breadth 8, multiplied by 12.5 produceth 100, which is equal to the Geometrical-Square $ABDC$, required.

P R O B L E M III.

To Reduce a Geometrical-Square into a Long-Square, whose Length is limited by a Line given.

E X A M P L E.

Let $ABCD$, be a Geometrical-Square given, to be reduced into a Long-Square, whose Length shall be equal to the Line ZX : First, continue the Line AB towards L , and set the Line ZX from A to L , drawing the Line DL , on the middle whereof erect the perpendicular OK , cutting the Ground-Line in K ; where setting one Foot of the Com-



passes

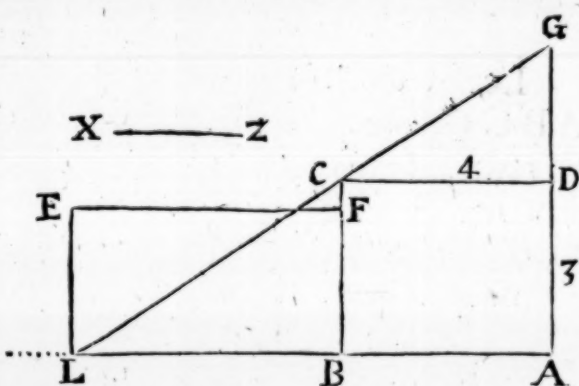
passes, extend the other to L, and describe the Semicircle LDM, which cuts the Line LB in M; so will AM be the breadth of the Long-Square sought; of which Breadth, and the given Length, make the Long-Square AFEL; which is equal in Area to the Geometrical-Square ABCD.

PROBLEM IV.

To Reduce one Long-Square into another Long-Square, whose Breadth is limited by a Line given.

EXAMPLE.

Let the Long-Square ABCD, be given to be reduced into another Long-Square, whose Breadth shall be equal to the Line XZ: First, Continue the Line AB towards L, and the Line AD towards G; then set the Line XZ from D to G, and draw out the Line GC, to cut the Ground-line AB, in L: So shall BL be the Length of the Long-Square; with which Length and the given Breadth XZ, make the Long-Square EFL, which shall be equal to the Long-Square ABCD given, which was required.



PROBLEM V.

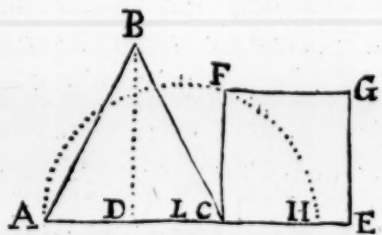
To Reduce a Triangle into a Geometrical-Square.

THEOREM.

In the given Triangle find the Mean Proportion between half the Perpendicular and the Base, and it gives you the Side of the Geometrical-Square, by Problem X. of Part III.

EXAMPLE.

In the Triangle ABC, the Perpendicular is BD, whose half set from C towards E, which endeth in H; then take the midft of AH, which is L, on which describe the Semicircle AFH; then raising the Perpendicular from the point C, observe where it intersects the Arch, which is in F: So that CF is the Side of the Geometrical-Square, containing the Triangle ABC.



Arithmetically Reduced.

Multiply the Perpendicular into half the Base, and from that Sum extract the Square-Root, which shall be the Side of the Square required.

Z 2

PRO-

P R O B L E M VI.

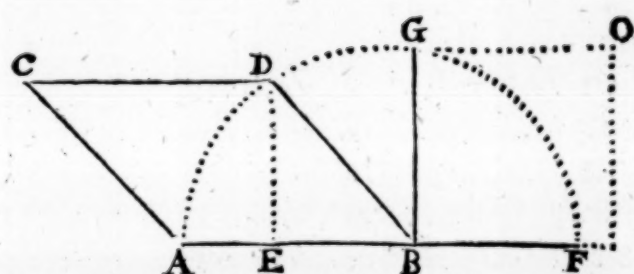
To Reduce a Rhombus into a Geometrical-Square.

T H E O R E M.

Open your Compasses of any one sides length, and to it add the Perpendicular; the Mean proportion between the Perpendicular and the side, is the side of the Geometrical-Square, equal to the Rhombus.

E X A M P L E.

Let the Rhombus ABCD, be given to be reduced into a Geometrical-Square; first, to the side AB, add the perpendicular DE, which makes the Line



AF; then on the point of their joining B, Erect the perpendicular BG; which is the mean proportion between the Base, and the perpendicular; and is the side of a Geometrical-Square, containing the Rhombus; which was required.

Arithmetically Reduced.

Multiply the side of the Rhombus by the perpendicular, the Square-Root of that Product, is the side of the Geometrical-Square required.

P R O B L E M VII.

To Reduce any Regular Polygon into a Geometrical-Square.

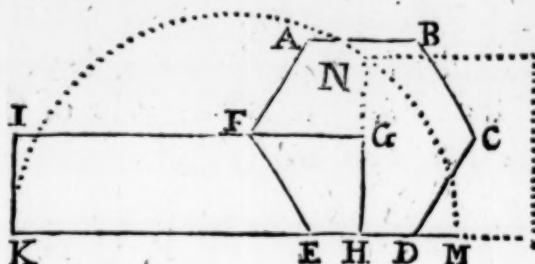
T H E O R E M.

To Reduce any Regular Polygon into a Geometrical Square, there is one General Rule, which is this: Find a mean proportion, between the Semi-perimeter and the Perpendicular; and that is the side of a Geometrical-Square, containing the said Polygon.

E X A M.

EXAMPLE.

Let there be given the *Hexagon* ABCDEF: First, lay down the Semi-periphery, and to that add the Perpendicular GH, which makes the Line KM; so that I make that, the Diameter of the Semicircle KAM: Then raise the Perpendicular from H to N; so that HN is the Side of the Geometrical-Square required.



Note; In all Regular Polygons the Long-Square made of the Semi-periphery and the Perpendicular, is equal to the said Polygon, as appears by the foregoing Figure.

Arithmetically Reduced.

Multiply the Perpendicular into the Semi-perimeter, the Square-Root of that Product is the Side of the Geometrical-Square.

PROBLEM VIII.

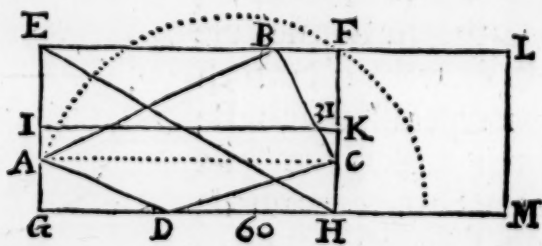
To Reduce a Trapezium into a Geometrical-Square, Parallelogram, or Right-Angled Triangle.

THEOREM.

If in a Trapezium a Line be drawn from any one Angle, and by that a Parallelogram be made, comprehending the Trapezium, and parallel to the Line so drawn; then half that Parallelogram is equal to the Trapezium; so that finding a Mean Proportion between the two Sides of the Long-Square, you shall have the Side of a Geometrical-Square required.

EXAMPLE.

Let there be a Trapezium given, as ABCD; first, draw the Line AC, then by the Angles B, D, draw two Lines parallel to AC, and from the extreme parts of one to the other, draw the Lines FH, and EG; so have you a Parallelogram double to the Trapezium; which if you cut in the half by the Line IK, you have the Parallelograms equal; so that finding a Mean Proportion between the two Sides thereof, you have the Side HF, which is the Side of the Geometrical-Square required.



A a

So

So $IKHG$, or $EFKI$, are the Parallelograms; EGH , or EFH , the Right-Angled Triangle, and $FHML$ the Geometrical-Square, equal to the Trapezium $ABCD$.

Arithmetically Performed.

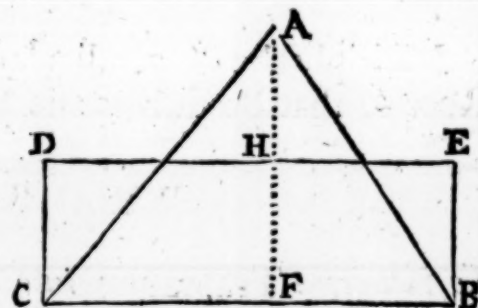
Multiply half GH 60, by FH , or EG 31, the Square-Root of that Product is the Side of the Geometrical-Square, equal to the Trapezium.

PROBLEM IX.

To Reduce a Triangle into a Parallelogram.

EXAMPLE.

Let ABC be a Triangle given to be reduced into a Long-Square: First, Draw the Perpendicular AF , which divide into 2 parts equally, as at H ; take one half thereof, HF , for the Breadth, and the whole Base BC , for the Length of the Parallelogram $DEBC$, which is equal to the Triangle ABC , required.

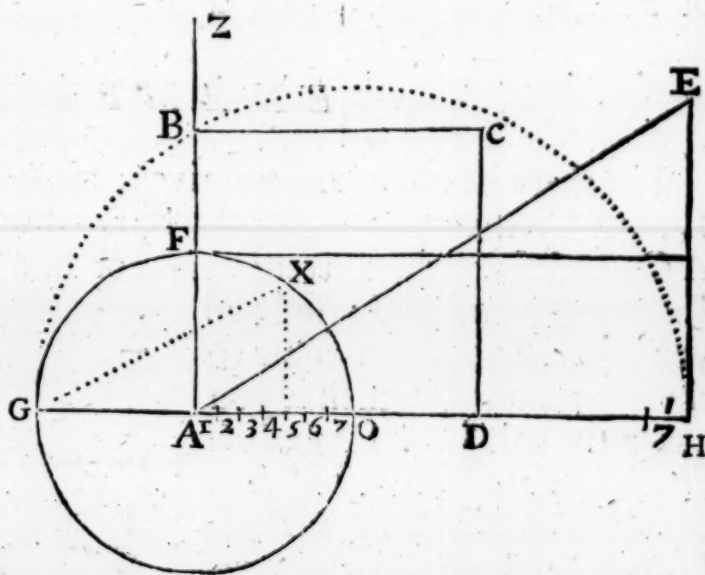


PROBLEM X.

To Reduce a Circle into a Geometrical-Square.

EXAMPLE.

Let A be the Circle given to be reduced into a Square; continue the Diameter GA towards H ; then on the Center A , erect the Perpendicular AZ ; then set three times the Semidiameter of the Circle, and $\frac{1}{7}$ part thereof, from A to H , and on the Line GH , describe the Semicircle GBH , which cutteth the Perpendicular in B ; hence AB is the Side of the Square requir'd; therefore the Square $ABCD$ is equal to the Circle A .



Arithme-

Arithmetically Reduced.

Note; That the Square-Root of the Area of any Circle is the Side of a Square equal to the Circle.

P R O B L E M XI.

To Reduce a Circle into a Right-Angled Triangle.

E X A M P L E.

Again; The Circle may be reduced into a Right-Angled Triangle; for by the XX. *Problem* of the *second* Part, every Circle is equal to that Right-Angled Triangle, of whose containing Sides, the one is equal to half the Periphery, and the other to the Diameter; and seeing now the Line AH is equal to half the Circumference, and the Line HE is equal to the Diameter of the Circle GO; therefore the Right-Angled Triangle AHE, is equal to the Circle A required.

P R O B L E M XII.

To Reduce a Triangle or a Circle, into a Long-Square.

E X A M P L E.

According to *Problem* XIV. of *Part* II. every Triangle is half that Long-Square, whose Length and Breadth is equal to the Perpendicular, and the Side cut thereby; therefore let the Triangle given, be AHE, in the former Diagram, and it is required to reduce the same into a Long-Square; Take half the length of the Side of the Triangle HE, and divide the same into two equal parts at K; then is HK equal to AF, the Breadth of the Long-Square AFKH, equal to the Triangle AHE, or to the Circle A: For the Side AH, is equal to half the Circumference, and the Breadth AF, to the Semidiameter.

P R O B L E M XIII.

To Reduce a Circle into a Square.

T H E O R E M.

Having laid down a Square, to be reduced into a Circle; Take any side of it, and divide it into 11 equal parts, describing a Semicircle to it; then on 8 of those parts erect the Perpendicular, which extend to the Circumference of the Semicircle; then draw a Line from the extreme parts of the Diameter, intersecting the Perpendicular in the Circumference of the Circle,

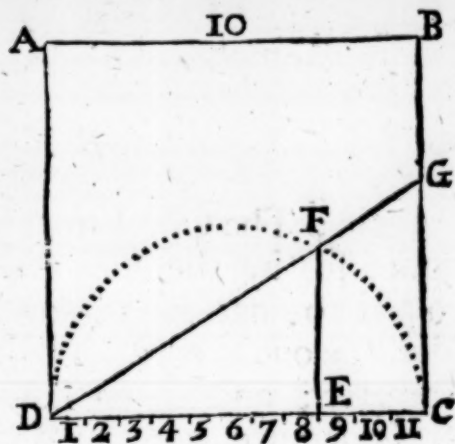
A a 2

and

and continue that Line till it touch the side of the Square; so will that Line be the Diameter of a Circle, answerable to the Area of the Square.

E X A M P L E.

Let the Square $A B C D$ be given, making $C D$ the Diameter; then describe the Semicircle $C F D$; and having divided the Diameter into 11 equal parts, at the 8th part erect a Perpendicular $E F$: Then draw a Line from the extreme parts of the Diameter, which intersecteth with the Perpendicular in the Circumference at F ; which being continued, gives the Line $D G$, the Diameter of a Circle, equal to the Square.



Arithmetically Reduced.

As 11 to the Square given; so is 14 to a fourth Number, the Square-Root whereof is the Diameter of the Circle (equal to the given Square) required.

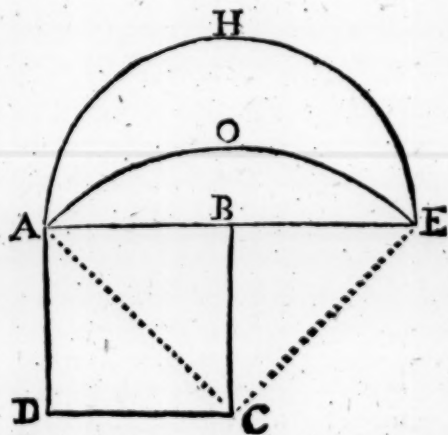
P R O B L E M XIV.

To Reduce a Square into a Lunular Form, and the contrary.

E X A M P L E.

Let $A B C D$ be a Square, given to be reduced into a *Lunula*; First, draw the Diagonal $A C$, and on the end thereof, at C , raise the Perpendicular $C E$, equal to $C A$; then continue the side $A B$ to E , and on the point B , with the Distance $B A$, or $B E$, describe the Semicircle $A H E$; and also on the point C , with the Distance $C A$, equal to $C E$, describe the Arch-line $A O E$, which two Lines will include the *Lunula* $A O E H$, equal to the given Square $A B C D$, as was required.

Again; Let the *Lunula* $A O E H$, be given to be reduced into a Square; First, draw the Line $A E$; then on the one half thereof, $A B$, or $B E$, make the Square $A B C D$, which will be equal to the *Lunula* $A H O E$, as was required.

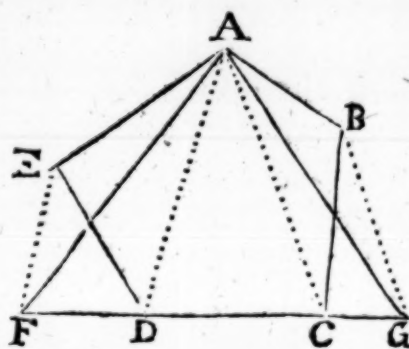


PROBLEM XV.

To Reduce an Irregular Figure into a Triangle.

EXAMPLE.

Let $ABCDE$ be the Figure of some Irregular Field, and it is required, from the Angle A , to reduce the same into a Triangle: First, continue the Side DC of convenient Length both ways, towards F and G ; then draw the Line EF , parallel to AD , till it intersect the extended Line CD in F , likewise draw the Line BG , parallel to AC , cutting the extended Line in G ; then from the Angle A , draw the Lines AF , and AG : So shall you have the Triangle AFG , equal to the irregular Pentagon, $ABCDE$, which was required.

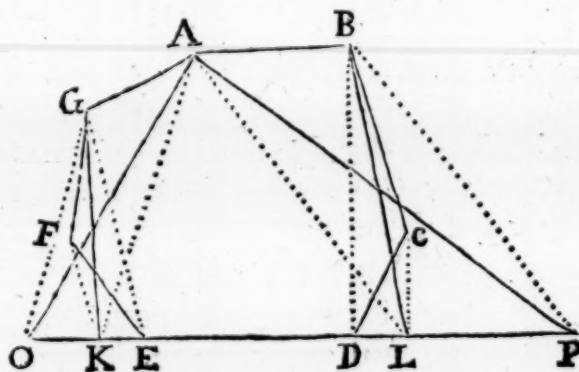


PROBLEM XVI.

To Reduce any Irregular-Multangled Figure into a Triangle.

EXAMPLE.

Suppose $ABCDEFG$, be an Irregular Figure or Plot, given to be reduced into a Triangle; first, draw the Line GE , and parallel thereto the Line FK ; then from G , draw the Line GK ; next, from B draw the Line BD , and parallel thereto the Line CL ; then from B , extend the Line to L ; so is the Plot of seven sides reduced to five, namely, to the Figure $ABLK G$. Secondly, according to the last Problem, extend the Side KL , towards O and P ; then draw the Line GO , parallel to AK , till it cross the Line KL in O ; also draw BP , parallel to the Line AL , till it cross the extended Side KL in P :



Lastly,

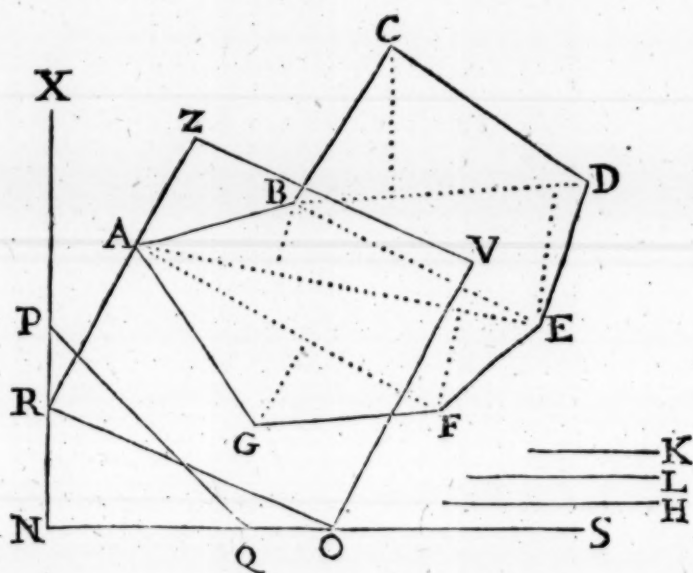
Laftly, draw the Lines A O and A P; fo fhall you include the Triangle A O P, equal to the Irregular Heptagon A B C D E F G, as was required.

P R O B L E M XVII.

To Reduce any Irregular Plot into a Geometrical- Square.

E X A M P L E.

Let A B C D E F G, be an Irregular Figure, given to be reduced into a Square; firft, draw the Lines B E and A F; fo will the Figure be divided into two Trapezia's, and one Triangle; then crofs the Trapezia's with the two Diagonals B D, and A E, and let fall the Perpendiculars from the Angles thereon, as from C, E, B, and F; and alfo from G, to the Base of the Triangle: Then, as is fhewed in *Problem X. of Part III.* find a Mean-proportional Line, between half the Base B D, and the two Perpendiculars falling thereon, which is equal to the Line H:



In like manner, find a Mean-proportional Line between half the Base A E, and the two Perpendiculars thereon falling, which will in this Example be equal to the Line L; fo alfo find out a Mean-proportional between half the Base of the Triangle A F, and its Perpendicular, which let be the Line K; which done, describe a Right Angle at pleasure, as X N S, wherein place the Line H, from N to P, and alfo the Line L, from N to Q, and draw the Line P Q; alfo place the Line K from N to R, then fetting the Line P Q, from N to O, draw the Line R O, which is the Side of the Square required; and confequently the Square R Z V O, will be equal to the aforegoing Irregular Figure A B C D E F G, as was required.

¶ I might have made a farther Progress in this part of Reduction ; but in respect, in the Practice of Surveying, all (or most) Plots are produced in an irregular Form, in which I have sufficiently supplied the Surveyor ; it is therefore needless to enlarge further. Likewise I might have added, how to have performed Geometrically, the Rules of Addition, Subtraction, Multiplication, and the Rule of Proportion ; but since they are not essential to the Practical Surveyor, I shall not burden the Book with them : Neither have I omitted to alter and add any thing in this Geometrical Performance, that may be any way truly subservient in the practical Part of Surveying : Those therefore that would be further inform'd in this Geometrical Science, let them consult *Euclid*, *Ramus*, *Pittiscus*, or *de Chales* ; which latter I chiefly recommend.

The End of the Fourth, and Last Part of Geometry.

T H E

T H E
Art of Surveying,
The T H I R D B O O K.
Containing the Dimensions of all
Right-Angled T R I A N G L E S,
With the C A N O N of
Artificial Sines and Tangents,
to every Tenth Minute of the
QUADRANT.

Together with
A TABLE of *Logarithms* to 10000.
Being of Singular Use in the Solution of
T R I A N G L E S.

As it was formerly Published by the Author
V I N C E N T W I N G, Math.

L O N D O N,
Printed for *Awnsham* and *John Churchill*, at the *Black-Swan*,
in *Pater-Noster-Row*, MDCXCIX.

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BOOK III.

Containing the Dimension of
all Right Lined Triangles.

BECAUSE the Triangle (in respect of its Admirable Use in the *Mathematicks*) may justly challenge the Superiority of all Geometrical Figures; by the help whereof there is not any Question, or Problem *Geometrical*, or *Astronomical*, but may thereby most exactly be resolved: It cannot therefore be unseasonable in this place, to insert all the Problems and Cases incident to Right-lined Triangles, and the rather, because the most of them are of extraordinary and common use for a Surveyor, in the taking of Heights and Distances, and in finding the Superficial Content, or Area of any Geometrical Figure, and more especially in the Dimension of all Regular Polygons, where their exact Superficial Capacities cannot otherwise be well obtained, as we shall have occasion afterwards to shew. And albeit I here intend not to speak of Spherical Triangles, as a thing without the Perimeter of an ordinary Surveyor's Use and Practice; yet I shall annex some Problems *Astronomical*, thereby performed, which will be necessary for him to understand; and for such as would be more fully satisfied in the Doctrine of *Trigonometry*, relating both to Right Lined Triangles and Spherical, I shall refer him to my *Astronomia Britannica*: But to my purpose:

S E C T. I.

Of the Dimension of Plain Rectangled Triangles.

P R O B L E M I.

The Angles and one Leg being given, to find the other Leg.

IN the Rectangled Triangle ABC, the Side CA is inquired from

The given $\begin{cases} \text{Leg AB } 1123.7943 \\ \text{Angle ABC } gr\ 28.19'.48'' \end{cases}$



Terms of Proportion.

$$R : t. B :: BA : CA.$$

Illustration by Numbers.

As the Radius 90 Degrees	10.00000
To the Tangent of the Angle ABC $gr\ 28.19'.48''$.	9.73168
So the Leg BA 1123.7943	3.05069
To the Leg CA 605.8601	2.78237

P R O B L E M II.

The Hypothenufe and Angles being given, to find either Leg.

In the Rectangled Triangle BAC, the Side AB is inquired from

The given $\begin{cases} \text{Hypothenufe BC } 1276.7067 \\ \text{Angle ACB } gr\ 61.40'.12'' \end{cases}$

Terms of Proportion.

$$R : s. ACB :: BC : BA$$

Illustra-

Illustration by Numbers.

Radius 90 Degrees	10.00000
Sine of the Angle A C B gr 61. 40'. 12".	9.94459
Hypothenuſe B C 1276.7067	3.10609
Leg A B 1123.7943	3.05068

P R O B L E M III.

The Angles and one Leg being given, to find the Hypothenuſe.

In the Rectangled Triangle A B C, the *Hypothenuſe* B C is inquired from

The given $\begin{cases} \text{Leg } B A & 1123.7943 \\ \text{Angle } B C A & \text{gr } 61. 40'. 12". \end{cases}$

Terms of Proportion.

$$s. A C B : R :: B A : B C.$$

Illustration by Numbers.

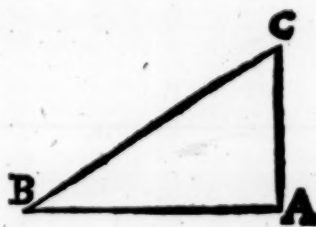
As the Sine of the Angle A C B gr 61. 40'. 12".	9.94459
To the Radius 90 Degrees	10.00000
So the given Leg A B 1123.7943.	3.05068
To the <i>Hypothenuſe</i> B C 1276.7067	3.10609

P R O B L E M IV.

The two Legs being given, to find either Angle.

In the Rectangled Triangle A B C, the Angle A B C is inquired from the

Legs given $\begin{cases} B A & 1123.7943 \\ C A & 605.8601 \end{cases}$



Terms of Proportion.

$$B A : C A :: R : t. A B C.$$

As the Leg B A 1123.7943	3.05068
To the Leg C A 605.8601	2.78237
So the Radius 90 Degrees	10.00000
To the Tangent of the Angle A B C gr 28. 19'. 48".	9.73169

P R O-

P R O B L E M V.

The Hypothenufe and a Leg being given, to find either Angle.

In the Rectangled Triangle B A C, the Angle A C B is inquired from

The given $\begin{cases} \text{Leg} & A B \ 1123.7943 \\ \text{Hypothenufe} & B C \ 1276.7067 \end{cases}$

Terms of Proportion.

$BC : BA :: R : s. A C B$

Illustration in Numbers.

As the Hypothenufe B C	1276.7067	3.10609
To the Leg B A	1123.7943	3.05068
So the Radius 90 Degrees		10.00000
To the Sine of the Angle A C B	gr. 61. 40'. 12".	9.94459

P R O B L E M VI.

The Legs being given, to find the Hypothenufe.

In the Rectangled Triangle A B C, the *Hypothenufe* B C is required from the

Given Legs $\begin{cases} A B \ 1123.7943 \\ A C \ 605.8601 \end{cases}$

The Terms of Proportion.

1. $BA : CA :: R : t. ABC.$
2. $s. ABC : R :: CA : BC.$

Illustration by Numbers.



1. For the Angle A B C.

As the Leg A B	1123.7943	3.05068
To the Leg A C	605.8601	2.78237
So the Radius 90 Degrees		10.00000
To the Tangent of the Angle A B C	gr. 28. 19'. 48".	9.73169

2. For the Hypothenufe B C.

As the Sine of the Angle A B C	gr. 28. 19'. 48".	9.67628
To the Radius 90 Degrees		10.00000
So the Leg A C	605.8601	2.78237
To the Hypothenufe B C	1276.7067.	3.10609

P R O-

P R O B L E M VII.

The Hypothenufe and a Leg being given, to find the other Leg.

In the Rectangled Triangle ABC, the Leg AC is inquired from

The given $\begin{cases} \text{Hypothenufe } BC & 1276.7067 \\ \text{Leg } AB & 1123.7943 \end{cases}$

Terms of Proportion.

1. $BC : BA :: R : s. ACB.$
2. $R : s. ABC :: BC : AC.$

Or it may be performed with more ease by one Operation.

Log. BA+BC plus ; Log. BA-BC, Divif. per 2 = Log. CA.

Illustration by Numbers.

Hypothenufe BC	1276.7067	Sum	2400.5010.	3.38030
Leg BA	1123.7943	Difference	152.9124.	2.18444
				Aggregate 5.56474
				Semi-aggregate 2.78237
Leg AC	605.8601			

S E C T. II.

Of the Dimension of Plain Oblique-angled Triangles.

P R O B L E M I.

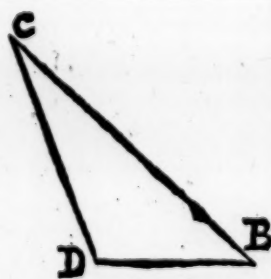
Two Sides and an Angle opposite to one of them being given, to find the Angle opposite to the other Side.

IN the Oblique-angled Triangle BCD, the Angle B is inquired from

The given Sides $\begin{cases} BC & 1276.7067 \\ CD & 865.1765 \end{cases}$

Terms of Proportion.

$$BC : s. BDC :: CD : s. CBD$$



Illustra-

Illustration by Numbers.

As the Side B C	1276.7067	3.10609
To the Sine of the Angle B D C	116d. 12'. 22".	9.95289
So the Side C D	865.1765	2.93710
		<hr/>
To the Sine of the Angle C B D	37d. 26'. 43".	12.88999
		9.78390

P R O B L E M II.

Two Sides with the Angle included by them being given, to find either of the other Angles.

In the Oblique-angled Triangle B C D, either Angle at C or D is inquired, from the given

Sides $\begin{cases} B C & 1276.7067 \\ B D & 631.5525 \end{cases}$
 Angle D B C 37d. 26'. 43".

Terms of Proportion.

$$BD + CD : BD - CD :: t. \frac{C+B}{2} : t. \frac{X}{2}$$

$$\text{Then } \frac{C+B}{2} + \frac{X}{2} = \text{Ang. } \begin{cases} B D C \\ B C D \end{cases}$$

Illustration by Numbers.

As the Sum of the Sides B C and B D	1908.2592	3.28063
To their Difference	645.1542	2.80966
So the Tangent of half the Sum of the opposite Angles	71d. 16'. 38".	10.46989

To the Tangent of half the Difference	44d. 55'. 44".	13.27956
		9.99892

To the half Sum of the Angles	71d. 16'. 38".
Add the half Difference	44. 55. 44.

It giveth the Angle B D C	116. 12. 22.
---------------------------	--------------

From	71d. 16'. 38".
Subtract	44. 55. 44.

The Angle B C D	26. 20. 54.
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P R O.

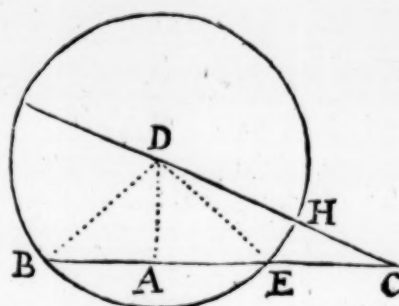
PROBLEM III.

The three Sides being given, to find an Angle.

In the Oblique-angled Triangle BCD, either Angle is inquired.

Suppose the Angle DBC from

The given Sides $\begin{cases} CB & 1276.7067 \\ BD & 631.5525 \\ CD & 865.1765 \end{cases}$



Terms of Proportion.

1. $BC : CD + BD :: CD - BD : CE$
2. $BD : R :: BA : \text{cs. } B.$

Illustration in Numbers.

1.
As the greater Side BC 1276.7067 3.10609
To the Sum of CD and DB 1496.7290 3.17514
So the Difference HC 233.6240 2.36851

To the Differ. of the Segm. of the Base CE 273.8858, 5.54365
2.43756

The Difference of this, and the Base BE 1002.8209
Whose half BA = EA 501.4104
Hence CA shall be 775.2962

2.
As the Hypotenuse BD 631.5525 2.80041
To the Leg BA 501.4104 2.70019
So the Radius 90 Degrees 10.00000
To the Sine of the Angle BDA 52 d. 33'. 16" 9.89978

Whose Complement ABD is 37 d. 26'. 44". The like course you are to take for the Angle ACD.

This Problem may more readily be resolved, and that at one Operation, by the following Precept; the Ground whereof is drawn from the Learned Mr. Briggs his *Arithmetica Logarithmica*, Cap. 10.

De dimidio collectorum laterum, latera sigillatim subducantur, &c.
From half the Sum of the Sides, Subtract the Sides one after another, and let the Sum of the Logarithms, of the half Sum of the Sides and Difference of the Sides subtending the Angle sought for, be subtracted from the Sum of the Logarithms, of the other Differences, and the double Radius; the half of the Remainder, shall be the Logarithm of the Tangent of half the inquired Angle.

Let the Angle subtended by the greater side, be inquired, viz. BDC.

Illustration by Numbers.

The Side $\begin{cases} BC & 1276.7067 \\ DC & 865.1765 \\ DB & 631.5525 \end{cases}$

The Sum of the Sides $\underline{2773.4357}$

The half Sum 1386.7178

The Difference of CB 110.0111

3.14199

2.04143

The Sum $5.18342 A$

The Difference of the Side CD 521.5413

2.71729

The Difference of the Side BD 755.1653

2.87804

The Double Radius

20.00000

The Sum $25.59533 B$

The Sum $5.18342 A$

The Difference 20.41191

The half Difference 10.20595 is

the Tangent of $58d. 6'. 11''$. the Double whereof $116d. 12'. 23''$ is the Angle inquired BDC.

P R O B L E M IV.

The Angles and a Side being given, to find either of the other Sides.

In the Oblique-angled Triangle BCD, the Side DC is inquired from the given

Angles $\begin{cases} DBC & 37d. 26. 43. \frac{1}{2} \\ DCB & 26. 20. 53. \frac{1}{2} \\ BDC & 116. 12. 23 \end{cases}$
Side BC 1276.7067 .

Terms of Proportion.

$s. D : BC :: s. B : DC$.

Illustration by Numbers.

As the Sine of the Angle FDC $63d. 47'. 37''$.

9.95289

To the Side FC, 1276.7067

3.10609

So the Sine of the Angle DBC $37d. 26'. 43''. \frac{1}{2}$

9.78393

12.89000

To the Side DC 865.1795

2.9371 .

P R O-

PROBLEM V.

Two Sides with the Angle included by them being given, to find the Third Side.

In the Oblique-angled Triangle BCD, the Side BC is inquired from

The given Sides $\begin{cases} DC 865.1765 \\ BD 631.5525 \end{cases}$

And the Angle BDC 116d. 12'. 23".

First, Let the other Angles be inquired by the *Second Problem* of this *Section*, and the Angles being found, the Side inquired may be had by the last *Problem*. Examples are needless.

Advertisement.

WHEREAS the following Tables of Sines and Tangents do extend only to every Tenth Minute of the Quadrant, and also the Table of Logarithms only to One Thousand; I thought good to give Notice to the Reader, That there is Printed a most Excellent and Useful Book for all Students in the Mathematicks, Intituled, **TRIGONOMETRIA BRITANNICA**, which contains the making of the Tables of Sines Tangents, and Logarithms; and also their Use in resolving of all Triangles either Plain or Spherical: In which Book you have the Sines and Tangents to every Degree, and Hundredth part of a Degree of the Quadrant; and the Logarithms of all Numbers, from One to an Hundred Thousand.

Canon Triangulorum :
O R, A
T A B L E
O F
Artificial Sines and Tangents,
To a Radius of 1000000. Parts, and every
10th Minute of the *Quadrant*.
Together with
A TABLE of Logarithms to
1000. Being of Singular Use in the Solution
O F
TRIANGLES.

*Cuncta Trigonus habet satagit quæ docta
Mathesis :
Ille aperit clausam quicquid Olympus habet.*

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.	Tang.	Cotang.	M.Gr.
0 0	0.	10.00000	0.00000	Infinita.	0 90
10	7.46372	9.99999	7.46373	12.53627	50
20	7.76475	9.99999	7.76476	12.24524	40
30	7.94084	9.99998	7.94086	12.05914	30
40	8.06577	9.99997	8.06581	11.93419	20
50	8.16268	9.99995	8.16274	11.83726	10
1 0	8.24185	9.99993	8.24192	11.75808	0 89
10	8.30879	9.99991	8.30888	11.69112	50
20	8.36678	9.99988	8.36690	11.63310	40
30	8.41792	9.99985	8.41807	11.58193	30
40	8.46866	9.99981	8.46385	11.53615	20
50	8.50504	9.99978	8.50527	11.49473	10
2 0	8.54282	9.99973	8.54308	11.45692	0 88
10	8.57756	9.99969	8.57788	11.42212	50
20	8.60973	9.99964	8.61010	11.38990	40
30	8.63968	9.99958	8.64009	11.35991	30
40	8.66769	9.99953	8.66816	11.33184	20
50	8.69400	9.99947	8.69453	11.30547	10
3 0	8.71880	9.99940	8.71940	11.28060	0 87
10	8.74226	9.99933	8.74292	11.25708	50
20	8.76451	9.99926	8.76525	11.23475	40
30	8.78567	9.99919	8.78649	11.21351	30
40	8.80585	9.99911	8.80674	11.19326	20
50	8.82513	9.99903	8.82610	11.17390	10
4 0	8.84358	9.99894	8.84464	11.15536	0 86
10	8.86128	9.99885	8.86243	11.13757	50
20	8.87828	9.99876	8.87953	11.12047	40
30	8.89464	9.99866	8.89598	11.10402	30
40	8.91040	9.99856	8.91185	11.08815	20
50	8.92561	9.99845	8.92716	11.07284	10
5 0	8.94029	9.99834	8.94195	11.05805	0 85
10	8.95450	9.99823	8.95627	11.04373	50
20	8.96825	9.99810	8.97013	11.02987	40
30	8.98152	9.99800	8.98358	11.01642	30
40	8.99450	9.99787	8.99662	11.00338	20
50	9.00704	9.99773	9.00930	10.99070	10.
Gr.M	Cofin.	Sin.	Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.	Tang.	Cotang.	M.Gr.
6 0	9.01923	9.99761	9.02162	10.97838	0 84
10	9.03109	9.99748	9.03361	10.96639	50
20	9.04262	9.99734	9.04528	10.95472	40
30	9.05386	9.99720	9.05666	10.94334	30
40	9.06480	9.99705	9.06775	10.93225	20
50	9.07548	9.99690	9.07858	10.92142	10
7 0	9.08589	9.99675	9.08914	10.91086	0 83
10	9.09606	9.99659	9.09947	10.90053	50
20	9.10599	9.99643	9.10956	10.89044	40
30	9.11570	9.99627	9.11943	10.88057	30
40	9.12519	9.99610	9.12909	10.87091	20
50	9.13447	9.99503	9.13854	10.86146	10
8 0	9.14355	9.99575	9.14780	10.85220	0 82
10	9.15245	9.99557	9.15688	10.84312	50
20	9.16116	9.99539	9.16577	10.83423	40
30	9.16970	9.99520	9.17450	10.82550	30
40	9.17807	9.99501	9.18306	10.81694	20
50	9.18628	9.99482	9.19146	10.80854	10
9 0	9.19433	9.99462	9.19971	10.80029	0 81
10	9.20223	9.99442	9.20782	10.79218	50
20	9.20999	9.99421	9.21578	10.78422	40
30	9.21761	9.99400	9.22361	10.77639	30
40	9.22509	9.99379	9.23130	10.76870	20
50	9.23244	9.99357	9.23887	10.76113	10
10 0	9.24967	9.99335	9.24632	10.75368	0 80
10	9.24679	9.99313	9.25365	10.74635	50
20	9.25376	9.99290	9.26086	10.73914	40
30	9.26063	9.99266	9.26797	10.73203	30
40	9.26739	9.99243	9.27496	10.72504	20
50	9.27405	9.99219	9.28186	10.71814	10
11 0	9.28060	9.99195	9.28865	10.71135	0 79
10	9.28705	9.99170	9.29535	10.70465	50
20	9.29340	9.99145	9.30195	10.69805	40
30	9.29965	9.99119	9.30846	10.69154	30
40	9.30582	9.99093	9.31488	10.68512	20
50	9.31190	9.99068	9.32122	10.67878	10 78
Gr.M	Cofin.	Tang.	Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M.	Sin.	Cofin.	Tang.	Cotang.	M.Gr.
12 0	9.31788	9.99040	9.32747	10.67253	0 78
10	9.32378	9.99013	9.33365	10.66635	50
20	9.32960	9.98986	9.33974	10.66026	40
30	9.33534	9.98958	9.34575	10.65424	30
40	9.34099	9.98930	9.35170	10.64830	20
50	9.34658	9.98901	9.35757	10.64243	10
13 0	9.35209	9.98872	9.36336	10.63664	0 77
10	9.35752	9.98843	9.36909	10.63091	50
20	9.36289	9.98813	9.37476	10.62524	40
30	9.36818	9.98783	9.38035	10.61965	30
40	9.37341	9.98752	9.38589	10.61411	20
50	9.37858	9.98722	9.39136	10.60864	10
14 0	9.38367	9.98690	9.39677	10.60323	0 76
10	9.38871	9.98659	9.40212	10.59788	50
20	9.39368	9.98627	9.40742	10.59258	40
30	9.39860	9.98594	9.41266	10.58734	30
40	9.40345	9.98561	9.41784	10.58216	20
50	9.40825	9.98528	9.42297	10.57703	10
15 0	9.41229	9.98494	9.42895	10.57195	0 75
10	9.41768	9.98460	9.43308	10.56692	50
20	9.42232	9.98426	9.44046	10.56194	40
30	9.42690	9.98391	9.44299	10.55701	30
40	9.43143	9.98356	9.44787	10.55213	20
50	9.43592	9.98320	9.45271	10.54720	10
16 0	9.44034	9.98284	9.45750	10.54250	0 74
10	9.44472	9.98248	9.46224	10.53776	50
20	9.44905	9.98211	9.46694	10.53305	40
30	9.45334	9.98174	9.47160	10.52839	30
40	9.45758	9.98136	9.47622	10.52378	20
50	9.46178	9.98098	9.48080	10.51920	10
17 0	9.46593	9.98060	9.48534	10.51466	0 73
10	9.46944	9.98021	9.48984	10.51016	50
20	9.47411	9.97982	9.49430	10.50570	40
30	9.47814	9.97942	9.49872	10.50128	30
40	9.48213	9.97902	9.50311	10.49689	20
50	9.48607	9.97861	9.50746	10.49254	10.72
Gr.M	Cofin.	Sin.	Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.	Tang.	Cotang.	M.Gr.
18 0	9.48998	9.97821	9.51178	10.48822	0 72
10	9.49385	9.97779	9.51606	10.48394	50
20	9.49768	9.97738	9.52030	10.47969	40
30	9.50147	9.97796	9.52452	10.47548	30
40	9.50523	9.97653	9.52870	10.47130	20
50	9.50895	9.97610	9.53285	10.46715	10
19 0	9.51264	9.97567	9.53697	10.46303	0 71
10	9.51629	9.97528	9.54106	10.45894	50
20	9.51991	9.97479	9.54512	10.45488	40
30	9.52349	9.97434	9.54915	10.45085	30
40	9.52704	9.97390	9.55315	10.44685	20
50	9.53056	9.97344	9.75712	10.44288	10
20 0	9.53405	9.97299	9.56107	10.43893	0 70
10	9.53751	9.97252	9.56498	10.43502	50
20	9.54093	9.97286	9.56887	10.43113	40
30	9.54432	9.97159	9.57274	10.42726	30
40	9.54799	9.97111	9.57658	10.42352	20
50	9.55102	9.97063	9.58039	10.41961	10
21 0	9.55433	9.97015	9.58418	10.41582	0 69
10	9.55761	9.96966	9.58794	10.41206	50
20	9.56085	9.96917	9.59168	10.40832	40
30	9.56407	9.96868	9.59540	10.40460	30
40	9.56727	9.96818	9.59909	10.40091	20
50	9.57043	9.96767	9.60276	10.39724	10
22 0	9.57357	9.96716	9.60641	10.39359	0 68
10	9.57669	9.96665	9.61004	10.38996	50
20	9.57978	9.96613	9.61364	10.38636	40
30	9.58284	9.96561	9.61722	10.38278	30
40	9.58588	9.96509	9.62079	10.37921	20
50	9.58889	9.96456	9.62433	10.37567	10
23 0	9.59188	9.96402	9.62785	10.37215	0 67
10	9.59484	9.96349	9.63135	10.36865	50
20	9.59778	9.96294	9.63484	10.36516	40
30	9.60070	9.96240	9.63830	10.36170	30
40	9.60359	9.96184	9.64175	10.35825	20
50	9.60446	9.96129	9.64517	10.35483	10.
Gr.M	Cofin.	Sin.	Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.		Tang.	Cotang.	M.Gr.
24 0	9.60991	9.96073		9.64858	10.35142	0 66
10	9.61215	9.96017		9.65197	10.34803	50
20	9.61494	9.95960		9.65535	10.34465	40
30	9.61773	9.95902		9.65870	10.34130	30
40	9.62049	9.95844		9.66204	10.33796	20
50	9.62323	9.95786		9.66537	10.33463	10
25 0	9.62595	9.95728		9.66867	10.33133	0 65
10	9.62865	9.95668		9.67196	10.32804	50
20	9.63133	9.95609		9.67524	10.32476	40
30	9.63398	9.95549		9.67859	10.32150	30
40	9.63662	9.95488		9.68174	10.31826	20
50	9.63924	9.95427		9.68497	10.31503	10
26 0	9.64184	9.95366		9.68818	10.31182	0 64
10	9.64442	9.95304		9.69138	10.30862	50
20	9.64698	9.95242		9.69457	10.30543	40
30	9.64953	9.95179		9.69774	10.30226	30
40	9.65205	9.95116		9.70289	10.29911	20
50	9.65456	9.95052		9.70404	10.29596	10
27 0	9.65705	9.94988		9.70717	10.29283	0 63
10	9.65952	9.94923		9.71028	10.28972	50
20	9.66197	9.94858		9.71339	10.28671	40
30	9.66441	9.94793		9.71648	10.28352	30
40	9.66682	9.94727		9.71956	10.28044	20
50	9.66922	9.94660		9.72262	10.27738	10
28 0	9.67161	9.94593		9.72567	10.27433	0 62
10	9.67393	9.94526		9.72872	10.27128	50
20	9.67633	9.94458		9.73175	10.26825	40
30	9.67866	9.94360		9.73476	10.26524	30
40	9.68098	9.94321		9.73777	10.26223	20
50	9.68328	9.94252		9.74077	10.25923	10
29 0	9.68557	9.94182		9.74375	10.25625	0 61
10	9.68784	9.94112		9.74673	10.25327	50
20	9.69010	9.94041		9.74969	10.25031	40
30	9.69234	9.93970		9.75264	10.24736	30
40	9.69456	9.93898		9.75558	10.24442	20
50	9.69677	9.93826		9.75852	10.24148	10.
Gr.M	Cofin.	Sin.		Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.		Tang.	Cotang.	M.Gr
30 0	9.69897	9.93753		9.76144	10.23855	0 60
10	9.07115	9.93680		9.76435	10.23565	50
20	9.07332	9.93606		9.76726	10.23278	40
30	9.70547	9.93532		9.77015	10.28985	30
40	9.70760	9.93457		9.77303	10.22697	20
50	9.70973	9.93382		9.77591	10.22409	10
31 0	9.71184	9.93307		9.77877	10.22123	0 59
10	9.71393	9.93230		9.78163	10.21837	50
20	9.71601	9.93154		9.78448	10.21552	40
30	9.71808	9.93077		9.78732	10.21268	30
40	9.72014	9.92999		9.79015	10.20985	20
50	9.72218	9.92921		9.79297	10.20703	10
32 0	9.72421	9.92842		9.79579	10.20421	0 58
10	9.72622	9.92763		9.79860	10.20140	50
20	9.72823	9.92683		9.80140	10.19860	40
30	9.73022	9.92603		9.80419	10.19581	30
40	9.73219	9.92522		9.80697	10.19303	20
50	9.73417	9.92441		9.80975	10.19025	10
33 0	9.73611	9.92359		9.81252	10.18748	0 57
10	9.73805	9.92277		9.81528	10.18412	50
20	9.73997	9.92194		9.81803	10.18196	40
30	9.74189	9.92111		9.82078	10.17922	30
40	9.74379	9.92027		9.82352	10.17648	20
50	9.74568	9.91942		9.82626	10.17374	10
34 0	9.74756	9.91857		9.82899	10.17104	0 56
10	9.74943	9.91772		9.83171	10.16829	50
20	9.75128	9.91686		9.83442	10.16558	40
30	9.75313	9.91599		9.83713	10.16287	30
40	9.75496	6.91512		9.83984	10.16016	20
50	9.75678	9.91425		9.84253	10.15747	10
35 0	9.75859	9.91336		9.84523	10.15477	0 55
10	9.76039	9.91248		9.84791	10.15209	50
20	9.76218	9.91158		9.85059	10.14941	40
30	9.76395	9.91069		9.85327	10.14673	30
40	9.76572	9.90978		9.85594	10.14406	20
50	9.76747	9.90887		9.85860	10.14140	10.
Gr.M	Cofin.	Sin.		Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr.M	Sin.	Cofin.	Tang.	Cotang .	M.Gr.
36 0	9.76922	9.90796	9.86126	10.13874	0 54
10	9.77095	9.90704	9.86391	10.13609	50
20	9.77267	9.90611	9.86656	10.13344	40
30	9.77439	9.90518	9.86921	10.13079	30
40	9.77609	9.90424	9.87185	10.12815	20
50	9.77778	9.90330	9.87448	10.12552	10
37 0	9.77946	9.90235	9.87711	10.12289	0 53
10	9.78113	9.90139	9.87974	10.12026	50
20	9.78280	9.90043	9.88236	10.11764	40
30	9.78445	9.89947	9.88498	10.11502	30
40	9.78690	9.89849	9.88759	10.11241	20
50	9.78772	9.89152	9.89020	10.10980	10
38 0	9.78934	9.89653	9.89281	10.10719	0 52
10	9.79095	9.89554	9.89541	10.10459	50
20	9.79256	9.89455	9.89801	10.10199	40
30	9.79415	9.89354	9.90060	10.09939	30
40	9.79573	9.89254	9.90320	10.09680	20
50	9.79731	9.89152	9.90578	10.09422	10
39 0	9.79887	9.89050	9.90837	10.09163	0 51
10	9.80043	9.88948	9.91095	10.08905	50
20	9.80197	9.88844	9.91353	10.08647	40
30	9.80351	9.88741	9.91610	10.08390	30
40	9.80504	9.88636	9.91868	10.08132	20
50	9.80656	9.88531	9.92125	10.07875	10
40 0	9.80807	9.88425	9.92381	10.07619	0 50
10	9.80957	9.88319	9.92638	10.07362	50
20	9.81006	9.88212	9.92894	10.07106	40
30	9.81254	9.88104	9.93150	10.06850	30
40	9.81402	9.87996	9.93406	10.06594	20
50	9.81548	9.87887	9.93661	10.06339	10
41 0	9.81694	9.87778	9.93916	10.06081	0 49
10	9.81839	9.87608	9.94171	10.05829	50
20	9.81983	9.87557	9.94426	10.05574	40
30	9.82126	9.87446	9.94681	10.05319	30
40	9.82269	9.87333	9.94935	10.05065	20
50	9.82410	9.87221	9.95190	10.04810	10.48
Gr.M	Cofin.	Tang.	Cotang.	Tang.	M.Gr.

A Table of Artificial Sines and Tangents.

Gr. M	Sin.	Cofin.		Tang.	Cotang.	M.Gr.
42 0	9.82551	9.87107		9.95444	10.04556	0 48
10	9.82691	9.86993		9.95698	10.04302	50
20	9.82830	9.86878		9.95952	10.04048	40
30	9.82968	9.86763		9.96205	10.03795	30
40	9.83106	9.86647		9.96459	10.03541	20
50	9.83242	9.86530		9.96712	10.03288	10
43 0	9.83378	9.86413		9.96966	10.03034	0 47
10	9.83513	9.86294		9.97219	10.02781	50
20	9.83648	9.86176		9.97472	10.02528	40
30	9.83781	9.86056		9.97725	10.02275	30
40	9.83914	9.85936		9.97978	10.02022	20
50	9.84046	9.85815		9.98231	10.01769	10
44 0	9.84177	9.85693		9.98484	10.01516	0 46
10	9.84308	9.85571		9.98736	10.01264	50
20	9.84437	9.85448		9.98989	10.01011	40
30	9.84566	9.85324		9.99242	10.00758	30
40	9.84694	9.85200		9.99405	10.00505	20
50	9.84822	9.85074		9.99747	10.00253	10
45 0	9.84948	9.84948		10.00000	10.00000	0 45
Gr. M	Cofin.	Sin.		Cotang.	Tang.	M.Gr.

Explanation of the Table by Example.

1. Suppose it be required to find the Sine and Tangent of 30. degr. 20. min. therefore I seek the same in the first Column on the left hand under Gr. 1. and find the Sine thereof 9.70332. and the Tangent 9.76726. its Cosine 9.93606, and the Cotangent 10.23278.

2. But suppose 9.73997. be a Sine given, and the Arch thereof is required; therefore I seek in the second Column amongst the Sines for 9.73997. and against it on the left hand, I find 33. degr. 20. min. which is the Arch answering thereunto.

But if you find not your just number, then take the nearest in the Table; which you shall find exact enough for Instrumental Observations.

A Table

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
0	0,00000	44	1,64345	88	1,94448	132	2,12057
1	0,00000	45	1,65321	89	1,94939	133	2,12385
2	0,30103	46	1,66276	90	1,95424	134	2,12710
3	0,47713	47	1,67210	91	1,95904	135	2,13033
4	0,60206	48	1,68124	92	1,96379	136	2,13354
5	0,69897	49	1,69020	93	1,96848	137	2,13672
6	0,77815	50	1,69897	94	1,97313	138	2,13988
7	0,84510	51	1,70757	95	1,97772	139	2,14301
8	0,90309	52	1,71600	96	1,98117	140	2,14613
9	0,95424	53	1,72427	97	1,98677	141	2,14922
10	1,00000	54	1,73239	98	1,99123	142	2,15229
11	1,04139	55	1,74036	99	1,99563	143	2,15534
12	1,07918	56	1,74819	100	2,00000	144	2,18836
13	1,11394	57	1,75587	101	2,00432	145	2,16137
14	1,14613	58	1,76343	102	2,00860	146	2,16435
15	1,17609	59	1,77085	103	2,01284	147	2,16732
16	1,20412	60	1,77815	104	2,01703	148	2,17026
17	1,23045	61	1,78533	105	2,02119	149	2,17319
18	1,25527	62	1,79219	106	2,02530	150	2,17609
19	1,27875	63	1,79934	107	2,02938	151	2,17898
20	1,30103	64	1,80648	108	2,03342	152	2,18184
21	1,32222	65	1,81291	109	2,03743	153	2,18469
22	1,34242	66	1,81954	110	2,04139	154	2,18752
23	1,36173	67	1,82607	111	2,04532	155	2,19033
24	1,38021	68	1,83251	112	2,04922	156	2,19312
25	1,39794	69	1,83885	113	2,05308	157	2,19590
26	1,41497	70	1,84510	114	2,05690	158	2,19866
27	1,43136	71	1,85126	115	2,06070	159	2,20140
28	1,44716	72	1,85733	116	2,06446	160	2,20412
29	1,46240	73	1,86332	117	2,06819	161	2,20683
30	1,47712	74	1,86923	118	2,07188	162	2,20951
31	1,49136	75	1,87506	119	2,07555	163	2,21219
32	1,50515	76	1,88081	120	2,07918	164	2,21484
33	1,51851	77	1,88649	121	2,08278	165	2,21748
34	1,53148	78	1,89209	122	2,08636	166	2,22011
35	1,54407	79	1,89763	123	2,08990	167	2,22272
36	1,55630	80	1,90309	124	2,09342	168	2,22531
37	1,56820	81	1,90848	125	2,09691	169	2,22789
38	1,57978	82	1,91381	126	2,10037	170	2,23045
39	1,59106	83	1,91908	127	2,10380	171	2,23300
40	1,60206	84	1,92428	128	2,10721	172	2,23553
41	1,61278	85	1,92942	129	2,11059	173	2,23805
42	1,62325	86	1,93450	130	2,11394	174	2,24055
43	1,63347	87	1,93952	131	2,11727	175	2,24304

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
176	2,24551	220	2,34243	264	2,42160	308	2,48855
177	2,24797	221	2,34439	265	2,42325	309	2,48996
178	2,25042	222	2,34635	266	2,42488	310	2,49136
179	2,25285	223	2,34830	267	2,42651	311	2,49276
180	2,25527	224	2,35025	268	2,42813	312	2,49415
181	2,25768	225	2,35218	269	2,42975	313	2,49554
182	2,26007	226	2,35411	270	2,43136	314	2,49693
183	2,26225	227	2,35603	271	2,43297	315	2,49831
184	2,26482	228	2,35793	272	2,43457	316	2,49969
185	2,26717	229	2,35983	273	2,43616	317	2,50106
186	2,26951	230	2,36173	274	2,43775	318	2,50243
187	2,27184	231	2,36361	275	2,43933	319	2,50379
188	2,27416	232	2,36549	276	2,44091	320	2,50515
189	2,27646	233	2,36736	277	2,44248	321	2,50650
190	2,27875	234	2,36922	278	2,44404	322	2,50786
191	2,28108	235	2,37107	279	2,44560	323	2,50920
192	2,28330	236	2,37291	280	2,44716	324	2,51054
193	2,28556	237	2,37475	281	2,44871	325	2,51188
194	2,28780	238	2,37658	282	2,45025	326	2,51322
195	2,29002	239	2,37840	283	2,45179	327	2,51455
196	2,29226	240	2,38021	284	2,45332	328	2,51587
197	2,29447	241	2,38202	285	2,45484	329	2,51720
198	2,29666	242	2,38381	286	2,45636	330	2,51851
199	2,29885	243	2,38561	287	2,45789	331	2,51983
200	2,30103	244	2,38739	288	2,45939	332	2,52114
201	2,30340	245	2,38917	289	2,46090	333	2,52244
202	2,30535	246	2,39093	290	2,46240	334	2,52375
203	2,30750	247	2,39270	291	2,46387	335	2,52504
204	2,30963	248	2,39445	292	2,46538	336	2,52634
205	2,31175	249	2,39620	293	2,46687	337	2,52763
206	2,31387	250	2,39794	294	2,46835	338	2,52892
207	2,31597	251	2,39967	295	2,46982	339	2,53020
208	2,31806	252	2,40140	296	2,47129	340	2,53148
209	2,32015	253	2,40312	297	2,47276	341	2,53275
210	2,32222	254	2,40483	298	2,47422	342	2,53403
211	2,32428	255	2,40654	299	2,47567	343	2,53529
212	2,32634	256	2,40824	300	2,47712	344	2,53656
213	2,32838	257	2,40993	301	2,47856	345	2,53782
214	2,33041	258	2,41162	302	2,48001	346	2,53908
215	2,33244	259	2,41320	303	2,48144	347	2,54033
216	2,33443	260	2,41497	304	2,48287	348	2,54158
217	2,33646	261	2,41664	305	2,48430	349	2,54283
218	2,33846	262	2,41830	306	2,48572	350	2,54407
219	2,34044	263	2,41996	307	2,48714	351	2,54531

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
352	2,54654	396	2,57769	440	2,64345	484	2,68484
353	2,54777	397	2,59879	441	2,64444	485	2,68574
354	2,54900	398	2,59988	442	2,64542	486	2,68664
355	2,55023	399	2,60097	443	2,64640	487	2,68753
356	2,55145	400	2,60206	444	2,64738	488	2,68842
357	2,55267	401	2,60314	445	2,64836	489	2,68931
358	2,55388	402	2,60423	446	2,64933	490	2,69020
359	2,55509	403	2,60530	447	2,65031	491	2,69108
360	2,55630	404	2,60638	448	2,65128	492	2,69196
361	2,55751	405	2,60745	449	2,65225	493	2,69285
362	2,55871	406	2,60853	450	2,65321	494	2,69373
363	2,55991	407	2,60959	451	2,65418	495	2,69460
364	2,56110	408	2,61066	452	2,65514	496	2,69548
365	2,56229	409	2,61172	453	2,65610	497	2,69636
366	2,56348	410	2,61278	454	2,65706	498	2,69723
367	2,56467	411	2,61384	455	2,65801	499	2,69810
368	2,56585	412	2,61490	456	2,65996	500	2,69897
369	2,56703	413	2,61595	457	2,65991	501	2,69984
370	2,56820	414	2,61700	458	2,66086	502	2,70070
371	2,56937	415	2,61805	459	2,66181	503	2,70157
372	2,57054	416	2,61909	460	2,66276	504	2,70243
373	2,57171	417	2,62014	461	2,66370	505	2,70329
374	2,57287	418	2,62118	462	2,66464	506	2,70415
375	2,57403	419	2,62221	463	2,66558	507	2,70501
376	2,57519	420	2,62325	464	2,66652	508	2,70586
377	2,57634	421	2,62428	465	2,66745	509	2,70672
378	2,57749	422	2,62531	466	2,66838	510	2,70757
379	2,57864	423	2,62634	467	2,66932	511	2,70842
380	2,57978	424	2,62737	468	2,67024	512	2,70927
381	2,58092	425	2,62839	469	2,67117	513	2,71012
382	2,58206	426	2,62941	470	2,67210	514	2,71096
383	2,58320	427	2,63043	471	2,67302	515	2,71181
384	2,58433	428	2,63144	472	2,67394	516	2,71265
385	2,58546	429	2,63246	473	2,67486	517	2,71349
386	2,58659	430	2,63347	474	2,67578	518	2,71433
387	2,58771	431	2,63448	475	2,67669	519	2,71517
388	2,58883	432	2,63548	476	2,67761	520	2,71600
389	2,58995	433	2,63649	477	2,67852	521	2,71684
390	2,59106	434	2,63749	478	2,67943	522	2,71767
391	2,59218	435	2,63849	479	2,68033	523	2,71850
392	2,59329	436	2,63949	480	2,68124	524	2,71933
393	2,59439	437	2,64048	481	2,68214	525	2,72016
394	2,59549	438	2,64147	482	2,68305	526	2,72099
395	2,59660	439	2,64246	483	2,68395	527	2,72181

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
527	2,72181	571	2,75664	615	2,78887	659	2,81838
528	2,72263	572	2,75740	616	2,78958	660	2,81954
529	2,72346	573	2,75815	617	2,79028	661	2,82020
530	2,72345	574	2,75891	618	2,79099	662	2,82086
531	2,72509	575	2,75967	619	2,79169	663	2,82151
532	2,72591	576	2,76042	620	2,79239	664	2,82217
533	2,72673	577	2,76118	621	2,79309	665	2,82282
534	2,72754	578	2,76193	622	2,79379	666	2,82347
535	2,72835	579	2,76268	623	2,79449	667	2,82413
536	2,72916	580	2,76343	624	2,79518	668	2,82478
537	2,72997	581	2,76418	625	2,79588	669	2,82543
538	2,73078	582	2,76492	626	2,79657	670	2,82607
539	2,73159	583	2,76567	627	2,79727	671	2,82672
540	2,73239	584	2,76641	628	2,79796	672	2,82737
541	2,73320	585	2,76716	629	2,79865	673	2,82801
542	2,73400	586	2,76790	630	2,80034	674	2,82866
543	2,73480	587	2,76864	631	2,80003	675	2,82930
544	2,73560	588	2,76938	632	2,80072	676	2,82995
545	2,73640	589	2,77011	633	2,80140	677	2,83059
546	2,73719	590	2,77085	634	2,80208	678	2,83123
547	2,73799	591	2,77159	635	2,80277	679	2,83187
548	2,73878	592	2,77232	636	2,80346	680	2,83251
549	2,73957	593	2,77305	637	2,80414	681	2,83315
550	2,74036	594	2,77379	638	2,80482	682	2,83378
551	2,74115	595	2,77452	639	2,80550	683	2,83442
552	2,74191	596	2,77525	640	2,80618	684	2,83506
553	2,74272	597	2,77597	641	2,80656	685	2,83569
554	2,74351	598	2,77670	642	2,80753	686	2,83632
555	2,74429	599	2,77743	643	2,80821	687	2,83696
556	2,74507	600	2,77815	644	2,80889	688	2,83759
557	2,74585	601	2,77887	645	2,80956	689	2,83822
558	2,74663	602	2,77960	646	2,81023	690	2,83885
559	2,74741	603	2,78032	647	2,81090	691	2,83948
560	2,74819	604	2,78104	648	2,81157	692	2,84011
561	2,74896	605	2,78175	649	2,81224	693	2,84073
562	2,74973	606	2,78247	650	2,81291	694	2,84136
563	2,75051	607	2,78319	651	2,81358	695	2,84198
564	2,75128	608	2,78390	652	2,81425	696	2,84261
565	2,75205	609	2,78462	653	2,81491	697	2,84323
566	2,75282	610	2,78533	654	2,81558	698	2,84385
567	2,75358	611	2,78604	655	2,81624	699	2,84448
568	2,75435	612	2,78675	656	2,81690	700	2,84510
569	2,75511	613	2,78746	657	2,81756	701	2,84572
570	2,75587	614	2,78816	658	2,81822	702	2,84634

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
703	2,84695	747	2,87332	791	2,89818	835	2,92169
704	2,84757	748	2,87390	792	2,89872	836	2,92221
705	2,84819	749	2,87448	793	2,89927	837	2,92272
706	2,84880	750	2,87506	794	2,89982	838	2,92324
707	2,84942	751	2,87564	795	2,90037	839	2,92376
708	2,85001	752	2,87622	796	2,90091	840	2,92428
709	2,85065	753	2,87679	797	2,90146	841	2,92480
710	2,85126	754	2,87737	798	2,90200	842	2,92531
711	2,85187	755	2,87795	799	2,90215	843	2,92582
712	2,85248	756	2,87852	800	2,90309	844	2,92634
713	2,85309	757	2,87910	801	2,90363	845	2,92686
714	2,85370	758	2,87967	802	2,90417	846	2,92737
715	2,85431	759	2,88024	803	2,90472	847	2,92788
716	2,85491	760	2,88081	804	2,90526	848	2,92840
717	2,85552	761	2,88138	805	2,90580	849	2,92891
718	2,85612	762	2,88195	806	2,90633	850	2,92942
719	2,85673	763	2,88252	807	2,90687	851	2,92993
720	2,85733	764	2,88309	808	2,90741	852	2,93044
721	2,85793	765	2,88361	809	2,90795	853	2,93095
722	2,85854	766	2,88423	810	2,90848	854	2,93146
723	2,85914	767	2,88479	811	2,90902	855	2,93197
724	2,85974	768	2,88536	812	2,90956	856	2,93247
725	2,86034	769	2,88592	813	2,91005	857	2,93298
726	2,86094	770	2,88649	814	2,91062	858	2,93349
727	2,86153	771	2,88705	815	2,91116	859	2,93399
728	2,86213	772	2,88762	816	2,91169	860	2,93450
729	2,86273	773	2,88818	817	2,91222	861	2,93500
730	2,86332	774	2,88874	818	2,91277	862	2,93551
731	2,86392	775	2,88930	819	2,91328	863	2,93601
732	2,86451	776	2,88986	820	2,91381	864	2,93651
733	2,86510	777	2,89042	821	2,91434	865	2,93701
734	2,86570	778	2,89093	822	2,91487	866	2,93752
735	2,86629	779	2,89154	823	2,91540	867	2,93802
736	2,86688	780	2,89209	824	2,91593	868	2,93852
737	2,86747	781	2,89265	825	2,91645	869	2,93902
738	2,86806	782	2,89321	826	2,91698	870	2,93952
739	2,86864	783	2,89376	827	2,91751	871	2,94002
740	2,86923	784	2,89431	828	2,91803	872	2,94052
741	2,86982	785	2,89487	829	2,91855	873	2,94102
742	2,87040	786	2,89542	830	2,91908	874	2,94151
743	2,87099	787	2,89597	831	2,91960	875	2,94201
744	2,87157	788	2,89653	832	2,92012	876	2,94250
745	2,87216	789	2,89708	833	2,92064	877	2,94300
746	2,87274	790	2,89763	834	2,92117	878	2,94349

A Table of Logarithms.

N.	Logar.	N.	Logar.	N.	Logar.	N.	Logar.
877	2,94300	908	2,95809	939	2,97267	970	2,98677
878	2,94349	909	2,95856	940	2,97313	971	2,98722
879	2,94399	910	2,95904	941	2,97359	972	2,98767
880	2,94448	911	2,95952	942	2,97405	973	2,98811
881	2,94498	912	2,95999	943	2,97451	974	2,98856
882	2,94547	913	2,96047	944	2,97497	975	2,98900
883	2,94596	914	2,96095	945	2,97543	976	2,98945
884	2,94645	915	2,96142	946	2,97589	977	2,98989
885	2,94694	916	2,96189	947	2,97635	978	2,99034
886	2,94743	917	2,96237	948	2,97681	979	2,99078
887	2,94792	918	2,96284	949	2,97727	980	2,99113
888	2,94841	919	2,96331	950	2,97772	981	2,99167
889	2,94890	920	2,96379	951	2,97818	982	2,99211
890	2,94939	921	2,96426	952	2,97864	983	2,99255
891	2,94988	922	2,96473	953	2,97909	984	2,99299
892	2,95036	923	2,96520	954	2,97955	985	2,99344
893	2,95085	924	2,96567	955	2,98000	986	2,99388
894	2,95134	925	2,96614	956	2,98046	987	2,99432
895	2,95182	926	2,96661	957	2,98091	988	2,99476
896	2,95231	927	2,96708	958	2,98137	989	2,99520
897	2,95279	928	2,96755	959	2,98182	990	2,99563
898	2,95328	929	2,96802	960	2,98227	991	2,99607
899	2,95376	930	2,96848	961	2,98272	992	2,99651
900	2,95424	931	2,96895	962	2,98317	993	2,99695
901	2,95472	932	2,96941	963	2,98363	994	2,99739
902	2,95521	933	2,96988	964	2,98408	995	2,99782
903	2,95569	934	2,97035	965	2,98453	996	2,99826
904	2,95617	935	2,97081	966	2,98498	997	2,99869
905	2,95664	936	2,97128	967	2,98543	998	2,99913
906	2,95713	937	2,97174	968	2,98587	999	2,99956
907	2,95761	938	2,97220	969	2,98632	1000	3,00000

*An Explanation of the former TABLE
of Logarithms.*

EVERY Page in the former *Table of Logarithms*, is divided into eight Columns, or Spaces; whereof the first, third, fifth, and seventh, having the Letter N. at the Head thereof, are the Numbers successively continued from 1. to 1000. So that to find the *Logarithm* of any Number under 1000, you must find the Number given; and against the same, towards the Right Hand, you have the Logarithm thereof.

E X A M P L E.

Suppose the Number given be 720, and its Logarithm is required; therefore in the third Row, under the Title N, I seek the said Number, and against the same stands 2,85733, which is the Logarithm desired.

But if a Logarithm be given, and the absolute Number there-to belonging is required; then seek out the Logarithm under the Title, and against the same towards the Left Hand, is the absolute Number answering to that Logarithm.

If you cannot find in the Table the just Logarithm you seek for, you must take the nearest thereunto; or in the Table of Sines and Tangents, you may (if you please) make proportion; so shall you take the Logarithm to a Minute: but in such cases your own Judgment may best inform you.

The End of the Third Book.

THE

THE
Art of Surveying,
The FOURTH BOOK.

Wherein is shewed,
How to take the Exact PLOT
of all Manner of GROUNDS whatsoever,
after Several Ways:

BY THE
PLAIN TABLE.

AND
How to Cast up the Just Quantity, and Content
thereof, in *Acres, Roods, and Perches.*

And also, How to Inclose, and Take in a
LORDSHIP,

That lieth in Common, or in Open Fields,
And to Draw a Perfect Map thereof.

AND ALSO
How *Statute-Measure*, may be Reduced to *Custo-
mary-Measure*; and the Contrary.

As it was formerly Published by the Author
VINCENT WING, Math.

LONDON,
Printed for *Awnsham* and *John Churchill*, at the *Black-Swan*,
in *Pater-Noster-Row*, MDCXCIX.

THE
ART
OF
SURVEYING.

BOOK IV.

The P R O E M.

THIS was the Sixth Book, which is now made the Fourth, being the Essential part of the whole Book, as my Uncle, Mr. Vincent Wing, Printed it, for the Practical part of Surveying; and has gained the Approbation of most of the Ablest Surveyors of this Nation: I have therefore only taken out his Twentieth Chapter, and added it with Additions in the Second Book; viz. in the Third Part of the Book of Geometry, being the Ninth Problem; being (as I conceive) in a more convenient place for that purpose. And what is deficient, or wanting in this Fourth Book, I have largely supplied in my Appendix hereunto adjoyned; to which I refer the Ingenious Surveyor for further Satisfaction.

C H A P.

C H A P. I.

A Description of the Plain Table, with its several Parts, and Composition, &c.

AMONGST the manifold Instruments which have hitherto been invented, for the Exact and Speedy Plotting and Measuring of all kinds of Land, there is none so plain and perspicuous in Use and Practice, as this Instrument, and therefore it aptly receiveth the Name and Appellation of the *Plain-Table*: And albeit this Instrument (as well as any other) may be slighted and abused by the Ignorance of the Common Mechanics, and other Illiterate Pretenders to the Art, that scarce ever understood what the *Mathematicks* were; yet why should it deter any Artist from the Use and Practice thereof, seeing we may not only, with more ease and exactness, and with less fear of Errors and Mistakes, attain our desired Aim far better thereby, than can (possibly) be done with any other Instrument whatsoever, as is well known to all Practical Surveyors, who are acquainted both with the Use of this and the rest? And yet I can't but highly commend the *Theodolite*, *Circumferenter*, and the *PeraCTOR*, as Instruments very useful upon some occasions; neither dare I reject, as useless, either the *Topographical Instrument*, and *Cross-staffe* of Mr. Diggs, the *Familiar Staffe* of Mr. John Blagrave, the *Geodetical Staffe*, and *Topographical Glass* of Mr. Arthur Hopton, the *Sector*, *Cross-Staffe*, and the *Pandoron* of my late Worthy Friend Mr. George Attwell, or any other commodious Invention that hath hitherto been wittily devised, for the exact Plotting, and speedy Mensuration of all manner of Superficies, as Land, and the like. But in regard the Authors themselves have in their own Works (to their exceeding Commendation) described both the Making and Use of the said Instruments, I should here but tire my Readers to reiterate what they have already shewed elsewhere, and so make these few Lines swell beyond their intended Bounds: And besides, Mr. Aaxon Rathborne, in the beginning of his *Third Book*, and my Loving Friend, Mr. William Leybourn in the first five Chapters of his *Second Book*, have very well saved me that labour; where they have excellently treated, both of the Composition and Use of the most Material and Commodious Instruments now in being, to which the *Semicircle* may be added, as being inferior to none of the forementioned. Wherefore I shall now come to speak of the Composition of the *Plain Table*, which indeed is the Instrument, of whose Use alone we shall afterwards treat.

This Instrument (commonly known by the Name of *Geometrical*, or *Plain Table*) is in the Fashion of a Parallelogram, or Long Square, containing in Length about 14 Inches and a half, and in Breadth

Breadth 11 Inches; and were it not for warping, it might be made of one Board, but for avoiding that, and for the convenience of Carriage, the best way (as they are usually made) is to have it of three Boards in breadth, with a Ledge at each end for holding them together, and making the Table of due length; whereunto belongeth a joynted Frame, that when the five Boards are set together, and a Sheet of Paper put thereon, the Frame may bind the same so fast and smooth upon the Table, that when you come into the Field, you may neatly describe a Plot of your Land, Wood-Ground, or other Inclosure, upon the same, as shall be afterwards shewed.

Again, Let the Sides of the Frame of the Table be divided into equal parts, or Scales, for the drawing of Parallel Lines when you shift your Paper, and put on another Sheet. And on the other side your Frame, it would be very necessary to have projected upon it, the 360 Degrees of the Circle from a Center made about the middle of the Table, which will be of excellent use in Wet and Stormy-Weather (as my Worthy Friend Mr. *Leybourn* well adviseth) when as you cannot keep a Sheet of Paper upon the Table.

To this Instrument there belongeth a Rule, or Index of Brass, which must contain in length at least 16 Inches, in breadth about 2 Inches, and in thickness $\frac{1}{2}$ of an Inch. Upon this Index are to be placed two Sights, both of one length, the one having a Slit below, and a Thread above, and the other a Slit above, and a Thread below, serving to look forward and backward, when you are upon Plotting; and these Sights must be so placed upon the Ruler, either with Screws, or square Mortises, that both the Sights may be equi-distant from the fiducial edge of the Ruler. Moreover, upon the Face, or upper part of this Ruler, are several Scales of equal Divisions, as of 10. 12. 16. 20. 24. and 32 parts in an Inch; serving to lay down the Plot of a Field according to what proportion shall be thought most convenient for that purpose. There also belongeth to this Instrument a Box and a Needle, which is to be placed on the Side of the Table, with two Screws; and in the bottom of the Box is placed a Chard, divided into 360 Degrees, which is covered over with clear Glass.

Lastly, On the backside of the Table is a Socket of Brass fastened to the Table with three Screws, into which Socket must be put the Head of the Three-legged Staff, which for Portability, is usually joynted in the middle.

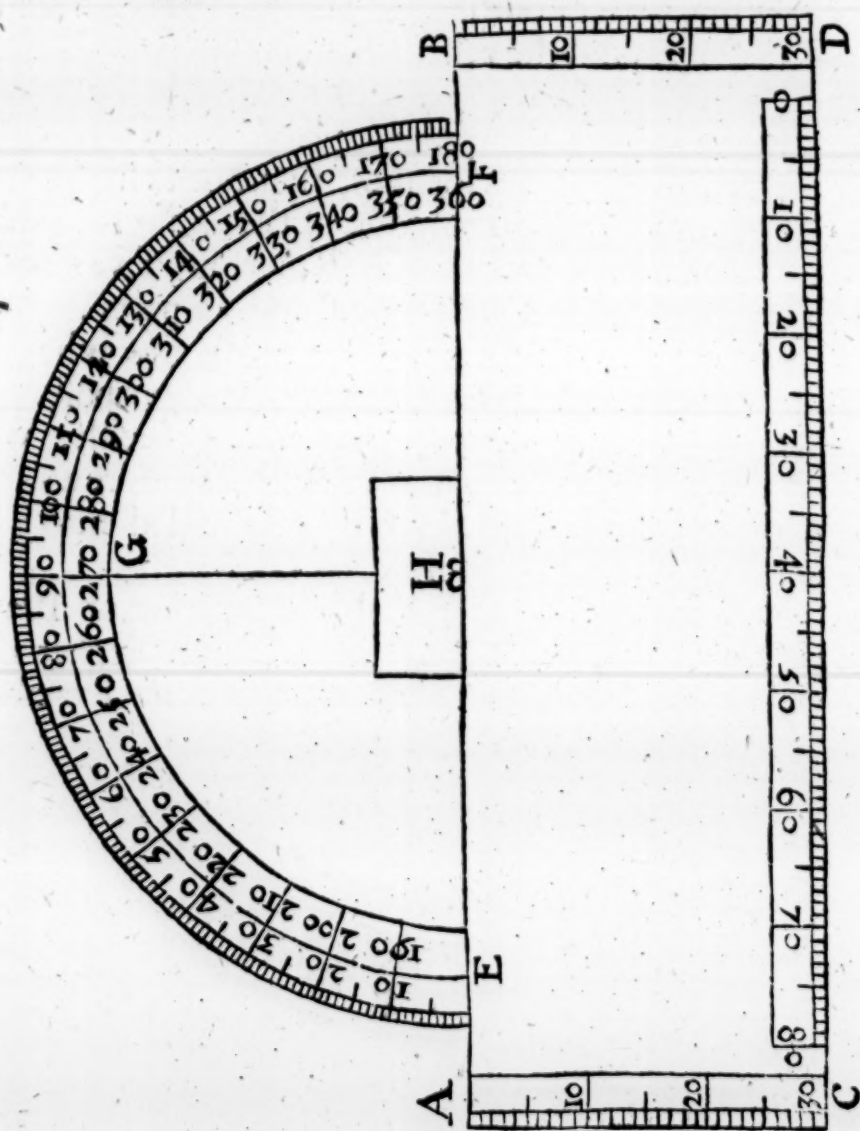
C H A P. II.

The Use of the Scale and Protractor.

UPON the Brass Rule are several Scales of equal parts, as I said before, as of 10. 12. 16. 24. and 32 parts in an Inch, whose Use are principally to lay down, upon Paper, the length of any Line taken in the Field in Perches.

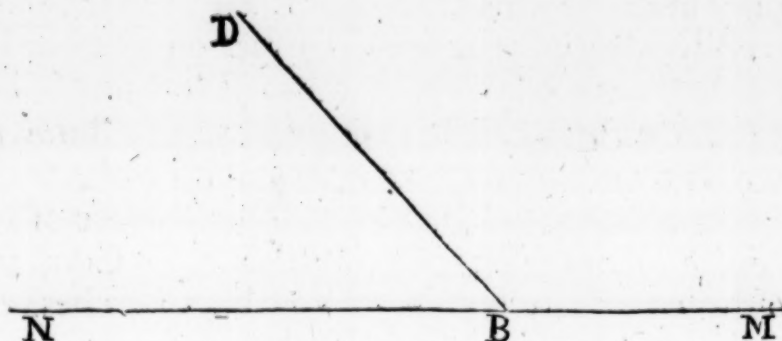
Upon the same Rule (or upon the Pocket-Rule) is a Scale of Chords, which serveth to protract and lay down upon Paper, the just quantity of an Angle; for if you open the Compasses to 60 Degrees thereof, and with that extent describe an Arch, you may therein set off what Degrees and Minutes you please, by taking the just Extension thereof from the Scale, with the help of your Compasses.

But in the Practice of Survey, when the Weather is moist, and you are forced to take the Quantity of Angles by the Degrees on the Frame of the Table, or by a Semicircle, you may speedily perform the Work thereof by the Protractor.

The Figure of the Protractor, and its Scale.

Suppose

Suppose it be required to lay down on Paper the true quantity of an Angle of 50 Degrees taken in the Field, upon the Line MN,



from the Point B, upon which Point place the Center of your Protractor, in such wise, that the Meridian Line thereof, noted with the Letters AHB, may lie exactly upon the Line MBN; so that the Center of the Protractor noted with H, lie exactly upon the Point B; then in the Limb of the Semicircle at 50 Degrees, note the Point D, and draw the Line BD; so shall the Angle DBM contain 50 Degrees.

But if MBD were an Angle given, and the Quantity thereof required, then place the Protractor as before, and the Limb of the Semicircle will tell you that the Angle DBM is 50 Degrees, and (laying the Meridian Line of the Protractor upon the Line DB) it will give you the Angle NBD to be 130 Degrees, it being the Complement of the Angle DBM to the Semicircle 180 Degrees. But these things you will find so easie, that I need not insist further thereon.

C H A P. III.

Of the Chain, with the Division and Use thereof.

SOME Surveyors still Work by a Chain of 16 parts in a Perch, others (as Mr. *Gunter* in his Description and use of the Sector, Cross-Staffe, &c.) divide the whole Chain of 4 Perches, into 100 Links; but Mr. *Aaron Rathborne* in his Surveyor, Printed Anno 1616. makes Division of every Perch into 100 parts: That is to say, first he divides each Perch into 10 parts, call'd Primes; each Prime whereof is again sub-divided into 10 parts more, which he calls Seconds; and this is commonly called the Decimal-Chain. But the Chain that I have usually made for my self, contains in each Pole 20 Links, so that in the Use thereof, I apply it to Decimal Operations, wherein to avoid Prolixity, I account two Links

to be one Prime, and one Link to be five Seconds; and yet notwithstanding in *Geodæsie*, or Land-measure (unless it be out of Curiosity) it is needless to go nearer than a Link of your Chain. But seeing my intent in this Chapter, is only to shew you how you may speedily Multiply the several Fractions of your Chain together, as if they were whole Numbers: I will first shew how to effect it by the Decimal-Chain invented by Mr. *Rathborne*; and then afterwards by my own of 20 Links in a Perch.

First therefore, Suppose I should measure a Piece of Land (lying in the Form of an Oblong, as most Lands in Common Fields do) and find the same to contain in Length 42 Perches, 6 Primes, and 4 Seconds; in Breadth 12 Perches, 8 Primes, and 4 Seconds; therefore to effect my Desire, I place my Numbers in all respects, as is usually done in Whole Numbers; and over every Fraction of the Multiplicand, place a Prick, or Point, and at the end of the Multiplier, place also as many Points as there are Fractions in that Number; then Multiply your two Sums together, as though they were Whole Numbers, and the Product will tell you how many Perches, and parts of a Perch, are in that parcel of Land; only you must observe, That so many Pricks as you made, so many Figures must you cut off from your Product to the Right Hand; so will you have the true Value of your Land in Perches, and parts of a Perch; as the Example following will more clearly demonstrate.

An Example of a piece of Ground, whose Length is 42 Perches, 6 Primes, 4 Seconds; the Breadth 12 Perches, 8 Primes, 4 Seconds; which are thus Multiplied together, as if they were Whole Numbers.

Here you see there are two Fractions in the Multiplicand, which are noted with two Pricks over Head, and as many in the Multiplier, as they are marked towards the Right Hand; so that, as you see, after the Operation is performed, because I have four Fractions, I must strike off with a Dash of my Pen, the four last Figures of the Product towards the Right Hand, and then will the Product stand thus, 5474|976. which intimate, that there are contained in this piece of Land, 547 whole Perches, and $\frac{4224}{10000}$ parts of a Perch, which is near upon half a Perch.

$$\begin{array}{r}
 \dots \\
 4264 \\
 1284.. \\
 \hline
 17056 \\
 34112 \\
 8528 \\
 4264 \\
 \hline
 5474|976
 \end{array}$$

But because a Chain of 20 Links in a Perch is more ready, and altogether as exact as the former, I will also shew you in one Operation how you may readily and truly work thereby. Therefore suppose a piece of Land be in length 36 Perches, and 16 Links, and in breadth 3 Perches, and 2 Links; and because I have 20 Links in a Perch, therefore that I may perform the Operation in a Decimal-way, I account but half the Number of my Links, and then the Sums will stand as follow.

Now

Now Multiplying the two Sums together, as before was done, and marking the Fraction, I find the Sum of the Multiplication to be 11408. and in regard of the two Fractions, I strike off the two last Figures of my Product towards the Right Hand, and then the Sum will stand on this wise, 114.08. which is 114 Perches, and one 8th part of a 100; and so much is the said piece of Land, according to Statute Measure.

$$\begin{array}{r} 368 \\ 31. \\ \hline 368 \\ 1104 \\ \hline 11408. \end{array}$$

But if the Land had been 36 Perches, and 9 Links in length; and 3 Perches, and 3 Links in breadth; then you are to place the Numbers thus.

Multiplying the two Sums together, and from the Product cut off the four last Figures, because of the four Fractions, and then the Sum will stand on this wise 114.8175, so that the Land contains 114 Perches, and above three parts of a *Perch*.

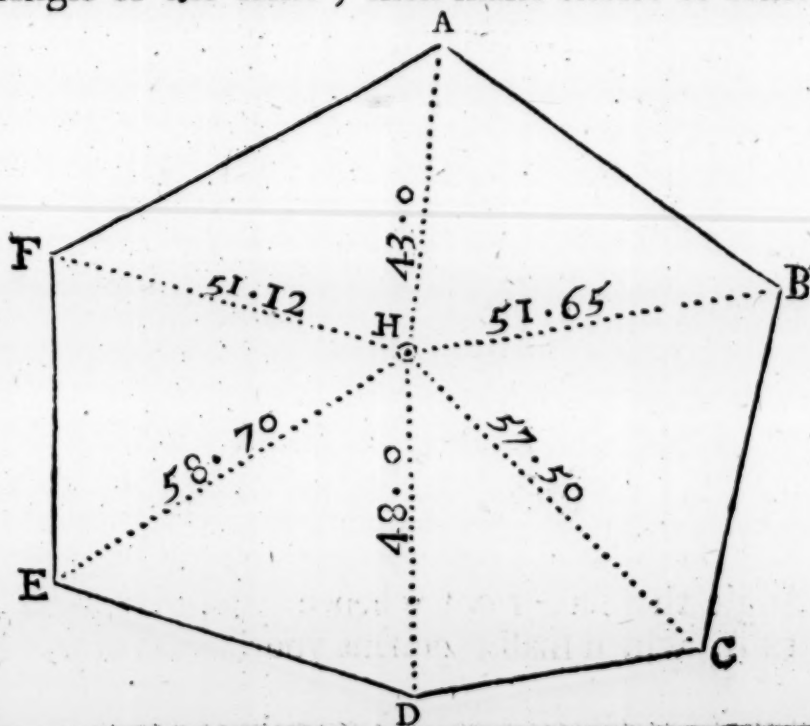
$$\begin{array}{r} 3645 \\ 315.. \\ \hline 18225 \\ 3645 \\ 10935 \\ \hline 1148175 \end{array}$$

But the Description and Use of this Chain, is more fully Illustrated in *Chap. 2.* of the *Appendix*; and in *Chap. 3.* of the said *Appendix*, is the Description and Use of a New Decimal Scale, exactly fitted to the Division of this Chain.

CHAP. IV.

To take the true Plot of a Field at one Station taken in any part thereof, from whence you may see all the Angles, or Corners, of the same.

Suppose ABCDEF, be a Field to be measured. First, cause white Papers, or visible Marks, to be set up in every Corner, or Angle of the same; then make choice of some conveni-



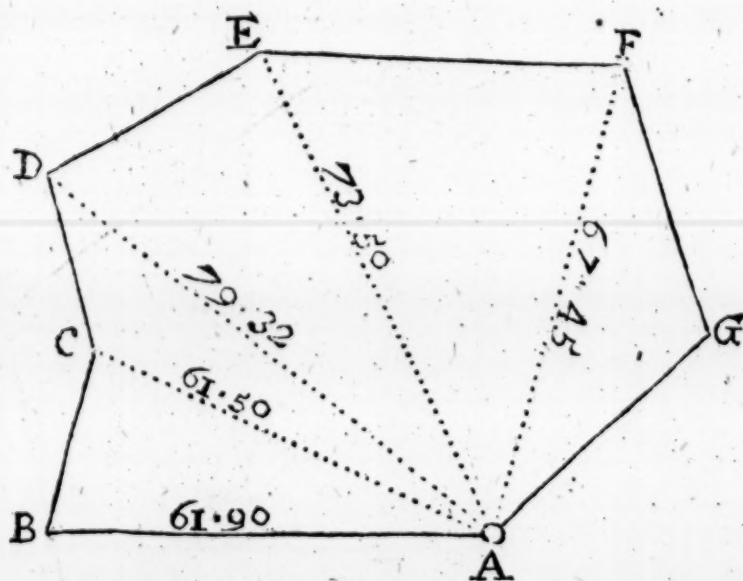
ent

ent place therein, from whence you may best view all the Angles thereof; in which place, as at H, plant your Table (covered with a Sheet of clean Paper), and so fasten it with the Skrew-pin, that the Table stir not, till your Work be finished. Then placing your Index upon the Table, lay the Fiducial-line thereof upon the point H, representing the place of your Station; and then direct your sight to A, and draw a Line with your Compass-point by the side of the Index upon the Paper; which done, direct your sight to B (still keeping the edge of the Index upon the point H) and draw a Line, as before; and so in like manner direct your Index to C, D, E, and F, drawing lines upon the Paper by the edge of your Index, with the point of your Compass, and having finished the same, measure with your Chain the distance of every of those Marks, from the place of your Station at H, and then by the help of your Scale and Compasses, set the same Distances, from the point of Station at H, in the Lines drawn upon the Table, making a small prick with your Compass-point, at the end of every of them; then with the point of your Black-lead Pencil, draw a small Line from one point to another, as namely from A to B, from B to C, and from C to D, &c. so shall you have upon the Table, the exact Plot of your Field.

C H A P. V.

To take the Plot of any Field at one station, in any one Angle thereof, from whence all the other Angles may be seen.

First, as before, set up Whites in every Corner of the Field, as at B C D E F and G; then make choice of the most con-



venient Angle therein, from whence you may best view all the rest, as A, which shall represent your place of station; and having

having fixed your Table there, as before is taught, apply the Index to the point A, and direct the sights to B; then draw the Line A B upon the Paper, and with your Chain measure the Length thereof, and set it down by the help of your Scale, from A to B.

Then, *secondly*, from the said point A, turn your sights to C, your second Mark; and then draw with the one point of your Compasses, upon the Paper, the Line A C, measuring the Distance, and setting down the Length by the same Scale, as you was before taught.

In like manner direct your sights to D, E, F, and G, and drawing Lines upon the Paper, measure with your Chain, the Distance of each of the same Angles from your Station-point at A, where your Table is planted; then, with your Compasses, take from the Scale the said Distances respectively, and set them down from the point A, upon the several Lines, A D, A E, A F, A G; so shall you have upon the Paper, the points A B C D E F, by which Marks you may, by the help of a Black-lead Pencil, finely pointed, describe the Lines A B, B C, C D, D E, E F, F G, G A, which will exactly represent the just Figure of your Field upon the Table, which will be greater, or lesser, according to the Scale you work by.

CHAP. VI.

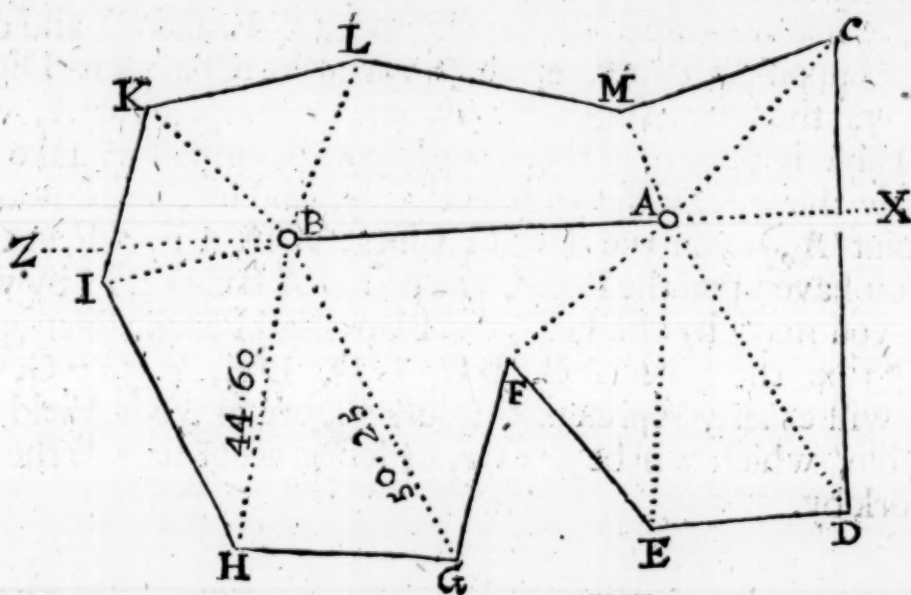
To take the Plot of a Field at two Stations, when as all the Angles thereof cannot be seen at one.

IT oftentimes hapneth, through Hills, or the Spaciousness of the Ground, that you cannot from any one place of the Field, see all the Corners and Angles thereof; in which Case it becometh the Surveyor to make choice of two of the most convenient places within the same: So that here you are to perform that by the help of two Stations, which before was effected at one.

Suppose therefore, that the Figure noted with the Letters C D E F G H I K L M, be a Field to be plotted, which lieth so, that from no one place all the Angles thereof can be seen; therefore I make choice of two places within the same, for my Stations, as A and B, where I can conveniently view all the Angles. And first, I plant my Table in A, from whence I can see the Angles M C D E F; then placing the Edge of my Index (after the Table is fixed) upon the point A, I direct my sights severally to all the Angles within my View, as to M C D E F, drawing Lines
as

as before is directed in the preceding Chapters; which done, I measure every of them with my Chain, and note them down from my Scale, as formerly I shew'd.

Then (my Table remaining fix'd) I view the other parts of the Field, and make choice of the Point B for my second Station, because from thence I can see all the other Angles of the Field; then setting up a white, or other Beacon there, I go back to my first Station at A, (where my Table stands fix'd, as I left it)



upon which point I move my Index, till through the sights thereof, I espy the Mark at B; which done, I strike a Line by the fiducial Edge of the Index, with my Compass-point, extending it quite over the Table, as is represented by the Line Z X; which being thus performed, I measure the stationary Distance A B, finding it 53. Perches, 5. Links (or 25. Seconds,) which I set down from A to B, the place of my second Station, by the help of my Scale and Compasses, in such sort as I have formerly shewed.

Secondly, I plant my Table upon the Point B, and laying the Edge of my Index upon the Line Z X, I turn the Table about, till through the sights I behold my first Station at A; then I skrew the Table fast to the Staff; afterwards moving my Index upon the point B, I direct the sights first to G, drawing the obscure Line B G, containing 50 Perches, 5 Links: Then again I direct the Index to the Angle H, and find it distant from my station 44 Perches, 12 Links, or 60 Seconds; and thus turning my Index about upon the point B, I draw obscure Lines towards the other Angles at I, K, and L, as I did before, and measuring their respective Distances with my Chain, I prick down the said points I, K, and L, upon my Paper, ever observing to take off with my Compasses, upon the Scale, the exact quantity of Perches and Parts, measured with the Chain. Lastly, the several Points, or Angles of the Field, at C D E F G H I K L and M, being found out, and mark'd upon my Paper, I draw the

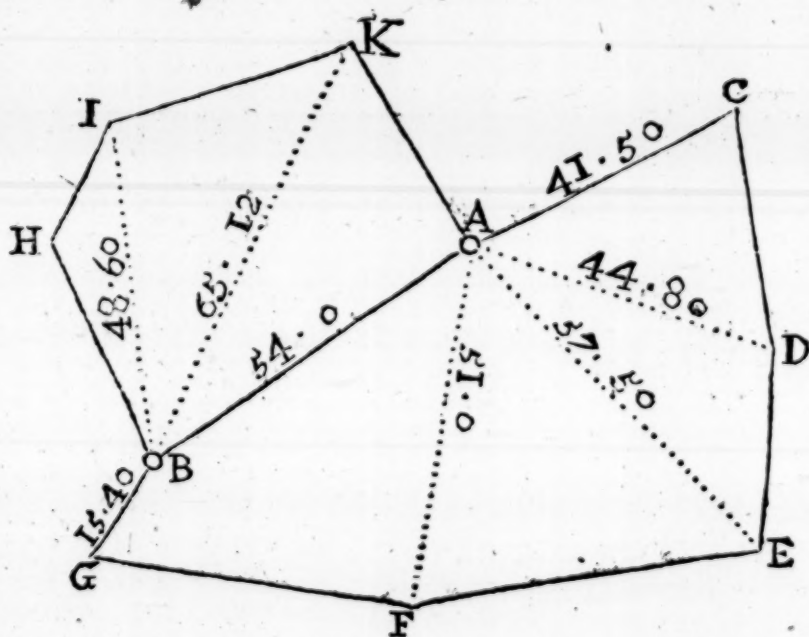
Lines

Lines CD, DE, EF, FG, GH, HI, IK, KL, LM, and MC, which will represent upon the Table, the exact Plot of the Field to be measured.

C H A P. VII.

To take the Plot of a Field from two Angles, when as all the said Field cannot be seen from one.

THis work differs little from the former, for whereas there you made choice of two places within the Field, for your two stations, from whence you may view all the angles; so here you must take two of the most convenient angles for the same purpose. Therefore suppose this figure A C D E F G B H I K, be a Field to be plotted, whose angles cannot all be seen from any one angle thereof, but as I go about the Field to view the same,



I immediately see, that the Angles A and B, are the most fit and convenient for my purpose, being seated upon higher ground than any of the other; wherefore, setting up a Beacon in the Angle B, I repair to A, where I plant my Table, and fasten it with the Screw-pin; Then upon the point A, I apply the fiducial edge of my Index, and direct the Sights thereof to C, and measuring the said distance with my Chain 41.50; prick it down upon the paper from A to C, according to its extention upon the Scale, and I make a prick with my compass-point, which will represent the point C. This done, I turn my index towards D, till
G through

through the Sights thereof I espie my Beacon there placed, then measuring the distance 44. 08, I set it down in the said line, and make a prick upon the paper, which will represent the point D. In like manner I deal with the Angles at E and F.

Then (my Table remaining fixed) I turn my Index about upon the point A, till through the Sights thereof I discover the point of my second station at B, and see the Thread cut the middle of my Beacon there standing: Then I measure the distance finding it 54. 00, which known, I open my Compasses to 54. upon my Scale of 32. to an inch, and prick it down in the line A B to B, where I again make a mark thus (⊙) upon my paper, for the place of my second station. Afterwards, I remove my Table from A to B (leaving a Beacon at A, when I came from thence) and placing my Index upon the stationary line B A, I turn the Table about, till at length I see (through the sights thereof) the Beacon I set up at the place of my first station; Then fixing my Table, as formerly I shew'd, I direct my sights to the severall marks, at G, H, I, and K, and strike lines upon the paper towards them; and measuring particularly their distances, I set 'em (by the help of my Scale) from B, to G H I and K, where I make small pricks with my Compass-point; and then drawing lines successively about the Perimeter, from point to point, you shall have the exact Simmetry and proportion of your Field, as it is represented in the figure by the former lines AC, CD, DE, EF, FG, GHI, IK, and KA.

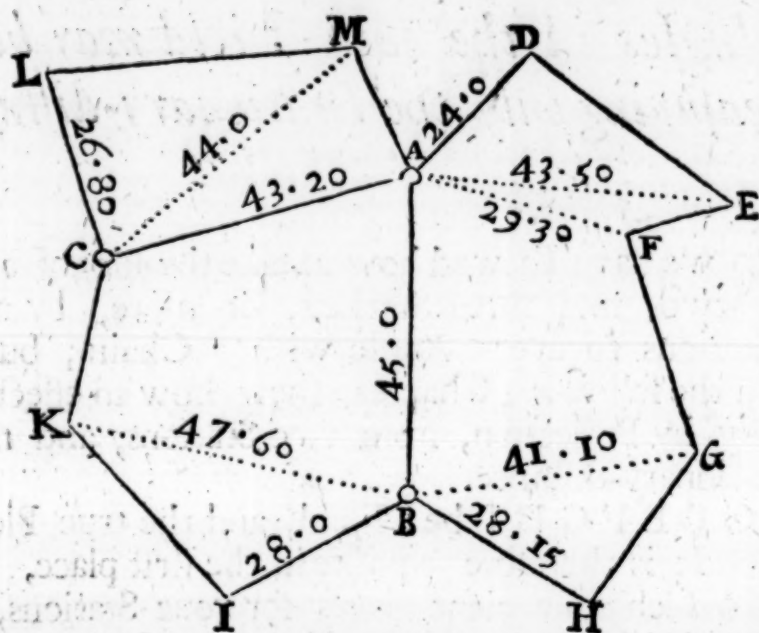
C H A P. VIII.

To take the Plot of a Field from three Angles when all the Angles cannot be seen from two.

Suppose this Figure be a Field to be plotted, and from no two Angles thereof, all the rest can be seen: Wherefore I make choice of three Angles, as A, B, and C; and beginning first at B, I turn my Index upon that point, directing it to I, H, and G, drawing forth the lines BI, BH, and BG, and setting down upon the same (by help of my Scale and Compasses) the particular dimensions found by the Chain, as is there expressed, I note the points I, H, and G.

Secondly, Setting the Index upon the point B, I turn it forward towards A, till thro' the sights thereof I see the Beacon there erected, to which I strike a Line upon the Paper along by the edge of the Index, as the Line B; A then I measure it with my Chain, finding it 45 Perches exactly, which taken off my Scale, I set the same extent, with my Compasses from B to A, making such a mark as this (⊙) which shall represent my second station, from whence (as before

before) having placed the Index, upon the Line A B, and set the sights thereof to cut the point B, I strike the Lines A D, A E, A F, and likewise measure them with the Chain, making a little prick upon the Paper at D, E, and F, which shall shew upon the Table the true Symmetry and shape of that part of the Field.



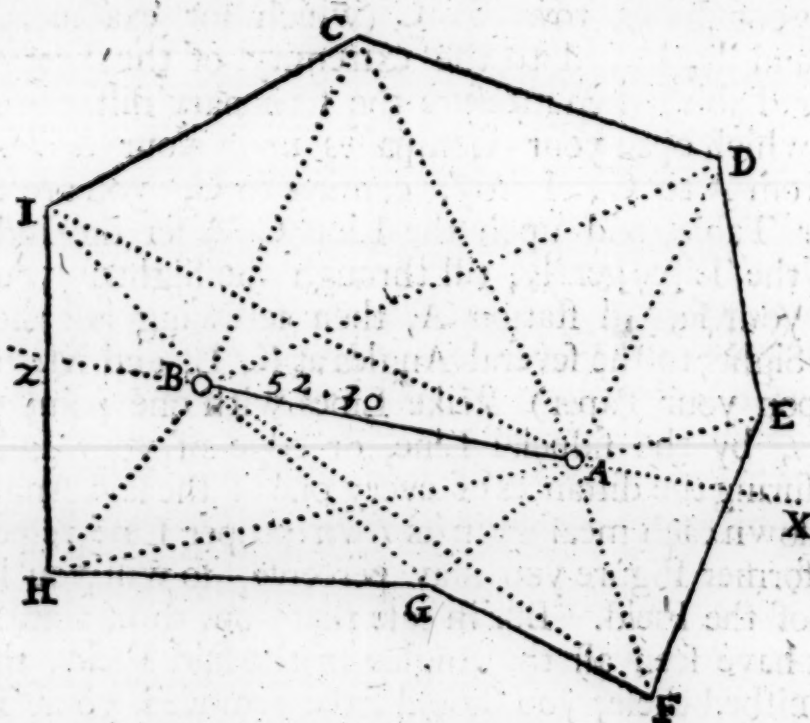
Thirdly, The Table standing steady, and fixed upon the point of that Second station A, and also rectified by the Line A B (for fear the Table should be alter'd) you are then to turn the Index upon the point A, towards C, and when you shall (through the sights thereof) espie the Beacon at C, draw a Line along by the edge of your Index towards C (which for exactness, extend forward and backward to the extremity of the sheet of Paper upon your Table) then measure the stationary distance A C, 43 P 20, to which open your Compasses upon your Scale, and set it down from A to C, Lastly, coming to C, you are there to erect your Table, and upon the Line C A set the Index, and then turn the Table gently, till through the Sights, you see the Beacon at your second station A, then screwing fast the Table, direct the Sights to the several Angles at K, L, and M, towards which (upon your Paper) strike Lines with one point of your Compasses, by the fiducial Line, or edge of your Index, and then measuring the distances of every one of the said Angles from you, set down each measure in its own proper Line respectively, as in the former Figure you may perceive, so will you have the true Plot of the Field. But in case that from three stations, you could not have seen all the Angles in the said Field; then after you had finished these, you should have removed your Table to a fourth, and there to have performed the rest, or as many as there you could, and if any remaining, to chuse a place for a fifth and a sixth station, &c. till you have finished; for the work will in effect be the same with the former.

C H A P. IX.

To take the Plot of a Field at two Stations within the same, from either of which all the Angles in the said Field may be seen, by measuring only the Stationary-distance.

Hitherto we have shewed how to take the Plot of a Field, at one, two, and three Stations, or more, by measuring from the Stations to every Angle with a Chain; but we shall now, and in the following Chapter, shew how to effect the same more speedily by Projection, from two Stations, and measuring only the Stationary-distance.

Suppose C D E F G H I be a Field, and the true Plot thereof is required. It is therefore requisite in the first place, to make choice of two such convenient places for your Stations, as from thence all the Angles in the said Field may be seen; as A and B, (which for the avoiding of Error, must be of a considerable distance,) then having set up Whites, or other marks in every Angle of the Field, plant your Table at A; where, upon the point thus marked (\odot), lay the edge of your Index, and turn it about towards C, till through the Sights thereof, you espie the White,



or other mark there placed, and then by the edge of your Index, draw the Line A C. Secondly, Turn your Index towards D, and draw the Line A D; and so in like manner proceed till you have

have drawn Lines from your point of Station A, to every Angle in the Field, as is lively exprest in the Figure.

Afterward (your Table standing fixed) direct your sights to your second Station at B, and draw a Line by the edge of your Index (and be sure to extend it far enough, that when you come to direct your sight back again to the first Station, you may not fail to lay your Index aright upon the Stationary Line,) Then exactly measure the interval of your Stations, which in this Example we find 52 Perches, 3 Primes, 0 Sec. which set down from A to B, then setting your Table at B, place the Index upon the Line Z, B, A, X, and turn it, till through the sights, you espie the point of your first Station at A, in which positure let your Table be fixed; which done, lay your Index upon B, and direct the Sights to all the Angles in the Field as you did from the first Station at A, drawing small Lines with the point of your Compasses along by the edge of the Index, and at the interfections of these Lines, are the Angles of the Field, as they are represented upon the Paper.

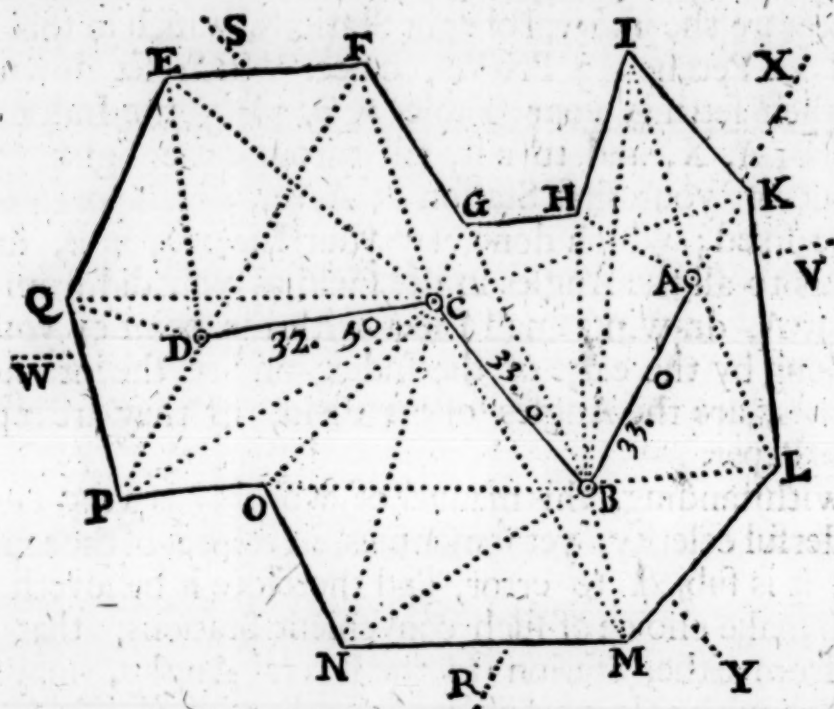
Notwithstanding, this manner of working is very facile, and of wonderful celerity, yet sometimes, in respect of the acuity of the Angles, it is subject to error, and therefore it behoveth my Surveyor to make choice of such convenient Stations, that all Lines drawn from either Station to the severall Angles, may intersect each other with as large Angles as may be: And if it be but discreetly performed, you shall not only find it of quick dispatch, but also accurate and marvellous useful; especially when you would on a sudden know the just quantity of a Field, and want time to measure it otherwise.

CHAP. X.

To take the Plot of a Field at divers Stations, by measuring only the Stationary-distances.

THE work of this Chapter differs not much from the last, and therefore I shall with brevity shew how to effect it. Suppose this Figure represent a Field, whose Plot is required. First, having set up Beacons in every Angle of the Field, make choice of the most convenient place for your first Station, which let be at A, where planting your Table, and setting the Index upon the Point A, direct your Sights to as many Angles severally, as are within your view, as to H, I, K, L, and accordingly strike Lines to every of them, as is before declared, which done, make

make choice of a fit place for your second Station, where you may not only see all the same Angles you beheld from the first Station, but as many more as you can, which imagine at B, then upon my Table standing fixed at A, I direct the sights to B, and measure the stationary distance A B 33 perches; then taking up my Table at A, and planting it at B, I place the Index upon the



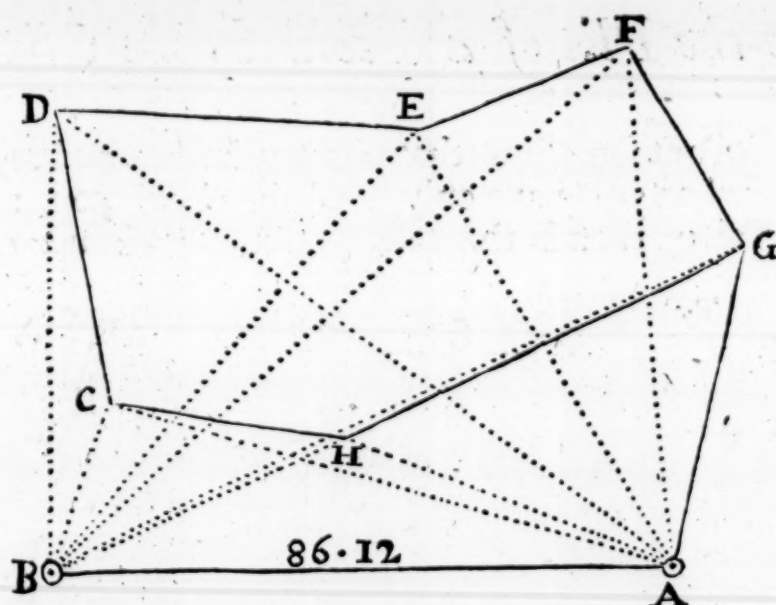
Line R B A X, and turn it gently about till through the Sights I see the Mark set up at my first Station A, and then removing the Index orderly, I direct the sights to all the former Angles (except K, which I cannot yet see) namely to H, I, and L, making a little prick where these Lines intersect the former; which done, observe what other Angles you can discover, as those at M, N, O, and G, and to these direct your Index, and accordingly, to each of them draw small Lines with the point of your Compasses, as before, then (letting your Table stand still at B,) find out your third Station, as at C, where you may not only view these former Angles at G, M, N, and O, and the Angle K, which at B could not be seen, but as many other yet unseen, as you can; then from B, direct your sight to C, till you espie the same, and measure from B to C 33 p. 0, which set from B to C in the Line Y S, When this is performed, plant your Table at C, and laying the Index exactly upon the Line S C B Y, move the Table till through the sights, you discover the point B, and then again direct the Index to those former Angles G, O, N, M, drawing small Lines till they intersect the former. Afterwards consider what other Angles you shall find within your view, as F, E, Q, P, being all the other Angles in the Field, till now unseen, to which direct your Index, and describe them as before. Lastly, your Table yet remaining fixed, set the Index upon C, and turn it to D (your last station) draw the Line V C D W, in which from C, measure the distance of your last Station 32 p. 50, placing it from

from C to D. Now having found the point D, lay your Index upon the line W D C V, and then turn the Table till you see the point C, and so placing the Index upon the point of the last station at D, I direct it to all those sever al Angles at F, E, Q, P, and where those lines intersect the former, make small marks, then draw a line from one Point to another where the lines intersect, as EF, FG, GH, HI, IK, KL, LM, MN, NO, OP, PQ, QE, which will represent upon your Table, the true Plot and Symmetry of the said Field.

C H A P. XI.

To take the Plot of a Field remote from you, at two Stations, when you are not permitted to come within it.

IT often times hapneth that you are call'd to measure a Field, and may not (either by Waters, Moorish ground, danger of Suit, or other impediment) enter into the same, yet you shall find the work easie enough to be performed, for it differs very



little from that manner of projection in the ninth Chapter, only that there your stations were both made within the Ground, and here they are without.

Suppose the figure C D E F G H, be a Field, wherein I may in no wise enter, yet of necessity must the Plot thereof be taken, and therefore I make choice of two convenient stations without the same, as A, and B, from each of which I can see all the Angles of the said Field; and having planted my Table at A, (the place of my first station) I place the Fiducial-Line of my Index

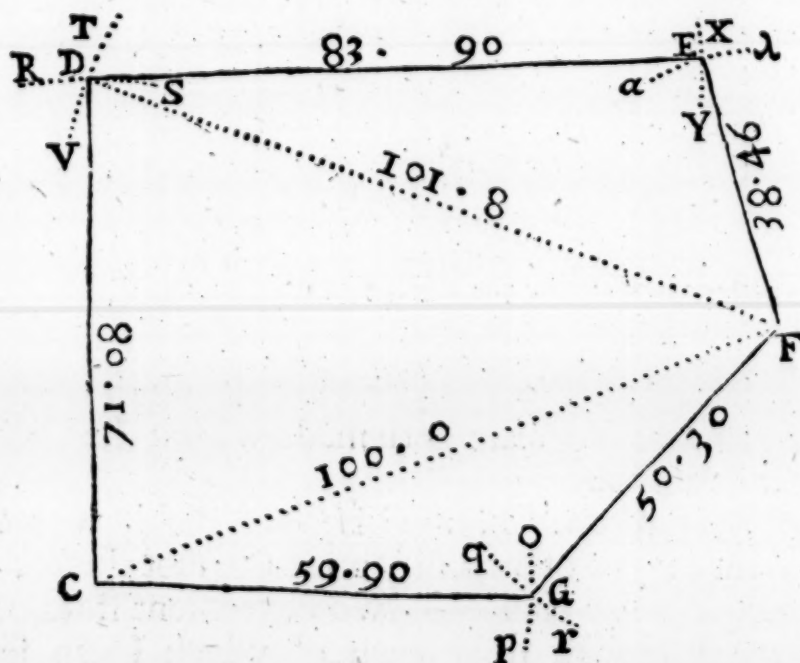
Index thereupon, and direct it (as before was shewed) to all the Angles of the Field respectively, drawing Lines with the point of my Compass, as AG, AF, AE, AD, AC, AH. Then (my Table remained fixed) from A, I direct the Index towards B, till through the Sights thereof, I espy the Beacon there placed, and having drawn out the Stationary Line A B of sufficient length, I measure the distance thereof in the Field, 86 p. 12 l. and place it on the Paper from A to B, then planting the Table at B, place your Index upon the Stationary Line B A, and then softly move the Table, till through the Sights, you behold the Beacon standing at A, which being effected, direct your Index to all the several Angles of the Field, as you did before at A; and the interfections of these Lines, will represent the several Angles of the Field, from which drawing the Lines CD, DE, EF, FG, GH, HC, it will shew the true Plot and Proportion of the Field.

But if all the Angles cannot be seen from two Stations, you may take three or four, and perform your work without, as you did within the Plot, in the last Chapter; but I need not further explain this Matter, for he that aright understands the one, cannot be ignorant of the other, they both depending upon one and the same Principle,

CHAP. XII.

To take the Plot of a Field by the Chain only.

IT may fall out sometimes that you may be required to measure a Field, when you have only a Chain about you, and cannot procure a Table, then in this case, you may make use of the way



here delivered, which in small inclosures, where the Lines are not much curved, will stand you in excellent stead. Let

Let this figure C D E F G represent a Field to be Plotted. First, I measure with my Chain from F to C, which contains 100 p 0, then I measure the side C G 59 p 90, and the side F G 50 p 30.

Which done, I open my Compasses upon the Scale to 100 p 0, and setting one Foot in the Point F, with the other I mark the Point C, next I take from my Scale 59 p 90, and setting one Foot in C, with the other I draw the Arch o P, then again with the distance F G 50 p 30, setting one Foot in F, draw the Arch q r, cutting the former Arch o P, in G; then drawing two lines from F and C to G, we have the Triangle F C G exactly described, according to the tenth Problem of the first Book.

Secondly, in the Triangle C D F, the side C D, contains 71 p 08, and the side F D 101 p 08, therefore (from my Scale) I take 71 p 08 and setting one Foot of my Compasses in the Point C, with the other I describe the Arch R S; next I take 101 p 08, (from my Scale) and setting one Foot in F, with the other I describe the Arch V T, crossing the former Arch R S in the point D, then drawing two lines from C and D to F, we have limited the Triangle C D F.

Thirdly, in the Triangle D E F, because the side D E contains 83 p 90, and the side E F 38 p 46; take 83 p 90, from your Scale, and placing one Foot in D, with the other describe the Arch X Y, then open your Compasses to 38 p 46, and setting one Foot in F, with the other draw the Arch α λ, intersecting the former Arch X Y in the Point E; Lastly extending two lines from D and F to E, you shall have the Triangle D E F, and so you have the entire Plot of the Field C D E F G, which is as exactly wrought, as if the Plot had been taken by your Index upon the Table.

More Examples I might add but he that rightly understands this, may perform any other. And albeit in the former Chapters, I have sufficiently shewed how my Reader may Plot any Piece of Ground whatsoever, several ways, after the most plain and easie Method that can be devised (which I hope will yield abundant satisfaction to all that Read and Practice it) yet forasmuch as it is often required to take the Plot of a whole Mannor (or any part of a Mannor) consisting of divers Severals, as Arable Pasture and Wood-grounds, it will be here necessary and convenient, to shew you an exact and perfect way how the same may speedily be effected; and to this End I shall, in the following Chapter, endeavour to explain the same, by setting forth to your view the best way to Plot any irregular ground, by going round about the same, and afterward shall give you a perfect and lively Model and Pattern of a Field, consisting of sundry Parts, wherein each Ground is to be Plotted and laid down together in an Intire Plot upon Paper, according to the just order and Proportion, as it lies in the Field.

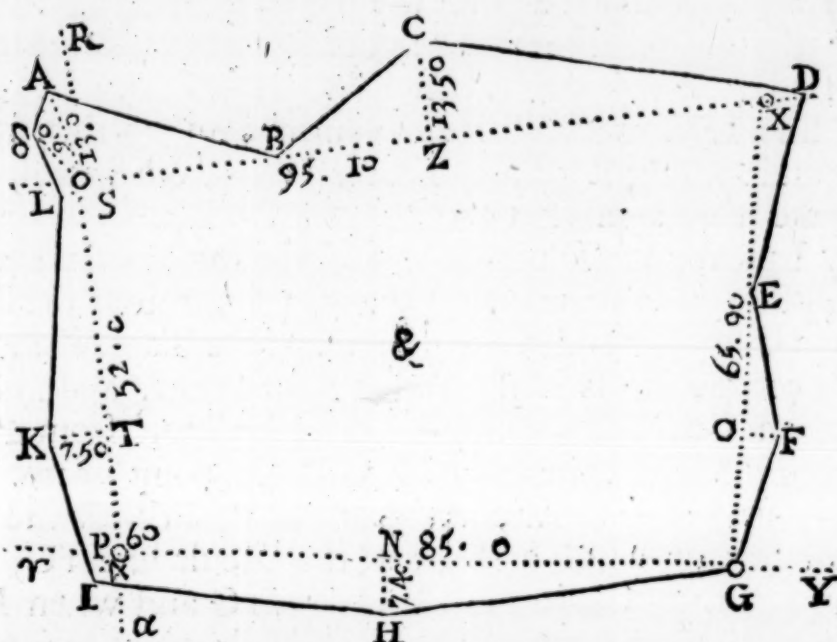
C H A P. XIII.

To take the Plot of a Field, by measuring, from one Angle to another, round about the same.

IN the former Chapters we have shewed after the most easie and artificial ways yet invented, how the Plot of a Field may be had and obtained several ways; yet because in Old Inclosure, it happens for the most part, that you can seldom find any of the Hedges straight, any considerable distance, and oft-times one side is bounded with some River, or other crooked Gutter, it will be requisite in this Chapter to shew you the most Common and Ordinary way used by my self, and other Practical Surveyors, which I shall here the more willingly do, in regard this manner of Working (which I know by long experience to be the most absolute of all others) is hitherto neglected by all former Authors, that have written upon this Subject; at least, they have so slenderly handled the same (perhaps for want of use and Practice) that very few, or none, that have Read their Works can reap any Profit from them, and therefore I shall here the more amply insist thereon. And to the end I might not omit any thing that may be Commodious to the Reader, it will in the first Place be very requisite to shew the young Practitioner what Scale is most fit for his purpose, in Plotting and laying out Inclosure, and other Grounds, First therefore in small Fields, that exceed not 60 or 70 Acres, you may Plot by a Scale of 10 or 12 parts in an Inch, and so bring your intended Plot all upon one sheet of Paper. But if your Field be larger, and under 200 Acres you may use a Scale of 16. If greater, and yet under 300 Acres, the Scale of 20, but if under 500 Acres, the Scale of 24, may serve your turn, however those of 16 and 20 in the Inch, are the ordinary and common Scales now used, for though your Ground contain 500, 1000, or 2000 Acres, yet may the Surveyor very aptly use them, by shifting of Paper, and afterwards in the House, putting the several Sheets together with Mouth-glew and so make an entire Plot thereof; yet if your Field consist of three or four thousand Acres, and you would have the Plot of a less proportion, you may use a Scale of 24 or 32 parts in the Inch, though for my part I never yet, these 25 years, that I have (in a manner) daily practiced the Art, ever used any Scale above 24. But because I would not exceed my intended limits, neither have the Diagrams too large for an ordinary Octavo, I shall (as before) in all my examples make use of a Scale of 32 in the Inch. But to my purpose.

Suppose

suppose this irregular Figure $ABCDEFGHIKL$ represent Field, into which when I first enter, I cause Whites to be set up in every Corner of the same, which done, I make choice of the most convenient Angles thereof for my Stations, not regarding their number whether I make 3, 4, 5, or 6. Stations, yet the fewer the better, but you must always take so many, as you



may clearly see from one to another. Thus in the former figure, I make choice of my first Station at X, as a place most fit for my purpose, in regard from thence I can see the Point L, and therefore I send one with a Beacon to S, so as when I go on in the Line XS, I may make a tangent at B, then planting my Table at X, I direct my Index to D, and strike the line XD, which I measure, finding it 5 p 30, and this I set down from X to D, and so make a Prick at D; this done, I direct the Index to S, And strike the line XS, then I measure one in the said Stationary line, till I come to Z, 47 p 30 from X, where laying my Index upon the line SZX, I direct the sights to X, and there fix the Table with the Screw-pin, then turning the Index upon the point Z, till through the sights I espie the White at C, I then strike the line ZC, and finding the distance 13 p. 50, I set it down from Z to C, where I make a point, and draw the line DC. Then I go on with my former measure till I come to B 68 p 40 and there I make a Point, and draw the line CB, which done, I go on carefully with my former Measure till I come to the place of my Second Station at S, finding the Stationary-distance XS 95 p 10, which from my Scale I apply from X to S, where I make for my second Station such a mark as this (⊙) then planting my Table there (as I shewed before) I direct my sights to A, & and L, and I find SA 13 p. 0, S & 9 p 0. and SL 3 p 0, which set down severally upon their respective lines, I have the points A, & and L upon the Paper, then drawing the lines AB, A & and & L we have one the side of the Field described.

Secondly, I plant my Table at S, and laying the fiducial line of the Index upon the line SX, I move the Table till through the sights I espie the Point X, then fixing my Table, I turn my Index about upon the point S, till through the sights I see the Beacon at P, and by the edge of the Index, I draw the line SP, which done, I proceed, and measure on the Stationary-distance, but as I go on and am come to T, 35 p from my second Station, I observe I am in a manner against the Angle K, wherefore I plant my Table there, and direct the sights to K, then I measure the distance, finding it 7 p 50, which I set down from T to K, and draw the line LK, which done, I continue my former measure ST to P, and finding it 52 p 0, I set it down from S to P, where again I make such a mark. (○)

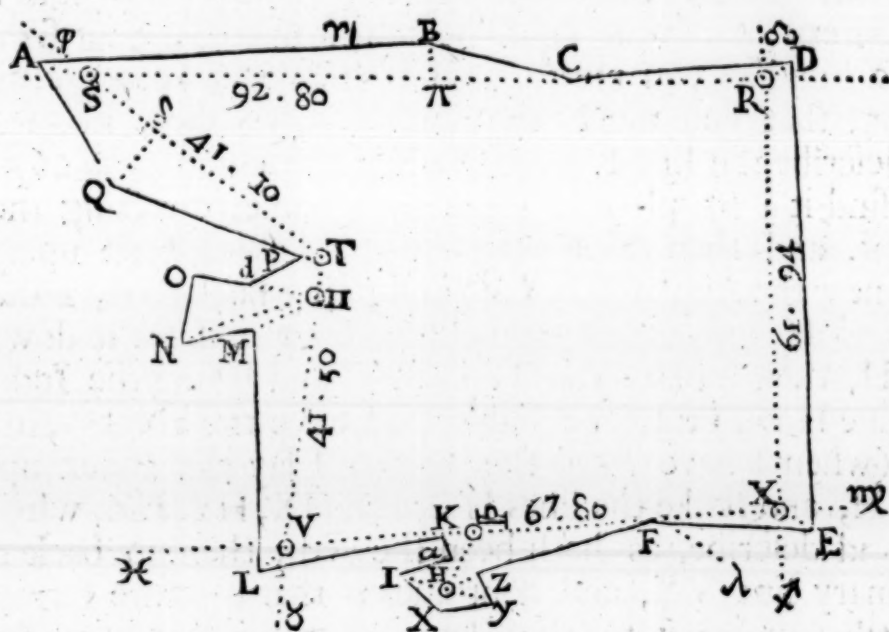
Thirdly I plant my Table there and laying my Index upon the line α PSK, I turn the Table about, till through the sights I see the place of my second Station S, then (the Table being there fixed) I direct the sights of my Index from P to I, and finding it (by the Chain) to contain 4 p. 60, I set it down from P to I, which done, I describe the line KI with the point of my Black-lead Pencil, as before. Afterwards from P, I direct the sights to my last Station at G and draw the occult line PG, then I measure on with my Chain from P towards G and when I come to N 37 p 10, (where I make a prick with the point of my Compasses) I perceive I am almost against the Angle H, then laying my Index upon the line PG, I turn the Table till I espie G with the Foresight, and P with the Back sight (by which you may know whether you be exactly in the line or no,) which done fix your Table, and direct your sights from N to H, pricking down the distance 7 p 40, and so with my Pencil describe the line IH, and after this is done, continue on your former measure began from P till you come to G (your last Station) which you shall find to be 85 p 0, which set down to G and mark it again thus. (○)

Lastly, At G plant your Table, and lay the Index exactly upon the Line YGP^r, then turn the Table gently (for fear of shaking the Index off the Line) till through the Sights you espie the Beacon at P, which done, fix your Table and remove the Index, directing the Sights from G to the place of your first Station at X, where you began, and if it cut the mark, it is very probable that your plot is exact; then I measure on towards X, and when I have gone to O, 18 p 60 from G, I describe the Angle F, drawing the Line GF, and measuring still on, I find the tangent point E 39 p 30 from G, which I note with the point of my Compass, drawing the Lines FE and ED; which done, I continue on my former measure in the Line GX, finding it to be exactly 65 p 90, then because the same extent taken from the Scale, falls upon the Plot precisely in the point X, where I first began, it is an infallible sign that the Plot of the Field is exactly taken.

Now because this manner of plotting ground is the most excellent

cellent of any other, and is that which the Surveyor shall find at all times most apt for his Purpose, it will not be amiss to give you another Example, wherea Field runs into many irregular Nooks and Corners, wherein I will use all possible brevity-giving you only a short demonstration, in regard I have explained the former figure so fully already, so that he that knows how to perform this one, may quickly apprehend the work of the other: for they are both grounded upon one and the same Geometrical principle.

Let us suppose this Figure noted with the Letters A B C D E F Z Y X I α L M N O d P Q be a Field, whose Plot is required. First, (when you have set up Beacons in every Angle thereof) plant your Table at R, and from thence direct your Sights to S,



remembering as you measure on the Line R S to mark the Tangent at C, which falls out at 26 p 30, and after you have measured on to π 45 p 70, take the distance of that Angle, from your Stationary line, at B 4 p 60, which note as before, then Measuring on to S, you shall find the whole length of the Stationary line RS to be 92 p 80, at the end whereof mark the Point S. Afterwards setting your Index upon the said Stationary line, turn the Table till through the sights you see the Beacon at R, and there fix it, then Direct the sights from S to T, and as you measure on that line, Remember when you come to δ , to take the Angle Q, as before was shewed, but go on still measuring the Stationary line to T 41 p 10, and on your Paper at T, make a mark thus (⊙) for your second Station: and this being done, lay the Index upon the line λ T S ϕ and turn the Table, till through the sights you see the Beacon at S, in which Situation fix your Table, and then direct the sights to your 4th Station at V, drawing the line T V, (noting it on the edge of the paper on both sides the Table as at π and δ) then from my Station-point T, I direct the sights to P, which I measure, and describe, as I formerly

merly taught, drawing black lines from point to point, for the out-bounds of my Plot, as I go on; which being performed, I measure the Stationary line $T V$ $41 p 50$ and mark the point V upon my Plot, but as I was measuring on that line, and had gone from the point of my third Station T to $116 p 0$, I find That a convenient Place to take the Angles d, O, N and M , and therefore setting down my Table there, place the line TV , upon my Table Answerable to that in the Field, which I do by my Index, as before is shewed, then I direct the sights severally to all the said points, and after they are measured, let them be set down upon the Paper as before.

Fourthly, plant the Table at V , and laying the fiducial edge of the Index on the line $\propto V T \propto$, turn the Table, till through the sights you see the Beacon at T , then fix the Table, and from the point V direct the sights to L , describing it as formerly. Afterwards (your Table being still fixed) set your sights from V to X , and as you measure on that line and are gone from V $21 p 95$, that you touch the hedge at K , there make a mark and describe the line $L K$, and when you come to $\approx 26 p 0$ from V , I find it a fit place to plant my Table, directing the sights to $V \propto$, and then (Screwing fast the Table) I set up a Beacon at H , near the Angles I, X, Y, Z , and going back to \approx , I direct my sights to H , and finding the distance $9 p 0$, I set it down from \approx to H , then I plant the Table at H and laying the Index upon the line $H \approx$, I turn the Table till I espie the Point \approx , in which scite (when I have fixed the Table) I lay the Index upon the point H , and strike the lines $H \alpha, HI, HX, HY, HZ$, which measure and describe, as hath been shewed; then go back to your Stationary line VX , and continue on that measure formerly began, till you come to the Tangent point F $50 p 0$, from V , where make a Mark with the point of your Compasses and draw the line ZF , and keeping on measuring to X , I find it $67 p 80$. Lastly, planting the Table at X in its due order, direct the sights to E striking the line XE , then measure its distance and set it down as before, drawing forth the lines FE and ED , which done lay the Index upon the line $\propto XR \propto$; and if through the sights you espie the point R , where you began, it is an argument your work is good, but for further Trial of the Truth thereof you are to measure the line XR upon the ground, and if it agrees exactly with your Plot, it shews that the Plot is truly taken.

In this like manner you may take the Plot of a Wood, or other Moorish Ground, by going round about, and making observation at every Angle, as you see it performed in the Work of this Chapter.

There is one thing necessary to be observed, that when you are Plotting of Ground how you may know by your Chard and Needle whether you set your Index upon the right line, or not, for sometimes when you have many lines upon your Plot, and are in hast of Business, you may soon (through the Multiplicity

of

of lines) commit an error of this kind, and so when you come to close the Plot, you may discover your error, and not before: To avoid this Inconvenience, you are (as soon as you have Planted your Table at your first Station) to observe at what degree the Needle standeth, and if you work true, and mistake not your line, you shall find it stand upon the same Degree, at every Station round about the Field, but if there be any error in your Work (as there must of necessity when you direct the Index back upon a wrong line) then will your Needle stand upon some other Point distant from the former, in which you began, which will be more or less from the same, answerable to the reflection of the line you took from the true one. Let me therefore advise, that at every Station you have special regard hereunto; so that if you chance at any time to fail, you may rectifie your error, before you depart from that Station.

And now I am speaking of the Chard and Needle in your Table, I will not advise you at any time to plant the Table thereby, as some do; for I well know it is too small and insufficient for that purpose; but rather (as I have all along taught) to make use of fore-sight and back-sight, from station to station round about the Field. And thus much I thought fit to admonish you of.

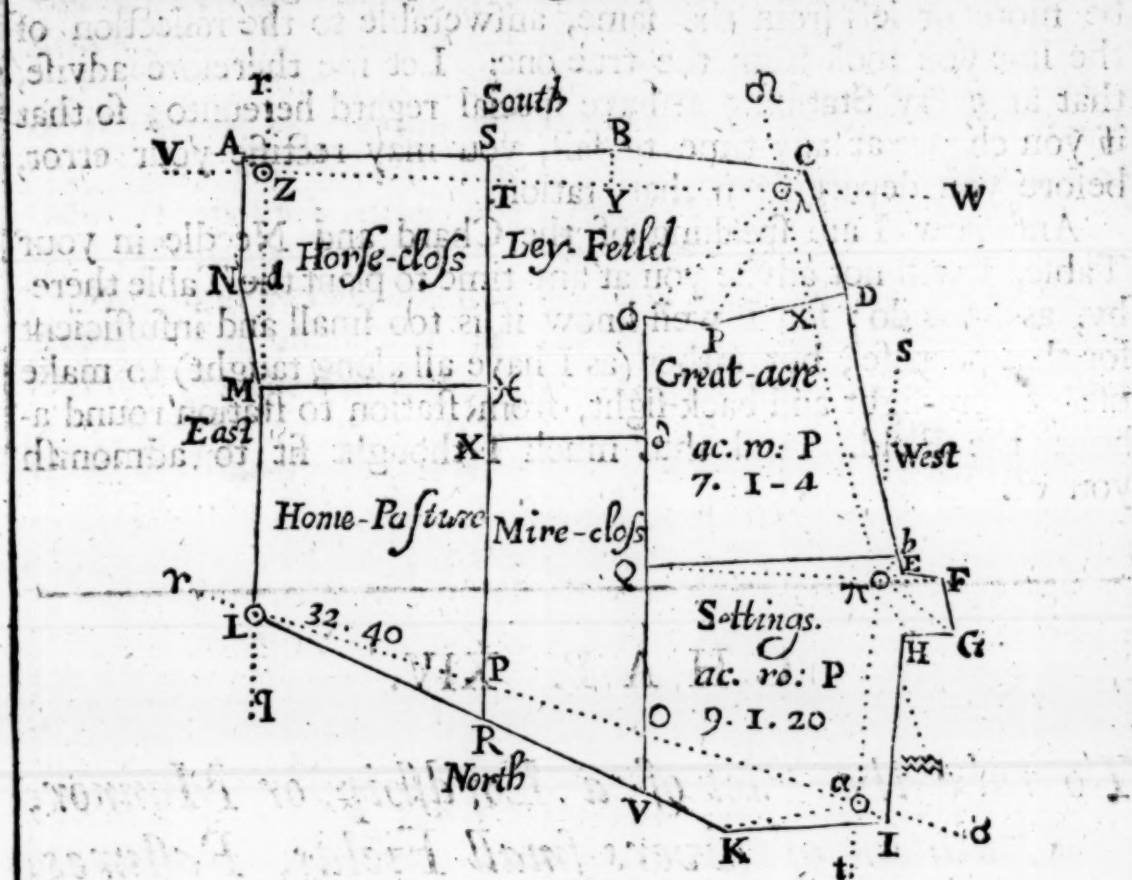
C H A P. XIV.

To take the Plot of a Lordship, or Mannor, Consisting of divers small Fields, Pastures, Wood-grounds and the like.

HAVING in the former Chapters sufficiently taught how to Plot all manner of Grounds whatsoever, I shall not here particularly reiterate my former Demonstrations, and yet shall shew how you are to proceed about the same.

Suppose this Figure, or Diagram, be part of the Mannor of *Burton-Lazers*, near *Melton-Moubrey*, in the County of *Leicester*, which is to be Measured and Plotted. First therefore, according to the directions before delivered, after I have made choice of convenient Places for Beacons, as at α , π , λ , Z and L) I plant my Table at α , where having described the Angles I and K, I draw the line K I, then I direct the sights to π , to which I measure and there planting the Table I direct the sights severally to H, G, F, e, b and Q, and by the help of my Scale and Compasses I describe them, as hath formerly been shewed, drawing the lines, IH, HG, GF, Fe, e b and b Q. Next (the Table remaining fixed) I set my sights to λ , which I measure finding it

it 56 p 55; but as I come on to X 39 p 0, from π , I intersect the Hedge DPO in the point X, which I note with the point of my Compass. Again I plant my Table at λ , in such manner as hath been formerly taught, and describe the lines λC , λP , λO , which I measure severally, and set them down from my Scale, drawing the lines ED, DC, DP, PO, then directing the sights from λ to Z, I measure the distance 71 p 60, which I prick down from λ to Z, and mark the point Z; but as I go on that line, when I come to Y, I take the depth of the Angle B 5 p 0, which I describe as in the Figure, drawing the line CB; and



likewise when I come to T, and intersect the Hedge TP, I make a mark there; and being arrived at Z, I plant my Table, where I rectifie the same in all respects, as is shewed in the former Chapters; which done, I describe the Angle A, then I set the sights to L, and measure the line, but coming to d , I describe the Angle N; and after I have measured 29 p 80, from Z, I touch the Hedge at M, where I make a Prick, drawing the lines AN, and NM. Afterwards measuring on to L 61 p 50, I describe the line ML, then I plant my Table at L, directing the sights back to Z, and the Table standing fixed, I lay the Index upon the line $\gamma L \alpha 8$, and if it cut the Beacon at α there is hope the Plot will close: next I measure on in the same line and when I come to P 32 p 40, from L, I make a mark drawing a line from P to S, (because the line is straight) in which line I measure from P to X, and find it 34 p 0, and from X to κ 9 p 60, which I describe drawing the line κM , so is *Horse-Cloffe* and *Home-Pasture* finished: Then I continue my measure forward

ward in the same line till I come to O 56 p 80, from my Station at L, and there making a mark, I draw the line O δ O; then I measure on in the same line to δ 41 p 10 and draw the line δ X, which done I perceive the whole work is finished, and I have obtained the Plot of the whole Field, and every Ground contained therein. And if there had been more Grounds you should have dealt in like manner with them, and proceed from one Close to another till the whole be finished: and if there be any Houses and Homesteads, you are to take them in and describe them; as also all *Streets*, *Lanes*, *High-ways*, *Mills*, *Trees* and the like; but Practice, better than many Words, openeth this: Yet one thing in this manner of working I cannot omit, that when you come to take the Plot of a Town that is Spacious, (which commonly lies within the body of your Plot) you must proceed from *Street* to *Street*, and from *Lane* to *Lane*, describing all the said *Streets*, *Lanes*, *Houses*, *Homesteads*, and other edifices, which lie within your view as you go; and if you cannot conveniently go about them, then at Gates and other open Places, you must (from your main Stationary-line) make little inward Stations, in meet and convenient places, which you shall find very commodious in making a true Plot. But if you can pass through back Lanes with your Table, and have the liberty to make fit Stations on the out-sides, it will better serve your purpose, but I leave this to your own Consideration, not doubting but that from what is already said, you will be thoroughly enabled, not only to take the Plot of a Single Field, but also of a whole *Mannor*, whenever the same is required.

Having now shew'd you (with some brevity) after what manner you are to proceed about taking the Plot of less and greater quantities, and many severals together, as a whole Lordship, or *Mannor*; and what course is most fitting in laying down and describing the true proportion and symmetry thereof upon Paper (which I might have done after a far larger Method; but I should then not only have been more tedious and Prolix, but also more obscure and less profitable to my Reader:) and therefore it may suffice to give you onely the Plot of a part of a *Mannor*, by which you may by Inspection, and the help of what hath been afore delivered; see the whole progress of my proceedings in doing the same and may thereby be able to do the like, as oft as occasion shall require it: See the Scheme in Chap. 27 of the following Appendix.

C H A P. XV.

To take the Plot of a Field by the Degrees on the Frame of the Table.

WHereas in wet weather you cannot keep a sheet of Paper upon your Table, it will be convenient in a few words, to shew you the way how to effect the same, by the Degrees on the frame of the Table. The use whereof is thus.

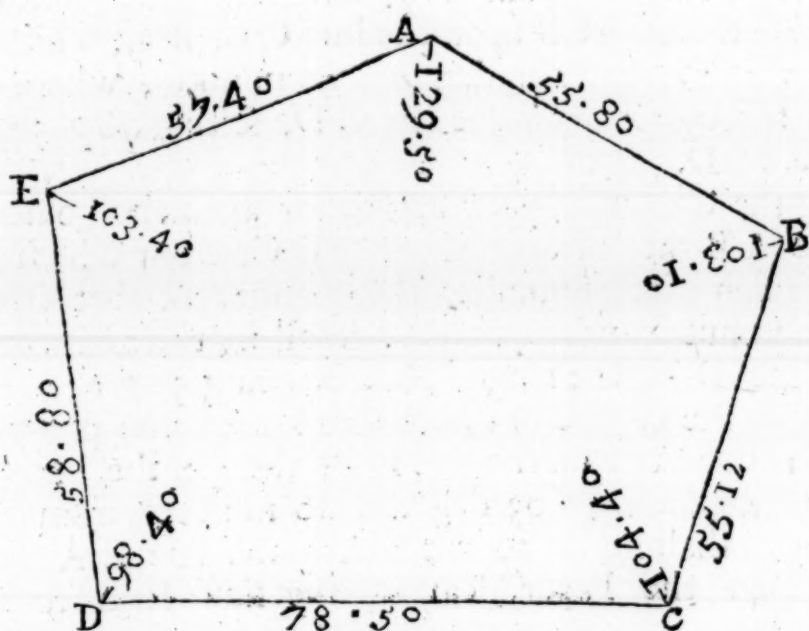
Place your Table at the Second Angle, and having Screwed it fast, turn the Index about upon the Centre, till through the Sights you espie your Beacon erected at the first Angle, and Note the Degrees cut by your Index, upon the frame of the Table; then, turning your Index about, direct the Sights thereof to your Beacon set up at the Third Angle, and observe the Degrees there cut upon the Frame, and so by the difference of them you shall have the quantity of the Angle at your first Station: then measure the distance from the first Angle to your Station, which you are to note down in your Book, as also the quantity of the Angle before taken; next measure on to your second Station (which is the third Angle) and there plant your Table as before, taking the quantity of the Angle there made and the Stationary distance, both which insert in your Book, and so proceed from one Angle to another, till you have finished the whole Field, taking the quantity of every Angle and all your Stationary-distances, as shall be more fully declared in the following example.

Let A B C D E be a Field to be measured, and being wet and moist weather, I cannot put a sheet of Paper upon my Table; therefore, after I have set up my Beacons in every Angle of the Field, I first measure the side E A 57 p 40, and then I plant my Table at A, from whence I direct the sights to E, and I find it cut upon the Frame at 30 Degrees 10 Minutes: next from A, I set the sights to B, and find it to cut at 160 Degrees 0 minutes, the difference is 129 Degrees 50 Minutes, which is the quantity of the Angle at A, which I note in my Book, as also the side E A. This done, I measure on from A to B 55 p 80, and at B, I again plant my Table, where I find (according to the former directions) the quantity of the Angle 103 D. 10 M. which I set down in my Book, together with the side A B; and in this manner I proceed from Angle to Angle, and from Side to Side, till all is finished: so in this Example will all the observations taken in my Book stand thus,

Angles.

	Gr. Min.			Per. Pts.	
Angles :	A	129 50	Sides	A E	57 40
	B	103 10		A B	55 80
	C	104 40		B C	55 12
	D	98 40		C D	78 50
	E	103 40		D E	58 80
Sum.	540 00				

Now, that you may know whether or no you have taken all the Angles of the Field exactly; you are to collect the quantity of all the Angles found at your several observations into one Sum then multiply, the Semicircle, 180 degrees by a Number less by two than the number of Angles in the Field, and if the Factus hereof be equal to the total Sum of the Angles, then is your Work right and good, if otherwise, it is to be corrected.



Example. In the former Work the sum of the Angles was found 540 Degrees 0. Minutes, and their number 5; therefore I multiply 180 by 3, (which is less by 2 than the number of the Angles) and the Product 540 degrees 0. minutes agreeing exactly with the Sum of all the Angles in the Field, it argues that the Work is exactly performed. The Geometrical ground hereof depends upon these two Propositions.

1. *In omni Triangulo tres Angli simul sumpti, sunt duobus Rectis aequales.* Euc. 1. 32. Ra. 6. 13.

In every Triangle, the sum of the 3 Angles are equal unto 2 right Angles, according to our first Book and 17th Problem.

2. *Cujuscunque Triangulati latera sunt binario plura Triangulis à quibus constat.* Ra. 10. 2.

The sides of a Triangulate are more by two than are the Triangles

angles of which it is made, as you may see in the eighteenth Problem of our first Book.

Note, That this Rule holds good when all the Angles of the Field are inward Angles, or less then 180 *d.* but if greater, you are to take their Complements, and then work as before.

Now having taken the quantity of all the Angles and Sides of your Field, I will here shew you how to Protract, and lay down the same upon Paper.

1. Therefore having drawn forth the line AB upon Paper, place the Centre of your Protractor upon the point A, and lay the Scale thereof upon the same, from which line (upon the Semicircle of your Protractor) set off the quantity of that Angle 129 degrees, 50 minutes, and draw forth the line AE, 57 *p.* 40, from your Scale, and the line AB 55 *p.* 80.

2. Lay the Centre of your Protractor upon the point B, and the Side thereof A F upon the line BA before described; and upon the Semicircle of your Protractor set off the Angle B 103 degrees, 10 minutes, drawing forth the line BC 55 *p.* 12, by your Scale and Compasses.

3. Lay the Centre of your Protractor upon the point C, and place the Side thereof AB upon the line CB, from which (upon the Semicircle) number 104 degrees, 40 minutes, where make a mark, and through it draw the line CD, setting 78 *p.* 50, thereon, from C to D.

4. Bring the Centre of your Protractor upon the point D, and set the Side AB thereof upon the line DC, from which (in the limb of the Semicircle) number the quantity of that Angle 98 degrees, 40 minutes, where make a small mark, and through it draw the line DE, the length thereof being 58 *p.* 80.

Lastly: Lay the Centre of the Protractor on the point E, and the Side thereof AB on the line ED, then in the limb of the Protractor, accounting 103 degrees, 40 minutes, from the said line ED, you shall find it to cut exactly the line EA formerly, described upon the Paper, leaving the side EA to contain 57 *p.* 40.

Thus have you now protracted the said Field, according to the observations you made by the degrees on the Frame of your Table: But you shall find that Practice, better than many words, will make this apparent; however this manner of working, as it is more troublesome and difficult than any of the former ways before described, so may the Surveyor be sooner mistaken in it, than in any of the rest; and therefore, as I have plac'd it last in order, so I would never have my Surveyor use it, but when necessity compels him, as in wet and stormy Weather; and the rather, because it takes up more time and labour than ordinary, to little purpose; but I leave it to the consideration of the Reader, to whom (I hope) I have given abundant satisfaction in the preceding Chapters.

C H A P. XVI.

Of the Measuring of Hills and Dales, with the best way of Plotting thereof.

First take the Plot thereof by the Perimeter, according to the 13 Chapter, and resolve it into the greatest Trapezium that the Plot will bear, then let fall Perpendiculars to the Base; which done, go into the Field, and measure with your Chain those lines which represent the Base and Perpendiculars, which you shall find longer than those lines in the Plot, and cast up the Plot by those Numbers, not by those lines, and you shall have, not only a true Plot thereof, but also the just quantity and content, as the ground is unlevel. Other ways I could shew you, but being troublesome and not so exact as this, I will at this time omit them.

C H A P. XVII.

To find the just quantity, or content, of any piece of Ground.

Although in the third Book I have shewed how to measure the superficies of any regular Figure whatsoever, as the Geometrical-square, Parallelogram, the Triangle, Trapezium, the Circle, and the like; and also how to measure any irregular Figure; yet I hold it necessary to adjoyn one Example more, which will illustrate the use thereof more fully.

Suppose this Figure A B C D E F G, be the Plot of a Field, drawn upon the Table by a Scale of 32 in an Inch, and the exact content thereof is required.

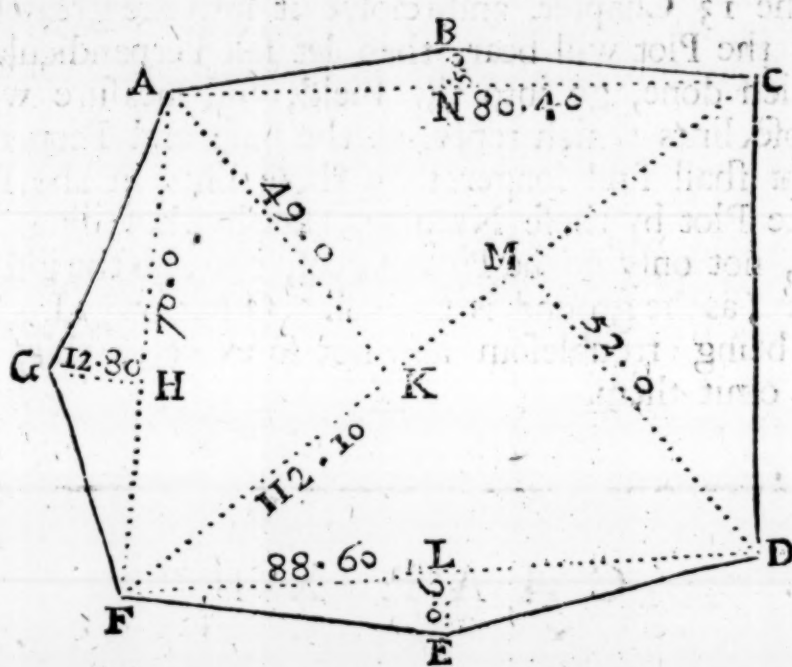
Now, because it is an irregular Plot, lying neither in the Form of a Square, Parallelogram, Trapezium, nor Triangle; therefore it must be reduced into some of these forms; which to effect, I first reduce the main body of the Field into the Trapezium A C D F, and the residue of it into three Triangles, as A B C, D E F, and A F G.

Then to know the just quantity of Acres the Field contains, I first measure the Trapezium A C D F, to which end I take the length of the Perpendicular D M from my Scale 52 p. 0, and the length of the perpendicular A K 49 p. 0, which I add together, and

and they make 101 p. 0, which I multiply in half the Base C F 56 p. 05, and the Product 5661 p. 05 is the Content of the Trapezium A C D F.

In like manner for the Triangle A B C, I multiply half the Base 40.20 by the Perpendicular B N 5 p. 0, and the Product is the content of the Triangle A B C 201 p. 00.

So, for the Triangle A G F, I multiply half the Base 35 p. 00, by the Perpendicular G H 12 p. 80, and the Product 448 p. 00, is the Content of the Triangle.



Likewise, in the Triangle D E F, the Base D F is 88 p. 60, and the Perpendicular E L 9 p. 0, therefore I multiply the half Base 44 p. 30 by the Perpendicular 9 p. 0; and the Factus 398 p. 70, is the Area, or content of the Triangle D E F.

Lastly, I add the several Sums together, and they give the Content of the whole Figure.

The Area, or Content of the	{	Trapezium A C D F	5661. 05
		Triangle A B C	201. 00
		Triangle A G F	448. 00
		Triangle D E F	398. 70

The Area or Content of the whole Field. 6708. 75

Which being reduced into Acres, yieldeth the Content of the said Field 41 Acres 3 Roods, 28 Perches, and three quarters of a Perch.

After this manner you may cast up the content of any irregular Field, by reducing it into Trapezias and Triangles and adding their several Products into one Sum, which ought heedfully to be regarded, as being one of the most material Things belonging to the Practice of the Surveyor; for unless he be perfect

fect herein, he can never perform any Work of that nature aright.

C H A P. XVIII.

To reduce Perches into Acres, & contra.

According to the Statute of 33 Ed. 1. *De terris mensurandis, & de compositione Ulnarum & Perticarum*, it is ordained, That 3 grains of Barley, dry and round, do make an Inch; 12 Inches do make a Foot; 3 Feet do make a Yard; 5 Yards and half do make a Perch; and 40 Perches in length, and four in breadth, do make an Acre. So that 16 Feet and a half, square, is a Perch, according to the Statute, and 160 of these Perches make an Acre; when therefore you are to reduce any number of Perches given into Acres, you must divide the number given by 160 (which are the number of Perches, contained in one Acre) and the Quotient will shew how many Acres are therein; and if any Perches remain after your Division, and that Number exceed 40, divide again by 40, and the Quotient will shew the Roods, and the remainder the Perches: Example, Suppose you were to turn 547 p into Acres, therefore first I divide 547 by 160, and the Quotient will be 3, and 67 remaining, which divide by 40, the Quotus will be 1, and 27 remaining; So that it amounteth to 3 Acres, 1 Rood, and 27 Perches.

Again if you would reduce 6708 Perches into Acres: Divide (as before) by 160, and the Quotient will be 41; and 148 remaining, which 148 being divided by 40, the Quotient will be 3, and 28 remaining, so that the true quantity in Acres will be 41 Ac. 3 R. 28 P.

But you may with more celerity reduce your Perches into Acres, if you cut off the first figure of your Sum toward the Right-hand, and then divide the sum remaining by 4, and the work will stand thus.

In this Paradigm, the 167 are so many Roods, and 28 Perches remaining.

$$\begin{array}{r} 6708 \\ 167 \end{array}$$

Then in like manner divide 167 by 4. and the Quotient is 41, and 2 remaining; so will the sum of the Perches given contain, 41 Acres, 3 Roods, and 28 Pole.

$$\begin{array}{r} 167 \\ 4 \\ \hline 41.3.28 \end{array}$$

C H A P. XIX.

To reduce Statute-measure to Customary measure, and the contrary.

ALtho an Acre of Land, according to the aforesaid Statute of 33. *Edward the First*, is to contain 160 square Perches, of 16 Feet and half to the Perch; yet in regard that in some places of the Nation, through long custom, there is at this day other Perches used, as 18, 20, 24 and 28 Feet to the Perch; it is therefore necessary to shew my Surveyor how he may readily reduce the Statute-measure into Customary, &c.

Suppose therefore you would reduce Statute-measure to Woodland-measure, of 18 Feet in the Perch, then say.

As the square of the greater Perch of 18 Feet, is to the square of the lesser Perch of 16 Feet and a half: So is the content in Acres according to the lesser Perch, to the content in Acres, according to the greater Perch.

Let it therefore be required to reduce 36 *Ac. 2 R. 10 P.* at 16 Feet and half to the Perch, into Woodland-measure of 18 Foot-Perch. *First*, You must observe that the square of 16 Feet and a half is decimally 272, 25, and the square of 18 feet is 324; then I reduce the said 36 *Ac. 2 R. 10 P.* into Perches, which make 5850, then I multiply the same by the square of the lesser Perch 272. 25, and the Product 1592662. 50 being divided by the square of the greater perch 324, the Quotus is 4915. 625.

Otherwise, You may find out the least proportional terms between 18 and 16½, which by their abbreviation by 1½, you shall find to be 12 and 11; then square these two sums 12 and 11, which produceth 144 and 121, which done, Reduce your 36 *Ac. 2 R. 10 P.* into Perches and they make 5850, as before, then multiply the square of 11, which is 121, by 5850, and it produceth 707850, which I divide by 144, and the Quotus is 4915. ½, which reduced into Acres, is 30 *Ac. 2 R. 35 P. ½*.

But, suppose you would reduce Woodland-measure into Statute measure, then say.

As the square of the lesser Perch of 16 Feet and half, is to the square of the greater Perch of 18 Feet: so is the content in Acres, according to the greater Perch to the content in Acres, according to the lesser Perch.

As in the former Example, I multiply the 4915 p. 625, given according to Woodland-measure, by 144, the greater square, and the Product is 707850. 00, which, divided by the lesser square 121, the quotient is 5850. Perches, which, reduced into Acres, is 36 *A. 2 R. 10 P.*

This

This course is to be observed in all respects in the reduction of other quantities, of what proportion soever, as those of 12, 20, 24, and 28 Feet in the Perch; and thus much briefly for the Reduction of Statute measure into Customary, and the contrary.

C H A P. XX.

Shewing the best way of measuring the several and particular quantities of Arable-Land, Leys, and Meadows, lying in the open or common Fields: With short directions for the taking in, and inclosing a Lordship.

FOrasmuch as this present Age hath so highly affected Inclosure, that a very great quantity of Land in the Nation is now reduced to that kind of quality, which before lay open, and in common; and seeing more is daily going in, and much more like to follow, it may therefore be expected, that I should give some directions about that matter, and shew what course is most requisite to take in the prosecution thereof. When therefore the Surveyor is to proceed about the Survey of a Lordship, or Mannor, wherein the Lord and Freeholders are agreed to improve it, in laying each Man's Land together, in several by it self (which in all common Fields lies dispersed, in many small parcels), it will be convenient to begin at one side of the Field, and there set down the Name of your first Furlong, in your Field-Book, and upon what point of the Compass you begin. And to the end you may the better express the just length, breadth, and quantity of each Part and Parcel of every Man's Land, as it shall rise in order; it will be necessary to provide a Book, of a quire of Paper, at the least, wherein each Page is to be divided into 6 Columns, so as the two first towards the Left-hand shall serve for the breadth of the Lands at each end; the third, or greater Column, shall contain the butting, bounding, and Number of every Man's particular Lands, Leys, Doles of Meadow, or the like; and the fourth, fifth, and sixth, for the reduced breadth, length, and quantity.

Next after you have thus done, and are come to the Furlong where you begin, express in your Book the Name of the Field, and particularly of that Furlong; then, in the Middle-

most, or greater Column, put down the Name of the Freeholder that first begins it, with the number of his Lands; against which, in the two first Columns toward the left-hand, write the breadth of the Lands at each end, and in the three last put the reduced breadth, length, and quantity; which done, set down the Name of the Freeholder that lies next, and the number of his Lands, together with the breadth, length, and quantity, as before. Afterwards set down him that riseth next, with his particular breadth, length, and quantity, and so proceed in order, till you have finished the Furlong.

Having compleatly finished one Furlong, go on to the next, where you are to write the Name thereof, and upon what Point you enter, and then set up the particular quantities of Ground belonging to each Land-holder, as they rise in order, till you have finished the same, as was before declared; afterwards go on to the third Furlong, and do the like there, and so on, from one Furlong to another, till you have finished the whole Field.

But that you may more fully understand the perfect Form and manner thereof, I shall (with much brevity) shew you in the following Example an absolute Method, how you may speedily effect the same.

The Form of the Field-Book.

North-Luffenham, Com. Rutland.

Oldham's-Hedge Furlong, beginning West, at the way leading to Edith-Weston.

5	7	4	15	Sam. Hunt 2 Lands	5	1	28	0	141	40
6	6	6	0	Jonathan Barker 3 l.	6	3	28	0	172	20
8	18	8	14	Sam. Hunt 5 lands	8	16	28	4	248	16
1	5	1	13	Vincent Wing 1 land	1	14	28	6	48	11
24	0	23	8	The Beadhouse piece	23	14	28	10	675	45
1	9	1	7	Tho. Freeman 1 land	1	8	28	12	40	04
2	16	2	12	John Weaver 2 lands	2	14	28	12	77	22
1	16	1	14	Vincent Wing 1 land	1	15	30	10	53	37
4	16	4	12	The Town 3 lands	4	14	30	18	145	23
1	0	1	0	John Weaver 1 land	1	0	31	6	31	30
1	4	1	2	The Town 1 land	1	3	32	0	36	80

The

The second Furlong begining West.

17	17	17	5	L. Camden	11	Lands	17	11	37	10	658	12
1	18	1	6	Parsonage	1	land	1	17	34	18	64	56
1	14	1	12	Vincent Wing	1	land	1	13	34	10	56	92
2	12	2	10	The Town	2	lands	2	11	34	10	87	97
1	11	1	11	L. Camden	1	land	1	11	34	10	53	47
1	10	1	8	Tho. Frezman	1	land	1	9	34	8	49	88

The Beck-Furlong begins West, at Brokenback.

1	19	1	17	Jonath. Barker	1	Ley	1	18	32	12	61	94
2	0	1	18	Vincent Wing	1	ley	1	19	32	12	63	57
6	16	4	0	James Digby Esq;	3	ley	5	8	33	17	182	79
8	17	4	3	Jonath. Bar.	a	piece	6	10	28	0	182	00
3	16	3	12	The Town	3	leys	3	14	26	12	98	42
1	14	1	12	Vincent Wing	1	ley	1	13	24	10	40	42

After this manner you are to proceed, from one Furlong to another, until you have finished your Field-Book; which being done, you are next to make a particular of every Mans Arable, Leys, and Meadow, severally, to which purpose, upon a fair sheet of Paper, you are to make so many Columns, as there are Freeholders, every one whereof is to be subdivided into three, so will the first serve for Arable, the second for Ley-ground, and the third and last for Meadow, if there be any: and if one sheet will not contain the whole, then may you take two or three, or so many as you see convenient. Then, turning to the Field-Book, I begin upon Oldhams-hedge Furlong, with 2 lands of Mr. Samuel Hunts, and write in the Particular, in its proper Column, under Arable, 141 p. 40: then Mr. Jonathan Barker 3 lands 172 p. 20: next Mr. Samuel Hunt 5 lands, 248 p. 16, which I place likewise under their Names, and in their due Place, and so I proceed till I have finished the Book; placing every Mans Arable land, Leys, and Meadow, in due order; which being performed, then make your *summa totalis*, as is done in the following Synopsis.

A Particular of all the Arable, Leys, and Meadow-ground, in the Lordship of N. Luffenham, Com. Rutland.

Samuel Hunt.		Jonathan Barker.		Vincent Wing.		Bead-house.		Thomas Freeman.	
Arable.	Leys.	Arable.	Leys.	Arable.	Leys.	Arable.	Leys.	Arable.	Leys.
141 40		172 20	61 94	48 11	63 57	675 45		40 04	
248 16			182 00	53 37	40 42			49 88	
				56 92					
389 56		172 20	243 94	158 40	103 99	675 45		89 92	

John Weaver.		The Town.		Lord Camden.		Parsonage.		James Digby, Esq;	
Arable.	Leys.	Arable.	Leys.	Arable.	Leys.	Arable.	Leys.	Arable.	Leys.
77 22		145 23	98 42	658 12		64 56			182 79
31 30		36 80		53 47					
		87 97							
108 52		270 00	98 42	711 59		64 56			182 79

After this manner, you are to make a Particular of the whole Field, and not make your *Summa totalis*, till all your Furlongs be inserted in the Particular: But this is a perfect Example, according to which you may effect the whole.

The next thing you are to do, is to take the Plot and general Survey of the whole Lordship; according to the manner delivered in the former Chapters, and see if the sum of all the particulars agree with the Total. Then you may conclude the Work is exact, but most commonly the Particulars (if they be exactly taken) will somewhat exceed the general Survey, especially where the lands lie high, as in *Leicestershire*; and in this case, that both may agree, you are to reduce the sum of every Mans Particulars, answerable to the Proportion of his Ground, which may speedily be effected by the Golden-Rule: For, if in the whole Field (which admit it be 1200 Acres) the Particulars exceed the general Survey 3 *Ac.* or 480 *P.* what shall 20 *Ac.* exceed? the Answer will be 8 *P.* and so much I am to deduct out of the sum total of such a Mans Particulars, according to which I am to Plot him 19 *Ac.* 3 *R.* 32 *P.* as is directed in the sixth Book: But before I proceed to set out any Plots in the Field, it is usual, in most places, for the Freeholders to choose Commissioners, who shall appoint in what part of the Fields every Mans Plot of Land shall lie, where you are exactly to measure and lay out the same, according to the quantity in your Particular. And lastly, when all the Plots are set out, and corrected, if need be, you are (as often as it shall be required) to draw a Plot of the Town, Streets, Lanes, Houses, Homesteads, Woods, and all the old and new Inclosure; not forgetting to describe every River, Gutter, Water-course, and Mills, if any be, as also
Trees

Trees, where they are standing, and that partly according to their number and quantity. Lastly, when you have drawn your whole Work upon Paper, you may speedily draw out the same upon Vellom, or Parchment, which being garnished with Water Colours of the best sort, will neatly shew the just proportion and Symmetry of the whole Mannor. But if you know not the way how to do it, then take these short directions.

Rub the Backside of your Paper-plot, all over, with Black-lead, or Sallow-cole, then lay your skin of Vellom upon a smooth Table, and upon that lay the leaded side of your rough Plot, which you are to fasten upon the Vellom, at the corners, with Mouth-glew, then take a Bodkin, and therewith gently trace over all the lines within the said Plot, and whatsoever else you would expresse, then taking off the rough Plot, you shall see upon the Vellom, the perfect Draught of your whole Work, which you may beautifie at pleasure, with neat Colours.

Before I conclude this Chapter, I shall speak something concerning Inclosure, by way of Caveat and advice, to all such as proceed that way. And first I say, that the laying of mens Land together in Plots, and Inclosing the same, is a thing, as I conceive, that in it self is very good and profitable, provided it be so performed, that there may be sufficient Provision made for the Poor, and no depopulation ensue. But we see the contrary in many Places, and especially where a Lordship lies in the hands of two or three men, and then what follows (in such places) but depopulation, for nothing (many times) will be allowed the Poor Tenant, no not upon indifferent Rents, but the Lord of the Mannor (in most places I have seen) presently sets all his land upon a Rack-rent, and if some allowance be made to the Poor Cottiers, at a little cheaper rate than ordinary, yet no sooner but when one Man dies the land is taken from the house, and the house is immediately pulled down, and so at length many a Town is depopulated and comes to nothing, and there is no Inhabitant left in the place, but, as our common Proverb hath it, the Shepherd and his Dog, whereas before it would contain two or three hundred People, to live upon in good sort and fashion. But let us observe what follows these Depopulators; doth not the Curse of God pursue them, to the Heels? How many great ones of this Nation, after they have effected their evil designs, in depopulating whole Lordships, have been suddenly taken away by Death? Others, tho' they have raised their Estates, yet presently come to nothing, whereby we see that of the Prophet verif'd. *Vae vobis, qui conjungitis domum ad domum: vo to them that joyn house to house, and lay land to land, till there be no place left for the Poor.* And the wise man tells them *Prov. 22. 16. Qui opprimit tenuem, ut amplificet rem suam, & qui dat diviti, tantum ad egestatem deveniet.* And sure I am, that the depopulation is a great Sin, and highly provoking the Lord to wrath. Let me therefore admonish all (that go upon designs of this nature) to be careful to make
such

such provision, that the Inhabitants of every Town and Village, where Inclosures are made, may have such quantities of Land laid to their particular houses, to be assured to them, and such as shall succeed them, for ever, and that such Provision and good orders may be taken, that Gods Blessing may follow upon their just designs and undertakings. But I would not have you think that I here speak against Inclosure in the least, but only against depopulation, for I have seen, and do daily see, much Inconvenience in many open and common Fields, where (Land lying intermixt) one Man continually intrrenches upon another, by plowing, and in their Common, and so it may do well in such places, especially where all the Town are Freeholders, in which case, their Land being laid out in several Parts, and inclosed by it self, all the Inhabitants may the more fitly and commodiously enjoy their own, and not be subject, so continually, to trespass upon one another, as is usual in common Fields. And besides it would be a thing very good for all such People, who have much Tillage, and little or no Pasture, to lay down some of their Land-Ground; and convert it into Pasture, whereby keeping a greater stock of Cattel, they may be the better enabled to uphold their Tillage, which would be an enriching to them, as I have seen it verify'd in sundry Places of this Nation, where by good Manuring thereof, they find more profit of one Acre, then they did of two before, and besides (keeping more Stock and better Dairys) they are better enabled to maintain their Families. And surely if the Inclosure be no more, but for the better management and upholding of Tillage, it cannot be offensive to the word of God, or destructive to the outward well-being of mankind, but will tend much to the good and welfare of the Nation. And thus much briefly touching Inclosure.

The End of the Fourth Book.

A N

A N
A P P E N D I X
T O T H E
Art of Surveying,

Demonstrated by a New Instrument,
C A L L E D
The E M P E R I A L T A B L E.

W I T H A
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and in all Respects, the Work of the Plain Table, Theo-
dolite, Circumferentor, Peractör, Chard and Needle.*

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O F
S U R V E Y I N G.

Illustrated in a more *Plain and Practicable*
Method than any hitherto Invented.

By J O H N W I N G, Math.

Pro captu Lectoris habent sua fata Libelli.

L O N D O N,
Printed for Awnsham and John Churchill, at the Black-Swan,
in Pater-Noster-Row, MDCXCIX.

AN
APPENDIX
TO THE
ART OF SURVEYING

Translated by a New Instrument

THE NEW METHOD OF SURVEYING

AND THE NEW METHOD OF SURVEYING
AND THE NEW METHOD OF SURVEYING
AND THE NEW METHOD OF SURVEYING

The only instrument yet made of this kind, and the only one which is adapted to the use of the new method of surveying.

THE NEW METHOD OF SURVEYING

OF THE NEW METHOD OF SURVEYING

Illustrated in a new and improved method than any hitherto published.

By JOHN W. G. Smith

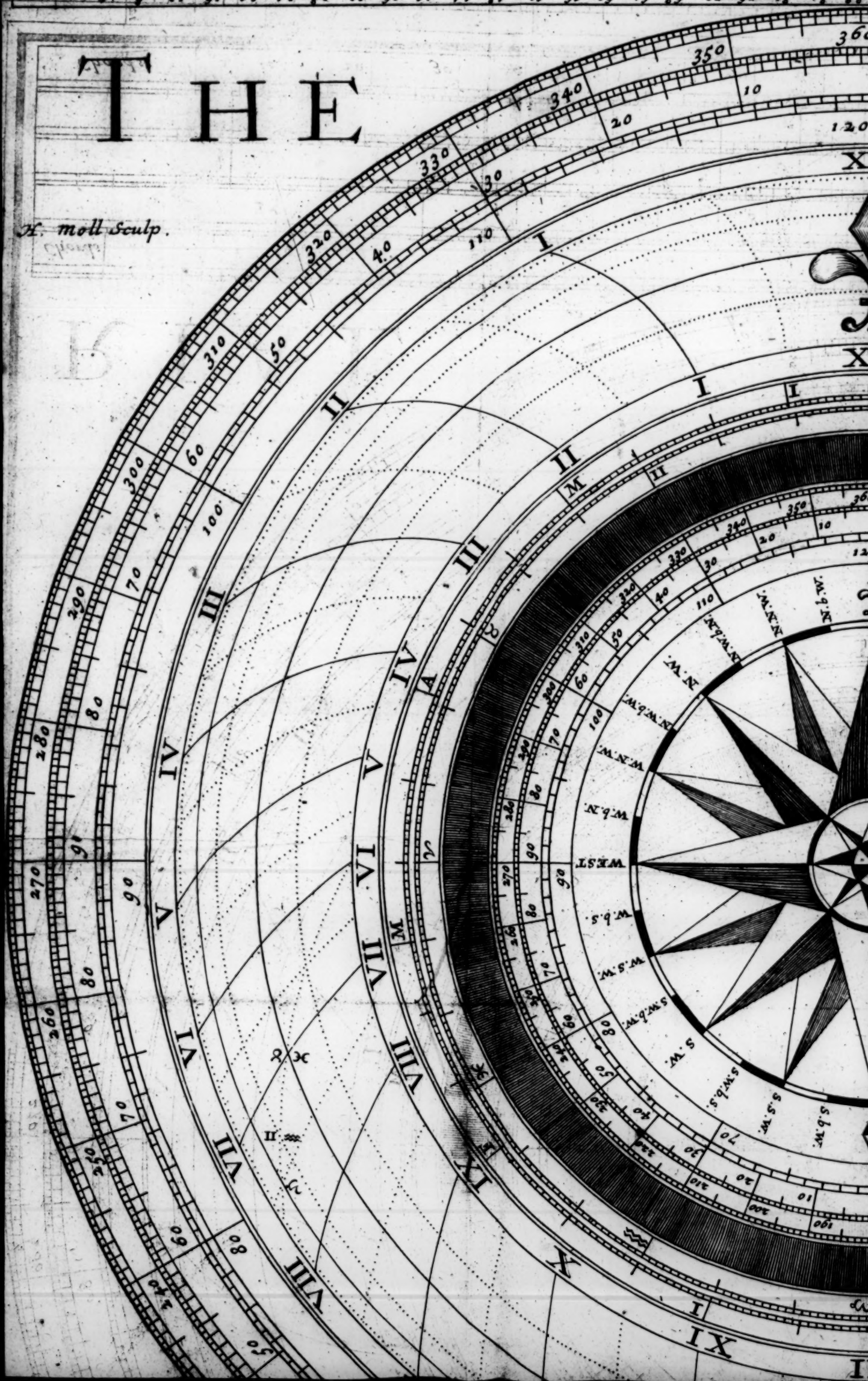
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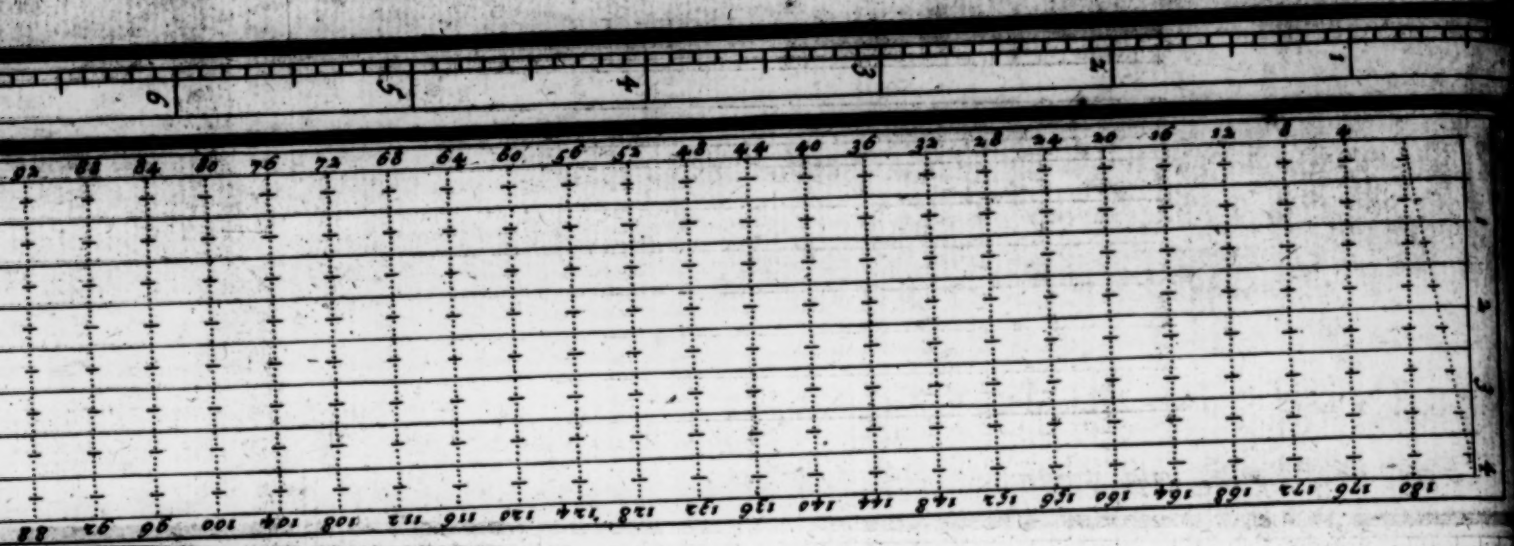
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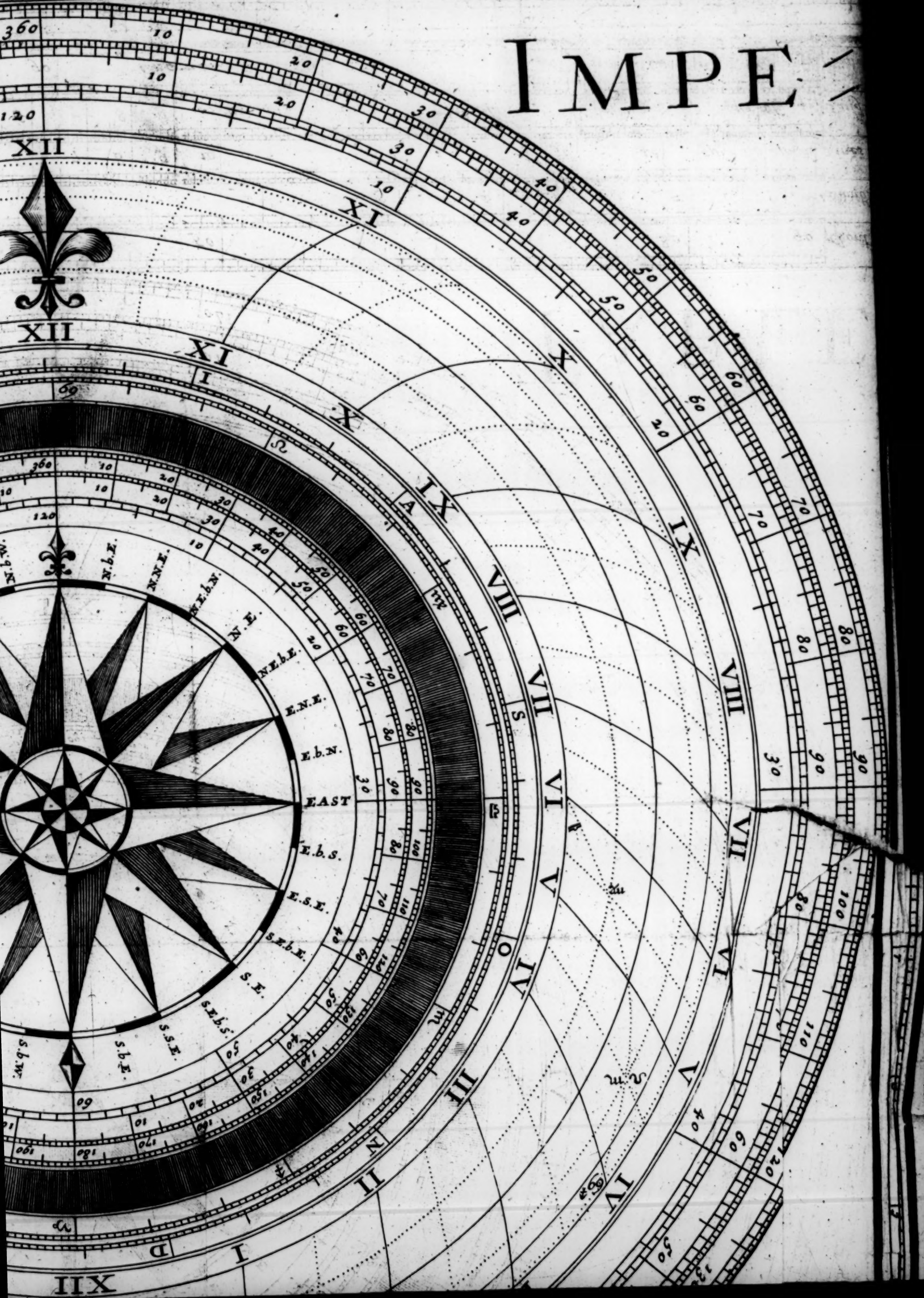
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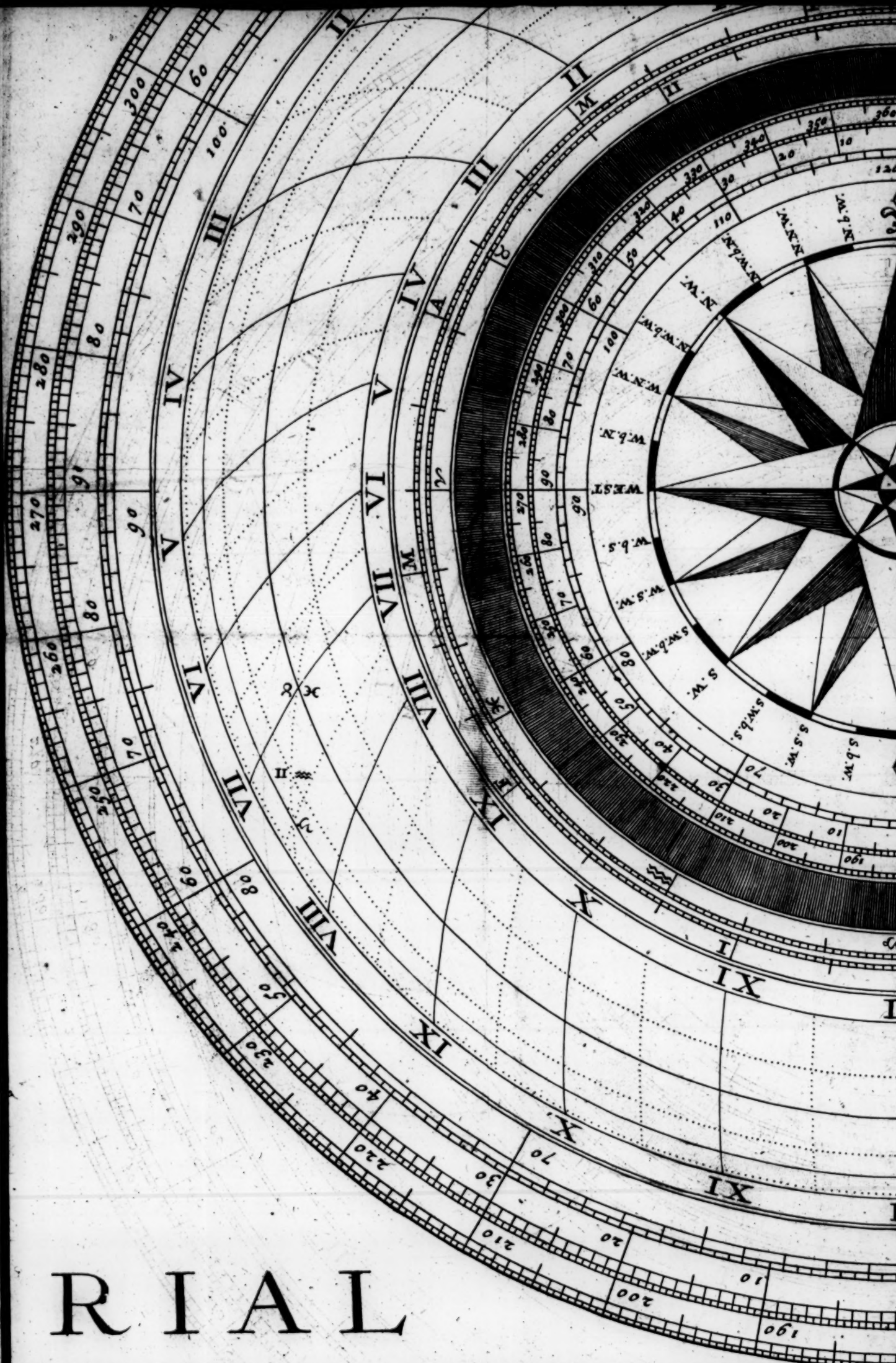
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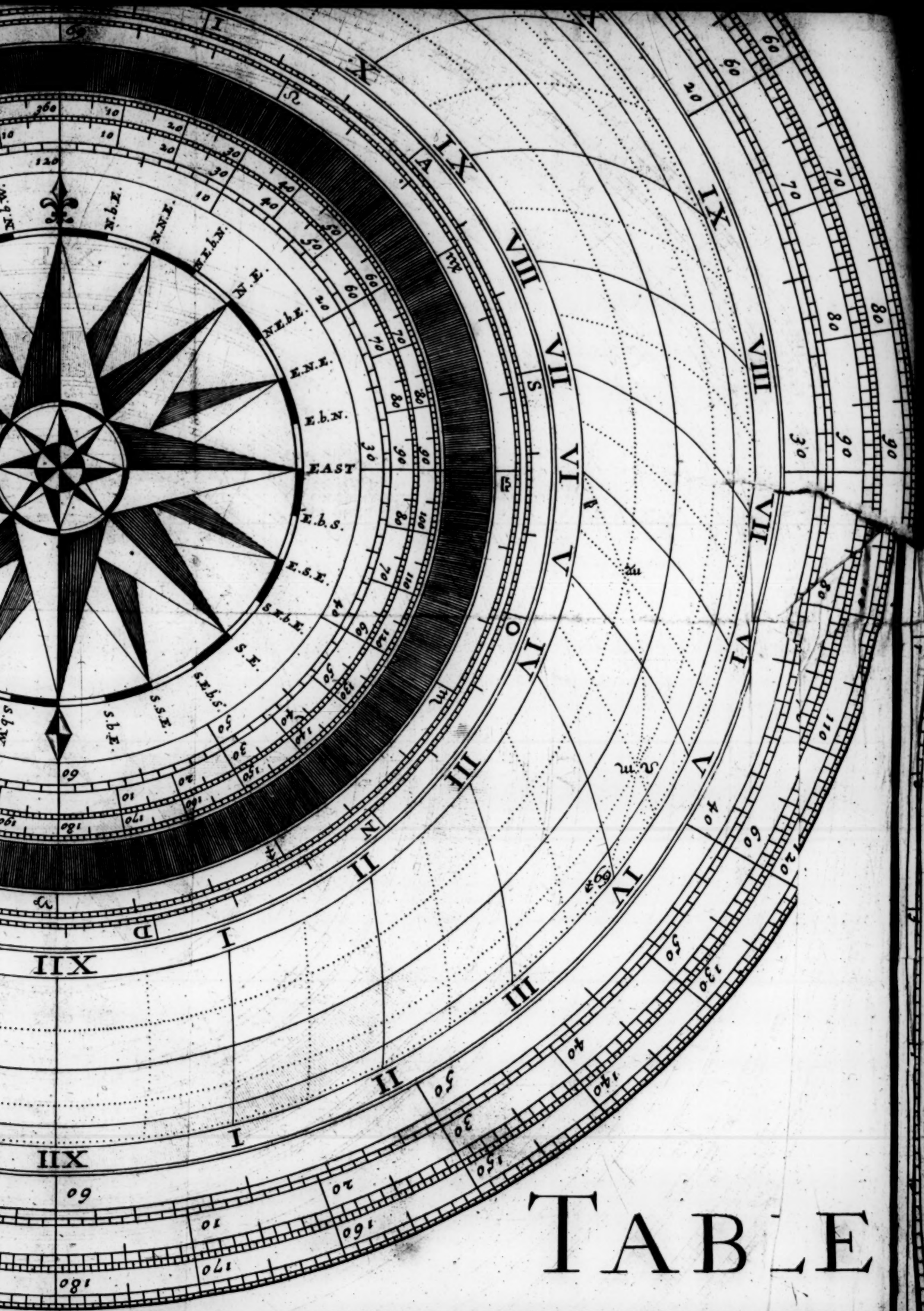
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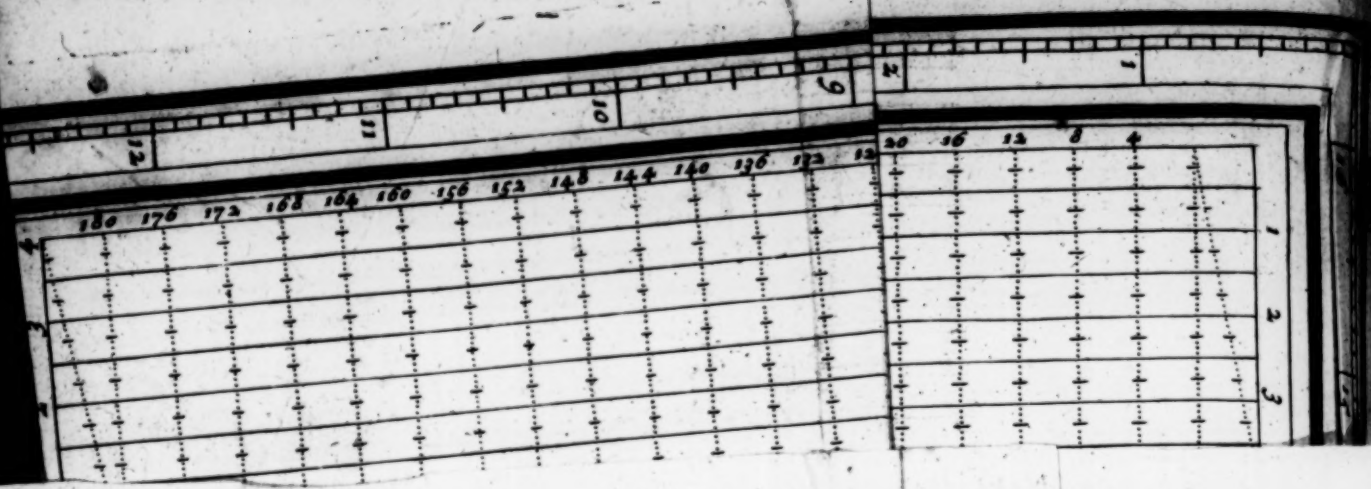
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Chords	10	20	30	40					
	2	3	4	5	6	7	8	9	1
	1	2	3	4	5	6			
	1	2	3	4	5	6			
Chords	10	20	30	40	50	60	70	80	90



TABLE

40										50										60										70										80										90										Chord.																																																												
1										2										3										4										5										6										7										8										9										10										Numb.																				
6										7										8										9										10										20										30										40										50										60										70										80										Sines
6										7										8										9										10										08										20										06										30										09										05										45										Tang.
90										Chords										10										20										30										40										50										60										70										80										90										Chord.										



A N N O
APPENDIX.

C H A P. I.

*The Reasons and Inducements of the Authors
Publication.*

HAVING spent many pensive thoughts about finding out some Instrument in Surveying, that might be truly Subservient in all the Variety of Cases, that may possibly happen in the Practical part of Surveying, which took me up some time in the consideration thereof, and the Reasons that induced me to it, was no other than (in my apprehension) the great want I found of such an one: And had not my Experience been equivalent to my Apprehension, I am really Induced to believe, I had not been so sensible of the want thereof, nor so happy as to have set about it, and tho' the Plain Table as Mr. *Lybourn* directs; comes nearest the matter in hand, yet 'tis very insufficient and defective in the Performance, (in several Cases) of the Work of the Theodolite, Circumferenter, and Peractor, and the Declinatory-Azimuth, or Needle, which Instruments in their proper places (if well understood) will perform what ever is, or may be required in the Practice of Surveying: Yet not any one of these is sufficient to be confided in, for all Cases that may happen in Surveying, as the experienced and well grounded Surveyor, must needs acknowledge; neither would I here be thought to condemn any of them, as First, being composed by able Artists, and Secondly, are all of good use in Surveying, tho' not generally for all Cases that may happen, as hereafter more fully will appear.

Now the Instrument I here insist on, I call the EMPERIAL TABLE, as being a perfect Plain Table, an exact Theodolite and Circumferenter, and the Peractor exactly adjusted, the Needle or Declinatory also fully Compleated thereon, in its own kind and order, which Instruments are all here fully compleated upon this one Instrument, without the least confusion of Lines or Parts. As will readily appear by the subsequent discourse.

C H A P. II.

*The Description and Use of the Chain.*I. *A Description of the Chain.*

IT has been no hard matter amongst our late Authors, to fix upon what Chain is the best and readiest in Practice, which is that of Mr. *Gunter's* Composing, consisting of 25 Links in a Pole, and the whole Chain containing 4 Poles or 100 Links, answering to Decimal Arithmetick. But the Chain which I make use of, and do here recommend as exact and Practicable as any, and in some cases better than any, is that of 20 Links in a Pole, and the whole Chain consisting of 4 Poles or 80 Links, which is applicable to Decimal Arithmetick, as well as any other Chain whatever, and more Essential to our purpose in Practice, if used with that Scale I have Composed proper to the Division thereof, as in the next Chapter more fully may appear; and by the several Examples in the following Part, to which I shall premise these following considerations, *Viz.* that of all the Methods I have yet observed (and those not a few) from all Authors, I have found none so Intelligible, Plain and Practicable (in my Opinion) as what I here deliver.

II. *The Use of the Chain.*

To prove this a Decimal Chain, and how to apply it to Decimal Arithmetick, I proceed thus, *Viz.* In taking the Dimensions, let it be done in Poles and Links, and accounting every two Links (that is for the odd Links over and above the number of Perches given) one Prime, and every odd Link 5 Seconds, always distinguishing these Fractions, or Decimal Parts of a Pole, by a Prick between the Poles, or Integers, and the Primes and Seconds, or Decimal parts of a Pole. As suppose 20 Poles, 10 Links, where given, place them thus, 20. 5, that is 20 Poles and 5 Primes. Again suppose a Length given to be 45 Poles 19 Links, write them down thus, 45. 95, that is 45 Poles, 9 Primes, and 5 Seconds, then for the Method, or way of resolving, or casting up any two Sums or Numbers given into a Product, observe to Multiply the given Numbers (in the order before-nam'd) as whole Numbers, cutting off so many figures of the Product towards the Right-hand, as there are Fractions or Decimal Parts in both Numbers; so will the Figures on the Left-hand be Perches, and those on the Right-hand the prick or stroak, parts of a Perch.

E X A M.

E X A M P L E.

Let it be required to Multiply 56 Pole, 15 Links, by 41 Pole 7 Links, being the length of two lines given, place them as above directed, and work them as in this Example, so will your Product be found (cutting off 4 figures towards the Right-hand, being the Number of Fractions in both Numbers) 2346 Perches and $\frac{6125}{10000}$ parts of a Perch, being above half a Perch more: Again take these two following Examples more to make all Plain.

$$\begin{array}{r} 56.75 \\ 41.35 \\ \hline 28375 \\ 17025 \\ 5675 \\ 22700 \\ \hline 2346.6125 \end{array}$$

II. E X A M P L E.

Admit 25 Pole 6 Links, were given to be Multiplied by 16 Pole 12 Links, as also if 45 Pole 18 Links given to be Multiplied by 12 Pole 15 Links, each Product will be found as following, *Viz.* the first is 419 Perches $\frac{28}{100}$, the second 585 Perches $\frac{225}{1000}$.

$\begin{array}{r} 25.3 \\ 16.6 \\ \hline 1518 \\ 1518 \\ 253 \\ \hline 419.98 \end{array}$	$\begin{array}{r} 12.75 \\ 45.9 \\ \hline 11475 \\ 6375 \\ 5100 \\ \hline 585.225 \end{array}$
--	--

These being all the Cases that can happen in the use of the Chain, *viz.* in taking the Dimensions in Poles and Links, being thus ordered and disposed.

C H A P. III.

The Description and use of a New Decimal Scale, exactly fitted to the Division of the former Chain.

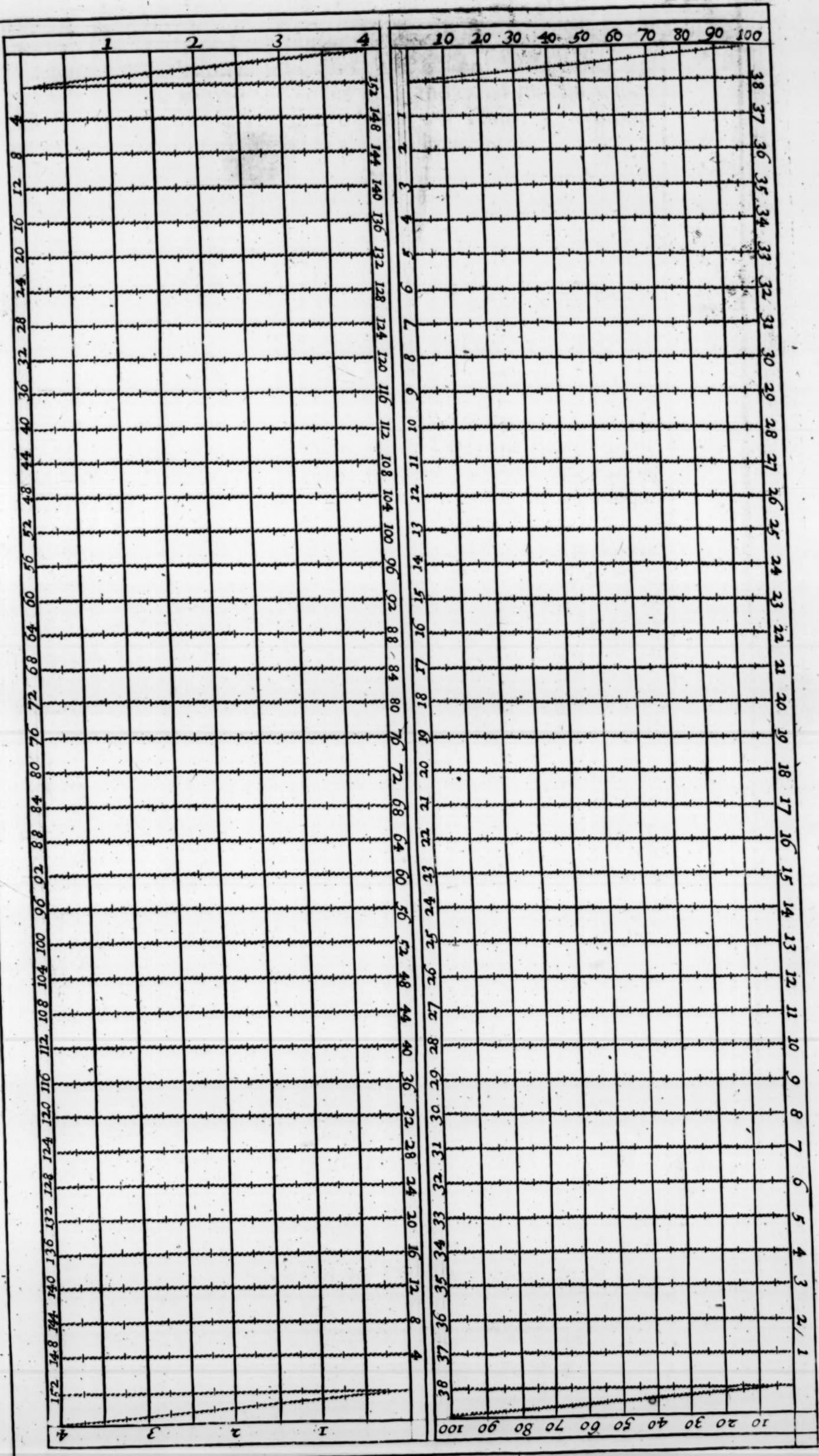
Very few (or indeed any) Authors writing upon this Subject have afforded us Scales proper to the Division of the several Chains they have treated of, so that those who knew no better (nor other) were forced to content themselves with the Vulgar Scales of equal parts, which could never be used otherways, than by halves, quarters, &c. of a Perch; so that Decimal-Arithmetick was wholly laid aside as useles in the use of these Scales, which all or most Authors have so extreamly cryed up, which indeed can never be too well spoke of, tho' in this Case it never before had a fit Object for its application, save what

what Mr. Wybeard has done in my Uncle Wing's *Geodates Practicus* for Gunter's and Rathbourn's Chain, which animated me to consider of such a like Scale, for this Chain I here recommend, and because the Chain consists of 80 Links, so will the Divisions on the Scale be more perceptible, freer from confusion, and more Practicable, for every Pole and Link may be very compendiously protracted from this Scale without the least Confusion or mistake, as will appear by its description and use following.

The description and Explanation.

First, the Scale is adjusted to a Scale of 16 parts in an Inch, as being the most usual in Practice, so that every quarter of an Inch, is equal to 4 Poles in length, or one Chain, which may be graduated on the Rular as far as the extent of a pair of middle-sized Compasses will extend, and numbering every such division down the side by 4, 8, 12, 16, 20, &c. being called the Perch-line, and it will be convenient to have the breadth of the Scale $2\frac{1}{4}$ Inches, and the length 21 Inches at least, that, when the Sights are placed upon it, may be of convenient length to fit the Table, and to be used as an Index as well as a Scale; and here Note by the way, that the Sights do not slide on the Rular, as they are now commonly made, but are to be fastned to the Rular with Brass-pins and Screws, so that they may be fitted upon either side of the Rular, for the Rular being graduated with the common Diagonal-Scale, by the side of which may be placed Scales of equal parts, as 12, 16, 24, &c. on the one side with a Scale of Chords, and with this New Decimal Scale on the other side, so that either side may be used, according to the will, Capacity, or Apprehension of the Artift. But to return to the Division of our Decimal Scale, the Division of the Side-line numbered and divided as before, I call the Pole or Perch-line, now in regard the Chain is 4 Poles long, the breadth of the Rular must be divided into 4 equal parts, and Lines drawn the proposed length, and Parallel to the side, and numbred on the Top with 1, 2, 3, 4, representing 4 Poles the length of the Chain, and if each of those divisions be divided into two equal parts, and lines drawn Parallel to the former, they will divide the Perch into two equal Parts, $\frac{1}{2}$ Poles, or 10 Links: Then each of those divisions divided in the middle by a small stroke representing $\frac{1}{4}$ of a Pole or 5 Links, and the intermediate Pricks represent each Link of the Chain, for there will appear to be 20 pricks and Divisions betwixt one Pole and another, and the whole breadth of the Chain thus divided into 80 equal Parts, being the number of Links contain'd in the whole Chain.

The Transvers-line on the Top extended from 0 to 4, is call'd the Link-line, and divided in all respects as the other overthwart lines are, that are drawn Parallel to the Top, and their distance $\frac{1}{4}$ of an Inch, through the limited length of the Rular, and to make the Index more useful and commodious, draw and divide another



Place this between P.172 & 173


another Transvers, or Link-line at the other end, and number the Divisions down the other side, and on the Top, as the other end and side directs, so will the Index be compleated for use which Side soever is towards you, but to make all Plain: I have here drawn the true Figure of the Scale as followeth.

The way of using the Scale.

Little need be said about directing how to use this Scale, if the former description and directions be rightly understood, but to clear the Point more fully, take these two following Examples.

Suppose I were to take from this Scale 38 Pole 15 Links, find the next lesser number on the side in the Pole-line, viz. 36, placing one Foot of the Compasses there and tracing that Foot along that line, as far as 2 Pole 15 Links (as the figure on the top of the Scale directs) extends, as the Divisions Plainly shew, that Foot resting there, extend the other in the same Parallel and division in the Link-line, which extent is the distance required to be taken from the Scale, viz. 38 Pole 15 Links.

Contrarily, if 38 Pole 15 Links, were a Length given to find its quantity upon the Scale, first try the length upon the Scale, to see what number it will fit in the Pole-line, to fall somewhere in the Link-line, which again is 36, so Tracing one foot of the Compasses (opened to the said extent) along that Line, till the other foot of the Compasses fall on the same Parallel in the Link-line, which will fall in 2 Poles (as the top-figure directs) 15 Links, which makes the 38 Pole 15 Links the thing required.

 Here Note that the Dimensions may be taken from this Scale in Chains and Links, as well as Poles and Links, for every division down the Pole-line is one Chain, and the Link-line being divided into 80 Parts equally, being the number of Links contain'd in one Chain, hence accounting the figure 1 on the top to be 20 Links, 2 to be 40, 3 to be 60, and 4 to be 80, it will then appear to the same purpose as the former way of dividing it.

C H A P. IV.

*The Description and use of Mr. Gunter's Chain,
and a Scale proper to the Division thereof.*

AS for these Surveyors that are Wedded to Mr Gunter's Chain, and do resolve to use no other, for their Sakes I have added the Scale proper to the Division thereof, to be placed on

on the other side the Index instead of the Scales of equal parts, the figure of which Scale is here placed by the side of the other Decimal Scale, which is to be used by Chains and Links, which need not be further Explained, if the use of the former be well understood, for Mr. Gunter's Chain of Four Poles length consists of 100 Links which is 25 Links in a Pole, so is it to be used in taking dimensions, viz. in Chains and Links, and not in Poles and Links as the former, hence the Chain-line down the side is numbered by 1, 2, 3, 4, 5, Chains &c. and the Link-line on the top by 10, 20, 30, &c. to 100 being the number of Links in the Chain.

The way of Casting up by Mr. Gunter's Chain.

The way of casting up the contents of any Dimensions taken by Mr. Gunter's Chain, is to multiply the Chains and Links together and cutting off 5 figures towards the Right-hand, the Remainder on the Left-hand will be Acres, then those figures cut off towards the Right-hand, multiply by 4, and from that Product also cut off 5 figures as before; so will the Figure on the Left-hand be Roods. Again, Multiply the remainder last cut off by 40, cutting off from this Product also 5 figures to the Right-hand, so will the figures on the Left-hand be Perches, so will the Content by multiplication only be given in Acres, Roods, and Perches.

E X A M P L E.

Suppose a piece of Land lying in the form of an Oblong whose length is 10 Chains 50 Links, and its Breadth 5 Chains 25 Links, which multiplied together, produceth 551250, from whence if 5 figures be cut off as before, there remains 5 Acres, and 51250 parts of 100000 of an Acre, which multiply by 4, so is the Product 205000, from which cutting off 5 figures as before, leaves 2 Roods and 05000 parts of 100000 of a Rood, which multiply by 40, the Product is 200000, from which cutting off the 5 Cyphers and there remains 2 Perches, so is the whole content cast up, found 5 Acres, 2 Roods and 2 Perches, as by the Example in the Margin.

<i>Exam.</i>	1050
	525
	<hr/>
	5250
	2100
	5250
	<hr/>
<i>Acres.</i>	5151250
	4
	<hr/>
<i>Roods.</i>	2105000
	40
	<hr/>
<i>Perches</i>	2100000

C H A P. V.

The Explanation and Use of several other Chains.

The Description and Use of Mr. Rathbourn's Chain.

There remains yet to speak of one more Decimal-Chain, Composed by that excellent Artist Mr. Aaron Rathbourn, which is most Proper in taking Dimensions of Gardens, Orchards, and Ground-Plots of Houses and small Inclosures, in respect of the smallness of the Divisions of this Chain, for the whole Chain (usually 2 Pole in length) is divided into Primes and Seconds, that is, each Pole is Divided into 100 Links, viz. First it is divided into 10 equal parts, which he calls Primes, and each of those parts divided into 10 more equal Parts call'd Seconds; but there is no Scale absolutely proper to the division of this Chain, neither have I leisure now to do it, but shall give you one Example, how the Dimensions taken thereby are cast up.

E X A M P L E.

Suppose a piece of Land, in form of an Oblong, be 52 Pole, 3 Primes, and 2 Seconds one way; and 13 Poles, 7 Primes, and 4 Seconds, the other way: first observe to put pricks between the Decimal parts and Integers, viz. betwixt the Poles and Primes, as in the Margent; then multiply them as whole Numbers, and the Product amounts to 7188768; now forasmuch as there are four places of Decimals, viz. 2 in the Multiplicator, and 2 in the Multiplicand, you must Separate by a prick or dott, four figures towards the Right-hand, and the product will stand as you see in the Example, that is 718 Perches, and $\frac{8768}{10000}$ parts of a Perch.

$$\begin{array}{r} 52.32 \\ 13.74 \\ \hline 20928 \\ 36624 \\ 15696 \\ 5232 \\ \hline 718.8768 \end{array}$$

Of the Vulgar Chain, and Statute-Measure.

There are some Surveyors that I am acquainted with, work by a Chain of $16\frac{1}{2}$ Links in a Pole, each Link being a Foot, and one Link of half a Foot in each Pole, to make it Statute-measure; for according to the Statute of 33 Edward the First, 16 Foot and a half is a Perch for Inclosure and Arable measure, but for Wood-land 18 is the usual Perch, and for Forrest-measure 24: This Chain of $16\frac{1}{2}$ Links in each Pole is only applicable to Vulgar-

Vulgar-Arithmetick, and the divisions too large to be Truſted in the Meaſuring of Leys or Arable, where Lands in open Fields are to be meaſured ſeverally, which perhaps many times are of great Length, and very Narrow, that it cannot be ſufficiently exact in the Operation, for the Reaſons before given.

Of the Foot Chain.

There is alſo another Chain, which I ſometimes make Uſe of, in meaſuring and Plotting the Ground-Plots of Houſes, and Gardens, Orchards, Yards, and ſuch like; as ſhall be Exemplified in its proper place, which Chain hath no reſpect for Land-measure, the whole length of the Chain conſiſts of 60 Links, each Link being one Foot in Length; hence the length of the Chain is 60 Foot, or 20 Yards; with this Chain I Uſe a Scale of equal Parts, a Yard being the Integer, ſo that the Content is given and Protracted, in Yards, Feet, and Inches, and this ſhall be farther explained in the following Part.

C H A P. VI.

To Reduce Perches into Acres ſeveral ways.

THe Content or quantity of any Land, Ground, or Incloſure is firſt found (by the two foregoing Chapters) in Perches, which muſt be reduced into Acres, which is here performed ſeveral ways.

Fiſt therefore, as 160 Perches is contained in an Acre, and 40 Perches in one Rood, it therefore follows, that theſe are the proper Diviſors, for if the Number of the Perches given be divided by 160, the Reſult in the Quotient is Acres, and if the Remainder exceed 40, divide it by 40, ſo is the Quotient, Roods, and the Remainder, Perches.

E X A M P L E.

Suppoſe 17996 Perches were given to be Reduced into Acres, Divide it by 160, the Quotient is 112 Acres and 76 remaining, which divide by 40, the Quotient is 1 Rood, and the remainder is 36 Perches, and this is the Old and uſual Method, and is practiſed by all or moſt Authors.

$$\begin{array}{r} 17996 \\ 160 \text{ Diviſor.} \\ \hline \end{array}$$

$$\begin{array}{r} 199 \\ 160 \text{ (112 Acres.} \\ \hline \end{array}$$

$$\begin{array}{r} 396 \\ 160 \\ \hline 320 \end{array}$$

$$\begin{array}{r} 76 \text{ Remains.} \\ 40 \text{ Diviſor.} \\ \hline \end{array}$$

Perches 36 (1 Rood.

II. E X A M P L E. Performed another Way.

But this Work may more readily be performed by Dividing the number of Perches by 4, first cutting off the Right-hand figure of the Perches, and that Quotient being again divided by 4, so will the Quotient appear in Acres, Roods, and Perches, as the Example in the Margent directs.

	133		
4)	1799	(6	
	449		
	A.	R.	P.
	112	1	36

In the Third place, I shall here deliver a more Concise Way, how to convert Perches into Acres, by Multiplication.

III. E X A M P L E. Performed by Multiplication.

First Therefore, Multiply the number of Perches given, by (this Constitute Number) .625, and from that Product cut off 5 figures towards the Right-hand, so will those on the Left-hand be Acres; then Multiply those figures cut off on the Right-hand by 4, and from that Product cut off 5 figures to the Right-hand, so will the figure on the Left-hand be Roods; then again Multiply the 5 figures last cut off by 40, and from that Product cut off 5 figures as before, so will the figures on the Left-hand be Perches as before; which is exemplified in the Margent by the former Numbers.

	17996
	.625
	89980
	35992
	107976
Acres.	112.47500
	4
Roods.	1.90000
	40
Perches	36.00000

C H A P. VII.

The Description and Explanation of the Imperial Table comprehending (and fully supplying) the Plain Table, Theodolite, Circumferenter, Peractor, Chard and Needle, never before Extant.

THIS Instrument is made either in Brass or Wood, but since the figure of it is too large to Insert in this Place, I shall briefly explain the making of it in Brass, by which both

M m

the

the Instrument-maker, and Surveyor may easily perceive how it may be made in Wood.

Let this Plate of Brass contain in length 16 Inches, and in breadth 13 Inches, and if the Brass be well Planished and Polished, $\frac{1}{8}$ of an Inch in Thickness is sufficient, in the middle whereof either way from the Centre 3 Inches, is cut out a round piece of Brass, which Plate will be 6 Inches Diameter, and Consequently the hole thus cut out; the same: to this hole or vacancy of the Instrument is underneath fixed a Box of Brass, falling below the Superficies of the upper side of the Table $\frac{1}{2}$ an Inch, or something more, to contain the Chard and Needle therein; upon the back side of the Box, let the Socket be Screwed on, that the head of the Three Legged Staff is to move in. And here observe, that the Needle is to be covered with clear Glass, the upper side of the Glass lying somewhat lower than the thickness of the Plate of Brass, from the upper side of the Instrument, so that when the Plate of 6 Inches Diameter (before cut out) comes to be laid over the Glass, it may rest upon two small cross Bars lying close upon the Glass, to prevent the breaking of the said Glass; These cross Bars are for other use as presently follows, and the upper side of this small Plate is to lye on in this Posture, when the Instrument is used as a Plain Table, and to be taken away when the Instrument is to be used as a Theodolite, Circumferenter, Peractator, or Needle. This Plate of Brass that covers the Needle, is to its largest extent made into a Quadrant, for the taking of Altitudes as also the hour of the Day, and for the resolving several propositions of the Sphere. There is also belonging to this Instrument a Frame of Brass (without Joynts) to go upon the Table, to fasten a sheet of Paper thereon, which Frame is Screwed down with Screws, from under the Table, through little Nebs of Brass fastned to the Table, that stand just the breadth of the Frame.

To this Instrument belongs a pair of Sights (which may be taken from the Index to supply this Place) to be Screwed upon the Table in the Diameter-line, agreeing with the North and South points of the Chard, which Sights thus placed are of excellent use with the Needle, and in respect of the Considerable distance they are placed one from another, will be more exact than any to this purpose before invented.

Thus far of the general explication of this Instrument, in the next place, *viz.* in the two following Chapters, we shall shew what Lines and Circles are thereon to be inserted, and what use they Generally serve for.

C H A P. VIII.

Of the Description and Division of the Chard, as it stands placed in the Centre of the Circles of the Instrument.

I **T**He Chard over which the Needle is to play, has its Limb divided into 360 equal parts or Degrees, and if Concentric Circles be drawn, then each of them Degrees to be again divided into as many equal Parts as the distance will admit of, as each Degree into halves being 30 Minutes, and these again into halves being 15 minutes, and these into 3 parts being to every 5th. minute, if the Divisions will bear it.

II. Next, within this Division (at a convenient distance) is another Circle divided into 120 equal parts or Degrees, which by the help of Concentric Circles, each degree may be divided into as many other lesser parts as the distance will admit of.

This Circle is adjusted equal to the Circle of the Instrument, for the expediting the work of the Circumferenter, and Peractor, and is the most excellent for use, in respect of its large Divisions.

III. There is also another Circle betwixt this and the Centre, divided into four times 90 Degrees, that is, the Circle is first divided into four Quadrants, and each Quadrant into 90 Degrees, Numbering them from the Meridian-Line of the Chard by 10, 20, &c. to 90, and thence backward, by 80, 70, 60, &c. to 0, and so likewise the other side of the Circle is to be numbered the contrary way.

IV. Betwixt this Circle and the Centre is placed the Several Concentric Circles, in the Inmost whereof is placed the Months and Days of the Year, and on the Outermost is Charactered the Hours, as also from an inward Concentric Circle, as the several lines drawn from each Circle directs, as also some other Circles Shewing the Suns Place and Azimuth.

C H A P. IX.

Of the several Circles and Scales upon the Imperial Table, their Division and Explanation.

I. **L**Et there be a Circle drawn to the utmost extent of the Instrument, whose Diameter will contain 12 Inches and an half, for the Table being 13 Inches broad, it may very well
M m 2 be

be extended within a Quarter of an Inch of either Side, which divide into 360 equal parts, or Degrees, and by help of Concentric Circles, this Limb may be divided into as many equal parts as the distance will admit of, which Circle performeth the work of the Theodolite, and here Note that this Circle thus divided, together with the Needle as 'tis placed on the Table, is a perfect Theodolite, and better for use than the ordinary one, First in respect 'tis larger, and secondly in respect of the other Circles placed by it, which doubly confirms it, as will sufficiently appear in the following part of this Book.

II. The next Circle (betwixt this and the Centre) is divided into four Quadrants, and each Quadrant into 90 Degrees, answerable to that in the Chard divided into four 90^s, and tho' this division of the Circle is taken little or no Notice of, in the Practick part of Surveying, by any Authors I have yet met with, yet I shall have more respect for it, as may appear in the following Part.

III. Next, within this aforementioned Circle is projected another Circle, which is divided into 120 equal parts or Degrees, which by the help of the Concentric Circles each Degree may be divided into halves and quarters, and consequently into every 5th. Minute at least: and here Note that any of the 3 degrees in any of the former Circles, makes but one of these, and every 10 of these makes 30 of them, so that more exactness may be expected from the Circle thus divided, than from any of the former, which Division performs the worke of the Circumferenter and is a perfect Peractor, according to Mr. Rathbourn's Composition; as you may see in his Surveyor, *Lib. 3. Chap. 5th.* Page 129, which includes all the Circles upon this Instrument.

IV. At one end of this Table, betwixt the Limb and the Frame, may be placed the new Decimal Scale, as is treated of and described in the 3 Chapter of this Book, which will be useful when you have no occasion to take your Index with you, which may fall out at such times as you use the Needle only, with the Sights fastened to the Table, as I before Described, which Way is most proper to be followed in Surveying of Woods, Forests, and such like Places, where you cannot see any considerable distance before you, which Scale will be ready to use with the Protractor, or Line of Right Sines, when you come to transfer the lines taken in the Field therefrom upon Paper, and to shew the true Map as well as the content thereof, for when the Map is thus given, your Scale is here ready to find the true Content also of your Map, as will necessarily be required.

V. On the other end of the Table betwixt the Limb and the Frame, may be graduated the Lines of Artificial Sines and Tangents, and Numbers, which will be found of great use in the Solution of Triangles, which will be of considerable consequence, in the Practice of Surveying.

VI. 'Tis Requisite to have a Line of Chords, which the Limb of the Quadrant affordeth, being a Line of Chords of a very convenient Size, however betwixt the innermost Circle, and the Chard and Needle, is a convenient place to insert several lines of Chords to several *Radius*'s, and also lines of Right Sines, to be used instead of a Protractor.

VII. The Frame of the Table is graduated with lines of equal Parts call'd Inches, round about, and serving chiefly for shifting of Paper upon the Table.

VIII. Note that there goeth two small Cross Bars over the Glas and Needle, Centring just over the Centre of the Needle, with a little Hole in the Centre of the Bars, and exactly over the Centre of the Needle, to place one of the Compass-points in, to lay the edge of your Index by, when you are to direct the Sights to any Mark (or Object) set up in the Field; which Cross Bars will also keep the quadrantal (or round) plate before cut out, from falling upon the Glas, to preserve it from danger of breaking.

IX. I have only one more Principal Matter to insist on in this place, *viz.* That, which way soever your work by this Instrument (the PLAIN TABLE way excepted) you may make your Observations by every one of these ways at once, which are before mentioned: I do not mean only at every Angle taken in the Field, but the whole will be confirmed, as well as each particular Angle; all which may appear at one and the same time from this Instrument, by working according to the THEODOLITE, CIRCUMFERENTER, PERACTOR, and NEEDLE; and since I shall in the following Part make this Assertion experimentally good, I shall not need to say any thing more of it in this place.

CHAP. X.

Of the Protractor and its several Divisions and Scales, fitted to the Imperial Table.

THE PROTRACTOR is made of a Plate of fine thin Brass, containing Six Inches in length and three Inches and half in breadth, whose Limb or Semicircle must be Divided into 180 Degrees, numbered from the Left side, by 10, 20, 30, to 180: Then beginning at the same side again with 190, and so progressively to 360; which Division of the Protractor, serves

serves for the Protraction of those Lines and Angles that are made by that Division upon the TABLE, *viz.* The Circle of the THEODOLITE divided into 360 Degrees. But when you are to Protract the Angles given by that Circle that is Divided into a 120 Degrees, (which Circle performs the work of the CIRCUMFERENTER and PERACTOR) then your PROTRACTOR must be Divided accordingly, *viz.* The Semicircle thereof Divided into 60 equal Parts or Degrees, and beginning at the same end again, and numbered to 120, which is answerable to that Circle on the TABLE; which Division may be put upon the other side of the PROTRACTOR, so that it will be compleated to all the several Circles comprehended upon the EMPERIAL TABLE. For the first Division, *viz.* That of 360 Degrees will serve for that Circle of four 90s as well as one for that purpose; for as the first Quadrant of the Limb is Numbred to 90, so tis but counting on from 90 backwards, *viz.* 80, 70, 60, &c. to 0, as a little practice, in its proper place, will make plain. Then on both sides are Scales of equal parts, Numbered by 10, 20, 30, &c. and at the bottom is a Line of equal parts also, and Numbered by 10, 20, 30, 40, &c. which Scales are to be graduated on both sides of the PROTRACTOR.

The use of this Instrument in all its parts, will best appear by laying down therefrom the several Observations taken in the Field; as the several Examples in the following Part exemplifieth.

The making of this Instrument is so well known to every Mathematical Instrument-Maker, that I shall not need to insert its Figure here.

C H A P. XI.

Of the several Instruments for Reducing Plots to a greater or lesser proportion, and what Method is safest to follow.

THere hath been Variety of RULARS and other Methods, contrived for the Reducing of Plots to a greater or lesser proportion, as shall be required; and that most of them to very good purpose: As that especially of Mr. Aaron Rathbourn's Invention; which is a Rular of what convenient length you please, and a Line drawn the length thereof, and divided into 100 equal parts, from the Centre-hole of the Rular, and also Numbered from the Center by 10, 20, 30, &c. to 100; through which Centre-hole is a Bodkin, Pin, or Needle, put through and fastened (through the Plot you intend to Reduce) to the Table, so that the Rular may have its liberty to move about its Centre so
con-

confir'd. But the way of Reducing a Map to any proportion assigned that I most affect as the surest way, is to Plot your Map over again (from the Map you have taken) by a lesser or greater Scale as the Matter is required, though indeed I cannot say, that the way of Reducing by Squares is much inferiour to any, for 'tis both plain and practicable; for if the Map to be reduced be incompass'd with one great Square, *viz.* Taking in and leaving out some little matter of your Plot to be reduced, then divide that Square into several little Squares as occasion requires, which are laid down by some known Scale of equal parts, then observe to make the like number of Squares (lesser or greater according as the Matter requireth) by a Scale fitting the proportion assigned, then observe what part of the Square, any Angle or Remarkable Accident falls in, and accordingly prick it off by your proposed Scale in your new or intended Map, and by observing the Method, this whole Work may be perfected, as shall be Illustrated by Examples in its proper place.

C H A P. XII.

The Manner or Way of making a Field-Book, proper to the several Instruments Issuing from the Imperial Table.

FOR The effecting this Matter, provide a quantity of Paper, more or less, as the Work shall require; which bind up into a Long Octavo, or Semi-Folio, and Divide each side according to the following Directions: Let the side of each Leaf be divided into five Columns; the first is to contain the Names of each Angle Alphabetically, as the Angles A, B, C, D, &c. The second and third Columns, are for the Degrees and Minutes, Cut by the Index upon the THEODOLITE, or the PERACTOR, or the Angles observed by the NEEDLE upon the Chard, for the CIRCUMFERENTER and the Magnerical way; the fourth and fifth are for the length of the Lines in the Field-Book, in Poles and Links.

The Form of the Field-Book.

Angles.	Degrees.	Minutes.	Poles.	Links.
A	51	20	80	11
B	21	45	29	17
C	76	50	78	12
D	80	30	42	15

There

There may be two Columns more added to the Right-hand, for taking Notice of the off-Sets, both to the Right and Left-hand, and here Note, for working by the NEEDLE with that Circle of the Chard divided into four 90's, that when the Degrees cut by the Needle in taking of an Angle exceed 90 Degrees, from the South-point of the Meridian-line on the Chard, then observe to insert its quantity and Coasting above 90 Degrees, *viz.* from the East or West-Points.

But I shall here insert the method of another FIELD-BOOK to more purpose, which includes all the Observations taken at once, *viz.* the THEODOLITE, PERACTOR, CIRCUMFERENTER, and NEEDLE, which take as followeth.

The Form of the New Field-Book.

The Angles.		Circle 360		Circle 120		Circle four 90's			Measure.	
		D.	M.	D.	M.	Coast	D.	M.	Po.	Li.
1	A	16	45	5	35	N E	16	45	35	18
2	B	100	15	33	25	S E	79	45	35	8
3	C	111	20	37	7	S E	68	40	30	15
4	D	136	50	45	37	S E	43	10	38	19

The very Titles of this Field-Book explains it, especially if the former be rightly understood, so that nothing more need be said here for Explanation.

C H A P. XIII.

Shewing what part of Surveying each way here delivered from the Imperial Table is most proper, and fittest to be used on all occasions.

VARIOUS are the Methods as well as Instruments that have been contriv'd and invented, for the perfection of this useful Art of Surveying, tho' not any one of them sufficiently to be confided in for all purposes, therefore I shall inform my Surveyor, what way or method is best to be observed and practised in all Cases that may happen, in the Practical part of Surveying, which this one Instrument I call the IMPERIAL TABLE will perform, with as much Celerity and exactness as all the Instruments that hath hitherto been invented, to proceed therefore methodically, I shall treat first of the

Plain

Plain Table,

Which is the only Instrument, that ever was invented, for taking the Map of small Inclosures, and for shewing the true Symmetry thereof, and for taking the Map of a Town-ship, together with the Laying all the Lands, Meadow, and Inclosure, in the same Lordship, to the Town, as they lie respectively in the Field, by which Instrument may be described (very aptly) all Rivers, Water-courses, Mountains, Mills, Ponds, Lakes, Quarries, Woods, Trees, and Bushes, where-ever standing, as also the Roads, Foot-paths, Gates, Stiles, with what-ever else is remarkable in the same Lordship. The Plain-Table is very excellent for taking of small distances, as not exceeding a Mile, and whatever is required in this kind, it will not fail to perform with admirable plainness and perspicuity: And so I come to the

Theodolite,

Which is best and most Applicable for the taking of a Map of a whole Country: For as the Plain Table is best and fittest for taking the Map of a Lordship, as the laying the particular Grounds one by another, and for the expressing what is remarkable therein: So is the Theodolite fittest for the describing a Country, and the laying each Lordship, in its due place, true shape, and quantity, within the said County-Map; on which may be described all the Rivers, Water-courses, Towns, Ancient and Depopulated Places, and whatever places there are of Remark.

This Instrument is very useful in taking the Map of a Lordship in Gros, viz. as tho' it were one intire Ground, which way is very helpful in the Inclosing of a Lordship, which is the first thing in that case that ought to be done, and this way may be safely practiced, in taking the Map and Content of any large Forest, Park, Chase, Wood, or such like, and for taking of distances, whether Accessible or Inaccessible; in short, 'tis fittest for large and spacious performances, and so I come to the

Circumferenter and Peractor.

Both these Instruments being partly to the same purpose, and in respect of the largeness of the Degrees, (which in both Instruments are the same) it will be of tolerable good use in taking the Map, and finding the Content of Inclosure, or of a Lordship, and will indifferently serve for large matters, as what we before Intimated in the use of the *Theodolite*, and may very well

merit the Applause of all Artists, for the taking of Distances, whether Accessible or Inaccessible; and so we proceed to the

Chard and Needle.

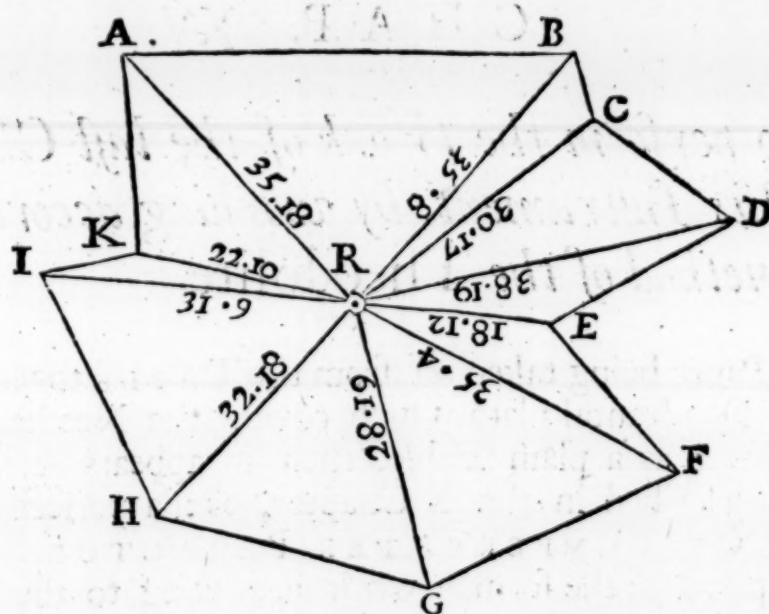
Tho' I know some Surveyors that have so far confided in the Chard and Needle only, as to give in a Map and Content of a Lordship taken thereby, or other small Inclosures, yet I cannot advise any Surveyor to lay so great a Stress upon this Way, that must necessarily have so little congruity with truth; For first, in taking Angles in small Grounds, the Angles lying near together, or the many small Crooks in a River or Watercourse, when the NEEDLE shall scarce shew the difference betwixt one Angle and another, by reason of its Parvity and Restlessness. Secondly, it is subject to Variation, both in respect of Weather and of Iron, that may some times accidentally happen to be near it unknown to the Artist, or Stones of an Iron Nature, in the Ground where the Instrument is planted, which may also cause the NEEDLE to stand from its true Point or resting Place, therefore ought not to be rely'd upon, as so precisely exact, as the other ways before mentioned. But that which I recommend it for, and indeed cannot well be done any other way, is the taking of the Map and Content, of a Wood or Forest that is bounded with another Wood or Forest, that you are not concern'd in to measure (as very often happens in Practice) so that you cannot see any considerable Way before you; then by the direction of the NEEDLE you may be able to keep a straight line, as near the Wood side as you can guess, and so take the Angles either to you or from you, according as you are placed. Otherways by Observing at every Angle you plant your Instrument at, what Angle the NEEDLE makes with the Meridian-Line, which distance shall be the true quantity thereof, and by measuring these distances with your Chain, and inserted into your FIELD-BOOK, and so proceeding round the whole Wood or Forest: then you may, by the help of your PROTRACTOR and FIELD-BOOK lay down the true Map thereof, and therefrom find its just content or quantity, as shall be exemplified in its proper place.

And here observe, the Sights taken from the Index, and fixed (as in the description page 177 or 178) upon the TABLE, that is here to be used.

C H A P. XIV.

How to take the Exact Plot of a Field at one Station, from whence may be seen all the Angles of the Field, by the Plain Table.

BEfore you place your TABLE, cause Marks to be set up in every Corner of the Field, as in A B C D E F G H I K, which let be the Field given to be measured; then plant your Table at some convenient Place in the Ground, from whence may be seen all the Angles or Corners therein, as at R, there plant your TABLE covered with a sheet of fair Paper, which is put upon the Table as is directed *page 87*: Your Table thus planted, lay your Index upon it, having one Foot of your Compass-points pricked down on the Paper near the Centre of the Table; then bring the edge of your Index to the Compass-point, as it Remains fixed in the point R, having your Compasses in your Right-hand thus placed and your Index directed by your Left-hand, turn the Index about till through the Sights thereof you espie the White or Mark set up at the Angle A, then by the edge of your



Index draw the line R A, which distance Measure on the Ground with your Chain, which is found 35 Poles, 18 Links, which take from your Scale with your Compasses, and place it from R to A, where make a prick with your Compass-point. So in Like manner from the point R direct your Sights to B, and draw the line R B, which distance Measured with your Chain, is found 35 Poles, 8 Links, which take in your Compasses from your Scale and set it from R to B, then with your Black-lead Pencil draw the line A B, thus observing the same Method till the whole Map or Plot of the Field is taken.

Or if you direct your Sights to every Angle in the Field, and draw lines at length from R, by the edge of your Index, then measure each length upon the Ground with your Chain, which several distances so found take in your Compasses from your Scale, and place them down upon their respective lines in your Map, Making a prick at the end of each extent, then with your Black-lead Pencil draw small Lines from one prick to another, as from A to B, and from B to C, from C to D, and so on, till the whole Plot be Included.

Concerning the Rules Authors have delivered about taking the Plot of a Field at one Station, from any one Angle thereof, from whence all the Angles thereof may be seen, I shall not trouble the Reader, here with an Example, in respect, 'tis the same with the former; for if the TABLE be planted at any Angle in the Field, from whence all the Corners or Angles may be seen, 'tis but directing your Sights (from the Angle assigned) to all the Angles, drawing lines by the edge of your Index; then measuring their respective distances upon the Ground, with your Chain, which Dimensions take in your Compasses from your Scale, and place them upon each correspondent Line, making pricks at the full extent thereof, from which with your Black-lead Pencil draw lines, which shall include the Plot required.

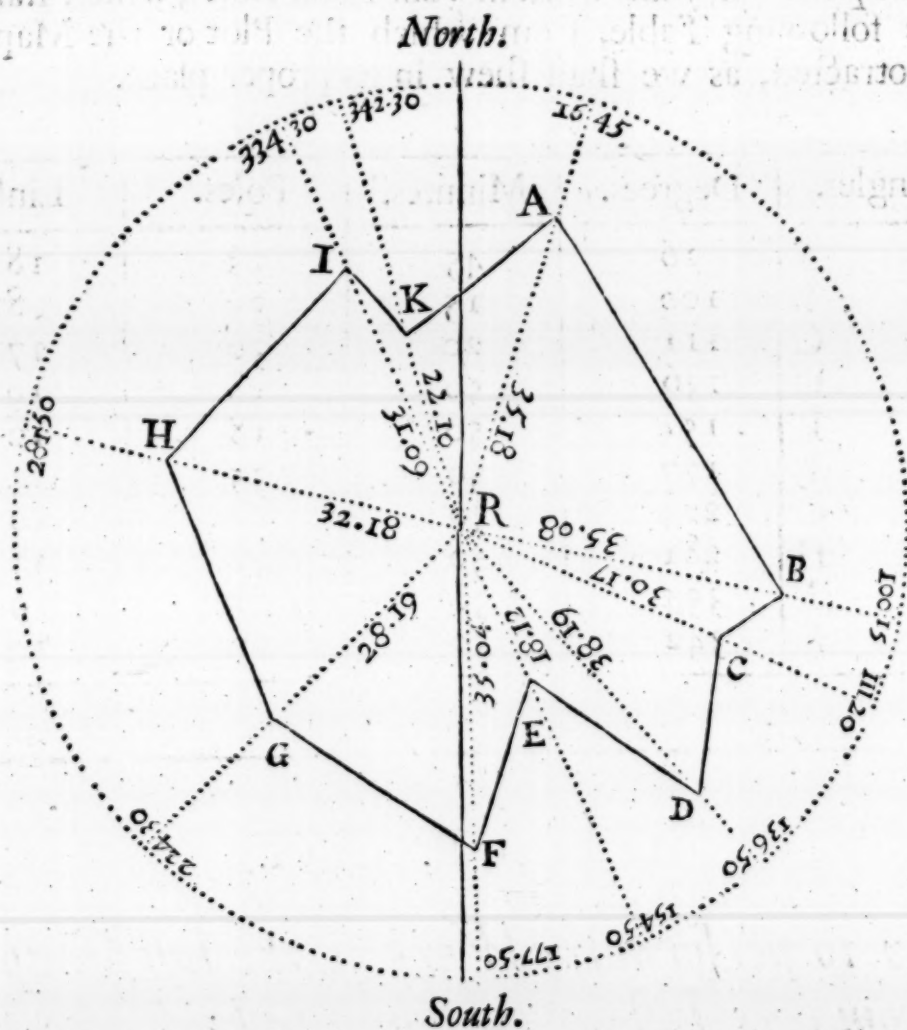
C H A P. XV.

How to perform the Work of the last Chapter, by this Instrument, by working according to the method of the Theodolite.

THE Paper being taken off from the TABLE together with the Quadrantal-plate which covers the Needle, at that time we use it as a plain Table, then it appears according to what we described in the IX Chapter, viz. a perfect THEODOLITE CIRCUMFERENTER PERACTOR, &c.

But to perform the former work according to the THEODOLITE, first plant your Instrument at R, turning the Table upon the head of the Staff till the NEEDLE shall hang directly over the Meridian Line in the CHARD, there Screw the Table fast, which done having your Index in your Left-hand upon the Table, and one of your Compass-points by your Right-hand placed in the Centre of the cross Bars, over the Centre of the CHARD and NEEDLE, to which Compass-point so fixed bring the edge of your Index, and direct the Sights to your first mark at A, observing (in the Innermost Circle divided into 360 Degrees) what Degrees the Index cutteth, which let be 16 Degrees, 45 Minutes, which

which put down in the Second and Third Column of your Field-Book against A, in the first Column, being the Angle Nominated, then with your Chain measure the distance upon the Ground, viz. from R, the place of your Instrument (or place of standing) to A, which is found 35 Poles, 18 Links, which place in the fourth and fifth Column of your Field-Book, against A; Then after the same manner direct your Sights to B, your second Mark, Noting the Degrees cut by the Index, which let be 100 Degrees, 15 Minutes, and the distance R B, is found 35 Poles, 8 Links, which note down in your Field-Book in the fourth and fifth Column (against B the Alphabetical name of the Angle in the first Column) and the 100 Deg. 15 Min. in the second and third Column. Then direct your Sights to C, finding the Degrees cut by the Index to be 111 Deg. 20 Min. and the Distance R C, to be 30 Poles, 17 Links, which 111 Deg. 20 Min. put down in the second and third Column of your Field-Book, and the length 30 Poles, 17 Links, in the Fourth and fifth Column thereof: Then again Direct your Sights to D, and note



the Degrees cut by the Index, which will be found 136 Degrees, 50 Minutes, then measure the distance R D 38 Poles, 19 Links; then put down D in the first Column of your Field-Book, and 136 Deg. 50 Min. in the Second and Third Columns, and 38 Poles, 19 Links in the fourth and fifth Columns thereof. Then Direct your Sights to E, and observe the Degrees the Index cuts, which

which let be 154 Deg. 50 Min. and the length R E, 18 Poles, 12 Links; which 154 Deg. 50 Min. and 18 Poles, 12 Links transfer into your Field-Book, in their proper Columns as before directed: Then direct your Sights to F, where finding the Index to cut 177 Deg. 50 Min. and the distance R F, 35 Poles, 4 Links, all which put down in your Field-Book according to the foregoing Directions: Then direct your Sights to G, and Note the Degrees cut by the Index to be 224 Deg. 30 Min. and the distance R G, 28 Poles, 19 Links; all which put down into your Field-Book as before: Then direct your Sights to H, still Noting the Degrees cut by the Index, which let be 281 Deg. 50 Min. and the distance R H, 32 Poles, 18 Links, which Note down in your Field-Book: Then direct your Sights to I, Noting the Degrees cut by the Index, which we find 334 Deg. 30 Min. and the length R I, 31 Poles, 9 Links, which accordingly put down in your Field-Book: Then direct your Sights to K, your last Mark, observing the Index to cut 342 Deg. 30 Min. and the distance R K, 22 Poles, 10 Links, these Note down in your Field-Book also: So will you have the whole *Epitome* of your work in your Field-Book, which stands as in the following Table, from which the Plot or the Map is to be protracted, as we shall shew in its proper place.

	Angles.	Degrees.	Minutes.	Poles.	Links.
1	A	16	45	35	18
2	B	100	15	35	8
3	C	111	20	30	17
4	D	136	50	38	19
5	E	154	50	18	12
6	F	177	50	35	4
7	G	224	30	28	19
8	H	281	50	32	18
9	I	334	30	31	9
10	K	342	30	22	10

C H A P. XVI.

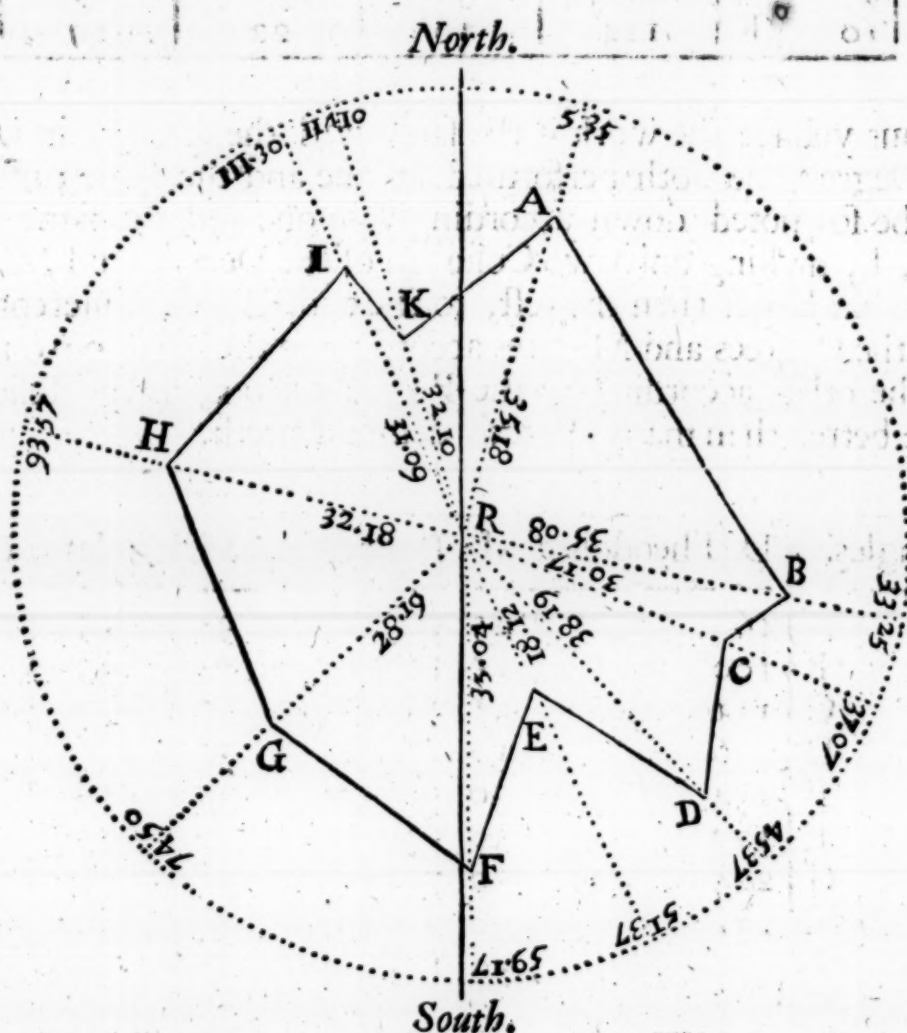
How to perform the Work of the last Chapter, from this Instrument, by working according to the Peractor.

THe difference between this way and the former consists only in the division of the Circle, for 'tis but making use of the Circle divided into 120 degrees, and the Angles cut accordingly by the Index, will shew the quantity of each Angle from

from that Circle also, which, with the length taken as in the last Chapter, and transfer'd into your Field-Book, in all respects as the former Chapter directs, will be the thing effected.

EXAMPLE.

Plant your Instrument at R, with the NEEDLE hanging directly over the Meridian-line, directing your Sights (as in the former Chapter) to A, Noting the Degrees cut by the Index, which let be 5 degrees, 35 minutes, which with the length R A, 35 Poles, 18 Links, Note down in your Field-Book, as in the last Chapter, then direct your Sights to B, Noting the degrees the



Index cuts, which let be be 33 degrees, 25 minutes, which with the length R B, 35 Poles, 8 Links, put down in your Field-Book. According to which method proceed in taking the rest of the Angles, and express them, with the length of the lines, taken in the Field with your Chain, in your Field-Book, which will be the exact *Epitome* of your whole work, and will stand thus.

Angles.

Angles.	Degrees.	Minutes.	Poles.	Links.
1 A	5	35	35	18
2 B	33	25	35	8
3 C	37	7	30	17
4 D	45	37	38	19
5 E	51	37	18	12
6 F	59	17	35	4
7 G	74	50	28	19
8 H	93	57	32	18
9 I	111	30	31	9
10 K	114	10	22	10

Thus you see the work is the same with the former, in its kind and Degree, and both performed at one and the same time, and may be so noted down accordingly in one and the same Field-Book, by making only two Columns of the Degrees and Minutes, somewhat larger then the rest, to the end, that one thereof may shew the Degrees and Minutes according to the THEODOLITE, and the other according to the PERACTOR, as the following Table better than many Words demonstrateth.

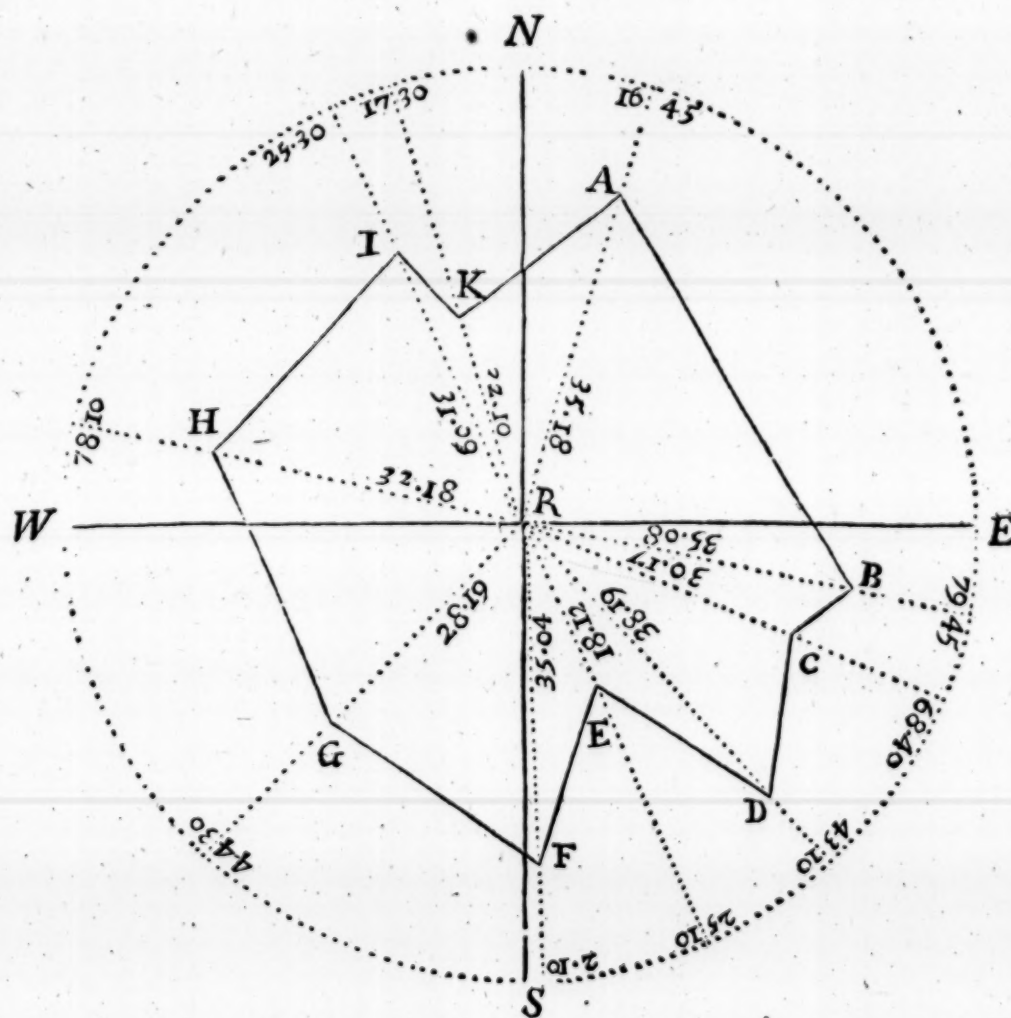
Angles.	D. Theodolite. M.	D. Peractor. M.	Poles.	Links.
1 A	16	45 5	35	18
2 B	100	15 33	25	8
3 C	111	20 37	7	17
4 D	136	50 45	37	19
5 E	154	50 51	37	12
6 F	177	50 59	17	4
7 G	224	30 74	50	19
8 H	281	50 93	57	18
9 I	334	30 111	30	9
10 K	342	30 114	10	10

By this Table, and what I have just now said, 'twill be easy to perceive the great advantage of this Instrument, which not only performs the work of these two Instruments at one and the same time, but confirms the work of both at the same Instant. And because the work is performed both these ways at one and the same time, and at the same labour also, I shall therefore in the following Chapters demonstrate the work of both the THEODOLITE and PERACTOR together, by observing the Angles in both Circles, and by transferring them into the Field-Book, as this last Table directs, in respect, 'tis much more helpful and intelligible,

C H A P. XVII.

To perform the work of the last Chapter, by the Circle upon the Table, that is divided into four 90^s; And also how the work of these three last Chapters (by this Instrument) may be most compendiously performed at the same time.

IN the performing of the foregoing work by the Circle on the T A B L E divided into four 90^s, you must have your Field-Book ordered accordingly, which is to be divided for this purpose into three Columns; the first is to contain the Letters and Figures progressively, being the Name and Number of each Angle; the



second must be of considerable breadth, so that it may contain the Number of Degrees and Minutes cut by the Index, and also the Quarter of the Compass in which the degrees are cut by the Index from the North or South points, towards the East or West; the
O O third

third Column is to contain the Poles and Links, being the length of each line taken in the Field. But before you proceed to plant your Instrument, set up marks in every corner of the Field, as at A B C D E F G H I K, which done plant your Instrument (as before) at R, with the NEEDLE hanging directly over the Meridian line in the CHARD, with the North end toward you, in which posture Screw it fast, then as in your former Chapter direct your Sights to A, Noting the degrees cut by your Index in the aforementioned Circle, which let be 16 degrees, 46 minutes, in the North-East quadrant, and the length of the line R A, 35 Poles, 18 Links, which put down in your Field-Book, as the following Table directs, viz. place in the first Column 1 and A, which denotes the first Angle, known by the Name A: Secondly set down in the second Column 16 Degrees, 45 Minutes, which is the quantity of the Angle, from the North towards the East: Thirdly place down in the third Column the length of R A, 35 Poles, 18 Links. Then direct your Sights to B, Noting the Degrees upon this Circle that the Index cuts, which let be 79 Degrees, 45 Minutes, S E, that is, so many Degrees from the South towards the East, and the length R B, 35 Poles, 8 Links, all which Note down in your Field-Book according to the former directions. Then direct your Sights to C, where finding the Degrees cut by the Index to be 68 Deg. 40 Min. S E, and the line R C, containing 30 Poles, 15 links, which Numbers as before write down in your Field-Book. Then direct your Sights to D, observing the Index to cut S E. 43 Degrees, 10 Minutes, and the line R D, containing 38 Poles, 19 Links, which accordingly place down in your Field-Book. Then direct your Sights to E, Noting the Degrees cut by the Index to be S E, 25 Deg. 10 Min. and the line R E, 18 Poles, 12 Links, which place in your Field-Book. Then direct your Sights to F, Noting S E, 2 Deg. 10 Min. and the line R F, 35 Poles, 4 Links, which place down in your Field-Book.

	Angles.	Coast.	D.	M.	P.	L.
1	A	NE.	16	45	35	18
2	B	SE.	79	45	35	8
3	C	SE.	68	40	30	15
4	D	SE.	43	10	38	19
5	E	SE.	25	10	18	12
6	F	SE.	2	10	35	4
7	G	SW.	44	30	28	19
8	H	NW.	78	10	32	18
9	I	NW.	25	30	31	9
10	K	NW.	17	30	22	10

By thus much 'tis easie to perceive how the rest of the Angles are to be taken, with the length of the several Lines leading to each

each Angle, and also how to place them in your Field-Book: which done, the whole Work stands in your Field-Book as the aforegoing Table directs, from which your Plot is to be Protracted.

Angles.		Circle. 360		Circle. 120		Circle four 90s		Measure.	
		D.	M.	D.	M.	Coast. D.	M.	P.	L.
1	A	16	45	5	35	NE.	16	45	35 18
2	B	100	15	33	25	SE.	79	45	35 8
3	C	111	20	37	7	SE.	68	40	30 15
4	D	136	50	45	37	SE.	43	10	38 19
5	E	154	50	51	37	SE.	25	10	18 12
6	F	177	50	59	17	SE.	2	10	35 4
7	G	224	30	74	50	SW.	44	30	28 19
8	H	281	50	93	57	NW.	78	10	32 18
9	I	334	30	111	30	NW.	25	30	31 9
10	K	342	30	114	10	NW.	17	30	22 10

And here Note, that the work of these three last Chapters may all be performed at one and the same time; for the directions are alike in all of them, only observing to enter the quantity of each Angle into your Field-Book from each Circle into its proper Column, as the Table Demonstrates. And tho' in these three last Chapters, I have largely treated of each several way, because it might best suit with the humours and qualifications of all Artists, yet I do wholly recommend the sober Artist, to make his Observation of all the three Circles at once, for the Index will cut all the Angles in the three several Circles at one time, and your Field-Book, as in this last Table, may be made with as little trouble to contain the Theodolite, Peractur, and Circle of four 90s the work of which three Instruments you see is performed at one operation, with the same ease and labour that any one of them takes or requires, which is a sure way also to prevent mistakes, by comparing the correspondent Numbers of your several Angles in your Field-Book, by considering the proportion one Circle bears to another.

C H A P. XVIII.

How to take the Plot of the aforementioned Ground, by using the Instrument as a Circumferenter, or Chard and Needle.

OUR First business is to fit this E M P E R I A L - T A B L E to a C I R C U M F E R E N T E R, &c. which is done by taking the Sights from the Index and Screwing them upon the Meridian line on the Table, as was directed in the 7th Chapter, so that the sights thus placed, are fixed to the Table, and move as the Table moves, and the Angles (by the Degrees in the Chard) are to be observed from the South end of the Needle, by any one or all the Circles in the Chard, as we have instanced in the work of the three last Chapters, for as the work of the three last Chapters was performed by the Index cutting the several Circles upon the Table, so the work may be effected by the three Circles so severally divided in the Chard, by the Needle (according to the moving of the Table) making the same Angles on the several Circles of the Chard; and because I would not be prolix I shall observe the Angles to each Circle the Needle makes, tho' I cannot but mostly recommend the Circle of the Circumferenter, divided into 120 Degrees: However since I shall exemplifie the work in all the three Circles at once, leaving the Surveyor to take his Choice which one, or all the Circles at one time he will make use of, and by referring to the Figures in the three former Chapters, which are applicable to the Divisions of the three Circles in the Chard; we Illustrate as followeth.

E X A M P L E.

First, set or place marks in all the Angles or Corners of the Field, as in A B C D E F G H I K, then plant your Table Horizontally at R, with the Flower-de-luce towards you, turning it gently upon the Staff till through the Sights you espie the Mark at A, there Screw your Table fast, and observe what Degrees in the Chard the Needle hangeth over in each Circle, which in the Division of that Circle of 360 Degrees it cuts 16 Deg. 45 Min. and in the Circumferenter-Circle divided into 120 Deg. the Needle cuts 5 Deg. 35 Min. and in the Circle of four 90's the Needle is found to rest upon NE. 16 Degrees, 45 Minutes, and the Length R A, measured on the Ground by the Chain, is found 35 Poles, 18 Links, all which Numbers note down in your Field-Book according to the last directions (for this purpose) of the last Chapter, in the Example of the Field-Book; which done,

done, unscrew your Table, and turn it about as before, till through the Sights you espie the Mark at B, there screw it fast, Noting the Degrees of the several Circles the Needle hangeth over, which in that of 360, is found 100 Deg. 15 Min. in that of 120, is found 33 Degrees, 25 Minutes; in the four 90s SE 79 Degrees, 45 Min. and the length R B, containing 35 Poles, 8 Links, all which Note down in your Field-Book as before, then according to the former directions, direct (by moving the Table) the Sights to C, where the Needle is found to rest upon 111 Deg. 20 Min. in the Circle divided into 360 Deg. and cutteth also 37 Degrees, 7 Min. in that Circle divided into 120, and also the Needle rests upon SE 68 Deg. 40 Min. in the Circle of four 90s and the length R C, is found to contain 30 Poles, 15 Links, all which Numbers accordingly place down in your Field-Book. And thus much is enough to ground a mean Capacity in the performance of the rest, for by observing the same Rule or Method, you cannot fail, and the Work in your Field-Book stands as the last Table in the last Chapter directs, from which the Plot is to be Protracted, as by the next Chapter.

Note, That whensoever the Plot of a Ground can be taken at one Station, be it in any Angle thereof, or in what other part of the Ground soever, the former directions hold good for the Performance thereof; for the Angles and Lines being taken according to the preceding directions (though different in respect of the Station's Situation) and accordingly entered into your Field-Book, the Plot may be Protracted thereby, and be the same as if drawn from observations made in any other place of the said Ground.

C H A P. XIX.

To lay down or Protract upon Paper, the Work of the former Chapters.

I. **F**IRST, draw a Line (your Field-Book lying before you) that shall represent the Meridian Line, or a line that shall point North and South, as in the figure of the 15th Chapter, which is Charactered at either end with N O R T H and S O U T H; then according to the Circle your Angles were observed by, whether upon the Table by the Index, or in the Chard by the Needle, make use of that side of your P R O T R A C T O R that is graduated accordingly; then make choice of a convenient Place upon your fair Paper, that may represent your Station, or place of Standing as at (by referring to the Figure in the 15th Chapter) R, upon which point, place the Centre of your Protractor, laying the Meridian line of your Protractor directly upon the Meridian line of

of your Paper, as it is before represented with the Arch towards your Protractor, resting in this posture, look in your Field-Book for the quantity of your First Angle at A, which (according to this division of 360) is found 16 Degrees, 45 Minutes; therefore against 16 Degrees, 45 Minutes, in the Limb of your Protractor, make a mark or prick upon the Paper.

II. Then finding your Second Angle at B, to contain 100 Degrees, 15 Minutes, make a mark upon the Paper against 100 Degrees, 15 Minutes, of your Protractor.

III. Also finding your third Angle at C to contain 111 Degrees, 20 Minutes, against which in the limb of your Protractor, make a mark also.

IV. Your fourth Angle at D, is found by your Field-Book to contain 136 Degrees, 50 Minutes, against which in the limb of your Protractor, make a mark upon your Paper.

V. The Degrees observed at your fifth Angle at E, is found 154 Degrees, 50 Minutes, against which Number in your Protractor make a prick upon your Paper.

VI. Accordingly observe what Degrees are at the sixth Angle at F, which is found 177 Degrees 50 Minutes, which prick off from the limb of your Protractor upon your Paper.

VII. Then observing what Degrees are made at the Angle G, which is found to contain 224 Degrees, 30 Minutes, wherein observe that as 224 Degrees, 30 Minutes, is greater then 180 Degrees, The Arch of your Protractor must therefore be turned downwards, still keeping the Meridian line of your Protractor upon the Meridian line of your Paper, in which posture it is to lye till your work be finished.

Then observe the 224 Degrees, 30 Minutes upon your Protractor, against which make a mark upon the Paper as before. Thus according to the preceding directions prick off the Angles H, I, and K, from the Degrees in the limb of your Protractor; which being done, take your Protractor from the Paper, then lay a Rular from the point R, to each prick-mark made from your Protractor and draw obscure Lines, as RA, RB, RC, &c. then take the particular length proper to each Angle (as your Field-Book directs) from your Scale, and place them upon their respective Lines, as from R, to A, 35 Poles, 18 Links, which take from the Scale treated of in the third Chapter, and place it from R, to A; likewise from R, to B, was found 35 Poles, 8 Links, which accordingly take from your Scale, and set from R, to B; thus by observing this method, being directed accordingly by your Field-Book, the length of all the other lines may be set off, as the Field-Book, and the Figure Demonstrates; which done, draw lines from prick to prick, as from A, to B, and from B, to C, from C, to D, and from D, to E, from E to F, and so round to A, which includes the Plot required.

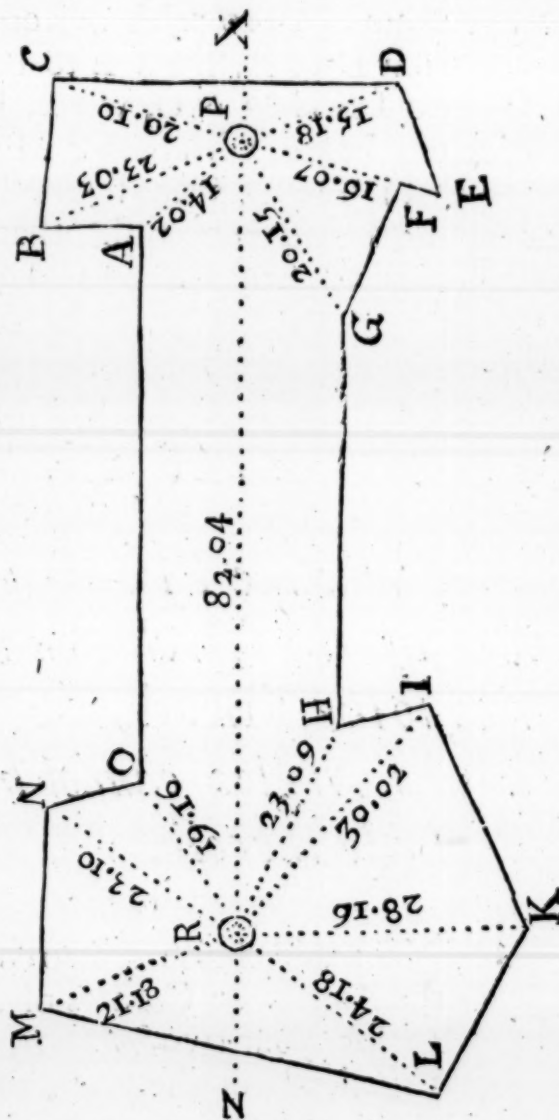
C H A P. XX.

To take the Plot of a Field at two Stations by the Plain-Table, when all the Angles cannot be seen from one place or Angle therein.

YOUR Quadrantal Plate laid over the Chard and Needle, and the Table covered with clean Paper, and the Sights first taken therefrom, and Screw'd upon the Index; having thus fitted your Instruments and in the Field you are to Measure and to take the Plot thereof, which cannot be done at less than two Stations, in respect all the Angles cannot be seen from any one place of the Ground. We will therefore suppose this following figure to be a Field or Ground to be Measured, Noted with the Letters A B C D E F G H I K L M N O, which is apparent enough (supposing no Hills to be in it) that it cannot be performed at any one Station, from any one Place therein, by reason all the Corners cannot be seen from any one place therein.

First then make choice of two convenient places, wherein all the Angles may be seen, which Stationary distance let be as long as convenient you can, as P and R, which are to be your Stations or places of standing, wherefrom all the Angles may be seen and taken: This considered, and Whites

set up in all the Angles, place your T A B L E at P, where let it be fast Screw'd, with respect to the Situation of the Ground, for the better bringing the Work all upon the Table, then direct your Sights (as directed in the 14 Chapter) to all the Corners or Angles, within Sight; as to A B C D E F G, drawing lines by the edge of your Index towards each Angle, as the prickt lines here denote, which done



done measure every one of the lines on the Ground with your Chain, and Note them down from your Scale upon the correspondent lines; your TABLE remaining fixed, direct your Sights to the other Station at R, and draw a line at length at the end of your Index as X Z, then take up your Table, and measure (as you go along) the stationary distance PR, which is found 82 Poles, 4 Links, which place from P, to R, by help of your Scale and Compasses.

Secondly plant your TABLE at R, laying the edge of your Index upon the Stationary line R P, and turn the Table gently about (upon the head of your Staff) till through the Sights you espie your first Station at P, there screw it fast; then direct the Index from your Station at R, to all the other Angles, as to H I K L M N O, and draw obscure lines by the edge of your Index as before: which done, measure with your Chain from your Station to each Angle, which several distances take in your Compasses, from your Scale, and set them from your Station at R, to H I K L M N O; lastly draw lines from prick to prick, as from A to B, from B to C, from C to D, from D to E, from E to F, thence to G, and so to H, and so on to I K L M N O, which Includes the Plot upon your Table, being the exact Map of the Field, as was required.

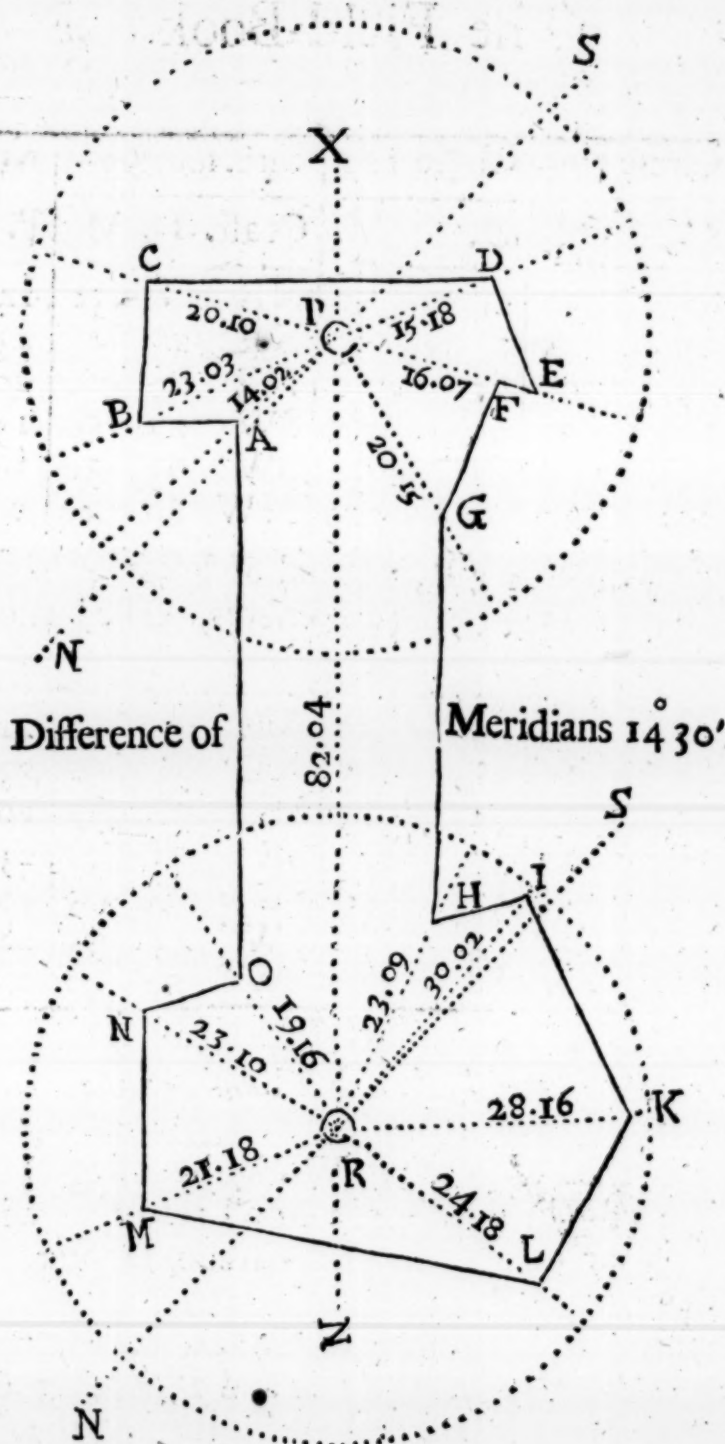
Note, that it often happens by the Irregularity of the Fences, or by Hills Obstructing your Sight, that more stations than two are required, of which Case the 23 Chapter will fully inform you.

C H A P. XXI.

How to take the Plot of a Field at two Stations, by the Circles on the Table, or according to the Theodolite, Peractor, &c. when all the Angles cannot be seen from one place or Angle therein.

HAVING made choice of two convenient places, (from which all the Angles or Corners of the Ground may be seen, as at P, and R) for your two Stations, plant your Table at P, turning it upon the head of the Staff, till the Needle hang directly over the Meridian line in the Chard, there screw it fast; then as is directed in the 15 Chapter, direct your Sights to all the Angles in view, viz. to A, B, C, D, E, F, G, and observe the Degrees cut by the edge of your Index, upon one or all the three Circles upon the Table, and Note the Angles (from each Circle) down in your Field-Book, with the length of each line, as here you see; which done, direct your Sights to R, your Second Station, where

where finding the edge of the Index (in the Circle of 360) to cut 41 Degrees, 30 Minutes, which note down in your Field-Book, in a space for that purpose, which 41 Degrees 30 Minutes, is called the difference of Meridians: Having thus finished this part of the Field, remove your Instrument to your other Station at R, (measuring the Stationary distance as you come on)



and laying the Index upon 41 Degrees, 30 Minutes, the difference Meridians, turning the Instrument about till through the Sights you espie the mark set up at your first Station at P, so will the Needle (as before) hang over the Meridian line in the Chard, in which posture Screw it fast, then direct your Sights to the remaining Angles viz. to M, N, O, H, I, K, L, noting the Degrees
 P p cut

cut by the edge of the Index, upon one or all the Circles on the Table, and accordingly note them down in your Field-Book, with the true measure of the Stationary Distance, which is here found 82 Poles, 4 Links, and likewise the measure of all the other Angles from the Station they were observed from, all which collect in your Field-Book as the following Table directs, so will your work in the Field be finished.

The Field-Book.

The Angles.	Circle 360		Circle 120		Circ. four 90s			Meal.		Sta- tions.
	D.	M.	D.	M.	Coast.	D.	M.	P.	L.	
A 1	8	30	2	50	NE	8	30	14	02	First Station at P.
B 2	24	45	8	15	NE	24	45	23	03	
C 3	64	00	21	20	NE	64	00	20	10	
D 4	209	50	69	57	SW	29	50	15	18	
EF 5	244	30	81	30	SW	64	30	16	07	
G 6	291	30	97	10	NW	68	30	20	15	

The Stationary distance P R, is found 82 Poles, 4 Links, and the Angle N P R, 41 Degrees, 30 Minutes, called the difference of Meridians.

M 1	27	30	9	10	NE	27	30	21	18	The Second Sta- tion at R.
N 2	81	10	27	03	NE	81	10	23	10	
O 3	103	10	34	23	SE	76	50	19	16	
H 4	161	15	53	45	SE	18	45	23	09	
I 5	173	55	57	58	SE	6	05	30	02	
K 6	223	35	74	32	SW	43	35	28	16	
L 7	264	40	88	13	SW	84	40	24	18	

Performed by the Chard and Needle.

To perform the foregoing Work, by using the three Circles in the Chard (being divided in all respects with those on the Table) or according to the Circumferenter, Chard and Needle.

First take the Sights from your Index, and Screw them on the Table as is directed in the 7th and 18th Chapters, then by directing the Sights (which is done by turning the Table upon the head of the Staff) to each Angle, viz. to A, B, C, &c. you will find the Needle to cut the several Circles in the Chard, on the same Degrees and Minutes as the Index did the Circles on the Table, which needs no further explanation to perform the whole Work; for the directions are the same in all respects, the Needle performing here what the Index did there, and the Field-Book no ways different, so that 'tis needless to make any tedious (or farther) repetitions.

C H A P.

C H A P. XXII.

How to protract the work of the last Chapter.

TO avoid trouble, we shall refer to the foregoing Figure. First then, draw the Meridian line SPN, let P represent your first Station, upon which point place the Centre of your Protractor, laying the Meridian line of your Protractor upon the Meridian line of your Paper, at which time having your Field-Book before you, prick off the Angles (according to the division of 360, in respect the difference of Meridians is noted from that Circle, which might at the same time also have been noted from both the other Circles, as every mean Capacity may understand) as your Field-Book directs; and draw lines from P, through these Marks, upon which lines set off the several lengths (taken in the Field) from P, as you find them Collected in your Field-Book.

The Observations of your first Station being thus finished, before you remove your Protractor make a mark against 41 Degrees, 30 Minutes, which is for the difference of Meridians, and draw the line PR, upon which line from P, set off (your Stationary Distance) 82 Poles, 4 Links, to R; then upon the Stationary point R, place the Centre of your Protractor, as before, moving it up and down until the line PR lyes Just under 41 Degrees, 30 Minutes, to which place hold it fast, and therefrom prick off all the Angles (taken at that Station) by the limb of your Protractor, as your Field-Book informs you; through which pricks draw lines from R, and set off therein the respective distances as they are noted down in your Field-Book: Lastly, through which Points thus prickt off, viz. A B C D E F G H I K L M N O, draw lines, which shall include the true Plot of the said Field upon your Paper.

Here Note also that if all the Angles could not have been observed but that of necessity more Stations would have been required to have perfected the Work, it had been but observing the next Stationary distance, or difference of Meridians, viz. by directing your Sights from Station to Station, in the same order as in the last Chapter is directed, taking all the Angles (with the length of the lines) in View at each Station, and so proceeding from Station to Station till the whole be finished, as presently we shall further explain.

C H A P. XXIII.

To take the Plot of any Irregular Field at divers Stations, when all the Angles cannot be seen from one, two, or more Stations, by the Plain-Table, by going round about the same.

LET this Irregular Plot Noted with A B C D E F G H I K &c. represent some Irregular Field or Ground whose Map or Plot is required.

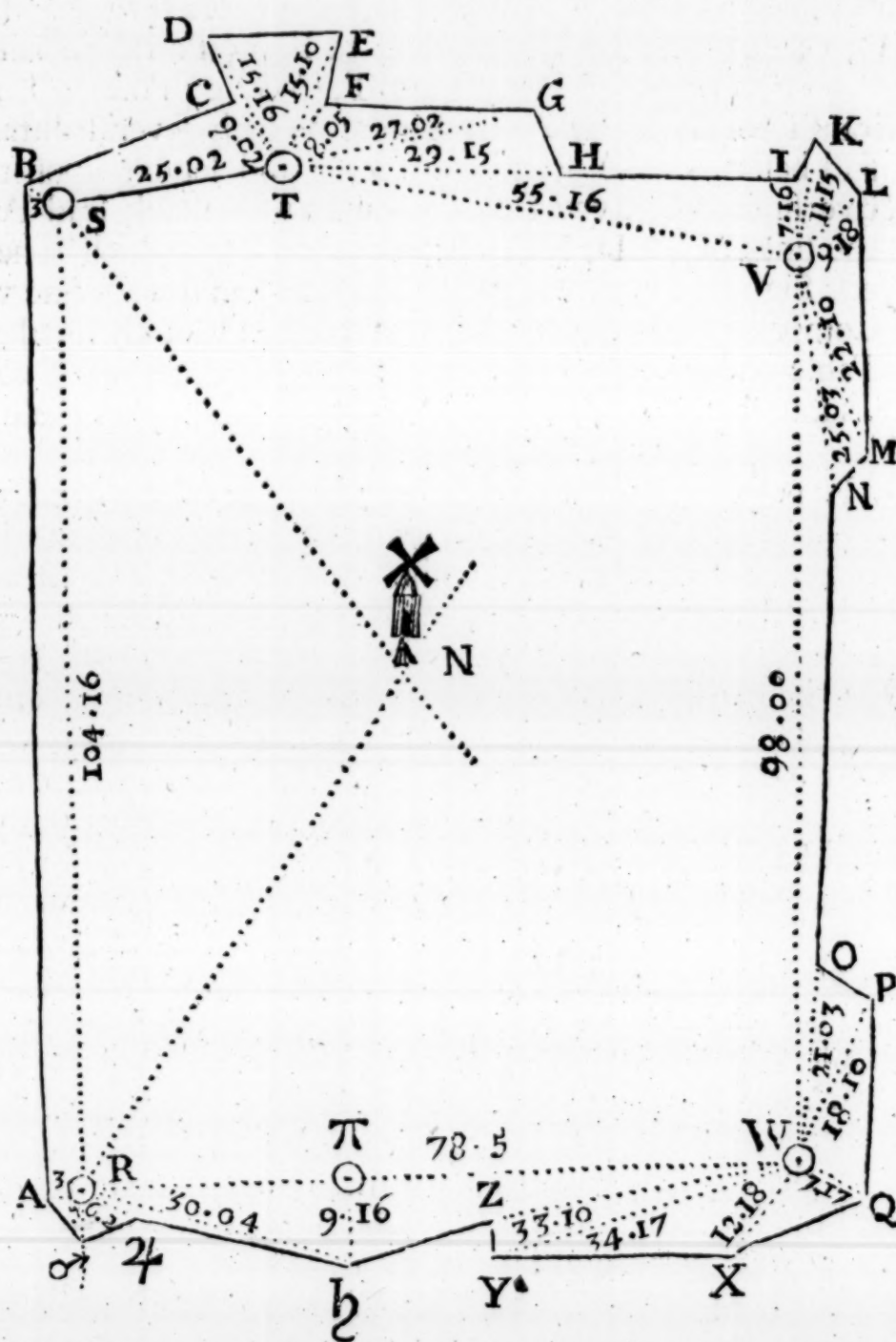
I. First therefore, make Choice of the most convenient places for your Stations, which are at R, S, T, V, W, which 5 Stations will perform the Work of the whole Ground, viz. all the Angles may be seen from them.

II. Secondly, set up Whites in all the Angles of the Field, otherways you must cause a Man to move from Angle to Angle, as you go along, with a sheet of White Paper pinn'd upon his breast.

III. Then plant your Table at R, fitting it to the Situation of the Ground, which is easily done by bear inspection, and Screw it fast; then from your first Station at R (upon the Table which represents the Place of your standing in the Field) direct your Sights to your second Station at S, and draw a line by the edge of your Index, which call your first Stationary line; then direct your Sights to all the Angles in View, as to A, δ , φ , h , drawing lines by the edge of your Index; then measure their respective distances with your Chain, from your Station-hole under the Table, hence the distance from R to A, is found 3 Poles, which take from your Scale and set from R to A; Then from R to δ , is 5 Poles, 10 Links; from R to φ , 6 Poles, 2 Links; and from R to h , 30 Poles, 4 Links: All which distances take severally from your Scale, and place them upon their respective lines; then with your Black lead-pencil draw lines from these points, viz. from A to δ , from δ to φ , from φ to h , so are all the Angles taken, at your First Station: But before you remove your Table, direct your Sights to the Wind-Mill at N, and draw a line at length by the edge of your Index, then take up your Table and Measure your Stationary line from R to S, which is found 104 Poles, 16 Links, which set from R to S.

IV. Plant your Table at S, laying the edge of your Index upon the edge (or close by the side) of your Stationary line, and turn the Table gently about upon the head of the Staff, till through the Sights you espie your first Station at R, there Screw it fast; then from your Stationary mark upon your Paper at S (which always

always represents your place of standing on the Ground) direct your Sights to B (which is all the Angles in View at that Station) which distance on the Ground is found 3 Poles, which take from your Scale and set from S to B; then with your Black lead-pencil draw the line A B: Then direct your Sights to the Wind-Mill, and draw a line at length by the edge of your Index, and



where these two lines Intersect one another at N, there place the Mill: By which Method you may Protract any thing that's remarkable in the Ground, as Ponds, Trees, Bushes, &c. Then direct your sights to T your third Station, and draw a line by the edge of your Index, then take up your Table and measure the Stationary distance from S to T, which is 25 Poles, 2 Links, which take from your Scale and set from S to T.

V. Plant

V. Plant your Table at T, laying the edge of your Index upon the Stationary line S T, and turning the Table gently about till through the Sights you espie your Stationary mark at S, there Screw it fast; then direct your Index to all the several Angles in view, as from T to C, from T to D, from T to E, from T to F, from T to G, and from T to H; then measure these several distances upon the Ground, which several distances taken from your Scale, and prickt off from your Station at T, upon their respective lines, as from T to C, is found 9 Poles, 2 Links; from T to D, 15 Poles, 16 Links; from T to E, 15 Poles, 10 Links; from T to F, 8 Poles, 5 Links; from T, to G, 27 Poles, 2 Links; and from T to H, 29 Poles, 15 Links: Which several distances (as I said before) take from your Scale and set off upon their respective lines as here you see; then with your Black lead-Pencil draw the lines BC, CD, DE, EF, FG, and GH; which done direct your Sights to V, your fourth Station, and draw a line with your Compass-points by the edge of your Index; then take up your Table and measure your Stationary distance from T to V, which is found 55 Poles, 16 Links, which take from your Scale and Place from T to V.

VI. Plant your Table at V, laying the edge of your Index upon your Stationary line T V, turning the Table upon the head of your Staff, till through the Sights you see your Station at T, in which posture Screw it fast; then direct your Sights from your Station at V, to all the Angles in view, as to I, K, L, M, N, and measure their distances (from your place of Standing) on the Ground, which from V to I is found 7 Poles, 16 Links, which take from your Scale and set from V to I, upon your Paper; the distance V K is found 11 Poles, 15 Links, which take from your Scale and set from V to K; likewise the line V L, is found 9 Poles, 18 Links, which set off from your Scale from V to L; then measure the distance V M on the Ground, which is 22 Poles, 10 Links, which take from your Scale and set from V to M; then measure the distance V N, which is found 25 Poles, 3 Links, which also take from your Scale and set from V to N; then take your Black lead-Pencil and draw the lines, HI, IK, KL, LM, and MN; then direct your Sights to your last Station at W, and draw a line by the edge of your Index, which done take up your Table; and the Stationary distance V W, which is found 98 Poles, take from your Scale and set from V to W.

VII. Lastly, plant your Table at W, laying the edge of your Index upon the Stationary Line V W, and turn your Table gently about till through the Sights you see your last Station at V, there screw it fast; then from your Stationary mark at W, direct your Sights to all the remaining Angles, as to O, P, Q, X, Y, and Z, which done measure each several line with your Chain upon the Ground, which from W to O, is found 21 Poles, 3 Links, which take from your Scale and set from W to O; then from W to P is 18 Poles, 10 Links, which set off by your Scale from W to P; then from W to Q, is 7 Poles 17 Links, which take from your Scale and

and set from W to Q; then from W to X is 12 Poles, 18 Links, which set from W to X; likewise from W to Y is 34 Poles, 17 Links, which set from W to Y; lastly from W to Z, the length of the Ground-line, is found 33 Poles, 10 Links, which also take from your Scale, and set from W to Z; then with your Black-lead-Pencil draw lines from prick to prick, *viz.* from N to O, from O to P, from P to Q, from Q to X, from X to Y, from Y to Z, and from Z to h, which includes and compleats the whole Plot or Map of your Field as was required.

Performed another Way by the Plain-Table.

In very Irregular Grounds where you meet with the advantage of drawing long Stationary lines, you cannot see all the Angles from each Station, but in going on your Stationary line, all the little Crooks in the Hedge, River, Gutter, &c. may be seen: Therefore that you may Plot all your Angles as you measure on your Stationary line, observe this General Rule, *viz.*

A General Rule.

In going on your Stationary line, mark where an Angle falls in a Right line (or as near as you can guess) to your Stationary line, there plant your Table, laying your Index upon the Stationary line, and turning the Needle upon the Head of the Staff, till you either can see your Station you last came from, or that you are then going to (for you must always observe to measure in a straight line from Station to Station (for if you should any ways deviate from a Right line, it would cause an error in your Work) there Screw it fast; then observe how far you have measured on your Stationary Line, *viz.* from your last Station, to the place where you plant your Table; which distance take from your Scale and place from your last Station on your Stationary line, there make a prick with your Compass-point, and there take the Angle.

E X A M P L E.

As suppose (in the last Figure) you were going on your Stationary line R W, *viz.* from R to W, where the Angle h we will suppose to be untaken: Now having measured from R on the Stationary line towards W, as far as π , being against the Angle at h, we find the distance R π 28 Poles, 15 Links, which take from your Scale and set from R to π , there make a prick; then lay your Index upon your Stationary line R W, and turn the Table about, so that be sure you do not shake the Index off from the line, till through the Sights you espy either the Stationary mark at R you came from, or at W where you are going, there Screw it fast; then from π direct your Sights to the Angle h, drawing a line by the edge of your Index, and measure the

the said distance on the Ground with your Chain, *viz.* from π to h , which is found 9 Poles, 16 Links, which take from your Scale with your Compasses, and set it from π to h .

Thus by this one example, 'tis easie to discern how the rest of the Angles (be they never so many) may be taken as you go on your several stationary lines, which is an excellent way of Plotting, where Grounds run out into many Angles or Corners, as where a Ground is bounded by a River, Watercourse, &c.

C H A P. XXIV.

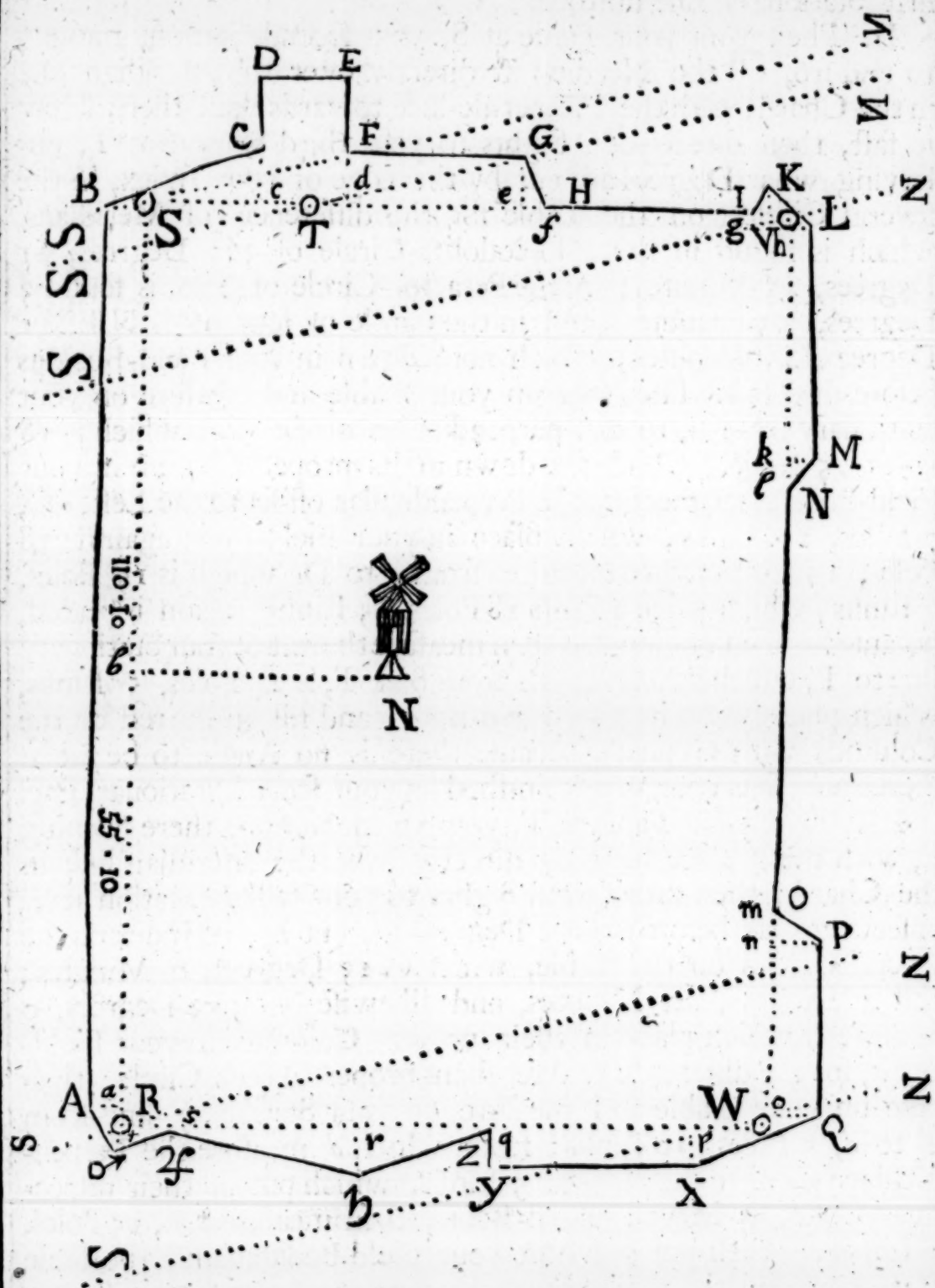
How to perform the Work of the former Chapter, by the Several Circles on the Table, representing the Theodolite, Peractor, Circumferenter, &c. all performed at one and the same time.

THE work of this Chapter may be performed according to the directions of the 21 Chapter, by observing all the Angles at every station, with the difference of Meridians also, from all the Circles upon the Table, with the length of each Ground-line from your stations also, which inserted in your Field-Book, in the same order that is there delivered; and accordingly proceed from one station to another, till the whole work be finished, which may be Protracted on Paper by the directions in the 22 Chapter. But because this way is something too intricate and hard and would take up too much time, I shall therefore exemplifie the work of this Chapter a much easier way, and more proper to the purpose in respect of going round the Ground, but I proceed as followeth.

I. First, let Beacons be set up for your several Stations, as at R, S, T, V, W, then plant your Instrument at R (being ordered as is directed at the beginning of the 15 Chapter) with the Flower-de-luce towards you, turning the Table gently upon the head of the Staff, till the Needle hang directly over the Meridian line in the Chard, there Screw it fast, then direct your Sights to your Second Station at S, noting the Degrees cut by the edge of your Index upon the Several Circles upon the Table, which in the Circle (360) of the Theodolite is found 283 Degrees, 30 Minutes; and in the Circle of the Peractor divided into 120 Degrees, is found 94 Degrees, 30 Minutes; and in the Circle of four 90s, N W 76 Degrees, 30 Minutes, which place down in the

second

second, third, and fourth Columns of your Field-Book, being the difference of Meridians observed from each Circle, then take up your Table, and begin and measure on your Stationary line from R to *a*, which is in a right line (or perpendicular) to A, 3 Poles, 8 Links, which put down in your Field-Book in the Column *Stat. Dist.* then measure the perpendicular off-set *a* A, 2 Poles, 10



Links, to the Left-hand, which place in its proper Column in your Field-Book ; then measure on your Stationary line till you come at Right Angles with the Wind-Mill at N, which from your first station R, is 55 Poles, 10 Links, which note down in your stationary Column, then the length of your Ground-line from *b* to the Mill, is 40 Poles to the Right-hand, which

Q q

note

note down in its proper Column into your Field-Book, then from *b*, measure on to *S*, your second Station; hence the whole length of your Stationary line *RS*, is found 110 Poles, 10 Links, which put down in your Field-Book as before; then measure the Perpendicular off-set *SB*, 4 Poles, 10 Links; and note it down in its proper Column in your Field-Book: So is the Work on your first Stationary line finished.

II. Then plant your Table at *S*, your second Station, moving to and fro, till the Needle rest directly over the Meridian line in the Chard; with the Flower-de-luce towards you, there screw it fast, then direct your Sights to your third Station at *T*, observing what Degrees are cut by the edge of your Index, in the several Circles on the Table for the difference of Meridians, which is found in the Theodolite-Circle of 360 Degrees, 11 Degrees, 45 Minutes; in the Peractor-Circle of 120, is found 3 Degrees, 55 Minutes; and in the Circle of four 90's, N E, 11 Degrees, 45 Minutes; which note down in your Field-Book as before directed: Then take up your Table and measure on your Stationary from *S*, to the perpendicular off-set at *c*, which is 18 Poles, 15 Links, which put down in its proper Column in your Field-Book; then measure the Perpendicular off-set to the Left, *cC*, 7 Poles, 10 Links, which place in your Field-Book against 18 Poles, 15 Links; then measure from *c* to *D*, which is 15 Poles, 2 Links, which place against 18 Poles, 15 Links, again repeated, because 'tis the same length; then measure the rest of your Stationary line to *T*, which whole length from *S* to *T*, is 24 Poles, 5 Links, which place down in your Field-Book, and fill up the rest of the Columns with Cyphers, because there is no Angle to be taken therefrom; so is your Work finished on your second Stationary line.

III. Plant your Table at *T*, your third Station, there fastning it, with the Needle hanging directly over the Meridian line in the Chard; then direct your Sights to your fourth Station at *V*, observing (as before) what Degrees are cut by the Index on the several Circles on the Table, which is 13 Degrees, 0 Minutes; and 4 Degrees, 20 Minutes, and likewise N E, 13 Degrees, 0 Minutes; which place in their proper Columns in your Field-Book, for the difference of Meridians proper to each Circle; then take up your Table and measure on your Stationary line from *T* to *d*, 5 Poles, 10 Links; from which *d* measure the Perpendicular set-off to *F*, 7 Poles, 5 Links, which put in their respective Columns in your Field-Book; then measure *dE*, 15 Poles, 4 Links, which put down in your Field-Book against the same Stationary length, again repeated; then measure on your Stationary line as far as *e*, (where the next perpendicular off-set falls) 26 Poles, 10 Links, and measure *eG* the off-set, 6 Poles, 5 Links; which lengths put into your Field-Book in their own Columns: Then measure on to *f*, which from your Station at *T*, is found 29 Poles, 12 Links, where it touches the Fence, being called a Tangent line, which length put down in your Stationary Column, filling up the other Columns with Cyphers, because there

is no distance to set off; then measure on your Stationary Line to *g*, which from *T* is 55 Poles, 5 Links, which place in its own Column, with Cyphers in the other Columns of your Field-Book; for the reason just before given; then continue measuring on your Stationary line to *b*, which from *T* is found 56 Poles, 17 Links; then measure *b K*, the perpendicular off-set, 3 Poles, 18 Links, all which put down in the respective Columns in your Field-Book; then measure on to your Station at *V*, being the whole length of your Stationary *T V*, 59 Poles, 7 Links, which put down in its proper Column; and since there is no Perpendicular Angle to take from it, put Cyphers in the other Columns, so is the work of your third Station finished.

IV. Plant your Table at your fourth Station at *V*, so that the Needle hang directly over the Meridian line, where screw it fast; Then direct your Sights to your fifth Station at *W*, observing the Index to cut the Degrees in the several Circles, as your Field-Book directs, for the difference of Meridians proper to each Circle; then take up your Table, and measure from your Station at *V* to *i*, 1 Pole, 10 Links; Measure also the perpendicular distance *i L*, 1 Pole, 18 Links; which numbers place down in your Field-Book according to the foregoing directions; then measure on to *k*, 29 Poles, 14 Links, and the perpendicular distance *k M*, 3 Poles, 1 Link, which place in your Field-Book; then measure on to *l* 33 Poles, 8 Links, which put down in your Field-Book in its proper place, and because it is a Tangent line, fill up the other Columns with Cyphers; then measure on to *m*, 85 Poles, 5 Links, being a Tangent line, therefore put down 85 Poles, 5 Links, in its own Column, and Cyphers in the rest; then measure on to *n*, 89 Poles, 6 Links, and also *n P*, the Perpendicular distance or off-set, 6 Poles, 4 Links, both which Numbers transferr into your Field-Book; then measure on to *o*, 110 Poles, 10 Links, and the Perpendicular off-set *o Q*, 6 Poles, which insert also into your Field-Book; then measure on to *W* (being the whole length of your Stationary-line *V W*) 111 Poles, 13 Links, which place in its proper Column in your Field-Book; which compleats the Work of your fourth Station.

V. Plant your Table fast at *W*, with the Needle over the Meridian line in the Chard, then direct your Sights to *R*, your first Station, where the edge of your Index cuts 193 Degrees, 30 Minutes, in the Circle of 360; and 64 Degrees, 30 Minutes, in the Circle of 120; and *S W*, 13 Degrees, 30 Minutes, in the Circle of four 90s: This done, take up your Table and measure to the first off-set at *p*, 8 Poles, 15 Links, and the off-set *p X*, 4 Poles, and place them down in your Field-Book; then measure on to *q* 34 Poles, 10 Links, it being a Tangent put it down, and Cyphers in the other Columns; then measure the off-set *q Y*, 4 Poles, 2 Links, which place in its proper Column, against 34 Poles, 10 Links, again repeated; then measure to *r*, 52 Poles, and likewise measure the off-set *r h*, 4 Poles, 18 Links, which transfer into your Field-Book; then measure to *x* 73 Poles, 6 Links,

which note down in its own Column, with Cyphers in the rest; lastly measure to the Station R, where you began, whose length W R, is 79 Poles, 5 Links, which note down as in all the examples is directed, with the perpendicular off-set R δ 2 Poles, 3 Links, which concludes the whole work in the Field-Book, as well as in the Field.

Thus 'tis easie to perceive also how any remarkable objects of Note may be taken in order to Protraction, as Gates, Stiles, Trees, Bushes, Ponds, &c. either to the Right or Left.

The Field-Book.

Stations	Circ. 360		Circ. 120		Circ. four 90s.		Per. Set.		Per. Set.		Pol. Lin.	
	D.	M.	D.	M.	Coast.	D. M.	P. Left.	L.	P. R.	L.	Stat.	Diff.
1. Stat. R.	283	30	94	30	NW.	76 30	2	10	0	03	8	
							0	0	40	055	10	
							4	10	0	110	10	
2. Stat. S.	11	45	3	55	NE.	11 45	7	10	0	018	15	
							15	20	0	018	15	
							0	0	0	024	5	
3. Station. T.	13	04	20		NE	13	7	50	0	05	10	
							15	40	0	05	10	
							6	50	0	026	10	
							0	00	0	029	12	
							0	00	0	055	5	
							3	180	0	056	17	
							0	0	0	059	7	
4. Station. V.	104	034	40		SE.	76 0	1	180	0	01	10	
							3	10	0	029	14	
							0	00	0	033	8	
							0	00	0	085	5	
							6	40	0	089	6	
							6	00	0	0110	10	
							0	00	0	0111	13	
5. Station. W.	193	3064	30		SW.	13 30	4	00	0	08	15	
							0	00	0	034	10	
							4	20	0	034	10	
							4	180	0	052	0	
							0	00	0	073	6	
							2	30	0	079	5	

Note that for the proving your Field-work to be exactly taken, follows hereafter in a Chapter for that purpose.

CHAP. XXV.

How to Protract, or lay down upon Paper the Work of the former Chapter two several ways; First by a Scale of Chords; and Secondly by your Protractor, by the help of your Decimal Scale and Field-Book.

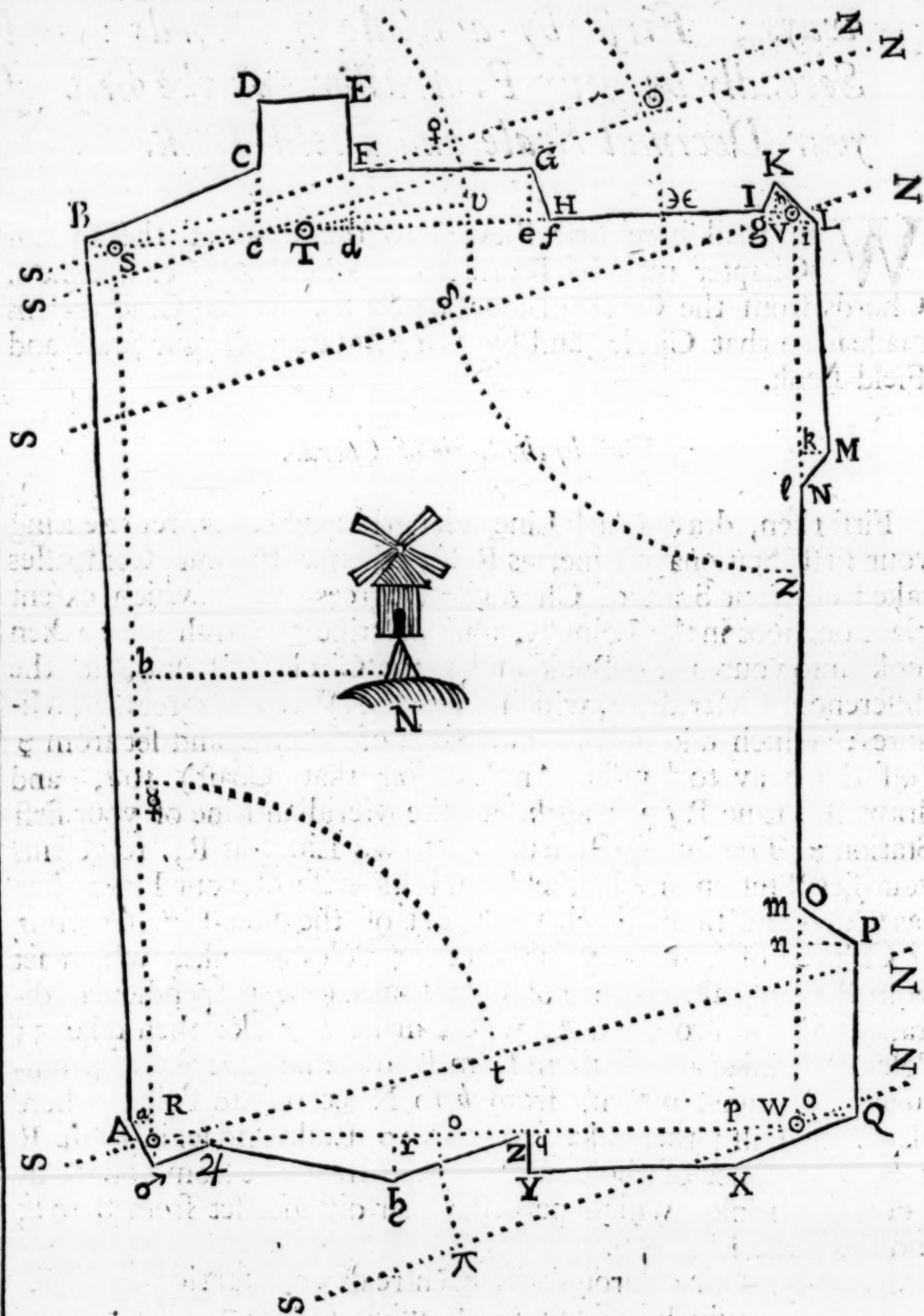
WE shall here first shew how the work of the former Chapter may be Protracted upon Paper, by a Line of Chords from the Circle of four 90's, viz. By the Observations made from that Circle, and by the Assistance of your Scale and Field-Book.

First by the Scale of Chords.

First then, draw a dark Line at length upon Paper, representing your first Stationary Line, as R S; then with your Compasses take from your Scale of Chords 60 Degrees, with which extent place one foot in the Point R, and describe the Arch $q\ t$; then look into your Field-Book under the Circle of four 90's for the difference of Meridians, which is found NW. 76 Degrees, 30 Minutes; which take from your Scale of Chords, and set from q (off that way to lay the Angle upon that Coast) to t , and draw the Line R t at length, for the Meridian Line of your first Station; The intersection of these two Lines at R, represents your first Station in the Field, and likewise of your Plot; then (as your Field-Book directs) take out of the Pole-Line-Column, or Column of Stationary distances, 3 Poles 8 Links, which set from R to a ; take also 2 Poles, 10 Links (the perpendicular distance) and set from a to A, where make a prick; then take 55 Poles, 10 Links, and set them from R to b , and raise the perpendicular $b\ N$, upon which, from b to N set off 40 Poles, where place the Mill; then take 110 Poles 10 Links and set it from R to S, the distance of those two Stations; then take from your Scale 4 Poles, 10 Links, which perpendicular distance set from S to B, and draw the Line A B.

Secondly, Draw through the Centre of your Station S, a Meridian Line, which is done by drawing a Line parallel to your first Meridian; then take 60 Degrees from your Scale of Chords, setting one foot in S, and with the other make the Arch $q\ v$; then from your Meridian Line at q , set off the difference of Meridians (as your Field-Book directs) 11 Degrees, 45 Minutes NE. from q to v ; then from S draw your second Stationary Line as S T; then (according to your Field-Book) take 18 Poles, 15 Links,

Links from your Scale, and set it from S to c ; then set it off from c to C, 7 Poles, 10 Links, where make a prick; again, upon the same perpendicular Line set off 15 Poles, 2 Links, where make a prick; then draw the Lines from these pricks, *viz.* From B to C, and from C to D; then by your Scale set off 24 Poles, 5 Links, from S to T, being the whole length of your Stationary Line.



Thirdly, Draw again through you first Station T, another Meridian Line, as before directed; which done take (as before) 60 Degrees from your Scale of Chords, and make the Arch $\odot \times$; then by the help of your Field-Book, take from your Scale of Chords the difference of Meridians, (at that Station) 13 Degrees, and set it from \odot to \times , and draw that Stationary Line T \times , at

at length; then take 5 Poles, 10 Links, and set it from T to *d*; then take 7 Poles, 5 Links, and set from *d* to F, where make a prick; then take 15 Poles, 4 Links from *d* to E, where make a prick also; then take 26 Poles, 10 Links, and set it from T to *e*; then take the off-set, 6 Poles, 5 Links, and set it from *e* to G, where make a prick; then take 29 Degrees, 12 Links, and set it from T to *f*, where make a prick; likewise take 55 Poles, 5 Links, and set it from T to L, where also make a prick; then take 56 Poles, 17 Links, and place 'em from T to *h*; then set off the perpendicular distance 3 Poles, 18 Links, from *h* to K; then set off 59 Poles, 7 Links, (your whole Stationary Line) from T to V; then draw Lines from the several Pricks, being the extent of the perpendicular off-sets, as from D to E, from E to F, from F to G, from G to H, from H to I, and from I to K; which concludes the Work of, or upon your Stationary Line T V.

Fourthly, Then through the Centre of your 4th Station at V, draw a parallel Line to any of your other Meridian Lines, which shall be your Meridian Line for that Station; then with 60 Degrees from your Scale of Chords, with one foot in the Station V, describe the Arch δz ; then from your Meridian at δ , set off the difference of Meridians SE, 76 Degrees to *z*, and draw the Line V *z* at length, for your 4th Stationary Line; then as before, set off all the off-sets by your Scale, as your Field-Book directs; and the length of your Stationary Line V W also, and draw Lines as before from prick to prick, *viz.* from K to L, from L to M, and so on to Q; which concludes the Work on that Stationary Line.

Fifthly, Draw a Meridian Line through the Centre of your last Station at W, then take (the common Radius) 60 Degrees from your Line of Chords, with one foot of the Compasses in W, describe the Arch πo ; then by your Field-Book the difference of Meridians is SW, 13 Degrees, 30 Minutes, which set from π to *o*, and draw the Line W *o* at length: Now if this Line intersect your first Station at R, your Work may be well protracted, therwise not; then by the help of your Field-Book, Scale, Compasses, prick off the distances against each off-set upon your Stationary Line, and from them the perpendicular off-sets, in the same manner as before directed; and there make pricks, and draw Lines from prick to prick (as before); which includes the Plot upon your Paper as was required.

To perform the former Work by your Protractor.

Secondly by your Protractor.

First, Draw a Meridian Line upon your Paper, and make choice of some convenient place thereon, as at R, to represent your first Station; then lay the Centre of your Protractor thereon in that posture,

posture, that the Meridian Line of your Protractor may lie on the Meridian Line of your Paper; then prick off from your Protractor (from any one Circle, or from all the three Circles, which are answerable to those on the Table, which your Field-Book was made from) the difference of Meridians as your Field-Book directs, which in the Circle of 360, is 283 Degrees, 30 Minutes; and in the Circle of four 90s, the complement to that, *viz.* 76 Degrees, 30 Minutes; and in the Circle 120, is found 94 Degrees, 30 Minutes, all which falls in the point *u*; then draw the Line R *u* at length, for your first Stationary Line; upon which set off, by the help of your Field-Book, Scale and Compasses, the several Stationary distances to the perpendicular off-sets, with the off-sets also, according to the directions in the former part of this Chapter, with the whole length of the Stationary Line from R to S also.

Secondly, From the Stationary point S, draw a Meridian Line parallel to the former, upon which Stationary point, place the Centre of your Protractor, with its Meridian Line directly lying upon the Meridian Line of your Paper; then, as your Field-Book directs, prick off from your Protractor the difference of Meridians (if you will) from each Circle, which is 11 Degrees, 45 Minutes, or 3 Degrees, 55 Minutes, or in the four 90s, 11 Degrees, 45 Minutes, which falls by the edge of your Protractor from these several Circles in the point *v*; then draw the Line S *v*, at length for your second Stationary Line; upon which, as your Field-Book directs, set off by your Scale and Compasses the several Stationary lengths and perpendicular off-sets, according to the preceding part of this Chapter, as also the length of the Stationary Line S T.

According to which Method proceed with the rest of the Angles; and lastly draw the Lines from prick to prick, as from A to B, from B to C, and from C to D, &c. which shall include your Plot upon Paper, as was required.

C H A P. XXVI.

To perform the Field-Work of the XXVIth Chapter, by using the Instrument as a Circumferenter, Chard, and Needle; with brief Directions to perform the Field-Work a more easie and readier way.

TO perform the Field-work by using the Instrument as a Circumferenter, &c. consult Chapter 18; for when the Sights are fixed upon the Table, as the 7th Chapter directs, the Angles (by turning the Table upon the Staff) are made and observed by the Needle upon the several Circles on the Chard; as by the Theodolite and Peractor they were observed, by the edge of the Index upon the Table; so that it will be but time lost to explain this further, for your Field-Book will appear in all respects the same, and consequently the work of Protraction.

To Perform the Work of the former Chapters another way.

And because I would not be too tedious, I shall here briefly exhibit another method to perform the Field-work of this and the former Chapters; which is by planting your Table in every Angle of the said Field, and by directing your Sights from Angle to Angle, observing the Degrees made at each Angle; which with the length of the Ground-Line insert in your Field-Book; thus proceeding round the Field from Angle to Angle till the whole be finished.

E X A M P L E.

As suppose (from any of the three last Figures) you plant your Table first in the very Angle A, in the extream part of the Fence, in the same order as before is taught; directing your Sights to B, observing the Angle there made, and the length of the Ground-Line A B, both which put down in your Field-Book; then plant your Table at B (as before) and direct your Sights to the Angle C, observing the number of Degrees made at that Angle; which with the measure of the Ground-Line B C, transfer into your Field-Book; then Plant your Table at C, and direct your Sights to D, and proceed as before, and so consequently from Angle to Angle till the Work be finished.

And here Note, I cannot but highly recommend this way, only one Inconvenience attends it, and that is, when your Table is planted in the very Angle of any Field, it will be a hard

matter to see the next Angle, so as to direct your Sights there-to, in respect of the Boughs of the Hedge, that generally obscure the Sight. But when you have the advantage of seeing and directing your Sights from Angle to Angle, I advise to make use of this way, when the Instrument is used as a Theodolite, Peractor, and Circumferenter.

Note, Thus have I shewed how to take the Plot of any Ground as at many Stations, as need requires, by the Instrument as a Plain-Table, Theodolite, Peractor, and Circumferenter, in respect my Surveyor may (through custom) have more respect for some one of these Instruments (comprised on this Table) than another, till he be convinced of the necessity of all of them, which one time or another will more naturally perform the Work than another, & *contra*.

Hence I shall proceed Methodically (according to my promise) shewing the nature of plotting all manner of Inclosures, as Lordships, with the Township included, as also the Inclosing of open Fields, the plotting of Woods, Parks, Chases, Rivers, Roads, and whatever else is necessary to be known, or done in the Practice of Surveying by that way, from this Table as is most natural and agreeable to the several Cases as may happen in practice, as you will find them exemplified in the following Chapters.

C H A P. XXVII.

How to take the true Plot of a Lordship, with the Township included, and to express it upon Paper, in the same Order, Form and Quantity it lyeth in the Field.

IN taking the Plot of a Lordship, Authors have described several Methods in their particular proceedings, which I shall not here trouble the Reader with, but briefly exhibit That which by long experience find I to be the best, tying none to the strict observation thereof till their Experience is able to convince them, or their Reason free to admit; And in order to this my Assertion I shall first lay down some general Rules or Directions, and then proceed to the particular exemplification thereof.

I. Walk over the Lordship two or three times, till you can bear the Map thereof in your head, that you may the better conceive to carry on the whole Work, and to make choice of the fittest places for your Stations.

II. Plot your Township first, beginning in the most convenient

ent place to make your first Station as long as possible you can ; and likewise from your mean Stations where the Houses, Homesteads, &c. stands close, make little inner Stations, taking therefrom all Out-Houses, Orchards, Yards, and little intermediate Offices, and returning to your mean Station again, observe this General Rule : Where you cannot from your mean Station see all the Angles, or backsides near Joining thereupon, to make inner Stations as before, and to perform the Work of each mean Station with inner Stations (if need requires) till the Township be finished

III. Where you conclude your Township (if your Table will bear it) from your last mean Station direct your Sights to a Station in some convenient place of the adjoining Field, so may you take the Plot thereof from as many Stations as need requires, so will such Grounds be joined to the Township, and so may you proceed with the next adjoining Ground, and so on as far as the Table will bear.

IV. Your Township being (by the preceding Rules) completed upon your Table, with as many of the adjoining Grounds, as will come thereupon, make marks upon your Plot as you proceeded with your Work where the next Ground joins or falls upon those Fences you have already Plotted, that you may know, when you have taken the Plot of the several Fields or inclosures joining upon your former Plot, how to join them thereto.

V. Proceed where you left off, and take as many of the Inclosures upon your Table as it will bear, and joyn them to their former work, by the directions of the marks before mentioned ; and in this order proceed till the whole Lordship be finished, observing to describe upon your Plot, all Roads, Foot-ways, Gates, Stiles, Trees, Mills, Mountains, Rivers, Bridges, Ponds, Lakes, and whatever is remarkable that you meet with in your Way.

VI. Observe to place the Trees, in each Hedge-Row into the Ground the Fences properly belong to ; so that the Landlord, or Owner thereof may know by inspecting the Map what Fences belong to each Ground : I shall here explain these Rules in part of the Lordship of *Belton* in *Lincolnshire*, by Me Actually performed in the Year 1690 for the Honourable *Sr. John Brownlowe* Baronet, and Member of this present Parliament.

The foregoing Rules or Directions exemplified.

Having set up your Beacons or Station-Marks in the most convenient places, as they are here expressed in the Map, where observe that the mean Stations are gradually numbered as you are to proceed with them, as 1, 2, 3, 4, 5, &c. that is, your First, Second, Third, Fourth, Fifth Station, and your inner Stations with Letters, as A, B, C, &c. to proceed then,

I. Plant your Table at 1, or first Station, and your Sights to all the Angles and places of Note observable in your Sight, and with your Chain, measure each distance on the Ground, as

to *a* and *c*, and with the help of your Scale and Compasses, prick off (from your Station) those distances upon the Paper of your Table; then before you proceed to your second mean Station, direct your Sights through the Gate, to the inner Station at *A*, noting as you go along the meeting Fences, *o o*, and *o o*; then plant your Table at *A*, and direct your Sights to all the Angles in view, as to *d*, *e*, *f*, and *g*, and measure each length upon the Ground; then by your Scale and Compasses lay them down upon your Paper, drawing lines from prick to prick: Then direct to your second inner Station at *B*, and there take the Hall and the Courts in the same order before mentioned; Then repair to your first Station again, planting your Table in the same order as it was at first, and direct your Sights to your third inner Station at *C*, from whence as before, observe and lay down all Angles in Sight from that Station; so have you finished the Work at your first mean Station: But before you remove your Table direct your Sights to your second mean Station, striking a line by the edge of your Index for your mean Stationary line.

II. Take up your Table and measure from your first Station on the Stationary line, to your second mean Station, and in your way, take the Angles, *o o*, and *o o*, and lay down the measure of your Stationary distance, viz. from 1 to 2, there plant your Table and proceed in all respects as in the work of your first Station, observing all the Angles, Houses, Streets, and what ever is within your view; then direct your Sights to your third mean Station, drawing a line by the edge of your Index for your Stationary line.

III. Take up your Table and measure the Stationary distance from 2 to 3, and lay that distance down upon your Paper, where plant your Table and take down (as before) all that is observable in your view; from which Station make an inner Station at *D*, and observe and lay down all the Angles, and places of remark therefrom upon Paper; So have you finished the Work at your third mean Station; and in this order may you proceed from one Station to another (as the work or plot here will sufficiently inform you) till the whole Township be finished.

IV. Note, Your Township being finished at your Eighth Station, direct your Sights therefrom into the further Angle of the Close, call'd the *Offer-Yard*, to the Ninth Station, and so proceed to take the Plot thereof; then proceed from one Ground to another Joyning to the Township, as the Plot hereof, better than many words, will by inspection inform you.

V. Having thus Plotted the Township with the several Inclosures thereto adjoining, as the Map directs; then in order to the carrying on your Work, proceed (having your Table covered with with a fair sheet of Paper) accordingly with the rest of the adjoining Grounds, which joyn to the former in their proper places, according to the directions aforegoing; by which method you see 'tis easy to take the exact Plot of the whole Lordship.

VI. For

PART

OF BERTON

14 ships in

GENCOLENS shore

The Butt Close

The Ofier

Yard

Part of N Deffers

Bottom Sand Close

The Roads

The Parke Pale

Parsonage

Church F

Part of the Parke

A Cannall

Flower Gardens

Water Mill

Kitchen Garden

The Orchard

The Hall

The Plantation

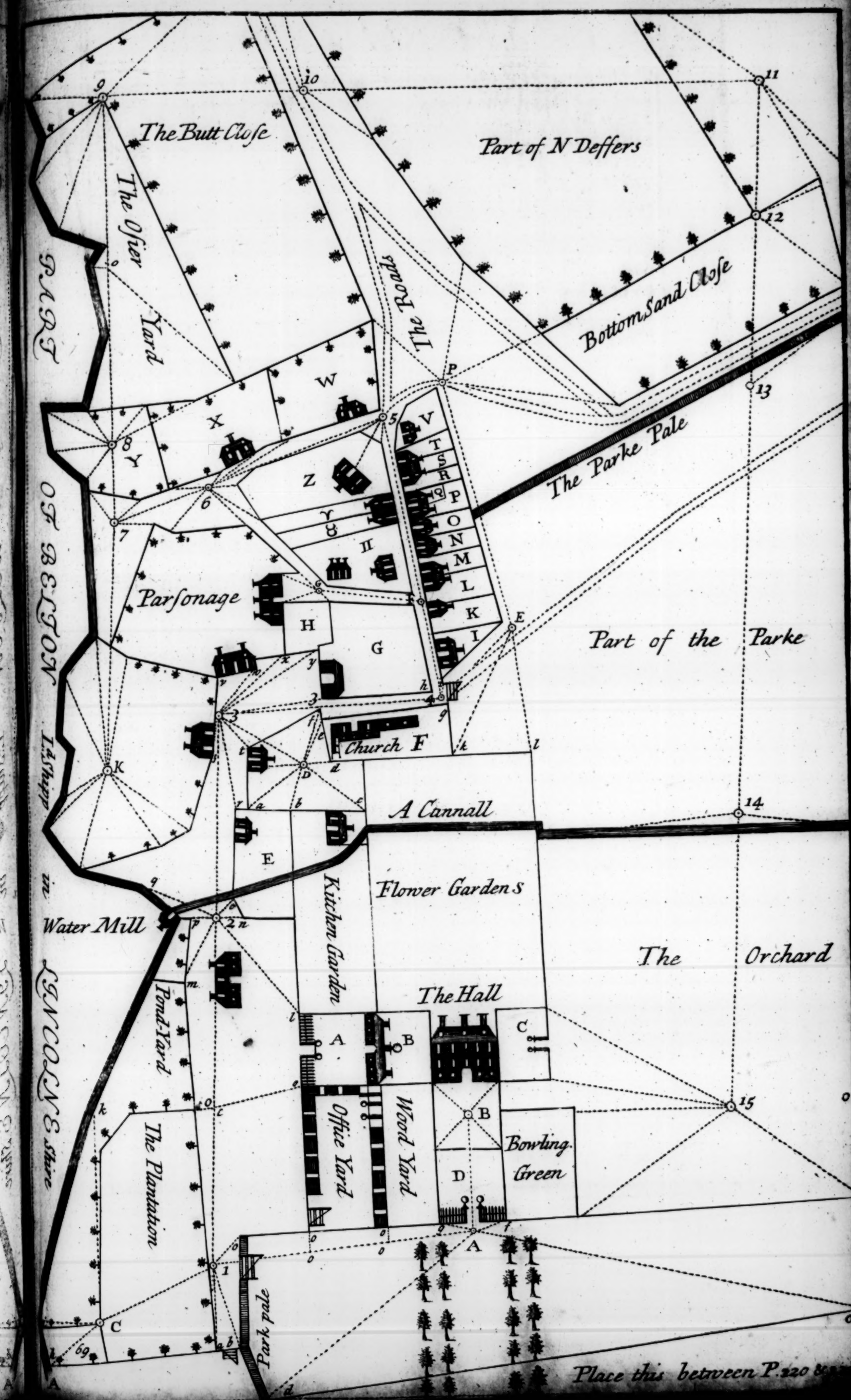
Office Yard

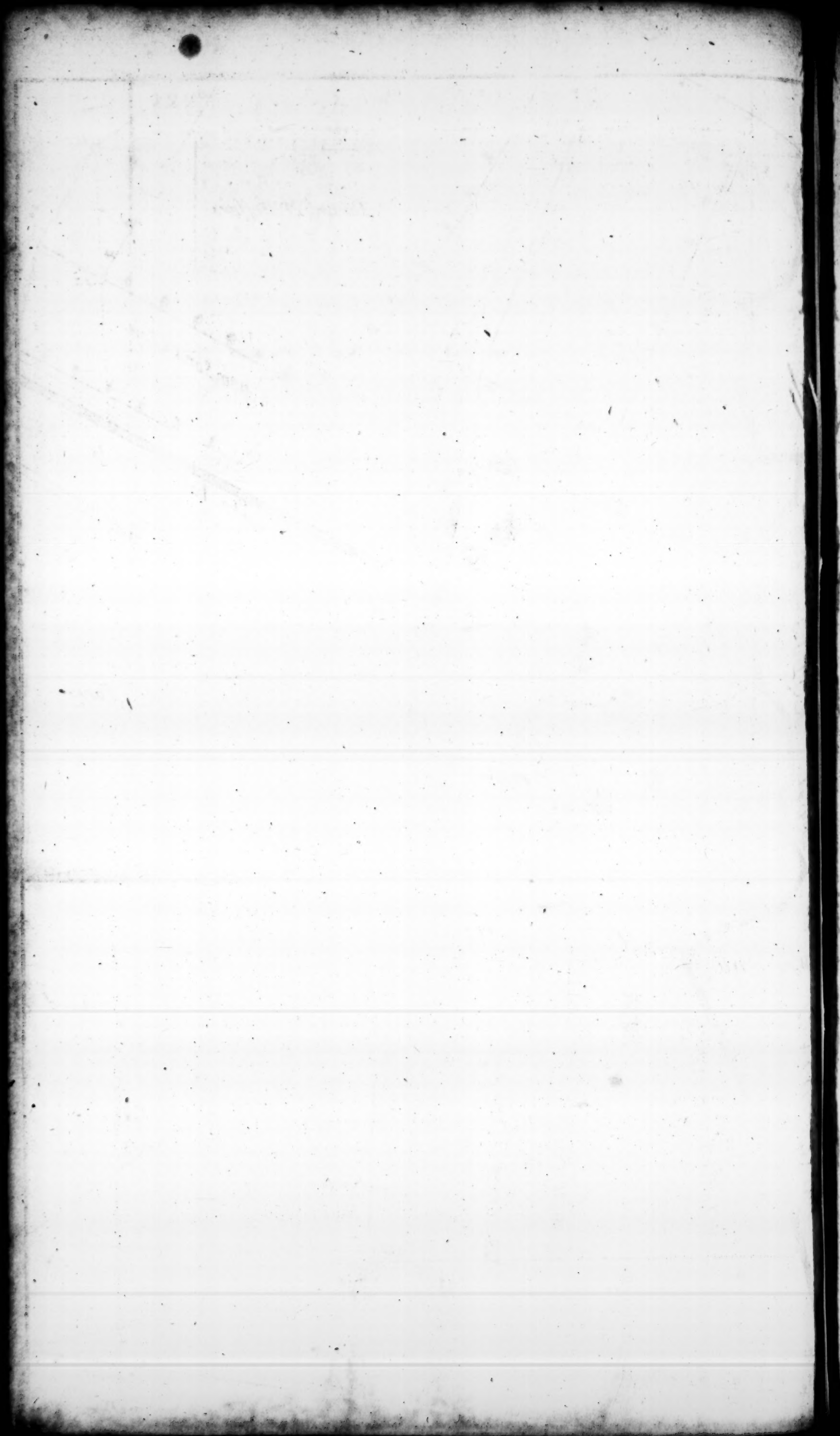
Wood Yard

Bowling Green

Park pale

Place this between P. 220 & 221





VI. For the further accomplishment of the Work, observe to express the just number of Acres, Roods, and Perches in each Ground, with the name it is called by; and in the Town where the Yards, Orchards, and Homesteads are small, Notifie them with Capital Letters; then Collect them into a Table, with the the Names of the Tenants so inhabiting; that the true quantity of each particular Homestead may appear, for the further satisfaction of the Landlord or Owner.

VII. Observe also what Lordships border upon the Lordship you are then Measuring, and take the Plot of, and where each Lordship terminates; where make Marks of distinction, and on the verge of your Plot betwixt the Marks of distinction of each Lordship so bounding, write, *Part of such a Lordship*, and consequently of all others that border upon it.

VIII. In your fair Draught, in some vacant place without the verge of your Plot, make several Square, Round, or Elliptical Tables, to contain an Epitomie of the whole Lordship, viz. The Names and Quaintity of every particular Ground; observe also to place the Fly in some convenient place thereof, to shew the Situation, or point of bearing; not forgetting to Beautifie your Map with the Coat of Arms belonging to the Landlord, or Owner thereof.

The foregoing Rules or Directions, well understood, are sufficient to perform the Plotting of any Lordship whatsoever.

C H A P. XXVIII.

The true Method of taking a Plot of Uneven, Hilly, or Mountainous Grounds, in respect of their true Quantity, and otherways, by the Plain-Table.

ALL Authors I have yet met with, are very Lane and Deficient in this particular; all that I find they take notice of, is to find the Quantity of the Hypothenuse and Horizontal Line of any Hill, and so resolve it as a Triangle for to find the quantity thereof, or by measuring the Diagonal of a Hill; in which 'tis observable, they all take it for granted, that the Hills are always of a Regular Form, all sides of one length, and stand upon a Horizontal bottom; otherways their Rules are defective and will not do: But this seldom or never happens in any Grounds, for it is certain in all Hilly Grounds, that the Hills are some higher, some lower, and of various irregular forms, or joyning or running confusedly one Hill into another; some near the top,
some

some nearer the bottom, making several little Planes and Valleys betwixt them. This material case wants Explaining, and Rules to perform it by, which I shall here furnish my Surveyor with; which are briefly in two respects: The first is, For to take the true Plot thereof that shall express the true quantity of the said Ground in Acres. The second is, To take the Plot thereof as a Plain and Even Ground, by going about the outsidess thereof; which way of Plotting is nothing different from the Work of the Twenty Third Chapter: The Map thus taken is to be joined to the Plot of your Lordship, in respect the greatest part of the Lordship consists of Plain and Even Grounds; in which Map you are to express all the several Hills as they lie in the Ground by shadowing them with your Pencil upon your Paper; so I proceed to explain the Rules by an Example for the Plotting a Hilly Ground that shall express the true quantity thereof.

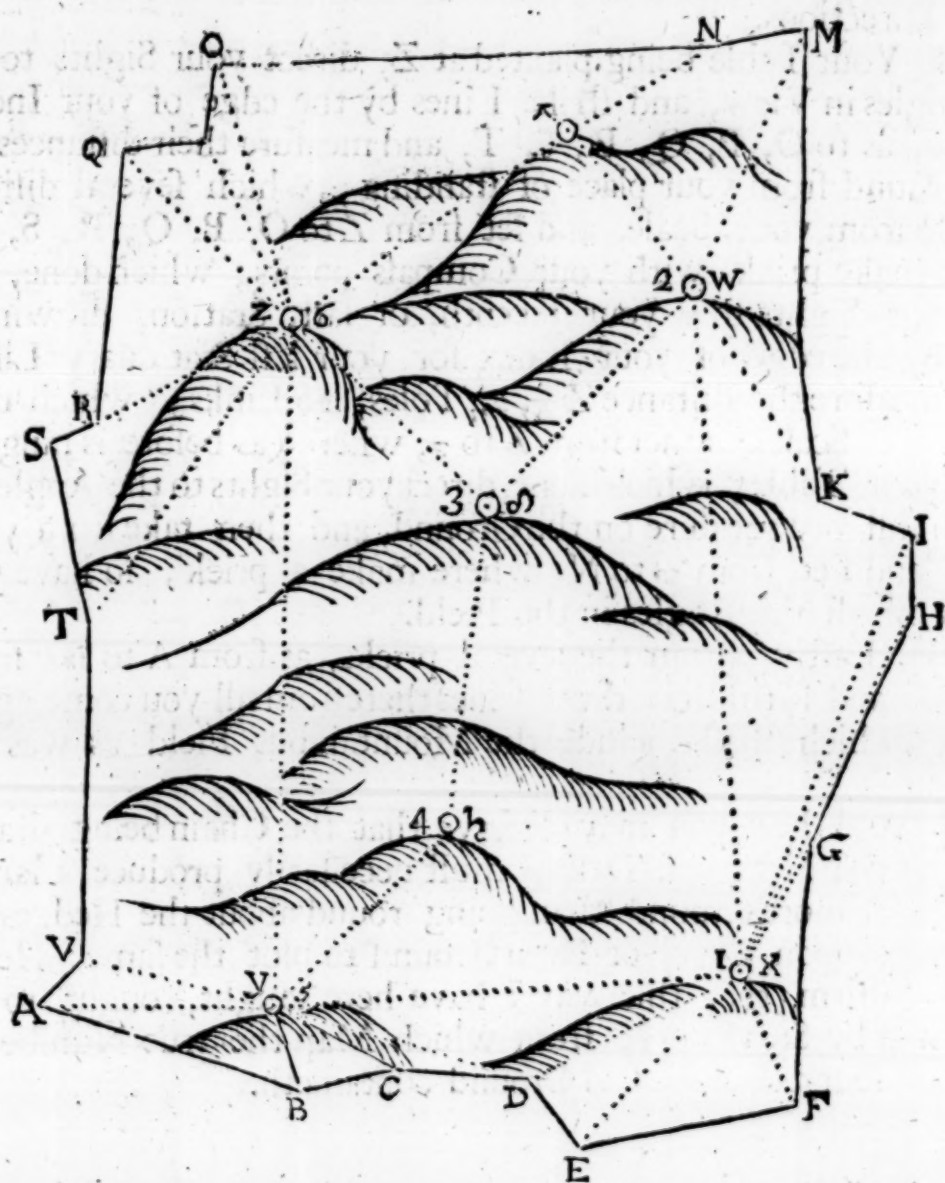
I. In a Ground where there are Multiplicity of Hills running one into another irregularly or confusedly, place Beacons on the top of several of the highest or most material Hills, whither you can see the Angles in the Hedges, or Hedges themselves from several of the said Hills, it matters not; and direct your Sights from Station to Station, laying down each Stationary Distance upon your Paper from your Scale; placing your Beacons or Station-Marks so, that your Chain in measuring these Stationary distances, and so on to other Stations, where the Hedges may be seen, may pass over all the (or the most material) Hills in the Ground, as we shall here demonstrate.

II. Admit the Figure Noted with A, B, C, D, E, F, &c. be a Hilly Ground to be Plotted, whose just number of Acres is required; set up Beacons or Stationary Marks upon the tops of most of the material Hills, as at X, W, δ , h , Y, Z, π .

III. Plant your Table at X, your first Station, directing your Sights therefrom to the Angle D; then with your Chain, measure the distance X D on the Ground, which is found 18 Poles, 15 Links, which take from your Scale and set from X to D, where make a prick; then direct your Sights to E, whose distance from X is found on the Ground 18 Poles, 8 Links, which take from your Scale, and prick off from X to E; then direct your Sights to F, whose Ground Line is found 10 Pole, which prick off from X to F, on your Paper; then again direct your Sights to G and H, whose Ground-Lines are found 9 Poles, 15 Links, and 29 Poles, 16 Links, which (with your Scale and Compasses) set off upon your Paper; so have you finished the Work of your first Station.

IV. Direct (before you alter your Table as it stands planted at your first Station) your Sights to your second Station at W, drawing your Stationary Line by the edge of your Index, and measure the length of the said Stationary on the Ground, which is 52 Poles, 10 Links, which take from your Scale, and set it from X to W, where place down your Table, laying the edge of your Index upon the Stationary Line X W; your Index resting in this posture,

posture, turn the Table gently upon the head of the three-legged Staff, till through the Sights you espie your first Station-mark at X, where screw it fast; then direct your Sights to all the several Angles in view, as to K, L, M, and measure their several distances from your Station at W, as W K, 18 Poles, 5 Links, and W L, 10 Poles, and W M, 21 Poles, 15 Links; which several distances take from your Scale, and prick them off upon their Respective Lines upon your Paper.




V. Then (as before) direct your Sights to δ your third Station, and draw a Line by the edge of your Index; then measure on the Ground from W to δ , which is found 23 Pol. 7 Links, which take from your Scale and set from W to δ , where plant your Table as was directed at your last Station: Now because you cannot see the Fences in any part of the ground by reason of the Hill from this Station, therefore direct your Sights to h , your fourth Station, which distance δh , measure on the Ground 23 Poles, 5 Links; which take from your Scale, and set from δ to h ; where plant your Table by the former Directions, and direct your Sights to Y, your fifth Station; then measure the Stationary distance, $h Y$, 20 Poles, which

which take from your Scale, and place from π to Y, where plant your Table.

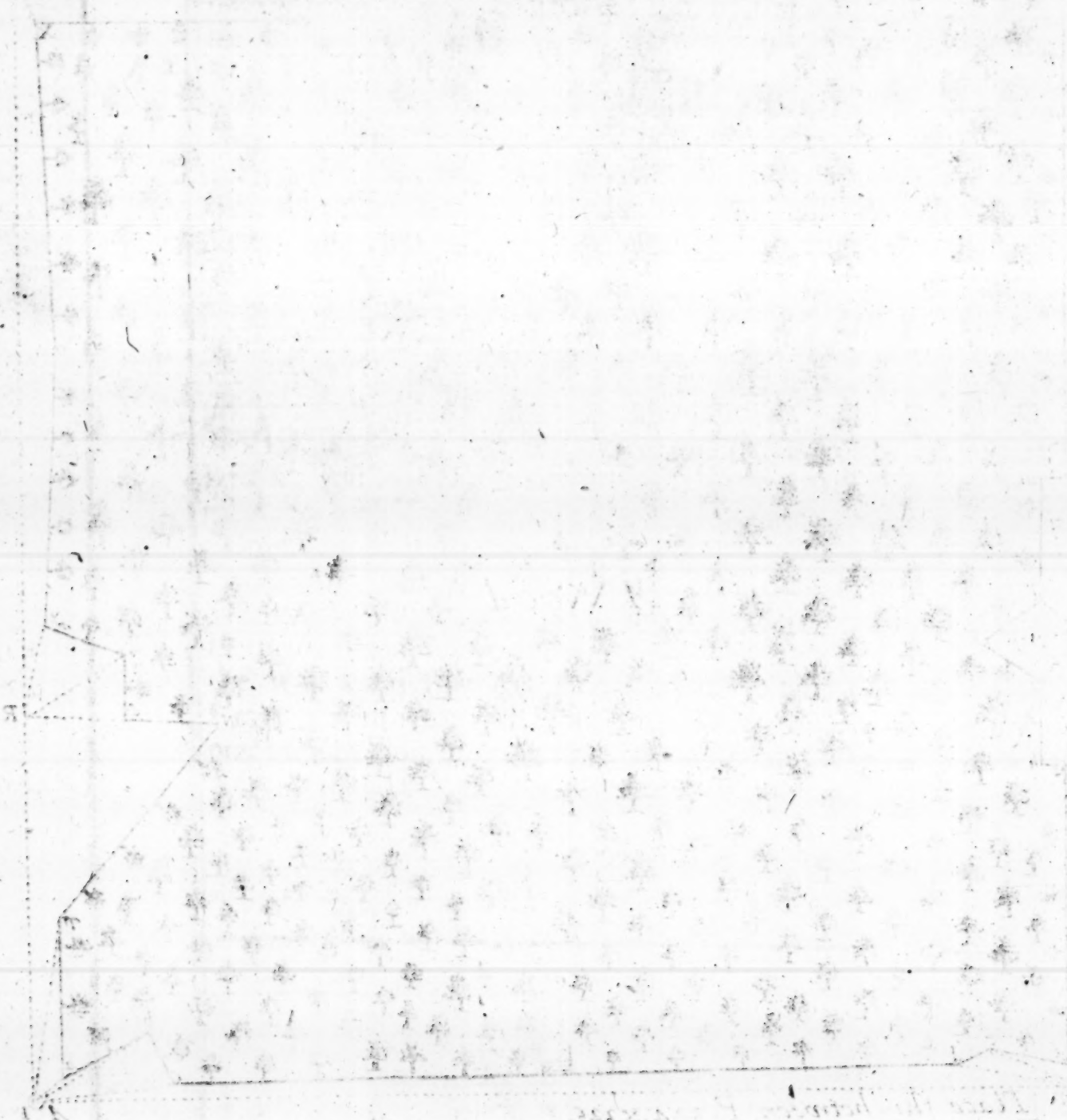
VI. Then direct your Sights from your Station at Y, and therefrom observe, measure, and lay down upon your Paper as you were directed at your first and second Stations; then direct your Sights to your sixth Station at Z, and strike a Line by the edge of your Index for your Stationary Line, whose length on the ground is found 50 Poles, 5 Links; which take from your Scale, and set from Y to Z; where plant your Table by the foregoing Directions.

VII. Your Table being planted at Z, direct your Sights to all the Angles in View, and strike Lines by the edge of your Index thereto, as to O, P, Q, R, S, T, and measure their distances on the Ground from your place of standing; which several distances take from your Scale, and set from Z to O, P, Q, R, S, T, where make pricks with your Compass points; which done, direct your Sights to π your seventh, or last, Station, drawing a Line by the edge of your Index for your last Stationary Line; then measure the distance Z π , 24 Poles, 10 Links; which take from your Scale, and set from Z to π , where (as before is taught) plant your Table; which done, direct your Sights to the Angle N, which distance measure on the Ground, and then take from your Scale and set from π to N, where make a prick; so have you prickt off all the Angles in the Field.

VIII. Lastly, From the several pricks, as from A to B, from B to C, and so to D, &c. draw Lines therefrom till you come again to A, which shall include the Mountainous Field as was required.

 And here you may observe that the Chain being drawn over all the Hills and Dales, must necessarily produce a larger Plot, viz. more Ground, than going round about the Hedges all the way upon Level or Even Ground to plot the same: Hence I may affirm that this way I have here taught, ought to be practised by Surveyors; from which Map the true Number of Acres is found that the said Ground containeth.

THE AMERICAN



C H A P. XXIX.

How to take the Plot of a Wood or Forest by the Plain-Table, when, by reason of the Wood growing thereon, you cannot see any convenient way before you; with brief Rules to perform the same by the Circles on the Table, according to the Theodolite, Peractor, and Circumferenter.

IN the performance of this Work I shall use as much brevity as conveniently I can; for if the work of the XXIII. Chapter be well understood, this must be so likewise: For the difference of Measuring and Plotting of a Wood or Forest from other Grounds, consisteth in this one particular, *viz.* Whereas by reason of the Thick Wood growing on the Ground, you cannot see any convenient distance before you, therefore proceed on the outside, as in other Grounds you do on the inside, by setting up Station-Marks in the most convenient places in the Grounds adjoining, and so take all the Angles from you, as the following Figure and Directions will further inform you.

E X A M P L E.

Admit the Figure Noted with the Letters, *a, b, c, d, e, f, g, h, i, k,* &c. be a Wood or Forest, whose Plot (retaining the true quantity of Acres) is required.

I. Place your Beacons or Station-marks in the adjacent Grounds round about the said Wood, as at A, B, C, and D; then plant your Table at A, and direct your Sights to all the Angles in view; as to π , *a, b,* and *c*, striking Lines by the edge of your Index; then with your Chain measure the length of each Line on the Ground, as from A to π , is found 16 Poles, 15 Links; which take from your Scale, and prick off upon your Paper from A to π ; then from A, to *a*, on the Ground, is 2 Poles, 17 Links; which likewise take from your Scale, and set from A, to *a*, upon your Paper; then the Ground-Line A *b*, is found 11 Poles, 7 Links, which accordingly take from your Scale, and set from A to *b*; your next Ground-Line A *c*, is found 11 Poles, 12 Links, which likewise take from your Scale, and set upon your Paper from A to *c*: Thus having taken and laid down upon your Paper all the Angles in view at the first Station, direct your Sights to your second Station at B, drawing a Line by the edge of your Index; which done,
S f
take

take up your Table, and with your Chain measure the Stationary distance, which is found 90 Poles, 2 Links; which take from your Scale, and set from A to B, where place your Table.

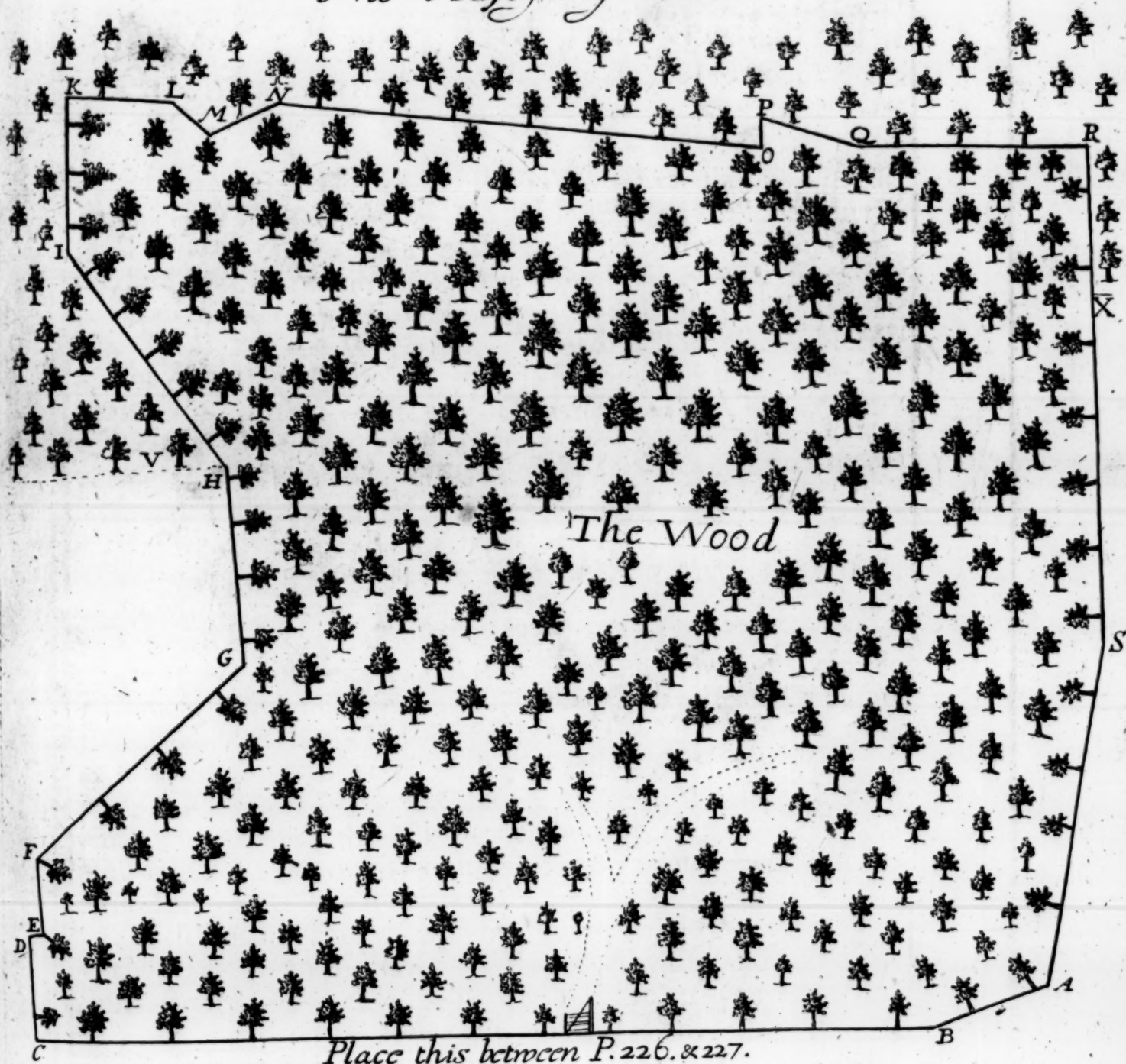
II. Your Table being set down at B, lay the edge of your Index upon the Line A B, and turning the Table upon the Head of the Staff, till through the Sights you espy your first Beacon or Station-Mark at A, there screw it fast; then direct your Sights to all the Angles in view, as to *d, e, f*; then measure with your Chain their lengths on the Ground, which lengths take severally from your Scale, and prick them off from B to *d, e, and f*, according to the direction at your first Station; which done, direct your Sights to your third Station at C, drawing a Line by the edge of your Index; then take up your Table and measure on the Stationary Line B C, till you come at X; which distance take from your Scale, and set from B to X, where plant your Table according to the preceding Directions, directing your Sights to the Angles *g, h, i, k, l, m, n*, drawing Lines by the edge of your Index, and measuring their respective distances on the Ground; which several lengths take from your Scale, and set from X to *g, h, i, k, l, m, and n*; that done, take up your Table, and measure on to your third Station at C, and there proceed in all respects as is taught in the Work of the first and second Station; and so consequently from one Station to another till the whole Work be finished; and lastly, draw Lines from prick to prick, *viz.* from *a* to *b*, from *b* to *c*, from *c* to *d*, so to *e*, and so on till the whole Plot be included; as the Figure or Plot foregoing, better than many Words will inform you.

Performed by the Circles on the Table.

The former Work may be as exquisitely performed by the Circles on the Table, according to the Theodolite, Peractör, or Circumferenter; and because I would not be guilty of Tautology, I refer the Reader to the XXIV. Chapter of this Book, this Work being no other than what is there plainly taught; and though in the performance hereof you go round on the outside, as you are there directed on the inside, yet it makes no difference in the carrying on the Work; for the Field-Book having Columns for the Set-offs both to the Right and Left, demonstrates the Work to be performed after the same way; and the XXV. Chapter shews how to protract the Plot thereof upon Paper, as it is taken from the Circles of the Table, which being understood, will not need my further Explanation here.

C H A P.

The Adjoyning Wood



Place this between P. 226. & 227.

C H A P. XXX.

How to take the Plot of a Wood or Forest, which joyneth to another Wood or Forest, that you are not concerned to measure, when you cannot (by reason of the joyning of the Woods) see any convenient Way before you, by the Chard and Needle, as a Circumferenter.

TO take the Plot of a Wood or Forest that is in part bounded by another Wood or Forest, as we hinted in the XIII. Chapter of this Book, in the description of the Chard and Needle; may be performed by the Chard and Needle from the Circle of four 90's, two several ways: The first is by planting your Table near the Wood-side, and by direction of the Needle you may be able to keep a straight Line, and therefrom take the Angles either to you or from you, as the XXIV. Chapter hereof Directs. The second way is by planting your Table in every Angle, directing your Sights (as they are fixed on the Table, by turning the Table about upon the Head of the Staff) straight on the Fence or Hedge-Row; whether you can see the next Angle or no it matters not, and by observing the Angle the Needle makes with the Meridian Line, which note down in your Field-Book, with the length of each Line also: And this is the method I most approve of, and shall further Explain it by the Example or Demonstration following: And here observe to fix your Sights on the Table, as the VII. Chapter hereof directs; then suppose the following Figure Noted with the Letters A, B, C, D, E, F, G, H, I, K, L, M, N, O, P, Q, R, S, to be a Wood or Forest, which is bounded on the North-side, and on part of the East and West-side, with another Wood, which you are not concerned for, as the Lines V and X express.

I. First then, Plant your Table in the Angle A, turning it gently about upon the Head of the Staff, till you direct your Sights straight on the Hedge-Row, or Fence, to your next Angle at B, *viz.* from A to B, where screw it fast; then observe what Quadrant or Quarter of the Circle the Needle rests in, and what Degrees it there cuts; which we find SW, 47 Degrees, 30 Minutes, which put down in your Field-Book; then measure with your Chain the length of the Ground Line A B, which is found 10 Poles, 18 Links, which place down in your Field-Book also.

S f 2

II. Plant

II. Plant your Table at B, turning it upon the Head of the Staff, directing your Sights exactly on the Fence or Hedge-Row, *viz.* from B to C, where screw it fast, observing the Needle to rest in the N W. Quadrant, on 83 Degrees, 30 Minutes, which put down in your Field-Book; then measure with your Chain the length of the Line B C, which is found 81 Poles, 15 Links; which put down in your Field-Book also.

III. Plant your Table at C, turning it upon the Head of the Staff till you have directed your Sights on the Hedge-Row, *viz.* from C to D, screw it fast, and you'll find the Needle rests just over the Meridian Line in the Chard; for which write North and South in your Field-Book; then measure the Line C D with your Chain, whose length is found 8 Poles, 14 Links, which put down in your Field-Book also.

IV. Plant your Table at D, directing your Sights to E, where screw it fast; finding the Needle to rest NE, 76 Degrees, 30 Minutes; which put down in your Field-Book, with the length of the Line D E, 2 Poles, 8 Links also.

V. Plant your Table at E, and by turning it about, direct your Sights on the Hedge-Row to F, where screw it fast; and again you'll find the Needle to rest over the Meridian Line; hence write North and South again in your Field-Book; then measure the length of the Line E F, with your Chain, which is 6 Poles, 3 Links; which accordingly put down in your Field-Book.

VI. Plant your Table at F, directing your Sights (by turning the Table) on the Hedge-Row to G, where screw it fast; in which posture you'll find the Needle to rest upon 52 Degrees, 30 Minutes NE, which put down in your Field-Book; then measure with your Chain the length of the Fence or Hedge F G, 26 Poles, 14 Links; which transcribe into your Field-Book as before.

VII. Plant your Table at G, and, as in all the former Angles, direct your Sights on the Hedge-Row to H, where screw it fast; and finding the Needle again to rest directly over the Meridian Line, note down North and South in your Field-Book; then measure with your Chain the length of the Ground-Line G H, 17 Poles, 12 Links; which also put down in your Field-Book.

VIII. Then again plant your Table at H, where you find the other Wood begins to joyn upon you, still observing the same Method, by directing your Sights on the Fence or Hedge-Row from H to I, where screw it fast; and finding the Needle to rest over 31 Degrees, put them down in your Field-Book, with the length of the Ground-Line H I, 24 Poles, 10 Links: And in this order may you proceed from one Angle to another, till you have finished or gone round the said Wood.

The rest of the Angles are taken as the Field-Book directs, according to the foregoing Directions, which being well understood, are sufficient to perform any thing in this Nature.

I have

I have been the larger upon this useful performance, because I have met with no Directions in any Authors to this purpose.

The Field-Book.

The Angles.	Circle four 90 ^s .			Measure.	
		Coast.	D.	M.	P. L.
1	A B	SW.	74	30	10 18
2	B C	NW.	83	30	81 15
3	C D	North and South.			8 14
4	D E	NE.	76	30	2 8
5	E F	North and South.			6 3
6	F G	NE.	52	30	26 14
7	G H	North and South.			17 12
8	H I	NW.	31	00	24 10
9	I K	NE.	5	00	14 5
10	K L	SE.	83	00	9 18
11	L M	SE.	38	50	4 0
12	M N	NE.	73	30	6 10
13	N O	SE.	80	30	44 5
14	O P	North and South.			2 4
15	P Q	SE.	70	20	10 5
16	Q R	SE.	85	00	20 0
17	R S	SW.	3	50	45 0
18	S A	SW.	15	30	31 7

C H A P. XXXI.

How to protract upon Paper the Work of the former Chapter.

First lay your Paper (which let be of that bigness that may contain your Plot) before you, smoothe upon a Table, with your Field-Book also before you; then fixing upon some convenient place of your Paper, as at A, draw a Line at length as A a, for a Meridian Line, noted (as here) with North and South; then look into your Field-Book, and see which way the first Angle coasts, which is SW; Then lay the Centre of your Peractor upon A, keeping the Meridian Line of your Protractor, upon the Meridian Line of your Paper A a, with the Semicircle of your Protractor to the same Coast your Field-Book directs; and therefrom

from (according to the Direction of your Field-Book) prick off 74 Degrees, 30 Minutes, drawing the Line A B, which is to contain 10 Poles, 18 Links.

II. Through the point B draw another Meridian Line (which is nothing but a parallel Line to the former) as B b; then lay the Centre of your Protractor upon the point B, with its Semicircle towards the same Coast your Field-Book shall inform you, with the Meridian Line of your Protractor upon the Meridian Line of your Paper B b; then in the Field-Book, against the second Angle B, I find NW, 83 Degrees, 30 Minutes, which I prick off from the Semicircle of the Protractor, and draw the Line B C, which is to contain in length 81 Poles, 15 Links.

III. Then through the point C draw another Meridian Line as before, as C c, now in the Field-Book against the Angle C, is written North and South; so that I have no more to do here, but to set the length thereon taken from your Scale, as your Field-Book directs, which is 8 Poles, 14 Links; which (as I just now said) take from your Scale, and set from C to D, and draw the Line C D.

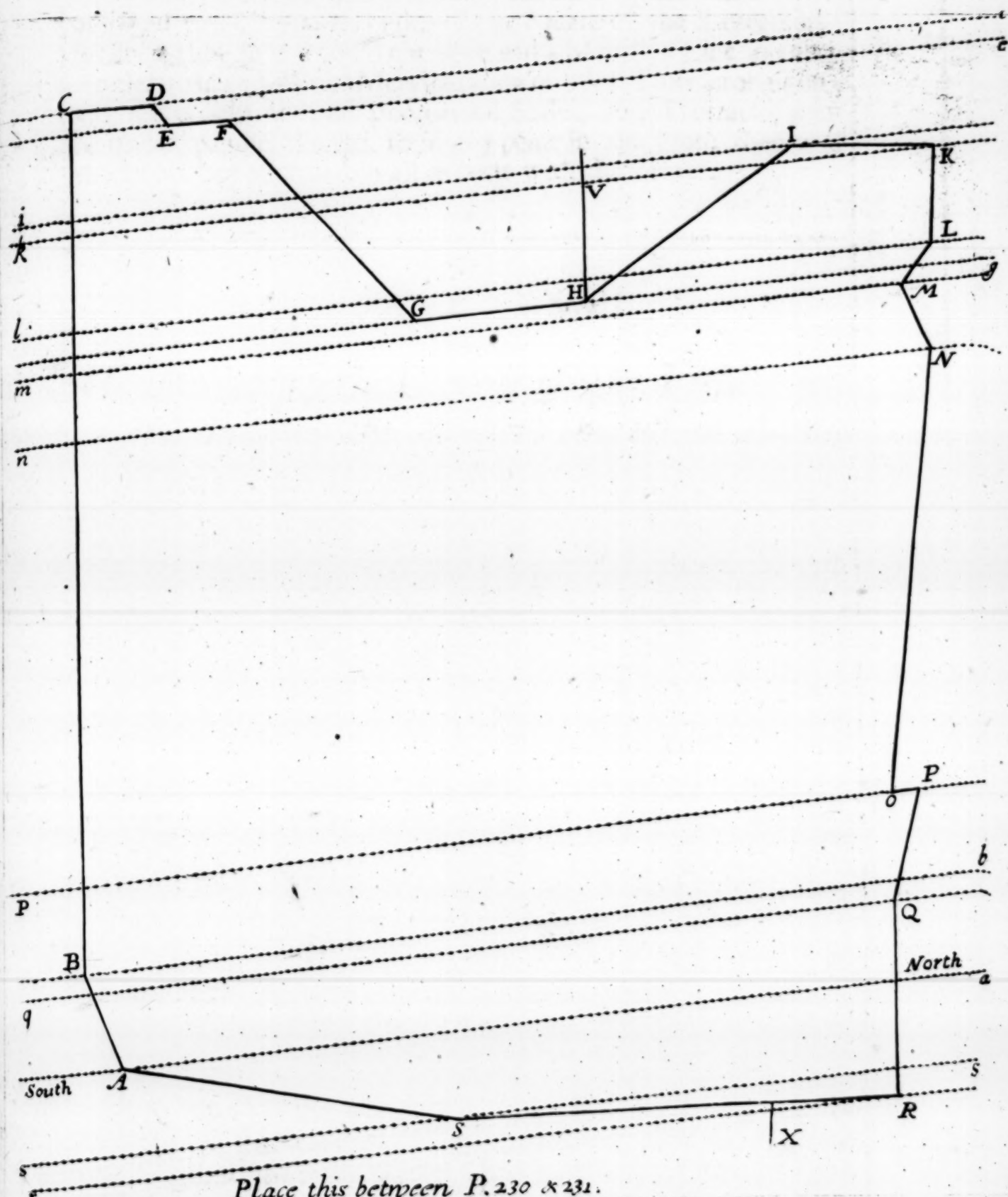
IV. Upon the Meridian Line last drawn, place the Meridian Line of the Protractor with its Centre upon the point D, and the Semicircle towards the Coast your next Angle bends to; your Protractor resting in this Posture, repair to your Field-Book, where finding against the fourth Angle D, 76 Degrees, 30 Minutes, NE, which prick off from the Semicircle of the Protractor, and draw the Line D E to contain 2 Poles, 8 Links.

V. Draw a Meridian Line through the point E, then against the fifth Angle E in the Field-Book, I find North and South; here I have only 6 Poles, 3 Links to take from my Scale and set from E to F, and draw the Line E F.

VI. Then upon the last Meridian Line E F e, upon the point F, I place the Centre of the Protractor, with its Meridian Line lying exactly on the Meridian Line E e, not forgetting the former caution of laying the Semicircle of the Protractor to the same Coast the Field-Book directs; which at the sixth Angle F, is NE, 52 Degrees, 30 Minutes, which prick off the Semicircle of the Protractor; and draw the Line F G in length 26 Poles, 14 Links, according to the direction of the Field-Book.

VII. Then through the point G, draw another Meridian Line; then repair to the Field-Book, where I find North and South, which proceed with to set off according to the third and fifth Directions.

VIII. Upon the last Meridian Line G H g, in the point H, place the Centre of the Protractor, as is taught in the fourth and sixth Directions, which I find by my Field-Book NW, 31 Degrees; which I prick off from the Centre of the Protractor and draw the Line H I, whose length I find by the Field-Book, 24 Poles, 10 Links, which I take from the Scale and set from H to I; and in this manner proceed with the rest of the Angles, till the whole Plot be protracted upon Paper: See here



Place this between P. 230 & 231.

2007 2007 2007 2007 2007 2007



here the whole demonstration, which will further the Judgment of my Reader.

Performed another Way.

And here Note, The foregoing Protraction might have been performed by drawing parallel Lines for Meridians at a venture, provided they had been nearer together than the length of the Scales, of equal parts, upon the sides of the Square of the Protractors; for then though you could not have had a Meridian Line in every Angle, to have laid the Meridian Line of your Protractor upon; yet by the help of those aforementioned Scales, your Protractor may be placed parallel thereto, to fit any point in the Plot; then will the Work be performed in all respects with the former.

C H A P. XXXII.

How to cast up the Content of any Field-Plot, and to find the Content thereof in Acres, Roods and Perches.

Although the Work of this Chapter is taught in the 17th Problem of the Second part of the Book of *Geometry*; yet we shall make it here more plain and applicable to our present purpose by the Example following.

Admit the following Figure Noted with the Letters A, B, C, D, E, F, G, H, I, be the Plot of a Field laid down from our new Scale, whose Content in Acres, Roods and Perches is required.

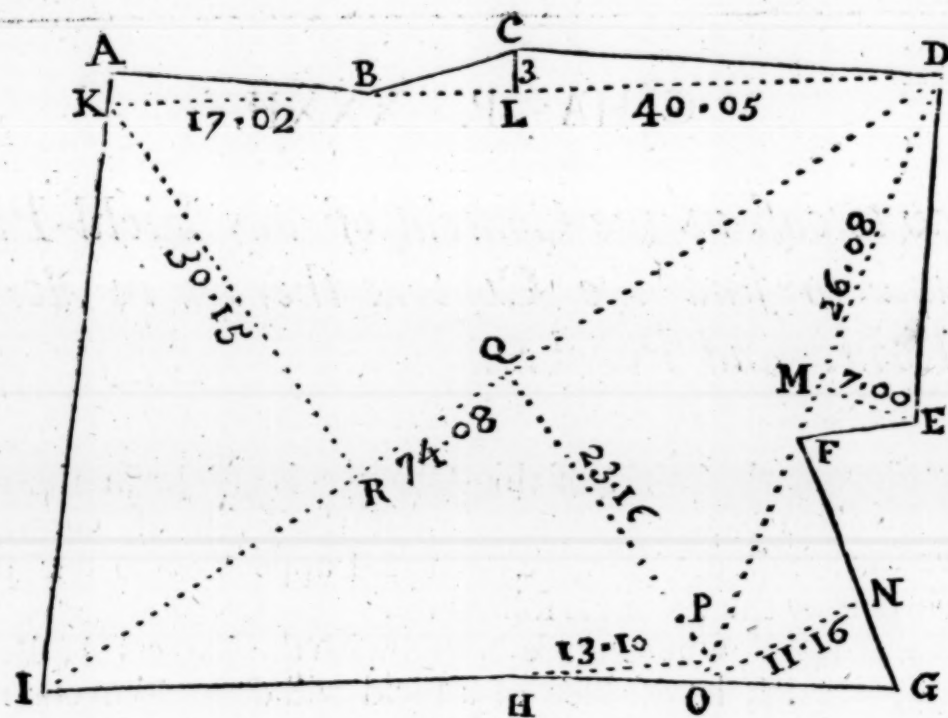
First, Then (and in all such Cases) divide your Plot into Trapezia's and Triangles; accordingly this Figure is divided into one Trapezium, as K, D, P, I, and five Triangles; for finding the Area of all which, begin with any one first, and multiply the whole of the Base by one half of the perpendicular, or (which is all one) the whole of the Perpendicular by the half of the Base; the Product eitherway is the Content of that Triangle in Perches.

E X A M P L E.

First, Measure the Trapezium K, D, P, I, by taking first the Diagonal or Base-Line, D I, into your Compasses, and applying that length to the Scale, which I find reaches 74 Poles, 8 Links; accordingly the Measure of the Perpendicular K R, is found 30 Poles, 15 Links; which added to the length of the other Perpendicular P Q, 23 Poles, 16 Links, the Summ is 54 Poles, 11 Links, or 54 Poles,

Poles, 5 Primes, 5 Seconds (as is taught in the Description and use of the Chain in the Second Chapter) which multiply into half the Base, 37 Poles, 2 Primes, gives in the Product 2019 Perches, and $\frac{25}{100}$ parts of a Perch. In the like manner in the Triangle A B K multiply 17 Poles, 1 Prime, the Base, by 1 Pole the half Perpendicular; which Product gives the Content of that Triangle 17.1; and in the same order I proceed to find the Contents of all the rest of the Triangles, which at last I collect, or add into one Sum; which is the Area or whole Content of the Field in Perches, and parts of a Perch, as it is here underneath adjusted.

And here observe the Measures of each Line are expressed upon the Plot.



		Perc.	Pts.
The Area or Content in Perches and the parts of a Perch.	Trapezium	K D P I.	2019 26
	Triangle	A B K.	17 10
	Triangle	B C D.	60 37
	Triangle	D E F.	92 30
	Triangle	F G O.	107 38
	Triangle	O H P.	6 75

The Area of the whole Field in Perches 2303 16

Then according to the Directions of the Sixth Chapter these 2303.16 Perches may be reduced into Acres according to any of the three ways there taught, which amounts to 14 Acres, 1 Rood, 23 Perches; and so much doth the former Field contain.

C H A P. XXXIII.

A ready and easie Way for Shifting of Paper.

IT very ordinarily falls out in practice, that your Table as it is covered with Paper is too little in several cases, especially in great Grounds, where the Lines outstrip or overrun the Table; in such a case (when you have proceeded so far till your Lines run off on the Paper or Table) you must shift your Paper, and put a fair sheet upon the Table.

First then upon your last Stationary Line which runs off on your Table, observe to shift that Sheet so far off or besides the Table, that your last Station marked thereupon may be marked just upon the Table; to which sheet (in this order) glew a fair Sheet with Mouth-glew, and so fasten them down with the frame of the Table.

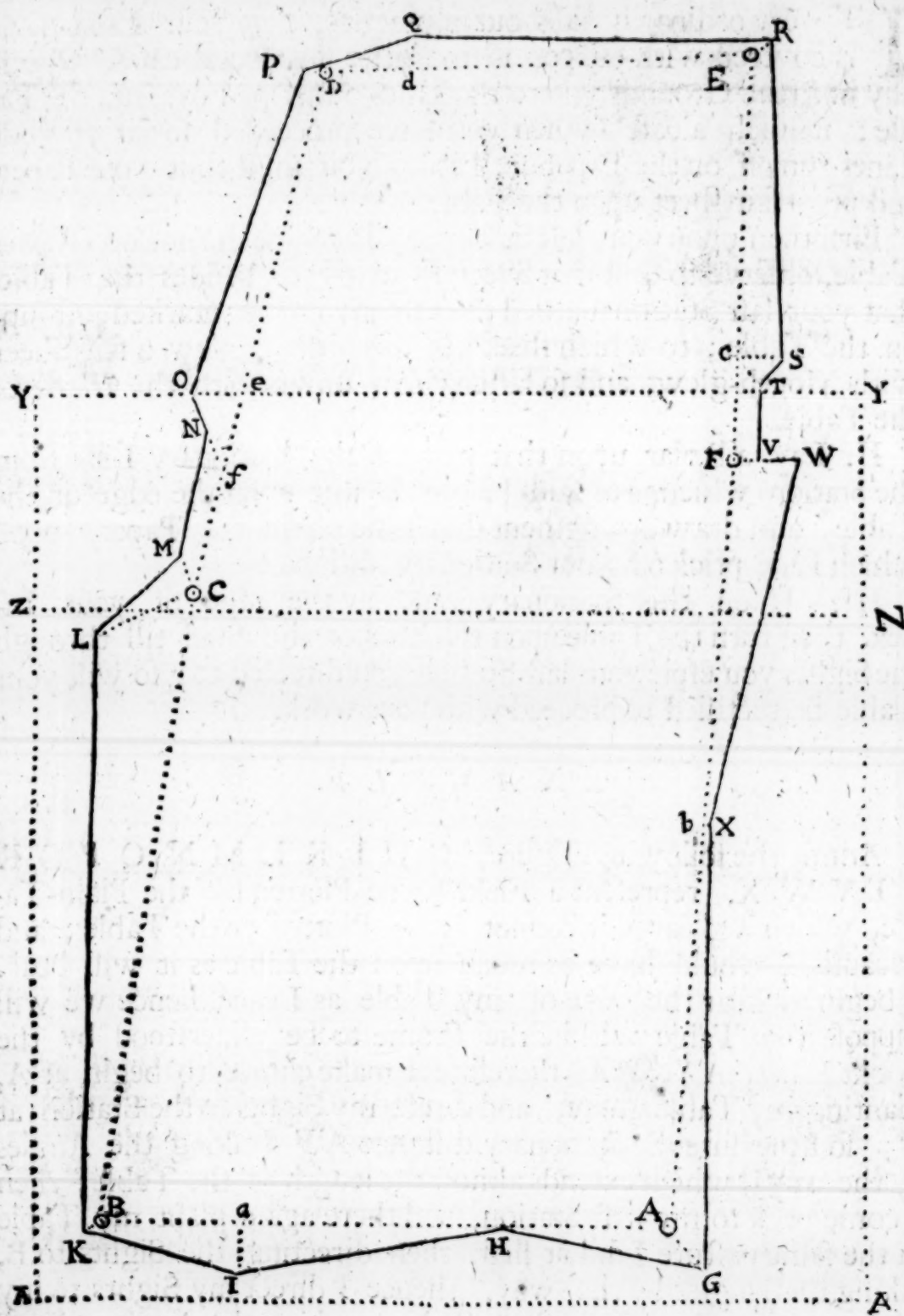
II. Lay a Rular upon that part of the Stationary Line from the Station which, as I said before, is just upon the edge of the Table, and draw or augment that Line on the fair Paper, upon which Line prick off your Stationary distance.

III. Upon this Stationary Line lay the edge of your Index, then turn the Table upon the head of the Staff till through the Sights you espie your last Station you directed to; so will your Table be rectified to proceed with your work.

E X A M P L E.

Admit the following Figure, G H I K L M N O P Q R S T V W X, represent a Field to be Plotted by the Plain-Table, which is so large it cannot all be Plotted on the Table; and because I would have as much upon the Table as it will bear, I begin as near the edge of my Table as I can; hence we will suppose the Table within the Frame to be understood by the prickt Lines, A Y, Y A, therefore I make choice to begin at A, planting my Table there, and direct my Sights to the Station at F; so I measure the Stationary distance A F (taking the Angles by the way) which extends almost the length of the Table; then I come back to my first Station, and there again plant my Table in the same posture I did at first, then directing the Sights to B, taking the Angles by the way, thence I direct my Sights to my Station at C, where I plant my Table, taking the Angles therefrom that are in view; then I direct the Sights to the Station at D, drawing a Line by the edge of my Index to the further end my Table, as C d, where it runs off on the Table; then because I can proceed no further before I shift my Paper, and put a clean Sheet upon the Table; I take this Sheet off, and with Mouth-glue

glew, I glew another sheet to it at Y Y; then I put them both upon the Table in this order, *viz.* I bring the Station C to the Station B upon the Table, and so fasten them down with the Frame, so that the Line Z Z, possesseth the place of the Line A B, so that, part of your Plot is yet upon the Table, *viz.* From C to e,



and the rest (being almost all) of the Table, being covered with fair Paper; then plant your Table again at the Station C, laying the edge of the Index upon that part of that Stationary Line which was drawn before your Paper was shifted, *viz.* C e, and extend it

it to D, upon your fair Paper, and then proceed to finish your Plot.

Note, There is another way to perform this Work by, *viz.* By the Scales of equal parts upon the Frame of the Table, which is taught in several Authors; so that I shall not trouble my Reader with it here, by reason this way I have here taught is much plainer, easier, and in all respects as exact as any way I have yet met with.

C H A P. XXXIV.

How to know whether a Plot be truly taken, and of proving the Work at every Station (as you go along) to be truly taken or not; and in case of Errour how to find and correct it before you be too far past it, taken by the Plain-Table.

First in the Plotting any Field or Ground by the Plain Table, be sure to let your Beacon or Station-marks stand up in every Station-hole till you have finished your Plot; and likewise Whites or Marks in most of the material Angles in the Field, all which will be of great use for proving the work of your Plot as you go along, or proceed with your Work; which by these few following Directions will inform you whether you have proceeded right or not; and in case of an Errour committed, how to find it where is.

II. When you are departed from your first Station, and have proceeded to your second Station, and taken all your Angles by the way, and planted your Table at your second Station, in order to proceed to your third Station; and would know whether the Work of your first and second Station be truly taken: Direct your Sights to one or more of the most material Angles you took, as you proceeded from your first to your second Station; and if the edge of your Index cut the Angles upon your Plot, your Work is so far, truly taken, otherwise not.

III. When you have planted your Table at your third Station, and taken all the Angles by the way; then direct your Sights from your first Station; and if you find the edge of your Index to cut your first Station upon your Plot, your Work is exactly performed to your Third Station, where you then are: But in case you cannot see your first Station-mark from your Third Station or Place of standing, then according to the last Rule of Direction

rection, direct your Sights to some Angle in the Field which you have taken upon your Plot, and if the edge of your Index cut the same Angle upon your Paper, your Work is right, otherwise not.

IV. Likewise when your Table is rightly planted at your fourth Station, and all the Angles betwixt your third and fourth Station being taken, cast your Eye into that part of the Field you have Plotted, and view which of your Station-marks you can see that you are already come from, *viz.* either first or second; as suppose you could see only your second Station-mark, then direct your Sights from your fourth Station, or Place of standing, to your Second Station; and if the edge of the Index cut the second Station upon your Plot, your work is so far perform'd right, otherwise not; and if at any time you cannot see some one or more of your Beacons, or Station-marks, besides the last you came from, that you have already passed, then make use of some Angle, to prove your Plot by, as I said before; and by observing this Method, 'tis easie to know whether you have committed any Errour or not, and if you have, how and where speedily to find it before you be gone far past it; which is so plain and easie that it needs no farther Demonstration.

C H A P. XXXV.

Of proving the Field-Work taken by the Circles on the Table, representing the Theodolite, Peractor, Circumferenter, &c.

According to the Way or Method of Plotting, delivered in the Thirtieth Chapter, by finding the quantity of every Angle by going round about a Field, there is one general Rule to prove the Field-Work by, if the Work be performed according to the Theodolite, *viz.* from the Circle of 360 Degrees, which most Authors make use of; which take as followeth: And,

First, Note that the quantity of Degrees each Angle contains are to be reckoned in the inside of the Plot, or their Complements to 360 without, *viz.* Of all those Angles that bend inward.

Therefore Multiply 180 Degrees, by a Number less by two than the Number of Angles in your Plot; the Product (if your Work be true) will be equal to the Sum of all the Angles observed added together.

But to prove the Field-Work according to the Natural performance of this Imperial Table, according to the several Circles there-

thereupon, and as the 24 Chapter directs, I need but only observe the proportion one Circle bears to another, as for Example.

In the Field-Book of the 24 Chapter, page 120, I add all the Angles of the Stationary distances together, taken by the Circle of 360 Degrees, which make 605 degrees, 45 Minutes; Then I add all the Stationary Angles taken from the Circle of 120 Degrees, which make 201 Degrees, 55 Minutes; Now the proportion betwixt these two Circles is as 3 to 1, so that adding 3 times 201 Degrees, 55 Minutes, makes 605 Degrees, 45 Minutes, agreeing with the Circle of 360 Degrees, which shews the Stationary Angles to be truly taken; then the Circle of four 90's, will either be the same with the Circle of 360 Degrees or its Complement thereto, as the bare Sight of the Field-Book will further inform you: So likewise may you prove the Field-Work of every Station as you proceed with your Work, which is very easie and of excellent use.

C H H P. XXXVI.

How to take the Plot of a Field only by help of the Chain, otherways than is taught in the fourth Book.

AT some time or other it may so happen that you may be required to take the Plot of a Field when you are destitute of all other Instruments but your Chain, Pocket-Rular, and Compasses; in such a Case observe these following Directions.

Admit this following Figure, Noted with the letters A, B, C, D, E, F, represents a Field, of which the Plot is required.

First, then measure the length of the Hedge or Fence AB, whose length is found 53 Poles, 13 Links; then measure the length of the Fence BC, which is 43 p. 05 l.; as also from A to C, (which is the Base-line proper to that Angle) which is found 67 p. 04 l.; all which write down in your Field-Book, as here it is denominated in the first Triangle ABC.

II. Then measure the second Triangle in the same order, beginning at C, and measuring to D, which length is found 19 p. 02 l.; then measure from D to E, which is 38 p. 00 l. and likewise the Base-line CE, to that Angle, 54 p. 10 l. all which put down for the second Triangle.

III. Then observe the last Angle which is an outward Angle, and must accordingly be measured on the outside of the Field, and likewise so Noted down in your Field-Book; so the length of the line EF, is 15 p. 10 l. and AF, 25 p. 12 l. and the

the Base-line to that Triangle A E, 38 p. 15 l. all which insert into your Field Book as follows.

First Triangle A B C inward.

	P.	L.
A B	53	13
B C	43	50
A C	67	04

Second Triangle C E D inward.

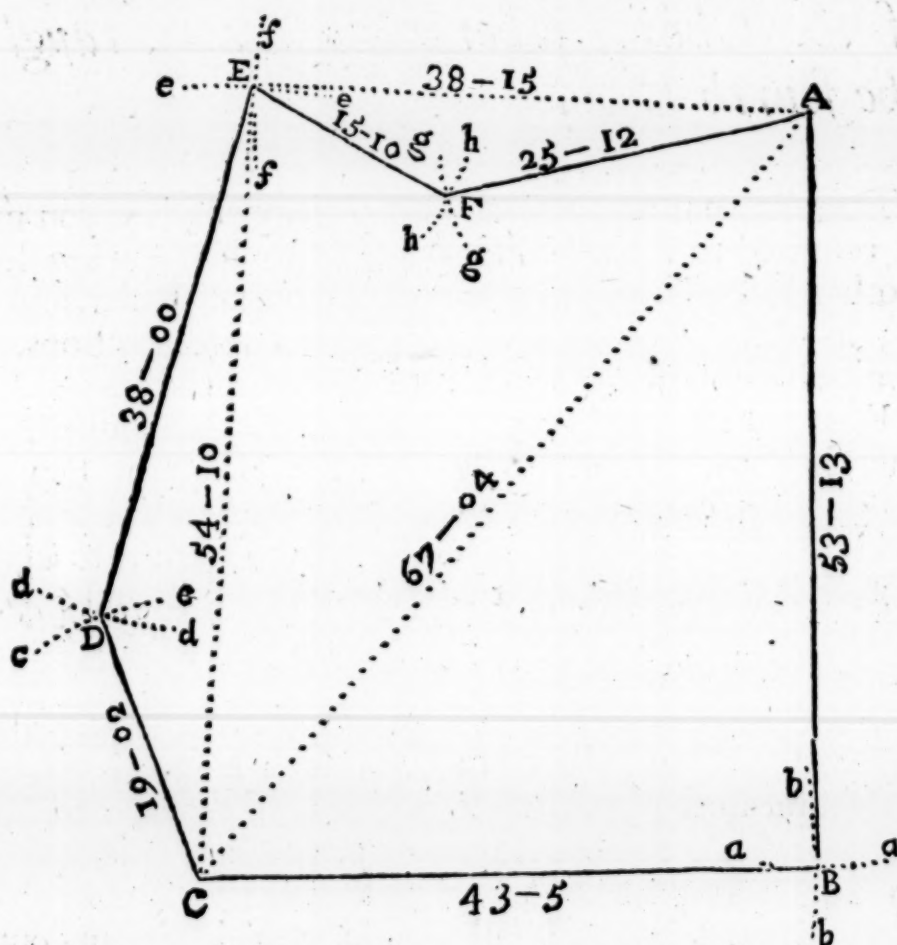
C D	19	02
D E	38	00
C E	54	10

Third Triangle A E F outward.

E F	15	10
F A	25	12
A E	38	15

Directions how to Protract the Former Work upon Paper.

First then draw a line upon your Paper at Pleasure as A C, and take from your Scale the length of that line, 67 p. 04 l. and set it



from A to C; then take from your Scale the length of the line A B, 53 p. 13 l. placing one foot in A, and with the other make the part of an Arch *aa*; then take the length of the line B C, into

into your Compasses from your Scale, placing one Foot in C, and with the other foot cross the former Arch at B, as *bb*, then draw the two lines A B and B C.

II. Take from your Scale 54 p. 10 l. the length of the Base-line CE, and placing one foot of the Compasses in C, with the other make the portion of the Arch *ee*, then take with your Compasses the length of the other Base line E A outward 38 p. 15 l. setting one foot in the point A, and with the other cross the former Arch at E, as *ff*, which point E is the extream Point or meeting Angle to both the other two Angles.

III. For the protraction of the Triangle C B D, take with your Compasses from your Scale the line C D, 19 p. 02 l. with which distance, place one foot of your Compasses in C, and with the other make the Arch *cc*, then with your Compasses take the length of the line D E, 38 p. 00 l. placing one of the Compass points in E, and with the other cross the former Arch at D, as *dd*, from which interfection and from the points C and E draw the two lines, *viz.* C D and D E.

Lastly from the Triangle A E F, take first into your Compasses 15 p. 10 l. the length of the line E F, placing one foot in E, and with the other strike the Arch *bb*, then take likewise A F, 25 p. 12 l. setting one foot in A, and with the other cross the former Arch at F, as *gg*, and where these two Arches intersect one another as at F, draw lines therefrom as from A to F, and from F to E, so is your whole Plot protracted upon Paper as was required.

And here Note, you must be careful to note down, as you measure the said Field, the Situation of the Angles, *viz.* inward and outward, for fear of committing a mistake when you come to protract the same.

C H A P. XXXVII.

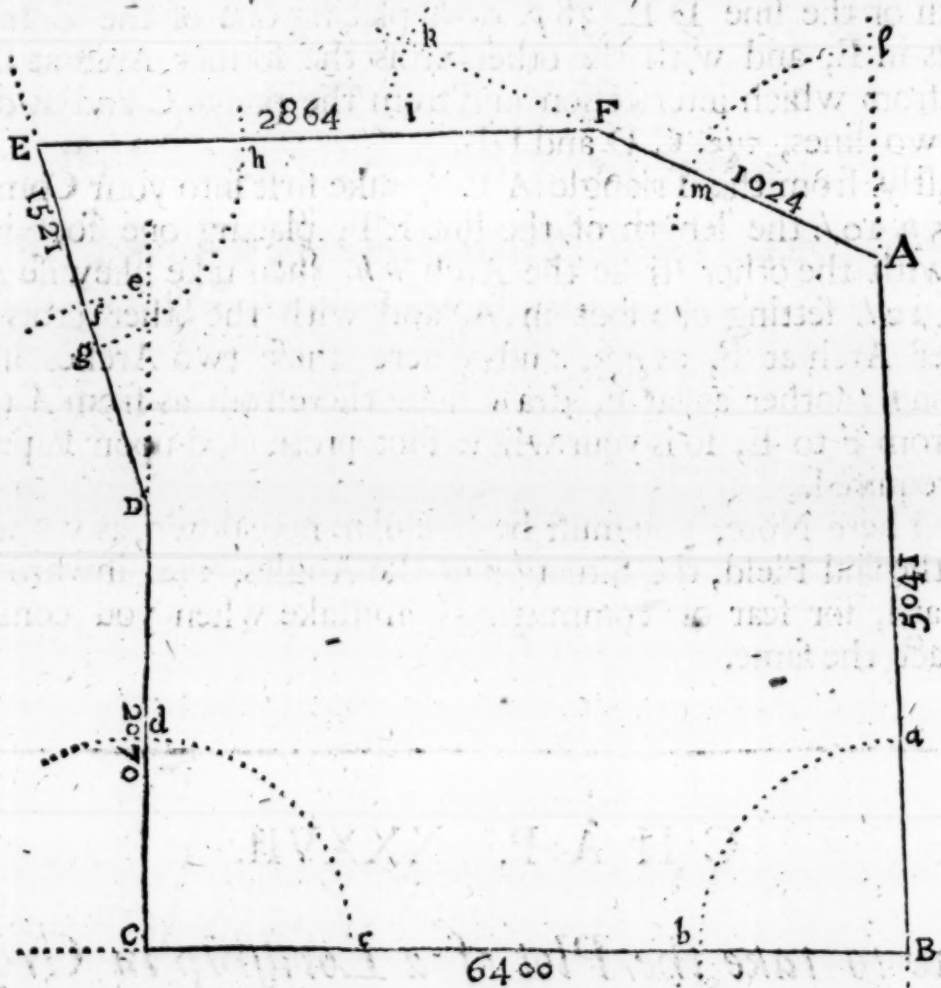
How to take the Plot of a Lordship in Gross, or of any Champain Field, without shifting the Paper, upon the Plain-Table, which may contain 2000, 3000, or 4000 Acres.

THIS way I am here about to illustrate is both easy, exact, and useful, for by placing your Table at every Angle, you are to take each Angle and his sides, without laying down from your Scale the true length of each Ground-line, as in the former Chapters, only measure the true length of each Hedge or Ground line, drawing it in its due order and Situation upon your Table, and write down its true length (not regarding the not closeing of

of your Plot at Last) and in this order proceed from one Angle to another, still keeping the limits of your Plot upon your Table, which is to be Protracted upon Paper according to its due proportion, when you come home.

EXAMPLE.

Suppose this following Figure Noted with the Letters A B C D E F, to be the Circumference of a Lordship, or some large Champain Ground, First place your Table at A, and direct your Sights to B, and draw a line by the edge of your Index, representing the line A B, then direct your Sights to F, and draw the line A F to any convenient length, then measure the length of the line A F 1024 Perches, and write it down upon the said line, then take up your Table and as you go on to B mea-



sure the line A B which is 5041 Poles, which write down upon the said line: Which done, plant your Table at B, according to the Rules delivered in the twenty third Chapter hereof: Then making choice in some convenient place of the line A B, as at B, for your Second Station, from thence direct your Sights to C, and by the edge of your Index draw a line at a convenient length, then measure the said line 6400 Perches which write down upon the said line, then in some convenient place of the line B C, as at C, plant your Table, and direct your Sights to D, drawing a line at length by the edge of your Index; then with your Chain, measure its length

length, viz. from C to D, 2070 Poles which write down upon the said line.

In the same manner plant your Table at D, and direct your Sights to E, drawing a line at length by the edge of your Index; then measure the length of the Ground-line D E 1521 Poles, which also write down upon the said line.

Lastly in some convenient place of the line D E, as at E, plant your Table, and direct your Sights to F, and draw a line by the edge of your Index as before, then measure with your Chain the length of the Ground-line E F, whose length is found 2864 Poles, which also write down upon the said line, so is your Field-work finished, because you have the length of each Ground-line, and the true quantity of each Angle.

Note. And here Note that it is not to be supposed that the Plot taken upon the Plain-Table will close or come together as here, for that is not to be expected, tho' I have so ordered and disposed this Figure in respect it should also shew (to save labour) the Way or Method of Protracting or laying down the exact Plot upon Paper, for tho' the Last and First lines will not meet nor come together, it matters not, in respect you have the length of each line written down, and the true quantity of each Angle taken upon the Table, which is sufficient to Protract the true plot thereof upon Paper by these short directions following.

How to protract upon Paper the former Work in its true Proportion and Quantity.

First then draw a line at length upon your fair sheet of Paper as A B, (which to avoid prolixity we shall referr to the former Figure, Supposing it in proportion to the greater Magnitude to be truly taken) then from the Scale you would have your Plot protracted from, take in your Compasses the length of the line A B, 5041 Perches, which place from A to B, then opening your Compasses to a convenient distance, strike the Arch-line (both upon that Map you took upon the Table, and here) *a b*, then take the quantity of that Angle as it was laid down upon your Plain-Table, and set it from *a*, to *b*, then draw the line B *b*, at length, and (as before) take from your Scale the length of the line B C, 6400 Perches, which extent set from B to C, then lay down the quantity of the Angle at C, as you did that of B, as *a b*, and in this order may you proceed from one Angle to another till you have gotten the exact Map upon your Paper, as the foregoing Figure better then many Words may better inform you.

C H A P. XXXVIII.

Short Notes or Directions for taking the Map of a County.

THis is a Work which very few Authors of Surveying have touched upon, and indeed for me to demonstrate it in all respects, will take up more time and room than I can spare; therefore I shall now treat of it with as much brevity as conveniently I may.

I. One common way that has been delivered by some Authors is by taking the Latitude and Longitude of the most Notable and Material Towns in the said County, especially all the Market-Towns, by which their distance has been laid down upon the Map; but this is very faulty: First, By reason the Latitude is erroneously stated in several great Towns, and not known to all: Secondly, The Longitude of places was never yet so well agreed upon, as to be either credited or trusted to by our late Geographers in such a case as this: And Thirdly, our English Miles are not near rightly adjusted to the Degrees in the Heavens; for which reasons I shall forbear explaining this way further.

II. The taking the Plot of a County may most exactly be performed by using this Instrument as a Theodolite, whose use is sufficiently taught in the former Chapters; and here note by the way, that the distances of Market-Towns, and the length of all other Lines you have occasion to measure, is best measured by the Wheel, which needs no description, since the making of it is so well known to our Mathematical Instrument-makers; which by driving before you, tells the distance in Miles, Furlongs, &c.

III. In the beginning of your Work observe to begin at some Great Market-Town, noting down its Church and what is material to be taken; and from thence proceed to measure the next Great Town, taking all the other intermediate Towns, and also all Parks, Rivers, Forests, Intersecting-Roads, &c. in your way, which you are carefully to note down into your Field-Book, which Protract upon Paper every Night; you may also describe the quality of the Country as you go, viz. Whether Hilly, Woods, or the like; and whatever is remarkable in your way; and to this way of Working, some of the exactest County-Maps may be very useful; and in this order proceed from one Town to another till the whole County-Map be finished.

VI. But that way I most affect, (and am well assur'd is best and most exactest of all others) is by taking the particular Map of each Lordship, which may be performed by this Instrument used as a Plain-Table, or more properly as a Theodolite; whose
uses

uses to this purpose may be consulted in the Twenty Fourth, Twenty Fifth, and Twenty Sixth Chapters of this Part ; and so by joining each Lordship to another, as you was directed to joyn each Ground to another in the Twenty Seventh Chapter, which Chapter duly considered, may be looked upon as an Epitomie of this whole Matter ; for the Work is indifferently the same ; for whereas that Chapter plainly Demonstrates the taking of the exact Map of a Lordship, laying down the particular Grounds one by another ; so in this 'tis but laying each Lordship down by another as you find they be in the County, which may be laid down by as small a Scale as you please, by which you may proportion your Map to what Magnitude you think most convenient

V. These brief Rules being well understood, and the Surveyor well grounded in the practical Part of the former Chapters, he will be sufficiently furnished for the taking of a County-Map ; which is all I shall here say concerning this matter.

John Wing.

The End of the Fourth Book.

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THE
ART
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BOOK V.

Wherein is shew'd *Arithmetically*, how to measure
exactly all kinds of *Superficies* and *Solids* ;

AS

<i>Walls,</i>	{	<i>Glass,</i>	{	<i>Roofs,</i>
<i>Wainscot,</i>		<i>Board,</i>		<i>Painting,</i>
<i>Tyling,</i>	{	<i>Pavement,</i>	{	<i>Timber,</i>
<i>Slating,</i>		<i>Brickwork,</i>		<i>Stone, &c.</i>

With a Detection of some Common Errors us'd
by several in the Performance thereof.

Formerly Published by
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FOR THE
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in *Pater-Noster-Row*, MDCXCIX.

THE
A R T
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BOOK

Wherein is shewed the Art and Mystery of Surveying
as well Land as Water

By
WILLIAM
GODFREY
Surveyor General
of the Colonies

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THE ART OF SURVEYING.

BOOK V.

CHAP. I.

The Way of Measuring Masons Work, as Walls, &c.

FOrasmuch as the difference between the measuring of Land and these is only this, that Land is measured by the Pole or Perch, but these, some by one kind of measure, and some by another; as Walls, Slating, Tiling, and such like, by the Rod of 18 Foot Square: Roofing, Partitions, &c. by the Square of 10 Foot: Pavement and Wainscot by the Yard or Foot: and Board and Glass by the Foot only.

Therefore in measuring any of these things, consideration must be first had to the just Form and Figure thereof; and then according to the Rules delivered in the Second part of the Second Book, you may find the Area, or superficial Content. And forasmuch as it is very requisite and necessary for a Surveyor to know how to measure all manner of Buildings, as Walls, Timberwork, Tiling, Floors, Joiners and Painters Work, and such like, I shall in the following Chapters make illustration thereof.

EXAM-

EXAMPLE.

Suppose there be a Wall that is 54 Feet in length, and 21 Feet in height, and it is required to know how many Rods, Yards and Feet are contained therein. First, I Multiply 54 by 21, and the Product is 1134 feet, which I Divide

by 324, (because there are so many Feet in one Rod) and the Quotient is 3 Rods, and 162 Feet remaining; which I Divide by 9 (for so many Feet are contained in one yard) and the Quotient is 18 Yards, and nothing remaining; so that when the Wall is 54 Feet long, and 21 Feet high, there are contained therein 3 Rods, 18 Yards 0 Foot, which is exactly 3 Rods and a half: For 36 Yards, or 324 Feet, make a Rod; 18 Yards, or 162 Feet, half a Rod; and 9 Yards, or 81 Feet a quarter of a Rod; the whole Work stands in the Margent.

But suppose another Wall be to be measured, whose length is 75 Foot 10 Inches, and its height 15 Foot 5 Inches, the Content will be found 1169 Feet and $\frac{1}{2}$ of a Foot. But this way of Operation, I must here explain, since my Uncle hath not touched upon it in any of his Examples; and because it is the most facile way in casting up the Contents of those Dimensions that are given in Feet and Inches.

EXAMPLE.

First then, Set down your Numbers as in the Margent, viz. 75 Feet, 10 Inches, the length of the Wall, and under them 15 Feet 5 Inches the height; then Multiply the Feet together, viz.

75 by 15, and place their respective Products orderly under them, viz. 375 and 75, then Multiply crossways, that is, 75 Feet, by 5 Inches, and the Product is 375; now because Feet and Inches are Multiplied together, the Product is long Inches, that is one of these long Inches is 12 Superficial Inches; therefore Dividing 375 by 12 (the number of long Inches in one Foot) and the Quotient is 31 Feet, and three long Inches, or $\frac{1}{4}$ of a Foot, which place down as you see in the Margent; then likewise Multiply 15 by 10, whose Product is 50 which Divide by 12, as before, and it gives 12 Feet, 6 Inches, which place down also as in the Margent, viz. Feet under Feet, and

54	
21	
108	
1134	Product.
324	Divisor
972	(3 Rods.
162	
9	(18 Yards.
72	
9	
72	
0	

F.	I.
75	10
15	5
375	0
75	0
31	3
12	6
0	4 $\frac{1}{4}$
1169	1 $\frac{1}{2}$

and Inches under Inches ; then Multiply the Inches together 10 by 5, which makes 50 Inches, which must be reduced to long Inches by Dividing the 50 superficial Inches by 12, which gives 4 long Inches and $\frac{2}{3}$ of an Inch ; your Figures thus placed, draw a Line under them, and add them together as in the Margent, so does the whole Content of the Wall appear to be 1169 Foot $\frac{1}{2}$ of a Foot, which divided by 324, as in the first Example, gives 3 Rods and 197 remaining, which Divided by 9, gives in the Quotient 21 Yards, and 8 Foot remaining ; hence it appears the Wall that is 75 Foot 10 Inches long, and 15 Foot 5 Inches high, amounts to 3 Rods, 21 Yards, 8 Foot, omitting the Fraction.

Note, Having thus largely explained this way of Cross-Multiplying, by casting up the Content in Feet and Inches in this Example ; I shall not need to explain it further in what follows.

Gavels or Dormant Pikes.

But in measuring Gavels or Dormant Pikes, and the like, which are Triangular ; you are to measure them as Triangular, as is taught in the Second Book ; as for Example, Suppose a Gavel or Dormant Pike, whose Base is 18 Foot, and the Height or Perpendicular 15 Foot : Here (according to the Ninth Problem of the Second Part of the Second Book) I Multiply the Perpendicular 15 by the Semi Base 9, and the Product 135 is the Content in Feet, which reduced into Yards, by Dividing it by 9, makes exact 15 Yards for the true content of the Gavel or Dormant Pike.

Measuring of Chimneys.

But in the measuring of Chimneys, which requires more accurateness of Workmanship than other ordinary Walls, they are usually accounted as double measure. But first to measure them as single measure, take the length of the Brest-Wall, and the two Sides or Angles, which Multiply in the height, and that Product being doubled yeildeth the Content, according to double measure which is customarily allowed ; yet some Workmen are so Covetous and Unconscionable, that they are not content to have double measure for the Brest-wall, and the two Angles, but would have the back of the Chimney double measure also whereas (for the most part) the Chimney is made against a Gavel, which is measured by it self ; and so they would have that three times measured, which is and ought to be accounted but as Single measure, except the Gavel, which is usually allowed Square-measure.

Suppose this Figure A B C D E F G H K, be a Chimney that hath a double Funnel towards the top, and a double Shaft, and is to be measured according to double measure.

First, I begin at the Base, and take the length of the Brest-wall O X, and the two Angles K X, and O H, which together are 23 Foot; then I take the height of the Square H F, 17 Foot, 3 Inches, which Multiplied together produce 396 Foot, 9 Inches, for the Content of the Figure, F G H K.

II. For the Square D a E π , the length of the Brest-wall and the two Angles D P E, is 14 Foot, and the height D a, 5 Foot, 3 Inches, which Multiplied together makes 73 Foot, 6 Inches or half a Foot, for the Content of the Figure D a E π .

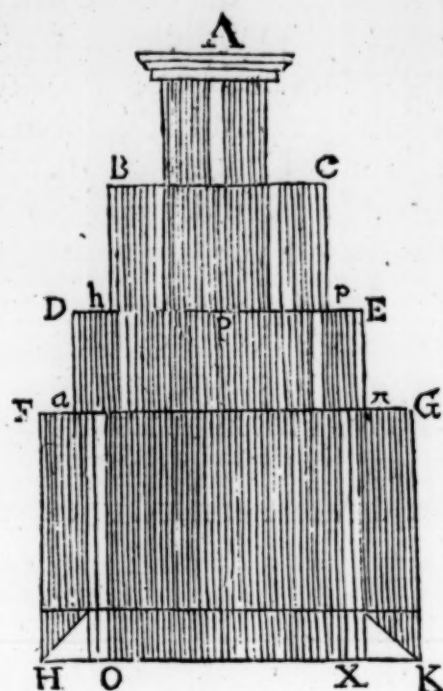
III. I take the length of the next Square B C h p which is 9 Foot, 3 Inches, being the length of the Brest-wall and two Angles, which Multiplied by the height B h, 8 Foot 3 Inches, produceth 76 Feet, 4 Inches almost, for the Content of the Square B C h p.

IV. The Compass of the Chimney-shafts is 12 Foot, 2 Inches, and the height 6 Foot, which Multiplied together, make 73 Foot for the Content of the Shafts.

V. The depth of the middle Fetter that parts the Funnels toward the top is 10 Foot, and its wideness 1 Foot, 3 Inches, which Multiplied together makes 12 Foot, 6 Inches.

Note. And here observe, in the measuring of a stack of Chimneys that stands length-ways, that is, one by the side of another, the same Method is to be observed, with this Addition, that all the middle Fadders or Partitions between Chimney and Chimney, is to be measured also; observe the same if a stack of Chimneys stand Square, and then you cannot easily err.

Lastly, Adding these five Summs together, and doubling the Aggregate, it produceth the Content of the whole Chimney, according to double or customary measure, as you see in this Paradigm.



	F.	I.
The Squares. { F G K H	396	9
{ D a E π	73	6
{ B C h p	76	4
The Shafts A	73	0
The middle Fetter	12	6
<hr/>		
Aggregate	632	1
The Double of it is	1264	2

The

the Content of the Chimney according to customary measure, which reduced into Rods, as shewed before, maketh three Rods, 32 Yards, 4 Foot, and $\frac{1}{2}$ of a Foot.

This is all the measure that can be allowed when the Chimney stands in a Gavel, or Side-wall: in which case, the Back of the Chimney (here not measured) is accounted as part of the Gavel, but if the Chimney or Chimneys stand by themselves, as all Stacks of Chimneys in great Buildings do, which in such a case is all Chimney work, and therefore ought to be measured double on all sides.

C H A P. II.

The measuring of Carpenters Work.

IN the measuring of Carpenters Work, we are to account it by the Square of 10 Foot every way, so that 100 Square Foot is one Square, where

Note, that $\left\{ \begin{array}{l} 25 \text{ Foot is 1 Quarter} \\ 50 \text{ Foot is 2 Quarters} \\ 75 \text{ Foot is 3 Quarters} \end{array} \right\}$ of a Square.

And here we may observe that Carpenters Work that is to be accounted for by the Square, consists chiefly of three parts, *viz.* Flooring, Partitioning, and Roofing, in which we shall give an Example in each particular as followeth.

1. *Of Flooring.*

Suppose there be a Floor laid with Boards, whose length is 18 Foot, 6 Inches, and its breadth 18 Foot, 3 Inches; now these two Summs Multiplied together, produce 556 Foot and an half, which is 5 Squares, and 2 Quarters or half a Square, and 6 Foot and an half.

Note. And here Note, That though 100 be the Divisor to Divide the number of Feet by, yet here is no occasion of making use at all of Division, but always to cut off from the Product 2 Figures toward the Right hand, so those Figures that remain on the Left hand shall be Squares, and the 2 Figures cut off to the Right hand parts of a Square.

2. *Of Partitions.*

Suppose a Partition between one Room and another should contain in length 20 Foot, 2 Inches, and in height 12 Foot, 5 Inches:

X x 2

ches:

ches; hence to find the number of Squares, Multiply 20 Foot, 2 Inches, by 12 Foot, 5 Inches, and you will have in the Product, 250 Foot, 5 Inches, that is two Squares and 2 Quarters or half a Square, and 5 Inches, which Inches are needless to be accounted for in such cases as these.

3. Of Roofing.

First take the length of the Roof on one side and double it, which gives the length of both sides; and likewise take the depth of the said Roof, which Multiply by the length on both sides, or the Girth of the said Roof if it be Culled, and the Product will be the Content.

EXAMPLE.

Suppose the Girth (or length of both sides) of a Roof to be 120 Foot long, and the depth 18 Foot, 6 Inches; which Multiplied together produces 2220 Foot, that is, 22 Squares, and 20 Foot, which wants 5 Foot of a Quarter of a Square more.

Other Measures.

Lastly, There are other things belonging to Carpenters Work, and are to be measured several ways, as Lintails and Discharges, with Cornishes, Rails, and Ballisters, &c. all which are measured by the Foot, running measure.

CHAP. III.

The measuring of Joiners Work, And Painters.

IN measuring of Joiners and Painters Work, observe these following Directions.

I. Joiners and Painters Work is computed by the Yard, or 3 Foot each way, which makes 9 Superficial Foot, which is accounted one Yard.

II. In taking the Dimensions in the height of the Room (which is to be taken with a Line) you are to Girth over every member of the Cornish, and other members of the Wainscot, which where the moldings swell much, considerably augment the height of the Room.

III. The Girth of the Room is only to be taken in its true length and breadth, without putting the Line into the Moldings
as

as you did in the height ; but some Painters have a custom (though for what reason I know not) to draw the Line over every member of the Wainscot in the Girth of the Room as well as the height.

IV. There is one thing in Joiners Work very observable, and that is, by measuring Doors and Window-Shutters, which are wrought on both sides ; for which they are always paid for work and half, and that they have just reason to claim, for the Work is double though the Stuff is Single.

V. All Window-Jaums, and Saphetaes are to be measured by themselves, and the Window-Lights and Chimneys (if any be in the Room) are to be deducted out of the whole at last.

VI. The Painters are not to account for work and half, but to account (in some cases) the Room once, twice, or three times done over, or so much *per yard*, considering the goodness of the Work.

The Dimensions being taken according to the preceding Directions, we will endeavour to explain the whole by one Example of a Room whose

Girth or Compass is 256 Foot 6 Inches,
And its height 15 Foot 9 Inches.

I. Multiply 256 Foot 6 Inches by 15 Foot 9 Inches, the Product is 4039 Foot 10 Inches, which divided by 9, gives in the quotient 448 Yards, 7 Foot, 10 Inches.

II. Let us suppose all the Window-Jaums, and Saphataes to be 56 Foot, 4 Inches, and their breadth 2 Foot, 2 Inches ; which Multiplied, produces 122 Foot, which Divide by 9, the quotient is 13 Yards, 5 Foot.

III. All the Window-Shutters about the Room is in Girth or Breadth 28 Feet, 3 Inches, and the length or height of them 5 Foot, 7 Inches, which Multiplied and Divided as before, makes 17 Yards, 4 Foot, 8 Inches ; and its half is 8 Yards, 6 Foot, 10 Inches, which added to 17 Yards, 4 Foot, 8 Inches, makes 26 Yards, 2 Foot, 6 Inches, for the true Content of the Window-Shutters for Work and half work.

IV. These several Sums added together as follows, give the Content of the whole Room, 488 Yards, 6 Foot, 4 Inches, from which take 19 Yards, 4 Foot, 6 Inches, being all the Deductions in the said Room, *viz.* Chimney and Window-Lights ; hence the Exact Content appears to be 469 Yards, 1 Foot, 10 Inches ; and this is the true way of measuring, and so much the the Workman ought to be paid for.

The Summs added together.

	T.	F.	I.	
The several parts	{ 448	7	10	} cast up
	{ 13	5	00	
	{ 26	2	06	
<hr/>				
The whole	488	6	04	
Deductions	19	4	06	
<hr/>				
The true Content	469	1	10	

C H A P. IV.

Of the measuring of Brick-Work and Tyling.

First, I shall join the Bricklayers and Tylers Work together, in respect they are commonly performed by the same hands, though the way of accounting for is different, for Tyling is commonly reckoned for by the Square of 10 Foot, as Carpenters work is, only they demand allowance of double measure for the Eaves, and Running measure for the Hips and Gutters but this depends upon the custom of the place; however some allowance in these cases ought to be had, in respect of measure or price.

II. Brick-walls are measured in some places by the Rod of 16 Foot and half each way, so that one of these Rods do contain $272\frac{1}{2}$ Square Foot; which is proved by Multiplying 16 Foot, 6 Inches into it self, and this is called Statute-measure, though it is used in very few places in the Country that I know of.

III. There is another sort of Rod of 18 Foot Square, which makes 324 Square Foot in a Rod; and this is a measure sometimes used in the Country, being the same Rod the Masons here make use of.

IV. But the Rod most in use here in the Country, contains only 54 Square Foot upon the Superficies, or 6 Square Yards, being one sixth part of the Rod last named of 18 Foot Square.

V. Hence the Surveyor is to examine (before he begins to measure) what Rod it is the Master and Workmen did agree upon, that he may do them both Justice.

VI. Because Brick-Walls are not always made of one thickness, they are to be reduced to the Standard-measure, viz. of a Brick and half thick; all which shall be further explained by the Examples following.

E X A M-

EXAMPLE.

Suppose a Brick-wall be 167 Foot long, and 16 Foot high, now by Multiplying these two numbers together, gives in the Product 2672 Foot, which to reduce into Rods according to any of the Rods before mentioned and explained; Divide the said 2672 Foot, by $272\frac{1}{2}$ for Statute-measure, or by 324 the Square of 18 Foot, or by 54, the Divisor of the lesser Rod; according to any of these ways you may see by this following Paradigm, what the number of Rods is.

			R.	Y.	F.
If Divided by	$\left\{ \begin{array}{l} 272\frac{1}{2} \\ 324 \\ 54 \end{array} \right\}$	there is contain'd in the Wall	$\left\{ \begin{array}{l} 9 \\ 8 \\ 49 \end{array} \right\}$	24	$3\frac{1}{2}$
				8	8
				2	8

Now when you have Divided by any of these Divisors, and that the Remainder exceeds 9 (as it did in all these Examples) you are to divide the said Remainder by 9 (it being the number of Feet in one Yard) so have you the content in Rods, Yards, and Feet as before; and this I think is sufficient to explain the whole matter,

Note. The next thing considerable is, that all Brick-walls of the same height and length do not contain the same number of Rods, in respect of the thickness of the Wall; for the thicker the Wall, the more Rods are contained therein, *viz.* If a Brick-wall be thicker than one Brick and half thick, then a Square Rod upon that Wall, will be more than a Rod; hence every Rod upon the Superficies of a Wall that is 3 Bricks thick, will contain 2 Rod; and a Rod upon a Wall of 4 Bricks thick, and half, will be 3 Rods; I shall therefore in the next place set down one General Rule to Reduce a Brick-wall of any thickness to the thickness of a Brick and half, the Standard-measure,

A General Rule for Reducing of Brick-walls to Standard-measure.

A General Rule.

Multiply the Number of Superficial feet which is contained in the Superficies of any Brick-wall, by the number of half Bricks the said Wall is in thickness; one third part of that Product is the Content of the said Brick-wall in Feet, reduced to a Brick and half.

Hence if a Wall of 5 Bricks thick should contain 2672 Feet, upon the flat or superficies; if you Multiply this number by 10 (the number of half Bricks the Wall is in thickness) the Product

pro-

produces 26720, one third part whereof is 8906 $\frac{2}{3}$ Foot, which is the exact number of Feet contained in that Wall, as it is reduced to a Brick and half thick, which how to bring to Rods, &c. I have just before shewed.

Of Tying.

Suppose a Roof in length 120 Foot on both sides, and the depth of one side (with the customary allowance at Eves) 18 Foot; these two numbers multiplyed together produce 2160 Foot, which is 21 Squares, and 60 Foot, that is, 10 Foot above half a Square more, according to the Directions of the 2d. Chapter.

CHAP. V.

The measuring of Plaisterers Work, and Slating.

First, Slate-Work is generally accounted for by the Rod of 18 Foot Square, which contains 324 Superficial Feet as I intimated in the last Chapter.

II. Where a Roof is covered with Slate, there ought to be an allowance at the Eves equivalent to the Projecture of the Eves over the Wall below the Roof, which is generally termed double measure at the Eves, which adds to the depth of the Roof, 18 or 20 Inches, sometimes 2 Foot.

III. Where there is Gutters or Valleys, there ought to be an allowance also, which is to take the Girth, or length of the Roof with the Gutter or Valley, all along the Ridge-Tile, which makes the Gutters double measure, *viz.* as much more as really it is, which in some places is allowed, and in some places not, which chiefly depends upon the Custom of the Place.

IV. If the length of the Roof be taken, in Feet and Inches, and the depth on both sides, with the usual allowance at the Eves, and in the Gutters, and Multiply'd together, and the Product thence arising divided by 324, and the remainder again by 9 (if it exceed 9) you will have the Content in Rods, Yards, and Feet.

EXAMPLE.

Of a Roof covered with Slate, whose length is 52 Foot, 6 Inches, and the Depth of the said Roof on both sides (with the usual allowance of the Eves) 34 Foot; that is, 17 Foot for the depth

depth of one side: Now 52 Foot, 6 Inches, the length, being Multiplied by 34 Foot, the depth on both sides, the Product is 1785 Foot, which divide by 324, the Quotient is 5 Roods, and 165 Foot remaining, which Remainder divide by 9, the Second Quotient is 18 yards, and the Remainder 3 Foot; so that you see that Roof that is 52 Foot, 6 Inches long, and 17 Foot deep, amounts to 5 R. 18 Y. 3 F. And because this sort of measuring is so plain, more Examples will be needless.

Of Plaisterers Work.

I. Plaisterers-Work is of 3 sorts, as first, The Running of Plaister-Floors; secondly, The Ceiling of Upper-Rooms with Reed, Nails, Lath, Lime, Sand, and Hair; and thirdly, The Pargin of bare Walls, with Lime, Sand, and Hair; before which there is generally laid first upon the Wall a Coat of Hay and Morter, otherways it would take up too great a quantity of Lime, Sand, and Hair.

II. All these several sorts of Plaisterers-work is generally accounted for by the Yard, or the Square of 3 Foot, which makes 9 foot in each yard; hence Examples are needless; for the Dimensions being taken in Feet, and Inches, and Multiplied together, and the Product Divided by 9, you will have the number of Yards in the Quotient, and the Remainder will be the odd Feet.

C H A P. VI.

The measuring of Board and Glass.

I. **I**N the measuring of Glass and Board, the Content is usually given in Feet, and Inches, therefore they may the better be joined together.

II. The Dimensions are mostly taken in Feet and Inches, and the Length and Breadth so multiply'd together, produces the Content.

III. In the measuring of Board, if the Breadth in Inches be Multiplied by the Length in feet, and the Product Divided by 12, the Quotient will give the Content in Feet, and what remains, is so many 12th parts of a Foot.

IV. Sometimes more Curiosity is required in measuring of Glass, and in taking the Dimensions Feet and Inches will not be near enough; therefore the Dimensions may better be taken in Inches and 10th parts of an Inch; which Multiplied together, and the Product Divided by 144 (the number of inches in one Foot)

Y y

fo

so will the Quotient produce the number of Feet, and the Remainder the odd Inches, or 144th parts of a Foot.

V. All these Cases will be better explained by the Examples following.

I. Of Glafs.

EXAMPLE.

Of a Window-Light of Glafs whose height is 4 Foot, 6 Inches, and $\frac{1}{10}$ parts of an Inch, or 54 Inches and $\frac{1}{10}$ of an Inch; and the breadth 20 Inches, and $\frac{1}{10}$ parts of an Inch; which Multiplied together as in the Margent, and the Product is 1124 Inches, and $\frac{1}{10}$ parts of an Inch; which is not worth taking notice of, therefore we omit it; hence 1124 Divided by 144, the Quotient is 7 Foot, and the Remainder 116 Inches or $\frac{116}{144}$, which is 8 Inches above three quarters of a Foot more.

$$\begin{array}{r}
 54.3 \\
 20.7 \\
 \hline
 3801 \\
 10860 \\
 \hline
 1124.01 \quad \text{Product.} \\
 144 \quad (7\frac{116}{144} \text{ quo.} \\
 1008 \\
 \hline
 116
 \end{array}$$

Note. And this one Example I think sufficient to explain the whole matter of Glafs-measure; with this caution, *viz.* That where the Windows are either Round or Elliptical, that the Workman be allowed as Square-measure; that is, by taking the Diameters as the sides of a Square; The reason of this allowance is, because of the great waste of Glafs that is made in fitting it to the Arch of the Window.

II. Of Board-measure.

EXAMPLE.

Suppose a Board 11 Foot in length, and 10 Inches broad, now if 11 Foot be Multiplied by 10 Inches the Product is 110, which Divide by 12 (because the Multiplication was made in Feet and Inches) and the Quotient is 9 Foot and $\frac{2}{3}$ of a Foot: Where note, if 3 had remained it had been a quarter of a Foot if 6 half a Foot, and if 9 three quarters of a Foot.

But if the Board had not been an even number of Feet in length, then the Dimensions may be taken in Inches, and 10th parts of an Inch; and the breadth also (if need require) which Multiplied and Divided, as in the Example of Glafs, will accordingly produce the Content.

C H A P. VII.

Of Stereometry, or the mensuration of Solid Bodies, as Timber and Stone; and first of that which is Square.

A Solid Body is that which hath both length, breadth, and thickness, as Timber, Stone, and such like, which are commonly measured by the Foot. And herein you are to observe, that a Foot of Timber or Stone is accounted a Foot Square every way, in the form of a Die; whereby it appears, that a Foot of Timber is 12 times more than a Foot of Board; so that a Foot of Board being 144 Inches, a Foot of Timber must be 1728 Inches.

For Timber-sticks that are Squared, you may find the Content thereof on this wise. Multiply the breadth by the thickness, and then Multiply the Product by the Inches of the length, so will you have the solid Content of the whole Piece of Timber in Inches; which being Divided by the Solid Inches in one Foot; namely 1728, the Quotient will shew how many Feet are in the Piece of Timber.

E X A M P L E.

Suppose a Piece of Timber be 9 Inches thick, 15 Inches broad, and 12 Foot or 144 inches long. First, I Multiply 15 by 9, and the factus 135 is the Area of the Plain; which I again Multiply by the length 144, and the Product 19440 is the Content in Solid Inches, which being Divided by 1728 (the Square Inches in one Foot) the Quotient will be $11\frac{7}{8}$, or 11.25, so that when a Piece of Timber is 9 Inches in thickness, 15 Inches in breadth, and 12 Foot in length, there is contained in it 11 Foot and a quarter of a Foot, according to the true and substantial Grounds of Art.

Performed another way.

To perform the former Work an easier way, the breadth and depth, 15 and 9 Multiplied as before, produces 135; which Multiplied by 12, the length in Feet, the Product is 1620, which Divided by 144, the Quotient is $11\frac{5}{4}$, or 11 Foot and a quarter, as before.

But yet I know it is a very common thing amongst Carpenters to add the broader and narrower sides together, and to take the half for the true Square, which way (though it be much used) is very erroneous, especially when the difference between the sides is much, as in the former Example; where the one

side is 15, the other 9, and the Summ 24; therefore they reckon 12 for the true Square; and so conclude there are 12 Square-Foot of Timber in that Piece, whereas there are exactly but 11 Foot and a quarter, as before is proved.

To find the true Square of a Piece of Timber when the one Side is broader than the other; Multiply the sides together, and the Square Root of that Product yieldeth your desire.

As in the former Example, I Multiply the one side 15 Inches, by the other 9, and the Product (as before) is 135, whose Square-Root is near upon 11.62; which is the true Square thereof.

C H A P. VIII.

To measure Round Timber.

TO measure Round Timber, you must first find the Area of the Circle (whose Circumference is equal to the Compass of the Tree) as you are taught in the Twentieth Problem of the Second Part of the Book of *Geometry*. And this shall be made clear by an Example or two, supposing the Areas of both ends of the Timber-Stick to be equal.

E X A M P L E. I.

Suppose there be a Round Piece of Timber, whose Compass is 5 Foot and a half, or 66 Inches, the Diameter or greatest Thickness thereof 21 Inches, and the length 12 Foot, or 144 Inches. First, I Multiply the Semidiameter (or half the thickness of the the Timber-Stick) 10.50 in half the Circumference 33; and the Product is 346.50; which again Multiplied by the length 144 Inches and the result 49896.00, being Divided by 1728, the Quotient is 28.875; so that there is 28 Foot of Timber, and above three quarters of a Foot in the Stick, whose Circumference is 5 Foot and a half, and the length 12 Foot.

Otherways.

Or if 346.50, the Area of the Circle be Multiplied by 12, the length in Foot, the Product will be 4158.00, which Divided by 144, the Quotient is $28\frac{3}{4}$, or 28 Foot, and something above three quarters of a Foot, as before.

But by the way, I shall divulge one common Errour in measuring Round-Timber, crept in for want of Art, which having got possession of the greater sort of Artificers, is (by long continuance) grown almost irrecoverable, and that is in girdling of the Round Piece of Timber, or Tree, and of that Circumference to take a fourth part for the Square. As

As in the former piece of Round Timber, the Circumference is 66, the $\frac{1}{4}$ whereof 16.50, they account the side of the Square, which Multiplied in it self produceth 272.25 for the Area of the Basis; which if you Multiply by the length 144, the Product is 39204.00 the Content in Inches, which Divided by 1728, the Quotient is 22 $\frac{1}{2}$ Foot, which is apparently erroneous, differing from the truth no less than 6 whole Foot, and that too little as appears before, which for further Trial, we shall also examine by Mr. Gunter's Rule in his Second Book of the Cross-Staff, Page 44. Prop. 9.

As 1000, to 2821, so are 66 Inches to 18.6186 the side of the Square, which Multiplied in it self, produceth 346.65; now this being Multiplied by the length 144, the Product is 49917.60, which being Divided by 1728 giveth 28 Foot, 88 Parts, agreeing nearly with our former way of mensuration.

But in such cases as these, Men commonly plead Custom, and will be ready to say, they make allowance for the Bark and waft in hewing, which indeed ought to be done in the Price, and not in false measuring; but in measuring a Round Column of Stone no such allowance can any way be laid claim to, because there is no waft.

CHAP. IX.

To measure Timber having 3, 5, 6, 7, or more Sides equally Squared.

IN Timber be neither Round nor four Square, but is either Triangular, or else consisteth of more than four Sides, you must still find the Area of the Plain, according as hath been taught in the Second part of the Book of *Geometry*, and then Work as in the former Chapters for the Content; but to explain it more fully, I shall add some Examples.

EXAMPLE.

Suppose a Piece of Timber consist of three equal Sides, each side being 18 Inches, the length of 6 Foot, or 72 Inches. First, I seek the Area of the Plain according to the 9th Problem of the the Second Part of the Book of *Geometry*, and find it 140.30, which I Multiply by the length 72 Inches, and the Product is 10101.60, which Divided by 1728, the Quotient is 5 Foot, 846, for the Content of the three equal-sided Piece of Timber.

But if a Piece of Timber consist of more sides than four, you must still find the Area of the Plain.

EXAM-

E X A M P L E.

Suppose a Piece of Timber have six equal sides, each side containing 10 Inches, the length 7 Foot, or 84 Inches. First, (according to the 18th Problem in the Second Part of the Book of *Geometry*) I take the Area of the Plain 259.80, which I Multiply by the length of the Stick 84, and the Product is 21823.20, which Divided by 1728, the Quotient is 12 Foot $\frac{2}{3}$, or Decimally 12.63.

The like you are to observe in all Pieces of Timber of Six, Seven, and Eight sides or more, and thus much briefly concerning Round and Square Timber.

C H A P. X.

The Dimension of Pyramids or Cones.

IF a Piece of Timber be right-lined, having but one base, and end in a sharp point, it is called a Pyramid; but if the base thereof be round it is a Cone, according to the common Definition.

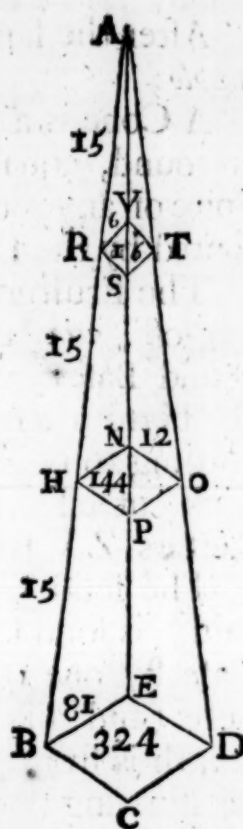
The Solid Content of either of these Figures is found by Multiplying the Superficial Content or Area of the Base, by a Third part of the length.

Suppose the Pyramid represented by the Figure A B C D be to be measured, whose side at the Base B C, or B E is 18 Inches, and the length A B 45 Foot, or 450 Inches. First, I Multiply the side of the Pyramid at the Base 18 in it self, and the Product 324 is the Area of the Base, which I again Multiply by a third part of the length, 180 Inches, and the Product will be 58320 the Solid Content in Inches in the whole Piece, which being Divided by 1728, the Quotient is 33 Foot, and 1296 Parts of a Foot, which is 33 Foot and 3 quarters.

The Operation in common Numbers.

18 side of the Pyramid	58320
18	5184
144	1728) 6480 (33 $\frac{1226}{1798}$
18	5184

324 Area of the Base.	1296 Remain.
180 Third Part of the length.	
25920	
324	
58320 The Product.	



The little Pyramid, noted with the Letters ARSTV, is but 6 Inches square at the Base, whose Area is 36; which multiplied by a third part of the Length, 60 Inches, produceth 2160, that is, 1 foot, and 432 parts, or 1 foot and a quarter.

But suppose the Content of the Segment ONHBCD were required; the Squares at the Base are 144, and 324, which multiplied together, produceth 46656, whose Square-Root is 216, for the Geometrical-mean Square.

Otherways.

Or otherways, find the part cut off, which taken out of the Pyramid leaveth the solid Content of the Fruustum. To find the whole length, use this Analogy; As the Difference of the Diameters length, to the length between them; so the Diameter of the greater Base, to the whole Length of the Pyramid: And consequently the part wanting comes to be known, which measured as a Pyramid (as indeed it is) whose solid Content being subtracted out of the whole Pyramid, leaveth the Content of the Fruustum, or tapering Timber-stick, which is the true Method of measuring squared tapering Timber, which shall be further exemplified in measuring of Cones.

Of

Of Cones.

After the same manner are Cones to be measured : As for Example ;

A Cone is a Figure having length, and only one Base, which is round, equally decreasing, and terminates in a point, as the Spire of any round Steeple, which is here represented by the Letters O X Y S.

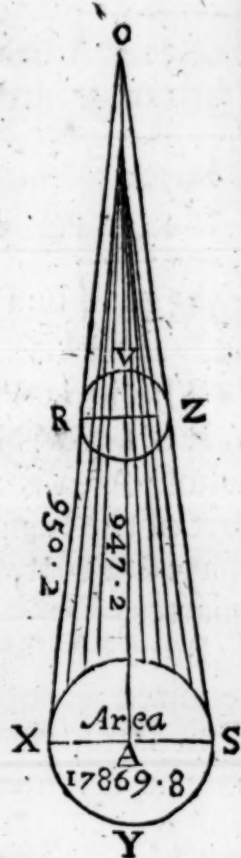
The Frustrum of a Cone, is part of the Cone cut off, viz. the bottom part, and hath two round Bases, whose Base is always greater at the bottom than at the top, more or less, according to the Taper, and parts of the Timberstick cut off, as it is here represented by the Letters Z V R X Y S.

The solid Content of a Cone (as in a Pyramid) is found, by multiplying the Area of the Base by one third part of the length; where note (and likewise in the Pyramid) the true length is from the Center of the Base, to the terminating point, as from O to A, and not the Hypothenufe O X, or O S, tho' I have follow'd my Author in that respect in the Pyramid, yet shall somewhat digress from him here, and shew how the true length is to be obtained.

First, Take the length of the Hypothenufe or Slope-line O X, or O S, which we will here suppose 950.2 Inches, and the Semidiameter X A, or S A, 75.4 Inches; square both these Numbers, that is multiplying them in themselves; so will the Square of 950.2, be 902880, and the Square of 75.4, is 5685: Then subtract the Square of the Semi-base, 5685, from 902880, the Square of the Hypothenufe, and the Remainder is 897195, whose Square-Root is 947.2 Inches, the true Height required.

Then to find the solid Content of the Cone, multiply the Area of the Base, 17869.8 Inches, by 316 Inches, a third part of the Length, the Product is 5646856.8 solid Inches, which divided by 1728, the Quotient is 3267 Foot, and $\frac{1728}{1728}$ parts of a Foot, the Content of the whole Cone in solid Feet.

To measure round tapering Timber, which is the Frustrum of a Cone, as is here represented by R X S Y; First then, find the Area's of the Circles at both ends, and then proceed in all respects to find the solid Content, as in the Frustrum of a Pyramid.



C H A P. XI.

The mensuration of a Globe or Sphere, and its Frustums.

A Sphere or Globe is a Solid every way Circular, made by the Motion of a Semicircle about its Diameter, being an exact round Solid, such as are the Balls of Freestone-Peers and Gates before the Front of any Spacious Building.

To find the solid Content, there are several ways ; As first, Multiply the Cube of the Diameter by 11, the Product thence arising divide by 21, the Quotient is the solid Content.

2. Or, Multiply the Area of the Circle, equal to the Diameter, by one sixth part of the Globe's Superficies, the Product is the solid Content : Or one sixth part of the Diameter multiplied by the Sphere's Superficies gives the same.

3. Otherways, Multiply the Area of the said Circle by two thirds of the Diameter, the Product is the solid Content : Or, Multiply the Diameter by two thirds of the Circle's Area, performeth the same.

E X A M P L E I.

Of a Sphere whose Axe is 54.6 Inches, and the Circumference 171.5 Inches, the Convex Superficies (according to the 29th Prob. of the Second Part of the Book of Geometry) is 9363.9, the Cube of the Axe is 162771, which multiplied by 11, gives in the Product 1790481 ; which divided by 21, gives in the Quotient 85261 solid Inches ; which divided by 1728, gives $49 \frac{1}{7} \frac{2}{3}$ Foot solid.

E X A M P L E II.

One sixth part of 54.6 the Axe, is 9.1, by which multiply 9363.9, the Product is 85212, which divided by 1728, the Quotient is $49 \frac{1}{7} \frac{2}{3}$ solid Feet, nearly agreeing with the former.

E X A M P L E III.

The Area of the Circle is 2341, which multiplied by 36.4, gives in the Quotient 85212, which divided as before, giveth $49 \frac{1}{7} \frac{2}{3}$ solid Feet, exactly agreeing with the former.

Of the Frustrums of a Sphere or Globe.

The Frustrum of a Sphere or Globe, is a part cut off, whose Base is a Circular Plain, and whose solid Content may be found by having the Diameter of the whole Sphere, with the Diameter and Height of the whole Frustrum; then use this Analogy; As the Remainder of the Axe, or Diameter, is to the Frustrums Height; So is the Semidiameter of the whole Sphere, to the solid Content of the Frustrum.

If two Frustrums be cut off from a Sphere, so that the Plains of the Bases are Parallel, and that the Solidity at the middle part is required; it is but finding the Contents of both Frustrums, which subducted out of the whole Globe, leaveth the Solidity of the Middle, or part left.

Thus far of measuring of *Buildings*. I shall, in the next place, conclude this Book with one useful Chapter, *viz.* of setting the Prices of Workmanship and Materials belonging to Buildings, which are the most material to be taken notice of, according to the custom of the Country, because I would not leave my Surveyor unfurnished in so useful a Part of his Profession, whereby the Master always may inform himself how to proceed in Bargaining both for Materials and Workmanship, before he proceed to raise his Intended Building.

C H A P. XII.

Containing the Rates and Prices of Workmanship and Materials belonging to Buildings, and first of Mason-Work.

Fence-Walls and ordinary Buildings is each (only the Workmanship) from 16 Shillings to 3 *l.* 10*s.* per Rod of 18 Foot Square which depends upon the goodness of the Work.

The setting of the Fronts of great Buildings, *viz.* Ashlar, Architrave, Windows, and Doors, with the Ground-Table, Fasha's, and other Members is Worth from 3 *l.* 10*s.* to 5 *l.* per Rod, which depends upon the height and well performing of the Building: Chimneys raising in such Buildings are worth 3 *l.* a Rod, or 1 *l.* 10*s.* double Measure.

Pavement laying is worth a half-penny a Foot.

Setting or Pitching with Rough Stone, is worth from 4 *d.* to 12 *d.* per Yard.

Of Free-Masons or Quarrie Work.

Ashlar (at the Quarrie) is worth 3 *d.* or 4 *d.* *per* Foot.

Random-Pavement at the Quarrie is worth 2 *d.* halfpenny or 3 *d.* *per* Foot.

Diamond-Pavement, is worth 3 *d.* halfpenny, or 4 *d.* *per* Foot.

Rustick Quonys, at 2 Foot and 1 Foot each face, at the Quarrie, are 1 *s.* 4 *d.* *per* Quonie or 1 *s.* 3 *d.* a piece, or 5 *d.* *per* Foot, in some places 4 *d.* *per* Foot or 1 *s.* *per* Quonie.

Architrave Doors, and Windows, are worth according to their Wideness or breadth of the Mouldings, a Penny an Inch, that is to say, if the Breadth of the Moulding (*viz.* from the outside to the inside of the Window-Frame) be 9 Inches, it is worth 9 *d.* *per* Foot, running measure, if 10 Inches, 10 *d.* *per* Foot, and so proportionably more or less.

Ground-Table is worth from 4 *d.* to 8 *d.* *per* Foot, running measure.

Frontish Doors in great Buildings, with their Ornaments, as Pillasters, &c. is worth (according to their Magnitude and variety of Workmanship included) some 3 *l.* some 5 *l.* to 10, or 20 *l.* perhaps more.

Chimney-Shafts for ordinary Buildings with Architrave Frize and Cornish, is worth from 15 *s.* to 20 *s.* according to their height and Substance, without Architrave and Frize, from 10 *s.* to 20 *s.* But in great Buildings they are usually done by the Foot, *viz.* at about 6 *d.* *per* Foot.

Chimney-Pieces of Free-Stone wrought plain are worth 10 *s.* but there may be such Moulding wrought in them, which with their Coves and other Members may be worth 20 *s.* 30 *s.* or 40 *s.* a piece.

A Pair of Peers, with Seat-Arches, 4 or 5 Foot wide, and 14 or 16 Foot high is worth 40, or 50 Pounds.

Rustick Peers a Pair, are worth 10, 12, or 14 Pounds, according to their height and Substance; Plain Peers 8, or 10 Pounds, Revailed and Pillaster-Peers, from 10, to 14 Pounds a Pair.

Cornishes are worth according to their Nature and Bigness; a Modillion-Cornish of about 18 or 20 Inches thick, is worth 5 or 6 shillings *per* Foot, running measure.

Of the Rates and Prices of Carpenters-Work.

Roofing and Flooring in ordinary Buildings is worth 7 *s.* or 8 *s.* *per* Square, but in great Buildings 10 *s.* or 11 *s.* *per* Square.

Ceiling-beams, Coveing and such like is worth 4 *s.* *per* Square.

Partitioning is worth 6 or 7 *s.* *per* Square.

Transom-Windows for great Buildings is worth making 1 *s.* 9 *d.* *per* Light, or 7 *s.* *per* Window.

Batten Doors worth making (for ordinary Door Cases, as about 6 or 7 Foot high, and 3 Foot wide) 4 Shillings.

Plain Doors, for such like Door-Cases are worth making 2 s. or 2 s. 6 d. *per Door*.

Rails and Ballisters on Balconies, or upon, or about the Platform of great Houses, is worth (only Workmanship) 4 s. *per Yard* running Measure.

Lucan-Windows making and setting up, are worth 9, 10, 12, or 14 shillings *per Window*, which price is varied according to their Bigness.

Coveing Work, Sawing and putting up with the sliders, is worth 10 or 11 s. *per Square*.

Of the Rates and Prices of Joiners-Work.

Wainscotting with *Norway Oak*, the Workman finding the Stuff, is worth 7 s. *per Yard*, but if the Master find the Stuff, then is the working Part worth 3 s. 6 d. or 4 s. *per Yard*, and where the Moldings are very large it is worth 5 s. *per Yard*.

Plain-Square Wainscoting (the Workman finding Deal) is worth 3 s. or 3 s. 6 d. *per Yard*.

Ordinary Bisection-Wainscoting (the Workman finding Deal) is worth 4 s. 6 d. *per Yard*.

Large Bisection-Work is worth 6 or 7 s. *per Yard* of *Dantzick* Stuff, and Large Picture-Frame of the same Stuff is worth 10 s. *per Yard*.

Modillion-Cornish with its Carved Work, is worth 7 s. *per Foot*.

A plain Modillion-Cornish of 12 or 14 Inches, will be worth 3 s. 6 d. or 4 s. *per Yard* running Measure.

Deals dressing are worth 1 s. *per Score*, or 6 s. *per Hundred*.

Deal-Floors, ordinary (the Working part) are worth, Laying, 5 s. *per Square*, but if the Workmen find Deals, 'tis worth from 24 s. to 30 s. *per Square*, which depends upon the goodness of the Deals.

Deal-Floors of Choice pick't Deals, laid either with Dufftail or Key-Joynts (without Pins or Nails) is worth 35 s. or 40 s. *the Square*.

Pallisado-Gates, &c. the Workman finding Wood, is worth 9 s. or 10 s. *per Yard* running measure, at about 6 or 7 Foot high, the working part is worth 6 or 7 s. *per Yard*.

Of the Rates and Prices of Brick-Work.

Bricks are worth from the Brick-Kiln about 12 Shillings *per Thousand*, which will nearly do a Rod of Work on a two Brick-Wall.

Building of Brick-Walls, the Workman finding Brick, Lime, and Sand, is worth as followeth, *viz.*

A Brick and a half Wall, 3 *s.* per Yard; A Two Brick-Wall, 4 *s.* per Yard; A Two Brick and a half Wall, 5 *s.* per Yard.

Brick-Walls, Building only, the Working part, is worth upon a Brick and half Wall, 4 *s.* per Rod, some places 3 *s.* 6 *d.* A Two Brick-Wall, 4 *s.* 6 *d.* or 4 *s.* 8 *d.* a Rod, and so proportionably, Six Yards to the Rod, which is all along to be understood in Brick-Walls.

A Chalder of Coals will burn about 4200 Bricks.

A Bricklayer with a Labourer, will lay about 1000 Bricks a Day.

Of the Rates and Prices of Tyling-Work.

Tyles are worth from 25 *s.* to 30 *s.* per Thousand; and may be laid on a Roof at about 3 *s.* per Square; some places 2 *s.* 6 *d.* or about 8 *s.* per Rod of 18 Foot Square.

Pan-Tyling is worth 5 *s.* 6 *d.* per Rod, Workmanship; and about 700, or 800 Tyles, doe 36 Yards, or a Rod.

Of the Rates and Prices of Slate-Work.

Slating, or covering a Roof with Slates, the Workman finding all Materials, is worth about 40 *s.* per Rod, *viz.* 36 Yards; but the Working part only is worth about 12 *s.* the Rod.

Slates, pointing, are worth 3 *s.* or 3 *s.* 6 *d.* per Rod, only the Working part.

Slates are worth at Pitts 12 or 14 *s.* a Thousand, which will nearly do a Rod, of 36 Yards.

Of the Rates and Prices of Plaisterers-Work.

Ceiling with Reed, Lime, and Hair (only Workmanship) is worth 3 *d.* per Yard, *viz.* 1 *d.* the Yard each Coat, but if the Workman find all, 'tis worth 5 *d.* or 6 *d.* a Yard.

Walls, drawing twice over, or two Coats, is worth 1 *d.* each, *viz.* 2 *d.* per Yard.

Plaister-Floors running, the Workman finding all, is worth 1 *s.* 4 *d.* per Yard, but the working part only is worth 4 *d.* 5 *d.* or 6 *d.* per Yard.

Plaister at the Pitts, may be had at 4 *s.* or 4 *s.* 6 *d.* per Load, *viz.* 40 C. Weight, which will do about 40 Yards of Flooring.

Rough-Casting upon the Fronts of Timber-Buildings, the Workman finding all Materials, is worth from 1 *s.* to 3 *s.* per Yard,

Yard, which depends upon the Variety and Goodness of the Work.

Of the Rates and Prices of Painting and Japan-Work.

White Painting is worth about 1 s. per Yard, Walnut-Tree-Painting is worth 1 s. 4 d. or 1 s. 6 d. per Yard; and ordinary-branch'd Painting is worth 12 d. 14 d. or 16 d. per Yard.

Japan-Work, plain, either black or white, is worth 3 s. 6 d. or 4 s. per Yard.

Gates and outward Doors are worth Painting 8 d. or 9 d. per Yard.

Of the Rates and Prices of Glasiers-Work.

A Table of *New-Castle* Glas does contain about 5 Foot; 45 of which Tables make or go to a Case, which is worth from 25 s. to 40 s. the Case, and depends upon the Coal-Ships coming in.

Normandy Glas is much finer and clearer, of which 25 Tables make a Case, and is much dearer.

Glazing done with Quarries, or Diamond-Glas, is worth $\frac{1}{2}$ 4 d. or 5 d. per Foot.

Glazing with Squares is worth 6 d. per Foot, of *New-Castle* Glas.

Of the Rates and Prices of Plumbers-Work.

A Fodder of Lead is 22 Hundred Weight and an half, and is worth from 9 l. to 12 l. which will cast 315 Foot of Sheet, at 8 pound in the Foot.

Sheet-Lead, and the Laying of it on in Roofing, &c. is worth 15 or 16 s. per Hundred Weight; if 14 s. per Hundred, then 1 s. per Foot, at 8 pounds in the Foot, is the same.

Old Lead Casting into Sheet is worth 1 s. 6 d. per Hundred; but Casting and Laying on a Roof is worth 2 s. the Hundred Weight: And here observe, that there is Loss in Casting of Lead, 2 s. 6 d. in every Hundred Weight.

Solder is usually sold at 9 d. the Pound.

Of the Rates and Prices of Stone-Cutters-Work.

Chimney-Pieces of *Egyptian*, or black fleak'd Marble, or of Rance, or Liver-colour'd Marble, is worth (of an ordinary Size) 12 or 14 *l.* a Piece.

Window-Stools of white or black-fleak'd Marble, are worth 2 *s.* 6 *d.* per Foot. Pavement of black or white Marble is worth about 2 *s.* per Foot, &c.

Of the Rates and Prices of Smiths-Work.

Casements are worth 7 *d.* or 8 *d.* the Pound; some 9 *d.* viz. Folding Casements.

Pallisado-Work, in Gates or otherways, is worth 4 *d.* the pound.

Of the Rates and Prices of Sawyers-Work.

Oak Sawing is worth 2 *s.* 8 *d.* per Hundred; some 3 *s.* to 3 *s.* 6 *d.* the Hundred.

Ash Sawing is worth, in all respects, 6 *d.* a Hundred more than Oak.

The End of the Fifth B O O K.

THE

Received of _____

the sum of _____

for _____

6

T H E
Art of Surveying,
B O O K VI.

Containing the
DESCRIPTION and USE
O F A
NEW QUADRANT,
B E I N G

Plain and easie in Resolving the Hour and Azimuth, the Right Ascension, Declination, Oblique Ascension, and Descension of all Points of the ECLIPTICK; and thereby the Rising, Southing, and Setting of the

Planets and Fixed Stars,

The Sun's Rising and Setting, with the Increase and Decrease of the Days, to a Minute, and several other QUADRANTAL Performances on the Fore-side.

On the Back-side the QUADRANT are inserted Lines for Erecting of a Scheme of the Heavens for any time; and also Lines shewing the Diameter, Circumference, Area, and Square equal, of a Circle; with an Useful ALMANACK.

To which is Added,
A NEW TABLE of *Refractions* for Correcting the Sun, Moon, and Stars Altitude; As also a Table of Equations, for the Adjusting of *Pendulum* Clocks and Watches.

By *J O H N W I N G*, Math.

L O N D O N,

Printed for *Awnsham and John Churchill*, at the *Black-Swan* in *Pater-Noster-Row*, MDCXCIX.

T H E
A R T
O F
SURVEYING.

B O O K VI.

C H A P. I.

*The Description and Inscription of the several
Lines on the Fore-side of the Quadrant.*

IN regard Mr. *Gunter's* Quadrant has gained (and indeed worthily) the popular applause, for finding the Hour and Azimuth, I have therefore proceeded in the Calculation and Projection of the Hour and Azimuth-Lines, according to that Author's Method; the rest (the Ecliptick and Horizon excepted) has no relation to *Gunter's* Quadrant, as is plain by what follows.

I. The Limb of the Quadrant (as in all others) is divided into 90 equal Parts call'd Degrees, and numbered by 10, 20, 30, &c. to 90, as being the 4th part of a Circle; the whole containing 360 Degrees.

II. Next above the Limb or 90 Degrees is placed a Line which is character'd at each end thereof R. A. being a Line of right Ascensions in time, shewing the R. A. of all points of the Ecliptick, in Hours and Minutes, being of Excellent Use in finding the Southing of the Planets and Fixed Stars, and may be projected into the Quadrant from this following Table of Right Ascensions, for 15 gr. in the Limb is 1 hour; 30, 2 hours, &c. And is numbered into Hours and Minutes, beginning at I, and ending at the other end at VI, which Divisions, backward and forward four times repeated, are Divided and Character'd into XXIV hours.

A a a 2

III. The

Tabula Ascensionum Rectarum.

	γ				δ				Π			
	gr.		h.		gr.		h.		gr.		h.	
0	0	0	0	0	27	54	I	52	57	48	3	51
I	0	55	0	4	28	51	I	55	58	51	3	55
2	I	50	0	7	29	49	I	59	59	53	4	0
3	2	45	0	11	30	46	2	3	60	56	4	4
4	3	40	0	15	31	44	2	7	61	59	4	8
5	4	35	0	18	32	42	2	11	63	3	4	12
6	5	30	0	22	33	40	2	15	64	6	4	16
7	6	25	0	26	34	38	2	19	65	9	4	21
8	7	21	0	29	35	37	2	23	66	13	4	25
9	8	16	0	33	36	36	2	26	67	17	4	29
10	9	11	0	37	37	34	2	30	68	21	4	33
11	10	6	0	40	38	33	2	34	69	25	4	38
12	11	2	0	44	39	33	2	38	70	29	4	42
13	11	57	0	48	40	32	2	42	71	34	4	46
14	12	53	0	52	41	31	2	46	72	38	4	51
15	13	48	0	55	42	31	2	50	73	43	4	55
16	14	44	0	59	43	31	2	54	74	47	4	59
17	15	40	I	3	44	31	2	58	75	52	5	3
18	16	35	I	6	45	31	3	2	76	57	5	8
19	17	31	I	10	46	32	3	6	78	2	5	12
20	18	27	I	14	47	32	3	10	79	7	5	16
21	19	33	I	18	48	33	3	14	80	12	5	21
22	20	20	I	21	49	34	3	18	81	17	5	25
23	21	16	I	26	50	35	3	22	82	22	5	29
24	22	12	I	29	51	36	3	26	83	28	5	34
25	23	9	I	33	52	38	3	30	84	33	5	38
26	24	6	I	36	53	40	3	35	85	38	5	43
27	25	2	I	40	54	42	3	39	86	44	5	47
28	25	59	I	44	55	44	3	43	87	49	5	51
29	26	57	I	48	56	46	3	47	88	55	5	56
30	27	54	I	52	57	48	3	51	90	0	6	0

III. The next line (or rather two lines) marked at the Left-hand side with O A, and O D, and at the Right-hand side with O D, and O A, are lines of Oblique Ascensions and Oblique Descensions in time, being Applicable, for finding the Rising and Setting of the Planets and Fixed Stars, and may be inserted into the Quadrant, from the following Table of Oblique Ascensions, as it is here converted into Time, and by the help of the Ecliptick-Line, is numbered by I. II. &c. (backward and forward) to XXIV hours, and is inserted according to the XVth of this Chapter.

IV. The next or uppermost Line next the Hour-lines marked at either end with *Dec.* is a line of Declinations divided into Degrees, &c. Number'd by 10, 20; to 23 Deg. 29 Minutes, which is the Suns greatest Declination, and may be inserted into the Quadrant from the following Table of Declinations, and by the XVIth of this Chap.

V. The uppermost Line upon which the Hour-Lines abutteth is also the line for the Tropics of *Cancer* and *Capricorn* which the Horizon and Ecliptic crosses, in their respective places.

VI. The next line which includes the Hour-lines is the Equator; upon which the Hours and Azimuths fall and are number'd.

VII. Between the two lines, last explained and described, are placed the Ecliptic from the Equator, crossing the Zodiac to the Tropicks of ☊ and ☋ characterized, with the 12 Signs, each Sign divided into 30 Degrees, and number'd by 10, 20, 30. the division of which line is taken from the aforegoing Table of Right Ascensions; for 'tis but laying a Rular to the Center, and to 27 gr. 54' in the Limb, and the point where the Rular crosseth the Ecliptick shall be the first point of ♈. In like manner the Right Ascension of the first point of ♈ is 57 or 48 Minutes. So if you lay a Rular to the Center, and 57 Degrees 48' in the Limb, the point where the Rular crosseth the Ecliptick, shall be the first point of ♈, and so for every 10, and 5 Degrees, and consequently every Degree, as you find it in the Table of Right Ascensions.

VIII. The Horizon also cometh from the same Point with the Ecliptick in the Equator, and falls upon the Tropicks, and is unequally divided into Degrees, and numbered by 10, 20, 30, &c. and by this following Analogy, you may find where the Horizon crosses the Tropicks for

As the <i>co. t.</i> of the Lat. 52° 00'	9.892810
to the <i>t.</i> of great. Dec. 23 29	9.637956
So the Radius 90 00	10.000000
to <i>s.</i> of Interfection 33 47	9.745146

Wherefore if you lay a Rular to the Centre, and to 33 gr. 47' in the Limb, the point where the Rular crosseth the Tropick, is the Point where the Horizon falleth upon the Tropicks: Then find a point on the Right side of the Quadrant for the Centre
to

*Tabula Ascensionum Obliquarum
Eclipticæ, ad Lat. 52°.*

S. D.	gr.	'	h	'	S. D.	gr.	'	h	'	S. D.	gr.	'	h	'
γ.	00	00	0	0	Ω.	094	66	16	16	ι.	0265	54	17	44
	41	37	0	6		499	42	6	39		4271	26	18	6
	83	15	0	13		8105	22	7	2		8276	50	18	28
	124	55	0	20		12111	47	24			12282	8	18	50
	166	35	0	26		16116	49	7	47		16287	16	19	9
	208	18	0	33		20122	35	8	10		20292	15	19	29
	2410	40	40			24128	22	8	33		24297	2	19	48
	2811	53	0	48		28134	8	8	56		28301	36	20	6
δ.	213	45	0	55	μ.	2139	54	9	20	ν.	2305	58	20	24
	615	42	1	3		6145	40	9	43		6310	7	20	41
	1017	45	1	11		10151	24	10	6		10314	1	20	56
	1419	52	1	20		14157	8	10	29		14317	41	21	11
	1822	8	1	29		18162	52	10	52		18321	9	21	25
	2224	31	1	38		22168	35	11	14		22324	24	21	38
	2627	2	1	48		26174	18	11	37		26327	26	21	50
Π.	029	42	1	59	π.	0180	0	12	0	π.	0330	8	22	1
	432	34	2	10		4185	42	12	23		4332	58	22	12
	835	36	2	22		8191	25	12	46		8335	29	22	22
	1238	51	2	36		12197	8	13	9		12337	52	22	31
	1642	19	2	49		16202	52	13	32		16340	8	22	40
	2045	59	3	4		20208	36	13	54		20342	15	22	49
	2449	53	3	20		24214	20	14	17		24344	18	22	57
	2854	23	3	36		28220	6	14	40		28346	15	23	5
Σ.	258	24	3	54	ι.	2225	52	15	4	κ.	2348	7	23	13
	662	58	4	12		6231	38	15	26		6349	56	23	20
	1067	45	4	31		10237	25	15	50		10351	42	23	27
	1472	44	4	51		14243	11	16	13		14353	25	23	34
	1877	52	5	12		18248	56	16	36		18355	5	23	40
	2283	10	5	33		22254	38	16	59		22356	45	23	47
	2688	34	5	54		26260	18	17	21		26358	23	23	45

Tabula Declinationum.

D.	gr.			gr.			gr.		D.
0	0	0		11	30		20	11	30
1	0	24		11	50		20	24	29
2	0	48		12	11		20	36	28
3	1	12		12	31		20	48	27
4	1	36		12	52		20	59	26
5	2	0		13	12		21	11	25
6	2	24		13	32		21	21	24
7	2	47		13	52		21	31	23
8	3	10		14	12		21	41	22
9	3	34		14	31		21	51	21
10	3	57		14	50		22	0	20
11	4	21		15	9		22	8	19
12	4	45		15	27		22	17	18
13	5	19		15	46		22	25	17
14	5	32		16	4		22	32	16
15	5	55		16	22		22	39	15
16	6	18		16	39		22	45	14
17	6	41		16	56		22	51	13
18	7	4		17	13		22	57	12
19	7	27		17	30		23	2	11
20	7	50		17	46		23	7	10
21	8	12		18	2		23	11	9
22	8	35		18	18		23	15	8
23	8	57		18	33		23	18	7
24	9	20		18	48		23	21	6
25	9	42		19	3		23	24	5
26	10	4		19	17		23	26	4
27	10	25		19	31		23	27	3
28	10	47		19	45		23	28	2
29	11	8		19	58		23	29	1
30	11	30		20	11		23	29	0
	天 度			度 分			度 分		

to draw the Arch of the Horizon from, that it may fall upon the limited Points in the Tropicks and Equator.

For the Division of the Horizon use this Analogie.

As the Rad.	90° 00'	10.000000
to the s. of the Latitude	52 00	9.896532
So the t. of the Horizon, viz.	10 00	9.246319
to the t. of the Arke in the Limb.	7 59	9.142851

Wherefore lay a Rular to the Centre, and to 7 Deg. 59 Min. in the Limb, and where the Rular crosseth the Horizon, shall be the Division of 10 Deg. in the Horizon, and so for the rest.

A Table of the Sun's Altitude at all Hours of the Day, at the Suns entrance into any of the XII Signs, and at every Tenth Degree thereof.

Ho. before N.	Ho. after N.	XII.	XI.	X.	IX.	VIII.	VII.	VI.	V.	IV.	III.	II.	I.
S. D.	S. D.	°	'	°	'	°	'	°	'	°	'	°	'
♈	♈	0 61	30	59	58	53	21	45	51	36	36	27	23
20	10 61	7	58	53	53	5	45	11	36	18	27	6	18
10	20 60	0	57	50	52	7	44	18	35	28	26	16	17
♉	♉	0 58	13	56	6	50	33	42	52	34	1	24	57
20	10 55	47	53	47	48	25	40	54	32	14	23	5	13
10	20 52	52	50	58	46	49	38	30	29	57	20	50	11
♊	♊	0 49	30	47	43	42	48	35	42	27	18	18	18
20	10 45	51	44	9	39	27	32	35	24	20	15	21	6
10	20 42	0	40	23	35	54	29	16	21	12	12	26	3
♋	♋	0 38	0	36	29	32	13	25	48	17	6	9	10
20	10 34	2	32	36	28	21	22	19	14	38	6	0	0
10	20 30	11	28	49	24	54	18	55	11	24	2	54	54
♌	♌	0 26	30	25	12	21	27	15	31	8	19	0	56
20	10 23	9	21	55	18	17	12	39	5	30	5	30	5
10	20 22	41	19	2	15	31	10	2	3	2	2	2	2
♍	♍	0 17	49	16	38	13	14	7	52	0	59	59	59
20	10 16	0	14	52	11	31	6	15	15	15	15	15	15
10	20 14	53	13	46	10	28	5	15	15	15	15	15	15
♎	♎	14	30	13	21	10	3	4	51	51	51	51	51

IX. The Hour-lines are included between the Equator and Tropicks, and are Character'd with Letters at the Equator, respecting the several Hours for the Morning, and with Figures at the Tropicks giving the Denomination to each Hour after Noon, both for the Summer and Winter-Hours, where Note, that the Hours

Hours for the Summer half Year extend themselves toward the Right-hand, and the Hours for the Winter half Year to the Left-hand; these Hour-lines are drawn upon the Quadrant from this Table of the Sun's Altitude, which must be taken in three several Places, *viz.* in the Equator, Tropicks, and some one Parallel of Declination, hence observe for the inserting the several Hour-lines into the Quadrant, that if you lay a Rular to the Centre, and to 61 Deg. 30' in the Limb, Observe then where it crosses the Tropick, and there make a Prick: then move the Rular to 49 Deg. 30' and Note where it crosseth the Parallel of 8 (the Sun there hath 11° 30' of Declination, which is the Parallel of Declination we here make use of) and there make a Second Prick: Again lay the Rular from the Centre to 38 Deg. in the Limb, and where it crosseth the Equator make a third Prick, now find a Centre to these three Pricks, which brings them all into an Arch-line which shall be the Hour-line for 12 a Clock in the Summer, observe the same Method for all the rest of the Hours in the Summer half Year, and also for those in the Winter. Note also that the Hours for 5 and 7, and 4 and 8, which Points fall between the Equator and Tropicks, those Points of the Summer and Winter-Hours meeting are best found (which fall by the edge of the Quadrant) by the line of Declinations, for 'tis but laying the String on the Degree of Declination, then bring the Bead to the Ecliptick, answerable to the Days of the Month that the Sun Rises at 4 and 5 in the Summer, or Sets at 4 and 5 in Winter (all which agrees) then move the String to the Left edge of the Quadrant, and there where the Bead falls is the Points for the said Hour-lines, and shews also the lines, or Points of the Sun's Rising and Setting, for 5 and 7, and 4 and 8.

A Table of the Altitude of the Sun in the beginning of each Sign for every 10th Azimuth. Latit. 52. Degrees.

Azimuth		10		20		30		40		50		60		70		80		90	
Merid.		gr.		gr.		gr.		gr.		gr.		gr.		gr.		gr.		gr.	
♈	61 30	51	14	60	22	58	52	56	38	53	33	49	29	44	14	37	58	30	24
♉	58 12	58	54	56	28	56	22	53	0	49	43	44	25	40	0	33	28	26	0
♊	49 30	49	9	48	3	46	11	43	26	39	44	34	58	29	6	22	15	14	40
♋	38 0	37	35	36	17	34	5	30	54	26	40	21	20	14	57	7	44	0	0
♌	26 30	26	1	24	31	22	0	18	22	13	26	7	42	0	48	6	46		
♍	17 48	17	16	15	36	12	48	8	49	3	37	2	45	10	6	18	0		
♎	14 30	13	56	12	12	9	18	5	10	0	13	6	49	14	19	22	30		

X. The Azimuth lines are placed on the Right-side the Quadrant, as the Hour-lines are on the left, and are drawn to every 10th Azimuth and Numbered by 10, 20, 30, 40, &c. to 120, and are inserted from this Table of the Sun's Altitude in the beginning of each Sign for every 10th Azimuth, and according to the same

Method the Hour-lines were from the former Table, for you must find by this Table, where each 10th Azimuth falls upon the Equator, Tropicks, and some Parallel of Declination. As suppose you would draw the 10th Azimuth from the Meridian, lay a Rular to the Centre and to 61 Deg. 14' in the Limb, and where the Rular crosseth the Tropick there make a prick; then move the Rular to 37 Deg. 55' in the Limb, and where it crosseth the Equator make a second prick; then lay the Rular in the Limb to 49 Deg. 9' and where it crosseth the Parallel of \varnothing (being the Parallel here made use of) make a third Prick; these three Pricks drawn into a Circle shall be the Azimuth line of 10 Deg. from the Meridian as was requir'd, observe the like for the rest.

XI. There is placed on either side the Ecliptick several fixed Stars, with their Names affixed to them, and are placed according to their Declination from the Equator, and fitted to the Longitude of this Age, whose Longitude, Latitude, and Declination are as in this Table, from which they may be inserted into the Quadrant, according to these following directions.

Names of the Stars.	Longitude.			Latitude.			Declination.		
	S.	o		o			o		
Pleiades.	\varnothing	25	47	4	0	N.	22	58	N.
Aldebaran.	Π	5	35	5	31	S.	15	45	N.
Sirius.	\varnothing	9	58	39	30	S.	16	13	S.
Cor Leonis.	Ω	25	40	0	26	S.	13	41	N.
V. Spick.	Π	19	49	1	59	S.	9	16	S.
Arcturus.	Π	20	23	1	2	N.	21	6	N.
S. Ballance.	Π	10	54	0	26	N.	14	30	S.

Let it be required to place *Aldebaran* in the Quadrant according to his Longitude, and Declination: First, lay the Thread upon $15^{\circ} 45'$ (being his Declination) in the line of Declinations, it resting there, bring the bead to the Ecliptick, which done move the String to $5^{\circ} 35'$ Π his place in Longitude, and where the Bead falls is the place where you are to place the Star *Aldebaran*: Observe the same Method for the rest, or for any other Stars you have a mind to fix upon your Quadrant.

XII. The Months are placed in the Circular lines above the Equator, each Month and Day being fitted to the Sun's place in the Ecliptick, and for inserting them into their several Circles in the Quadrant, 'tis but laying the Thread to the Sun's place in the Ecliptick answerable to each Month and Day, and so make their Divisions in their respective Circles: As suppose you would put on the 1st Day of *March*, the Sun's place that Day at Noon is $21^{\circ} 30'$ \times , upon which point of the Ecliptick lay the Thread, and where it falls in the Circle of Months make a Mark for the first Day of *March*: Again, let it be required to put on the 30th Day of *March*, the Sun that Day is in 20° of γ , to which point

point in the Ecliptick bring the Thread, and where it falls in the Circle of Months, make a Mark for the 30th Day of *March*; observe this Method for all the Months and Days in the Year.

XIII. On the Left-side the Quadrant is placed between the Tropicks and Equator, a double line shewing the time of Sun's rising and setting to a Minute for every Day in the Year, and may be graduated upon the Quadrant from this following Table; for if the Thread be laid to the Day of the Month, and the Bead brought to the Ecliptick; then move the String to the side of the Quadrant, and there where the Bead falls, put down the Sun's rising and setting according to the time from the Table: Where Note it being doubly to be understood according to the time of the Year, for it may be either the time of the Sun's Rising in the Summer, or his Setting in Winter, as 8 may be his Rising in Winter, and Setting in Summer, and 4 may be his Rising in Summer, and Setting in Winter; which is all one line upon the Quadrant, and if you look in the Table on the 3d day of *January*, you will find the Sun that Day to Rise at 8 in the Morning, and Set at 4 in the Afternoon (where Note that the Sun's *Semi-Nocturnal* Arch shews the time of his Rising, and his *Semi-Diurnal* Arch the time of his Setting). Again, the 16 Day of *May*, the Sun Sets at 8 at Night, and rises at 4 in the Morning, and likewise *July* the 6th Day the Sun Rises at 4 and Sets at 8, and also the 17th day of *November* he Rises at 8 in the Morning and Sets at 4 After Noon; So that laying the String (in the Quadrant) upon either of the aforementioned days (for the laying the String upon any one of them, it will at the same time fall on all the rest) and bring the Bead to the Ecliptick, then move the String to the Left-side of the Quadrant and where the Bead falls, there draw a line for the Sun's Rising and Setting as before; and so accordingly for the rest.

XIV. On the Right-side of the Quadrant, between the Tropicks and Equator, is another double line, shewing how many Hours and Minutes the days are Increased or Decreased, which Line discovers every day in the Year to one Minute, and may be inserted into the Quadrant, from this following Table, for the Thread being laid to what Month and Day you please, and there bring the Bead to the Ecliptick, then look in the Table for the same Month and Day, and by moving the Thread to the Right-side, and where the Bead falls, put on the Increase or Decrease of the Days at that time as you find it by the Table: As, suppose the Days be increased 2 Hours which in the Table you will find on the 31st Day of *January*, and there bring the Bead to the Ecliptick, then move the String to the Right-side of the Quadrant, and where the Bead falls, draw a line (or likewise the 4th Day of *August* when the Days are Decreased 2 hours, for this line serves for both the Increase or Decrease of the Days, as may be discovered by the Table) and this line so drawn shews the Day to be Increased 2 Hours, if it be the 30th of *January*, or

B b b 2

Decreased

A Table of the Sun's Semi-^{{Diurnal}_{Nocturnal} Arch
for the Latitude of 52 Degrees.

	Jan.	Feb.	Mar.	April.	May.	June.
D.	h. ' "	h. ' "	h. ' "	h. ' "	h. ' "	h. ' "
1	8 Noct. 2	7 13	6 17	6 44	7 39	8 13
2	8 1	7 11	6 15	6 46	7 41	8 13
3	8 0	7 9	6 13	6 48	7 42	8 14
4	7 59	7 7	6 11	6 50	7 43	8 14
5	7 58	7 5	6 9	6 52	7 45	8 14
6	7 56	7 3	6 7	6 54	7 46	8 15
7	7 55	7 1	6 5	6 56	7 48	8 15
8	7 53	7 0	6 3	6 58	7 50	8 15
9	7 52	6 58	6 1	7 0	7 51	8 15
10	7 51	6 56	6 Diur. 1	7 2	7 53	8 15
11	7 50	6 54	6 3	7 4	7 55	8 15
12	7 48	6 52	6 5	7 6	7 56	8 15
13	7 46	6 50	6 7	7 8	7 57	8 15
14	7 45	6 48	6 9	7 10	7 58	8 15
15	7 43	6 46	6 11	7 12	7 59	8 15
16	7 42	6 44	6 13	7 14	8 0	8 14
17	7 41	6 42	6 15	7 16	8 1	8 14
18	7 39	6 40	6 17	7 17	8 2	8 14
19	7 38	6 38	6 19	7 19	8 3	8 13
20	7 36	6 36	6 20	7 21	8 4	8 13
21	7 34	6 34	6 22	7 23	8 5	8 12
22	7 32	6 32	6 24	7 25	8 6	8 11
23	7 30	6 29	6 26	7 27	8 7	8 11
24	7 28	6 27	6 28	7 28	8 8	8 10
25	7 27	6 25	6 30	7 30	8 8	8 9
26	7 25	6 23	6 32	7 31	8 9	8 9
27	7 23	6 21	6 34	7 33	8 9	8 8
28	7 21	6 19	6 36	7 34	8 10	8 8
29	7 19		6 38	7 37	8 11	8 7
30	7 17		6 40	7 38	8 11	8 6
31	7 15		6 42		8 12	

*A Table of the Sun's Semi-[{]Diurnal
Nocturnal[}] Arch
for the Latitude of 52 Degrees.*

	July.	Aug.	Sep.	Octob.	Nov.	Dec.
D.	<i>h.</i>	<i>h.</i>	<i>h.</i>	<i>h.</i>	<i>h.</i>	<i>h.</i>
1	8 6	7 21	6 22	6 39	7 38	8 12
2	8 5	7 19	6 20	6 41	7 39	8 13
3	8 4	7 17	6 18	6 43	7 41	8 13
4	8 2	7 16	6 16	6 45	7 42	8 14
5	8 1	7 14	6 14	6 47	7 43	8 14
6	8 0	7 12	6 12	6 49	7 45	8 14
7	7 59	7 10	6 11	6 51	7 46	8 15
8	7 58	7 8	6 8	6 53	7 48	8 15
9	7 56	7 6	6 6	6 55	7 50	8 15
10	7 55	7 4	6 3	6 57	7 51	8 15
11	7 53	7 2	6 1	6 59	7 52	8 15
12	7 52	7 0	6 Noct. 0	7 0	7 53	8 15
13	7 51	6 59	6 1	7 2	7 55	8 15
14	7 50	6 57	6 3	7 4	7 56	8 15
15	7 48	6 55	6 6	7 6	7 58	8 15
16	7 46	6 54	6 8	7 8	7 59	8 14
17	7 45	6 52	6 11	7 10	8 0	8 14
18	7 43	6 50	6 12	7 12	8 1	8 14
19	7 42	6 48	6 14	7 14	8 2	8 13
20	7 41	6 46	6 16	7 16	8 4	8 13
21	7 39	6 44	6 18	7 17	8 5	8 12
22	7 40	6 42	6 20	7 19	8 6	8 11
23	7 38	6 40	6 22	7 21	8 7	8 11
24	7 37	6 38	6 24	7 23	8 8	8 10
25	7 35	6 36	6 26	7 25	8 8	8 9
26	7 33	6 34	6 28	7 27	8 9	8 9
27	7 31	6 32	6 31	7 28	8 9	8 8
28	7 29	6 30	6 33	7 30	8 10	8 8
29	7 27	6 28	6 35	7 32	8 11	8 7
30	7 25	6 26	6 37	7 34	8 11	8 6
31	7 23	6 24		7 36		8 5

A Table shewing the Increase and Decrease of the Days for the Latitude of 52 Degrees, for the first Six Months of the Year.

Days.	Jan.		Feb.		Mar.		April.		May.		June.	
	h.	'	h.	'	h.	'	h.	'	h.	'	h.	'
1	0	26	2	3	3	56	5	58	7	49	8	55
2	0	28	2	7	4	0	6	2	7	52	8	56
3	0	30	2	11	4	4	6	6	7	55	8	57
4	0	32	2	15	4	8	6	10	7	58	8	58
5	0	34	2	19	4	12	6	14	8	1	8	59
6	0	37	2	23	4	16	6	18	8	4	8	59
7	0	40	2	26	4	20	6	22	8	7	8	59
8	0	43	2	30	4	24	6	26	8	10	9	0
9	0	46	2	34	4	28	6	30	8	13	9	0
10	0	49	2	38	4	32	6	34	8	16	9	0
11	0	52	2	42	4	36	6	38	8	19	Days.	Dec.
12	0	55	2	46	4	40	6	41	8	22	0	0
13	0	58	2	50	4	44	6	45	8	24	0	0
14	1	1	2	54	4	48	6	49	8	26	0	0
15	1	4	2	58	4	52	6	53	8	28	0	1
16	1	7	3	2	4	56	6	57	8	30	0	1
17	1	10	3	6	5	0	7	0	8	32	0	2
18	1	13	3	10	5	3	7	4	8	34	0	2
19	1	16	3	14	5	7	7	8	8	36	0	3
20	1	20	3	18	5	11	7	12	8	38	0	4
21	1	23	3	22	5	14	7	15	8	40	0	5
22	1	26	3	26	5	18	7	19	8	42	0	6
23	1	29	3	30	5	22	7	23	8	43	0	7
24	1	32	3	35	5	26	7	27	8	45	0	9
25	1	36	3	39	5	30	7	31	8	46	0	10
26	1	40	3	44	5	34	7	34	8	48	0	11
27	1	44	3	48	5	38	7	37	8	49	0	12
28	1	48	3	52	5	42	7	40	8	51	0	14
29	1	52			5	46	7	53	8	52	0	16
30	1	56			5	50	7	46	8	53	0	18
31	2	0			5	54			8	54		

A Table shewing the Increase or Decrease of the Days for the Latitude of 52 Degrees, for the last Six Months of the Year.

	July.		Aug.		Sep.		Octob.		Nov.		Dec.	
D.	h. '		h. '		h. '		h. '		h. '		h. '	
1	0	20	1	48	3	46	5	48	7	46	8	54
2	0	22	1	51	3	50	5	52	7	49	8	55
3	0	24	1	55	3	54	5	56	7	52	8	56
4	0	26	1	59	3	58	6	0	7	55	8	57
5	0	28	2	2	4	2	6	4	7	58	8	58
6	0	30	2	6	4	6	6	8	8	0	8	59
7	0	32	2	10	4	10	6	12	8	3	8	59
8	0	34	2	14	4	14	6	16	8	6	9	0
9	0	37	2	18	4	18	6	20	8	9	9	0
10	0	39	2	22	4	22	6	24	8	12	9	0
11	0	43	2	25	4	26	6	28	8	14	Days Incr.	
12	0	46	2	29	4	30	6	32	8	17	0	0
13	0	48	2	33	4	34	6	36	8	19	0	0
14	0	51	2	36	4	38	6	39	8	22	0	0
15	0	54	2	40	4	42	6	43	8	25	0	0
16	0	57	2	43	4	46	6	47	8	28	0	1
17	1	0	2	47	4	50	6	50	8	30	0	1
18	1	3	2	51	4	54	6	54	8	33	0	2
19	1	6	2	54	4	58	6	58	8	35	0	3
20	1	9	2	58	5	2	7	2	8	38	0	4
21	1	12	3	2	5	7	7	6	8	40	0	5
22	1	15	3	6	5	11	7	9	8	42	0	6
23	1	18	3	10	5	15	7	13	8	44	0	7
24	1	21	3	14	5	19	7	17	8	46	0	9
25	1	24	3	18	5	23	7	20	8	48	0	10
26	1	27	3	22	5	27	7	24	8	49	0	11
27	1	30	3	26	5	32	7	28	8	50	0	13
28	1	33	3	30	5	36	7	31	8	51	0	15
29	1	36	3	34	5	40	7	35	8	52	0	16
30	1	40	3	38	5	44	7	39	8	53	0	18
31	1	44	3	42			7	42			0	20

Decreased 2 hours, if it be the 4th Day of *August*, and by this Method you may put on all the rest from this Table.

XV. To insert the Oblique Ascensions in time into the Quadrant, First lay the Thread to 4 Deg. 30 Min. 8, in the Ecliptick (which in the Table of O A. *Page* 278, gives 1 Hour) and where the String crosseth the line of O A. make a Mark for 1 Hour, being the O A in time agreeing to 4° 30' 8; Likewise you may find by the Table that 0° 15' 11 gives the O A, two Hours, wherefore lay the String to 0° 15' 11, and where it crosseth the line of the Oblique Ascensions, there make a Mark for 2 Hours: Again the String laid to 18° 50' 11, where it falls in the line of O A make a mark for 3 Hours, and thus may the Table direct you to put on the rest.

XVI. For the Inscribing the line of Declinations into the Quadrant in Degrees, do thus, lay the Thread to 2 Deg. 30 Min. 7, and where the Thread crosses the line of the Declinations, there make a mark for 1 Deg. of Declination: Again lay the Thread to 5 Deg. 7, and where the String then crosseth the line of Declinations make another mark for 2 Deg. of Declination, and so the rest, as the Table of Declinations *Page* 279 directs.

XVII. There is a Thread and Plummets to be put to the Quadrant with a small Bead upon the Thread to be moved up and down as occasion requires, there are also a pair of Sights with little holes in them fixed on the Right-side of the Quadrant, so it is fitted for use.

Note that by the foregoing Tables and Directions may a Quadrant be made to what Radius you please.

C H A P. II.

The Use of the Degrees in the Limb of the Quadrant, in takeing of Altitudes.

P R O P. I.

To find the Altitude of the Sun.

Hold up the Quadrant, so that the Sun-beams may pass thro' both the Sights, holding the Quadrant also in that posture, that the Thread with the Plummets may play easily by the side of it, Then observe the Degrees cut by the Thread in the Limb of the Quadrant, which is the Altitude of the Sun required.

E X A M P L E I.

Suppose on the 11th day of *June* at Noon, the Sun-beams passing through the Sights, the Thread falling upon 61 Degrees 30 Min. in the Limb, so much then is the Sun's Altitude, it being also the

the greatest Meridian Altitude of the Sun in the Latitude of 52 Degrees.

E X A M P L E II.

Suppose the same day at 4 after Noon, the Thread fall upon 28 Degrees in the Limb (by holding the Quadrant as before directed) such then was the Altitude of the Sun at that Time.

P R O B. II.

To find the Altitude of a Star by Night.

Suppose at any time of the Night I espie a Star upon the Meridian or any other place in the Heavens, and desire to know the Altitude thereof; hold up the Quadrant so that the Thread and Plummet may have free liberty to Play by the side of the Quadrant, and looking at the Star through the Sights, then will the Thread in the Limb fall on the Degrees of Altitude, of the said Star, which being so easy it needs no Example.

P R O B. III.

To find the Altitude of a Steeple, Tower, Tree, or the like.

The Steeple, &c. Standing upon a Level from you; if not, you must first find where the Level falls from your Eye to the Steeple, &c. Then hold the Quadrant to your Eye, and go backwards or forwards, till the String fall upon 45 Degrees in the Limb; Then add the height from your Eye to the Ground, to your Standing, backwards, and from that place to the Steeple, is equal to the height of the Steeple the thing required.

Note that if the String fall on 22 gr. 30', the height is but half the distance: And contrary, if the Thread fall on 67 gr. 30' the height is double the said distance, but if the distance given be more or less, the Case must be resolved by the Doctrine of a plain Right-Angled Triangle.

E X A M P L E.

Suppose the distance be 265 Foot, at which distance I look through the Sights of the Quadrant, to the top of the Steeple or Tower, and find the Thread to fall upon 25 Degrees in the Limb.

Then Say

As the Radius, 90 gr.	10.000000
to the Tang. of 25 gr.	9.668672
So the Distance, 265 Foot.	2.423246
to the Height required, 123.57 Foot.	2.091918

C c c

P R O P.

P R O B. IV.

The distance being given, to find the Hypothenufe, or distance from the Eye to the top of the Steeple.

Let the distance as in the last Example be 265 Foot, and the Angle at the Eye (as before) 25 Degrees, Hence the Analogy is.

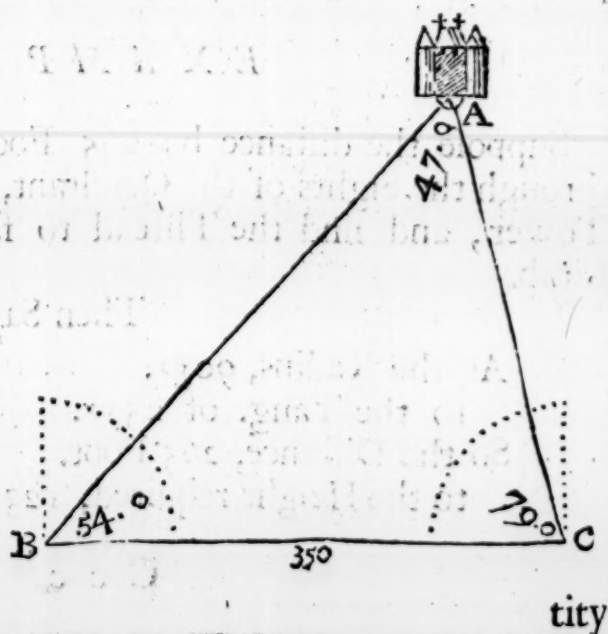
As the Co-sine of $25^{\circ} 00'$	9.957296
to the Radius, 90°	10.000000
So the Distance, 265 Foot	2.423246
to 292.40 Foot, the Hypothenufe required	2.465970

To the former Problems of *Altimetria*, I shall annex a Problem or two of *Longimetria*, whereby the distance of any such Places upon the Earth, that lye within the View of the Eye, may be found out and determined by the Solution of right-lined Triangles, and also by Projection, as we shall afterward shew; which will be most excellent and useful for Surveyors, Engineers, Miners, and such like, who may hereby perform many notable exploits in Militarie affairs, as Springing of Mines, approaching to Forts and Castles, and making Batteries: Neither can the Geographer be perfect in his Work, without a competent knowledge therein, for by the help thereof, a whole Region or Country may exactly be described, and all such Towns, Rivers, Marshes, and other remarkable Places lying within the same, may hereby be laid down in their due Place and Order; and if there be any errors in such Maps and Chards as are already extant, they may hence be corrected, as the Ingenious Artift will sooner find by Practice, than by many Words, and therefore I shall not make any tedious preamble but shall come to that which I intend upon this matter.

P R O B. V.

The Interval of two Stations being given, with the Quantity of the Angle at each Station, to find the Distance.

Suppose from some private place, as B, you espy a Castle, but for fear of Gun-shot, Moorish ground or some other Impediments, you cannot have an opportunity to make your second Station in any open place, but are forced to make it in some other secure place, as at C: In this case having planted your Instrument at B, and directed the Sights to A and C, take the quan-



tity of the Angle ABC , 54 Deg. 0 Min. and the quantity of the Angle ACB , 79 Deg. 0 Min. Which known, with the Interval of the two Stations B and C , 350 Yards, I say by the 4th Problem of the Third Book, Sect. 2.

1. To find BA .

As the sine of the Angle BAC , 47 D. 0 M.
To BC , 350 Yards
So the sine of the Angle ACB , 79 D. 0 M.

9.86413
2.54407
9.99194

To the Distance BA , 469.77

12.53601
2.67188

2. To find CA .

As the sine of the Angle BAC , 47 D. 0 M.
To BC , 350 .
So the sine of the Angle ABC , 54 D. 0 M.

9.86413
2.54407
9.90796

To AC the distance required, 387.17

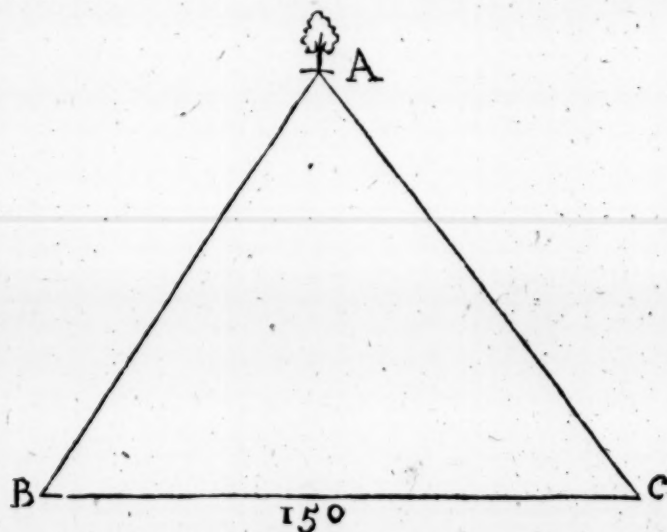
12.45203
2.58790

P R O B. VI.

To take the Distance of a Place at two Stations, by the Plain-Table.

Having made choice of the place of your first Station, as at B , there plant your Table, and direct your Sights to the Tree at A : Next direct the sights of your Index to the place of the second Station at C , and from B strike lines towards A and C : Then with your Chain, measure the Interval of the two Stations B and C , 150 Yards: Then plant your Table at C , where you may see both the Tree and

your first Station, and screwing fast the Table, lay the Index upon the line BC ; which done, turn the Table gently about, till through the Sights you see the place of your first Station at B ; then fixing the Table turn the Index about upon the point C , and directing the



Sights thereof to A , strike a line by the edge of the Ruler, and where it intersects the line AB (as at A) there make a mark;

C c c 2

then

then open your Compasses to the extent B A. which being applied to the same Scale, by which you laid down the Stationary distance, you shall find the distance B A 124 Yards, and the distance C A 135 Yards.

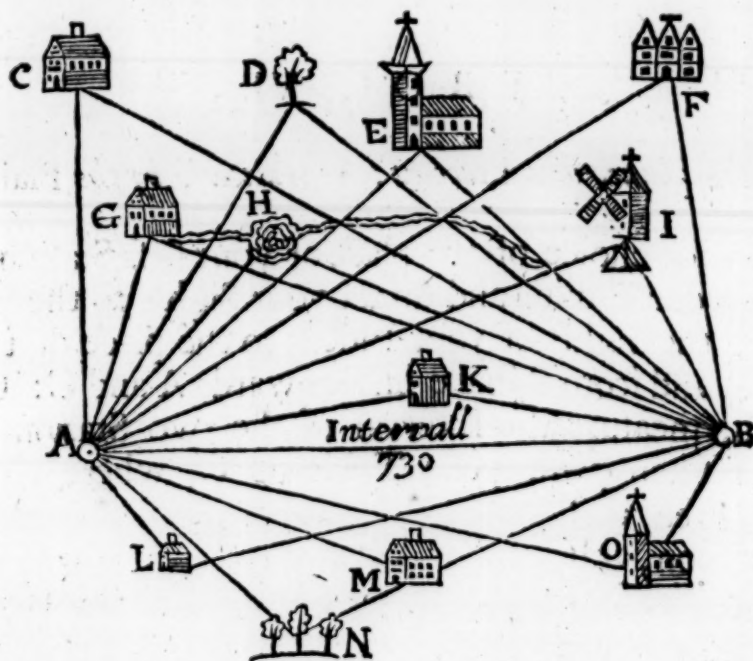
But it is to be noted (in Works of this Nature) that the larger the Interval of the Stations are, the more exactly will the distance be found.

P R O B. VII.

To take the distance of divers Places remote from You, by the help of two Stations.

This Problem serveth chiefly to describe upon Paper or Parchment, all the most Eminent and Remarkable places in a Country, Town, or City, whereby a Map thereof may be exactly made, as with a little Practice you may soon perceive.

Upon some Hill, or high piece of Ground, make choice of two Stations as A and B, from whence you may plainly discern all the principal Places which you intend to describe in your Map: Then at A plant your Table, and direct the Sights of the Index to B;



which done (your Table being fixed) set your Index upon the point A, upon which, turning it about, direct the sights severally to C, G, D, H, E, F, I, K, O, M, N, L, to every of which places, strike a line by the edge of the Rule: Next measure the Stationary distance A B, which you shall find 730 Perches, or two Miles and 90 Perches, which you are to place down from A to B, by the Assistance of your Scale and Compasses; Then planting the Table at B, lay the Index upon the Stationary line A B, and then turn the Table, till through the Sights you espie the place of your first Station at A, in which posture (the Table standing fixed) direct your

your sights again from B to all the former points, and where these and the lines drawn from A Intersect each other, there must you describe the several Places, to which you made observation, where you may write the name of the Place, as you see convenient.

Lastly, if you would know the distance of any of the places thus describ'd, one from another, you have no more to do, but to open your Compasses, to the two places upon the Paper, and then applying it to the same Scale, by which you laid down the Stationary distance, it will, without any further trouble, effect your desire. And thus much briefly touching this matter.

C H A P. III.

The Use of the Ecliptick-line.

P R O B. I.

The place of the Sun being given to find his Right Ascension.

THE Ecliptick-line is known by the Characters of the 12 Signs, as γ , δ , Π , &c. each Sign being unequally divided into 30 Degrees, and to be accounted according to the order and Succession of the Signs.

Lay the Thread on the Sign and Degree of the Sun's place in the Ecliptick, and the Degrees the String then cuts in the Limb is the Right Ascension required.

E X A M P L E. I.

Suppose the place of the Sun given be 25 Degrees of γ , the Thread laid thereon, cutteth in the Limb 23 Deg. 9 Min. which is the Right Ascension of the Sun at that time.

But if the place of the Sun be more than three Signs, or 90 Deg. from the beginning of γ , then more must be allowed than 90 Degrees to the Right Ascension, in respect this Instrument is but a Quadrant.

E X A M P L E II.

Admit the Sun be in 5 Deg. of α ; the String laid thereto, cutteth in the Limb 127 Deg. 22 Min. that is the whole Limb 90 Deg. and back again 37 Deg. 22 Min. which makes 127 Deg. 22 Min. the Sun's Right Ascension, as was required.

P R O B.

P R O B. II.

The R. A. of the Sun, being given, to find his place in the Ecliptick.

Lay the Thread on the R. A. in the Limb of the Quadrant, and without more adoe, it crosseth the place of the Sun in the Ecliptick; This in all respects is only the converse of the former, so needs no example to explain it.

C H A P. IV.

The Use of the Horizon.

P R O B. I.

The Sun's place, or day of the Month being given, to find the Amplitude of the Sun's Rising and Setting.

LAY the Thread to the day of the Month, and bring the Bead to the Ecliptick; which done, move the String till the Bead fall upon the Horizontal line, and there it will shew the Amplitude required.

E X A M P L E.

Admit the Day given be the 26th day of *May*, the Sun being then in $15^{\circ} 40' 11''$, the Bead rectified and brought to the Horizon, doth there fall upon 38 Deg. 50 Min. which is the Amplitude of the Sun's Rising from the *East*, and setting from the *West*.

Where Note that the said Amplitude is always *North* when the Sun is in *Northern* Signs, and *South* when he is in *Southern*.

P R O B. II.

The Sun's place or day of the Month given, to find the Ascensional Difference.

Rectifie the Bead for the time; which done, bring it to the Horizon, so the Degrees the Thread falls on in the Quadrant, shews the difference of Ascensions.

E X A M P L E.

The 26th Day of *May*, the Sun being in $15^{\circ} 40' 11''$, the Bead Rectified and brought to the Horizon, sheweth the Ascensional difference to be $31^{\circ} 17'$.

C H A P. V.

The Use of the Hour-lines.

P R O B. I.

The Day of the Month being given, to find the Hour of the Day.

LAY the Thread to the day of the Month, then bring the Bead to the Ecliptick, so is the Quadrant rectified for use, then hold the Quadrant, so as the Sun may Dart his Rays thro' both the Sights, the Thread and Plummēt playing easily by the side of the Quadrant, so will the Bead fall upon the Hour of the Day.

E X A M P L E.

On the 28th Day of *April* (the Bead being Rectified as above) I hold the Quadrant so as the Sun-Rays may pass through both the Sights; I find the Bead to fall upon the Hour-line of IX and III, so that if the Observation was made in the forenoon it was 9 of the Clock, if in the afternoon 3.

P R O B. II.

The Altitude of the Sun being given, to find the Hour of the Day.

Rectifie the Bead as before, then bring the Thread to the Altitude observed, so will the Bead fall upon the Hour of the Day.

E X A M P L E.

As on the first Day of *May* I observed the Sun's Altitude 47 Deg, bring the Thread to 47 Deg. in the Limb, so will the Bead fall on X, or II, so that if the observation was made in the forenoon it was 10 a Clock, if in the Afternoon 2 a Clock.

P R O B. III.

The day of the Month being given, to find the Sun's Place in the Ecliptick.

The Thread being laid to the Day of the Month, and where the said Thread crosses the Ecliptick, it shews there the Sun's place without more ado.

E X A M-

EXAMPLE.

Let the Day given be the 20th Day of *May*, to which Day bring the Thread, so will it fall upon 10 Deg. II, in the Ecliptick, the place of the Sun as was required.

PROB. IV.

The place of the Sun being given, to find the Day of the Month.

This is only the Converse of the former, for the Thread being brought to the Sun's place in the Ecliptick, will fall at the same time upon the Day of the Month.

EXAMPLE.

Let the Sun's place given be 10 Deg. II, the Thread laid thereon, it doth at the same time fall on the 20th Day of *May*, the thing required.

PROB. V.

The Hour of the Day being given, to find the Sun's Altitude.

Let the Bead be Rectified for the time, and then moved to the Hour of the Day, so doth the String fall on the Altitude of the Sun in the Limb of the Quadrant.

EXAMPLE.

Suppose the 20th Day of *May* (the Bead being Rectified to that time) at 9 of the Clock in the Forenoon, or 3 in the Afternoon, to which Hour bring the Bead, so will the String fall on 44 Deg. in the Limb of the Quadrant, which is the Sun's Altitude at that time, as was required.

PROB. VI.

The Hour of the Night being given, to find how much the Sun is depressed below the Horizon.

Note that the Sun is always as much below the Horizon, at any Hour of the Night as his opposite point is above the Horizon, at the same hour of the Day: Then, the Question being made for any Hour of the Night in Summer-time (the Bead being Rectified for the time) move the String till the Bead fall on the hour amongst the Winter-hours, otherways if it be any hour of the Night in Winter, then move the Bead to the Hour of the Day, amongst the Summer-Hours, so the Degree the thread falleth on
in

in the Limb, shews how much the Sun is depress'd below the Horizon at that time.

E X A M P L E.

Let it be required to know how much the Sun is below the Horizon the 20th day of May, at 2 of the Clock in the Morning, or 10 at Night, the Bead being Rectified, and brought to the Hour of 10 and 2, in the Winter-hours; so shall you find the Thread fall on 12 Deg. 30 Min. in the Limb of the Quadrant, and so much is the Sun below the Horizon at that time.

P R O B. VII.

The Sun's Depression being given, to find the Hour of the Night with us, or the Hour of the Day to our Antipodes.

First set the Bead according to the time; then bring the Thread to the Degree in the Limb of the Quadrant, to the Sun's Depression below the Horizon; so will the Bead fall (in the contrary Hour-lines) on the Hour of the Night with us, or hour of the Day to our Antipodes.

E X A M P L E.

The 20th day of May, the Sun being in 10 Deg. 11, and suppos'd to be depress'd 12 Deg. 30 Min. below the Horizon in the East, and the Bead set according to the Day; then bring the String to 12 Deg. 30 Min. in the Limb, the Sun's depression, so will the Bead fall (amongst the Winter-Hours) on the 2 a Clock-line; wherefore to our Antipodes 'tis 2 a Clock in the Afternoon, but to us 'tis 2 a Clock in the Morning.

P R O B. VIII.

The Sun's place or Day of the Month being given, to find when the Day breaks, and Twilight ends.

This Proposition is in Nature and Performance much like the former, for it is taken for granted that the Day is said to begin to break, and Twilight to end, when the Sun is just 18 Degrees below the Horizon, wherefore let the Bead be set for the time, then bring the Thread to 18 Degrees in the Limb, so will the Bead fall on the contrary Hour-lines (as before) and there shew the Hour of Twilight.

E X M P L E.

Let it be required to know at what hour in the Morning the Day breaks, or at what time of the Night Twilight ends, on the
D d d 20th day

20th day of *April*, the Sun being then in 11 Deg. 8 : First, set the Bead to the given line, then bring the Thread to 18 Deg. in the Limb, so doth the Bead fall on 20' before 2 a Clock in the Morning, for the time of the day breaking, or 20' before 10 at Night Twilight ends.

C H A P. VI.

The Use of the Azimuth-lines.

P R O B. I.

The Sun's Altitude being given, to find on what Azimuth he beareth from us.

THE Bead being set for the time, and the Sun's Altitude Observed as is taught in the first Proposition of the second Chapter; Then bring the Thread to the Complement of that Altitude, so will the Bead fall on the Azimuth required.

E X A M P L E.

The 20th Day of *April* (the Bead being set) you observe the Sun's Altitude 31 Deg, remove the Thread to the Complement of that Altitude, viz. 59 Deg. or which is all one, to 31 Deg. from the Right-side of the Quadrant, and the Bead will fall on the Azimuth-line 70 Deg. from the Meridian toward the *West*, if the observation was made in the Afternoon, or towards the *East* if the observation was made in the Morning,

P R O B. II.

The Azimuth the Sun bears from us being known, to find the Sun's Altitude.

This is but the converse of the former, for (the Bead first set to the time) 'tis but bringing it on to the Azimuth, so will the Thread fall on the Complement of the Sun's Altitude in the Limb, or upon his complete Altitude, by accounting from the Right-side of the Quadrant.

E X A M P L E.

The time given being the 20th Day of *April* (the Bead being set) and the Azimuth given 70 Deg. from the *South*, the Bead being brought there to the String falls on 59 Deg. in the Limb, whose comple-

complement, or distance from the Right-side of the Quadrant, is 31 Deg. the Sun's Altitude required.

The use of the Sun's Azimuth is chiefly necessary for finding a Meridian line, The Coasting of a Country, the Scituation, or Declination of a Building, and Variation of the Compass: But to treat of these severally, would be a digression, as not belonging to the use of the Quadrant.

C H A P. VII.

The use of the Double line of the Sun's Rising and Setting.

P R O B. I.

To find the time of the Sun's Rising and Setting.

First, rectifie the Bead to the time, then bring it to the Division in the Double line of the Sun's Rising and Setting, and it there falls upon the Hour and Minute of the Sun's Rising and Setting without further trouble.

E X A M P L E. I.

On the 20th day of *April*, I desire to know the exact time of the Sun's Rising and Setting: The Bead being set to the time, and brought to the time of the Sun's Rising and Setting, it falls on 40 Min. past 4 in the Morning, for the time of his Rising that day, and also on 20 Min. past 7 at Night for the time of his Setting.

E X A M P L E. II.

November the 2d day, the Sun's Rising and Setting is required: First set the Bead to the time, then bring it to the line of the Sun's Rising and Setting, and it there falls on 40 Min. past 7 in the Morning, for the time of his Rising, and on 20 Min. past 4 After Noon, for the time of Sun-Setting.

P R O B. II.

To find the length of the Day and Night.

For the length of the Day, 'tis but doubling the *Semi-Nocturnal* Arch, being the Hour and Minute of Sun-Setting and it gives

D d d 2

gives the length of the Day, and doubling the Sun's *Semi-Diurnal* Arch, or Hour and Minute of Sun-Set, the sum is the length of the Night.

E X A M P L E.

The 20th day of *April*, I desire to know the length of the Day and Night, and first

For the Length of the Day.

	b	'
20th day of <i>April</i> , Sun Sets at	7	20
<i>Simi-Nocturnal</i> Arch again	7	20
Length of the Day.	14	40

For the length of the Night.

20th day of <i>April</i> , Sun Rises at	4	40
<i>Semi-Diurnal</i> Arch again	4	40
Length of the Night.	9	20

C H A P. VIII.

For finding the Increase and Decrease of the Days.

First, let the Bead be Rectified to the time, and then moved to the line of the Increase and Decrease of the Days, so will the Bead shew how much the Day is either Increased or Decreased, according to the time of the Year.

E X A M P L E. I.

The 20th Day of *April*, I desire to know how much the Day is Increased: First, set the Bead for that time, then bring it to the lines of Increase and Decrease of the Days, so will the Bead fall on 7 Hours 22 Minutes, and so much are the Days Increased.

E X A M P L E II.

On the 2d day of *November*, I desire to know how much the Days are Decreased, first set the Bead for the time, then bring it to the aforesaid line, and the Bead will there fall on 8 Hours, and so much is the day Decreased.

These

These things are so plain and easy that they need no further explanation.

C H A P. IX.

The Use of the Line of Declinations.

P R O B. I.

*The day of the Month or place of the Sun being given,
to find his Declination.*

THE String laid upon the day of the Month, or upon the place of the Sun in the Ecliptick, so will the Thread at the same time fall on the Declination of the Sun in the Line of Declinations.

E X A M P L E.

The 20th Day of *May*, I desire to know the Sun's Declination, upon which Day I lay the Thread, or upon 10 Deg. of Π , the Sun's place at that time, so doth the String at the same time fall on 22 Deg. 2 Min. in the line of Declinations, being the Sun's Declination required.

P R O B. II.

*The Declination of the Sun being given, to find the day of the Month
and place of the Sun in the Ecliptick.*

This is the Reverse of the former, for the String laid to the Degree of the Sun's Declination, in the line of Declinations, so will the Thread at the same time fall on the Sun's place in the Ecliptick, and upon the day of the Month in the Circle of Months.

E X A M P L E.

The Sun's Declination given is 22 Deg. 2 Min. upon which in the line of Declinations lay the String, so will the Thread at the same time rest upon 10 Deg. Π , in the Ecliptick, which is the Sun's place at that time, and also upon the 20th day of *May*, in the Circle of Months.

C H A P. X.

The use of the line of Right Ascensions.


P R O B. I.

The place of the Sun or Day of the Month being given, to find the Sun's Right Ascension in Time.

LAY the String upon the Day of the Month, or on the place of the Sun in the Ecliptick, so will it fall (in the line of Right Ascensions) upon the Right Ascension of the Sun in time as was required.

E X A M P L E.

Let it be required to find the Sun's Right Ascension in time on the 30th day of *April* at Noon, at which time the Sun is in 20 Deg. 8, therefore lay the Thread on the 30th day of *April*, or on the 20 Deg. 8. at the same time the String falls on (in the line of Right Ascensions). 3 Hours 10 Min. the Sun's R. A. in time, as was required.

 Here Note, that 15 Deg. in the Limb, answers to 1 Hour in the line of Right Ascensions, and 30 Deg. to 2 Hours, &c. So that VI Hours in the line of R. A. is equal to 90 Deg. in the Limb, being the whole of both Circles and belongs to γ , δ , Π , then are these six Hours, or Divisions Numbred back again by VII, VIII, &c to XII. and the Signs belonging to them are ϖ , α , π ; Then beginning again and Number the same Divisions on again, by XIII, XIV, &c. to XVIII, which belongs to ϖ , π , ζ , and lastly upon the former Divisions Number the Hours back again by XIX, XX, &c. to XXIV hours, which belongs to η , ϖ , χ . Hence observe to make use of the proper Number of Hours according to the Signs they belong to.

P R O B. II.

Having the place of a Star, to find his R. A. in time.

Lay the Thread to the place of the Star in the Ecliptick, so doth it also at the same time (in the line of R. A.) fall on the Right Ascension of the Star.

E X A M P L E. I.

On the 18th Day of *April*, 1699 at Noon, I find by an *Ephemeris* that π is in 28 Deg. 7, therefore bring the String to 28 Deg.

28 Deg. 1, so doth it fall on 17 Hours 51 Min. in the line of R. A. and so much is the R. A. in time, according to his place in the Ecliptick at that time.

EXAMPLE II.

To find the R. A. of ♀ the 17th day of April. 1699, against which Year and Day at Noon, in the *Ephemeris*, I find his place 21 Deg. 30 Min. ♄, to which point in the Ecliptick bring the Thread, and it will also fall (in the Line of R. A.) on 23 hours 27 Min. which is the R. A. in time of Venus, as was required.

EXAMPLE III.

To find the R. A. in time of ♂ the 25th day of February, 1701, at which time by an *Ephemeris* I find ♂ in 24 Deg. 7; the Thread brought to that point in the Ecliptick, it doth at the same time fall on 1 Hour 29 Min. the thing demanded.

EXAMPLE IV.

To find the R. A. of ♄ the 16th day of July, 1701, at Noon, at which time by an *Ephemeris*, I find him in 0 Deg. 12, therefore laying the Thread upon that point in the Ecliptick, it will at the same time fall on 10 Hours 8 Min. for the R. A. of ♄ in time, the thing Sought.

These few Examples are sufficient to explain the whole Nature of this line of R. A. which hereafter we shall apply to the finding the Southing of the Planets and fixed Stars. This line is exact in the Numbering of Hours, and way of working tho' not admitting of equal divisions. And Note what is said against this may be understood of the Lines of Oblique Ascensions and Descensions, whose use is treated of in the following Chapter.

CHAP. XI.

The Use of the Lines of Oblique Ascensions and Descensions.

PROB. I.

The Sun's place being given, to find his Oblique Ascension or Oblique Descension.

Bring the Thread to the place of the Sun in the Ecliptick, so doth it fall on the Oblique Ascension of the Sun in the line of Oblique Ascensions.

EXAM-

EXAMPLE.

On the 30th day of *April* at Noon, I find the Sun to be in 20 Deg. 8, to which point in the Ecliptick bring the Thread, and you will at the same time find it fall (in the line of O. A.) on 1 Hour 34 Min. the O. A. of the Sun as was required.

For the Oblique Descension.

Lay the Thread to the opposite point of the Sun's place in the Ecliptick, and the Thread will fall on the Oblique Descension in the line thereof.

EXAMPLE.

Let the Oblique Descension at the time of the last example be required, to find which bring the Thread to 20 Deg. 11, which is the opposite point, so will the Thread fall on (in the line of O. D.) 16 Hours 48 Min. which is the O. D. of the Sun at that time.

PROB. II.

Having the Longitude and Latitude of a Planet or fixed Star, to find their Oblique Ascension or Descension.

The only difference between this and the last Proposition, is in respect of the Obliquity of the Ecliptick, for the Sun being always therein cannot be subject to Latitude, because Latitude is always accounted from the Ecliptick, but the Planets deviate more or less from it, according to their position, and the fixed are placed in several Latitudes, without being Subject to Variation tho' they have a Motion in Longitude according to the Progression of the Equinox.

Now to find the Oblique Ascension of a Planet or Star with Latitude, you are first to proceed as you are taught in the last proposition, by bringing the Thread to the place of the Star in the Ecliptick, so will it fall on the line of Oblique Ascensions, upon the Hour and Minute of the O. A. of the Star, which Note down, then observe this

RULE.

Rule, If the Star have *South-Latitude*, for every Degree thereof add 6 Min. to the O. A. before set down, but if *North-Latitude* then Subtract 6 Min. from the O. A. before found, so will the Sum or difference be the true O. A. required, and by this equation of adding or Subtracting of 6 Min. for every degree of Latitude, you shall have the O. A. at any time, without sensible error.

EXAMPLE.

EXAMPLE I.

The 1st. day of *November*, 1700, I find the Planet *Saturn* in 7 Deg. κ , with 2 Deg. of *South* Latitude, lay the Thread in the Ecliptick line to 7 Deg. κ , and the String will fall in the line of O. A. on 23 Hours 22 Min. now because *Saturn* hath 2 Deg. of *South* Latitude, I must add 12 Min. to 23 Hours 34 Min. the O. A. of $\frac{1}{2}$ for that time, with respect to his Longitude and Latitude.

EXAMPLE II.

Upon the 15th day of *November*, 1700. I find *Venus* in 18 Deg. \simeq , with 2 Deg. *North* Latitude; then, as before, bring the String to 18 Deg. \simeq , in the Ecliptick, and it falls on 13 Hours 43 Min. in the line of O. A. and because φ hath 2 Deg. of *North* Latitude, I Subtract 12 Min. from the 13 hours 43 Min, and the remainder is 13 Hours 31 Min. for the O. A. of *Venus*.

PROB. III.

For the Oblique Descension with Latitude

To find the Oblique Descension with Latitude, lay the Thread in the Ecliptick to the opposite Sign and Degree of the Planet or Star's place, so will the Thread fall on the O. D. in the line thereof, and by adding or Subtracting for every Degree of Latitude, (according to the Rule) 6 Min. by taking the Latitude of a contrary Denomination, so will the true Oblique Descension appear.

EXAMPLE.

Let it be required to find the O. D. of *Saturn*, the 1st day of *November*, 1700, at which time his place in Longitude is 7 Deg. κ , with 2 Deg. *South* Latitude: Lay the Thread in the Ecliptick to 7 Deg. κ , the opposite Sign and Degree, so doth the line fall on 9 Hours 47 Min. from which Subtract 12 Min. because I am to make use of the Latitude of a Contrary Denomination viz. *North*, according to the Rule, and there remains 9 Hours, 35 Min. the O. D. of $\frac{1}{2}$ as was required.

C H A P. XII.

To find the true time of any Planet or fixed Star's coming to the South.

TO the estimate time, find the Right Ascension of the Planet, or Star, as before is taught in the Xth Chap. and the Sun's R. A. for the same time, then Subtract the R. A. of the Sun, from the R. A. of the Star, or Planet (the Star's R. A. being Increased by 24 Hours, if need require) the Remainder is the true time of the Planet or Star's coming to the South.

E X A M P L E. I.

To know the true time of *Mars's* coming to the South the 1st day of *July*, 1700, which by his distance from the Sun, I guess may be about 7 at Night, *Mars* at that time is in 13 Deg. m , the String being brought to that Point in the Ecliptick, shews his R. A. (in the line of Right Ascensions) to be 14 Hours 42. Min. the Sun at the same time is in 20 Deg. e , whose R. A. (as before directed) is found 7 hours 27 Min. which taken from 14 hours, 42 Min. the R. A. of *Mars*, leaveth 7 Hours 15 Min. for the time of δ coming to the South that Night.

E X A M P L E. II.

To find the true time of *Venus's* coming to the South, the 1st day of *November*, 1700, at the estimate time thereof, *Venus* is in 3 Deg. e , and the Sun in 20 Deg. m , the R. A. of *Venus* by the Quadrant is found 12 Hours 10 Min. and the R. A. of the Sun 15 Hours 10 Min. Now because the Sun's R. A. is greater than the R. A. of *Venus*, I add 24 Hours to the R. A. of *Venus*, which makes the Sum 36 Hours. 10 Min. from which take the Sun's R. A. 15 Hours 10 Min. and the Remainder is 21 Hours 0 Min. from which taking 12 Hours, there remains 9 Hours 0 Min. in the Morning, for the time of *Venus* coming to the South.

E X A M P L E. III.

The time of *Aldebaran's* coming to the South is required *November* the 1st day, 1700, whose Longitude is 5 Deg. 40 Min. II , and the Sun in 20 Deg. 30 Min. m , the R. A. of *Aldebaran* is found by the Quadrant 4 Hours 15 Min. and the Right Ascension of the Sun 15 Hours 12 Min. Now because 24 Hours must first be added to 4 Hours 15 Min. by reason Subtraction cannot be made, It makes the Sum 28 Hours 15 Min. from which Subtract 15 Hours 12 Min. the Sun's R. A. the remainder is

is 13 Hours 3 Min. or 3' past 1, in the Morning, for the true time of *Aldebaran's* coming to the South.

C H A P. XIII.

To find the time of the Planets and fixed Stars Rising and Setting.

FIND the Oblique Ascension of the Planet or Star with Latitude, as is taught in the 11th Chapter, for the time given, and also the Oblique Ascension of the Sun for the same time: Then Subtracting the O. A. of the Sun, from the O. A. of the Star or Planet, and to the remainder add the time of the Sun's Rising, and if the Sum exceed 24 Hours, take 24 Hours from it; so is the Sum or difference the true time of the Planet or Star's Rising.

E X A M P L E. I. Of the Rising.

Let it be required to find the true time of *Jupiter's* Rising, the 1st. day of *February*, 1700, at which time he is in 19 Deg. 30 Min. \approx with no Latitude, the Sun at the estimate time of the Star's Rising is in 23 Deg. 30 Min. \approx ; then find the O. A. by the Quadrant as is directed in the XIth Chap. and place them down as here.

	<i>h</i>	<i>'</i>
O. A. of \approx , by the Quadrant is	21	34
to which add	24	00
O. A. of \approx Increased by 24 Hours is	45	34
O. A. of the Sun Subtract	22	59
	22	35
Time of Sun-Rising add	7	10
	29	45
24 Hours Subtract	24	00
	5	45
Hence the time of \approx 's Rising is at		
That is 45' past 5 in the Morning		

E X A M P L E. II. of the Rising.

The 10th day of *March*, 1700, I desire to know what time the *Virgin's Spick* rises, at which time he is in 90 Deg. 40 Min. \approx ,
 'E e e 2 with

with 2 Deg. *South-Latitude*, the Sun at the estimate time of the Star's Rising is in 1 Deg. 20 Min. γ ; then find by the Quadrant the O. A. of the *Virgin's Spick* with Latitude, as in the 2d Prob. of the XIth Chapter, and the Sun's O. A. also, then by Substracting the O. A. of the Sun, from the O. A. of the Star, and to the difference or remainder, add the time of the Sun's Rising, to which Sum, Add 12 Min. for the 2 Deg. of *South-Latitude*, according to the Rule, and the Remainder is the true time of the *Virgin's Spick's* Rising that Night.

The Operation.

	<i>h</i>	<i>'</i>
O. A. of the <i>Virgin's Spick</i>	13	54
O. A. of the Sun Subtract	0	02
	<hr/>	
	13	52
Remainder		
The time of Sun-Rising add	6	00
	<hr/>	
	19	52
Sum		
Because it exceeds 12 Hours Subtract	12	00
	<hr/>	
	7	52
Remains		
According to the Rule add	0	12
	<hr/>	
Hence the <i>V. Spick</i> Rises that Night at	8	04
That is 4 Min. past 8 at Night.		

For the Setting of the Stars

Find the Oblique Descension of the Planet or Fixed Star, with Latitude (if it have any) as is taught in the 3d Prob. of the XIth Chap. and likewise the Oblique Descension of the Sun, then Substract the O. D. of the Sun, from the O. D. of the Star, and to the remainder add the time of Sun-setting, then to, or from that sum, add or Substract for the Latitude (if the Star have any) according to the Rule, so will the Sum or Remainder be the true time of the Star's Setting

E X A M P L E. I. Of the Setting,

Let it be required to find what time of the Night *Venus* sets the 1st. day of *March*, 1700; *Venus's* place at the estimate time of Rising is 20 Deg. 20 Min. γ with no Latitude, the Sun's place at that time 22 Deg. 30 Min. κ .

Hence

	Hence the	<i>h</i>	<i>'</i>
O. D. of <i>Venus</i> is		13	56
O. D. of the <i>Sun</i> is		11	17
		<hr/>	
	difference	2	39
Time of Sun-Setting add		5	42
		<hr/>	
<i>Venus</i> Sets that Night at		8	21

That is 21 Min. past 8 at Night.

E X A M P L E. II. Of the Setting.

Let it be required by the Quadrant, what Hour of the Night the *Pleiades* Sets the 14th day of *March*, 1700, at which time the Seven Stars are in 25 Deg. 48 Min. 8, with 4 Deg. *North*-Latitude; the Sun's place at the Estimate time is 5 Deg. 30 Min. 7, then find the O. D. of the *Pleiades*, as in the 3d Prob. of the XIth Chapter, and the Sun's O. D. also for the same time, &c.

See the Work.

		<i>h</i>	<i>'</i>
O. D. of the <i>Pleiades</i> is		17	23
O. D. of the <i>Sun</i> Subtract		12	33
		<hr/>	
	Remainder	4	50
Time of Sun-Setting add		6	09
		<hr/>	
	Sum	10	59
For the Lat. (according to the Rule) add		00	24
		<hr/>	
Hence the Seven Stars Set that Night at		11	23

That is 23 Min. past 11 at Night.

Here Note, that I have apply'd the Minutes respecting the Latitude to the last Sum, which according to the Rule should have been apply'd to the O. A. or O. D. of the Star: But as it makes no alteration in the Work, each Person is at his Liberty to apply it to which place he pleases.

C H A P. XIV.

The Description of the Lines on the back-side of the Quadrant.

I. **T**HE several Circular lines, as they are divided, make a complete Table of Houses for the Latitude of 52 Deg. The bottom Circle is divided into 24 equal parts, or hours, being the line Intituled, Time from Noon. The next above it, is the line of the Xth House; the next above that, the Line or Table of the XIth House, the next is the XIIth, the next, the Ascend. The next above the Ascend. is the IId; and the uppermost is the line of the IIIId, and are Projected into the Quadrant from a Table of Houses for the Latitude of 52 Degrees.

II. On either side of the Quadrant, betwixt the Circular lines of Houses and the Centre, is placed 4 lines, viz. 2 on the Right-side, and 2 on the Left-side, viz. First, a line of Diameters, and Secondly, a line of Circumferences, agreeing thereto; On the Right-side is, First a line of Areas, shewing the Area or Superficial Content of a Circle, agreeing to the former lines of Diameters and Circumferences; and Secondly, a line of Square-Roots, shewing the true Square any Circle will bear according to the Diameter, and Circumference, and Area thereof, which shews the Square equal of any Cylindrical Solid, agreeing to the Diameter, Circumference, and Area of the Circle upon the lines before described.

III. In the middle (to supply a Vacant place) I have Inferted An *Almanack* shewing the Year of our Lord, the Day of the Month, Dominical Letter, &c.

C H A P. XV.

The Use of the Table of Houses.

TO Erect a Figure of the Heavens for any time of the Day, it must first be understood, that *Astronomers* account their day from Noon to Noon, each *Astronomical* Day consisting of 24 Hours, so that 1 Hour after Noon is accounted the first hour of the Day, and 11 a Clock, or 1 hour before Noon, is accounted 23 hours from Noon, this being understood.

First, get the time of the Day you Intend to erect your Figure for, or time from Noon, for which time by the Quadrant (by an *Ephemeris*, or by calculation) find the Sign and Degree of

of the Sun's place: Then repair to the Quadrant, and in the line of the Xth House find the aforesaid Sign and Degree of the Sun's place, upon which lay the String: Then observe what Hour and Minute the String at that time falls in the bottom-line, or line of Time from Noon, to which add the time after Noon, upon which Number or Sum lay the Thread, in the line of Time from Noon, So will the Thread fall on the Cusps of the Six Oriental Houses, which place down in your Scheme, observing that their opposite Houses have opposite Signs and Degrees.

EXAMPLE

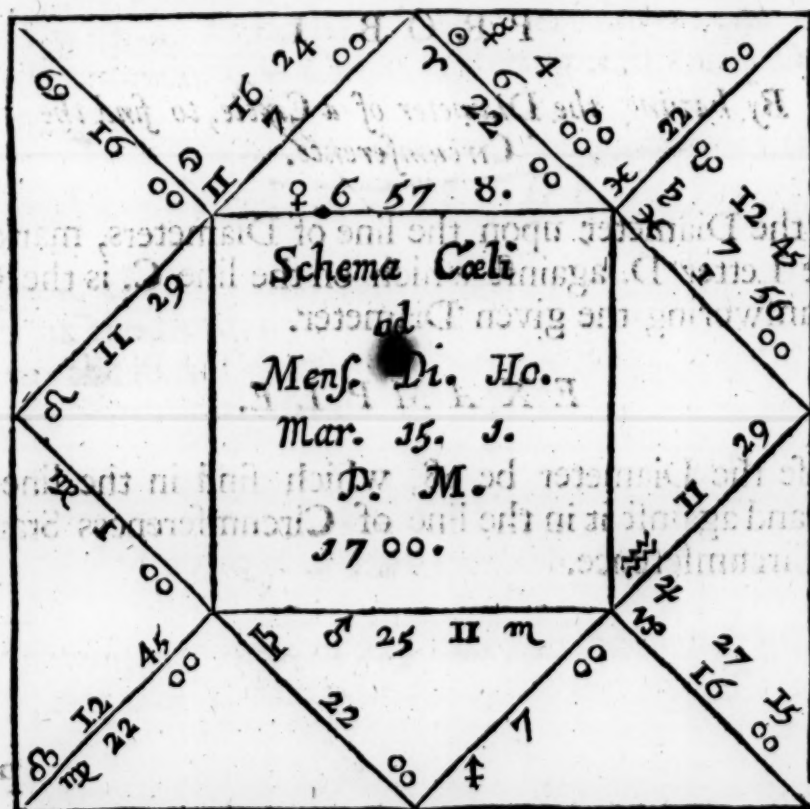
Let it be required to know how the Heavens are posited the 15th day of March, 1700. at 1 of the Clock in the afternoon, at which time (according to the 3d Prob. of the Vth Chapter) I find the Sun to be in 6 Deg. γ , to which bring the Thread in the line of the Xth House, so will it fall at the same time on 0 Hour 22 Min. in the line of Time from Noon, to which add 1 Hour, your Time from Noon, and the Sum is 1 Hour 22 Min. upon which, in the line of Time from Noon, lay the Thread, and it then falls upon the Six Oriental Houses as followeth.

Six Oriental Houses.

Six Occidental Houses.

X.	22°	00'	γ^s	Opposite Houses have Opposite Signs and Degs	IV.	22°	00'	π^s
XI.	7	00	Π		V.	7	00	ζ
XII.	16	00	\S		VI.	16	00	\wp
I.	11	29	Ω		VII.	11	29	\approx
II.	1	00	\mathfrak{M}		VIII.	1	00	\times
III.	22	00	\mathfrak{M}		IX.	22	00	ϵ

Which place into your Scheme in this following order..



Now the Planets places by the *Ephemeris*, at the same time, are thus.

{	h	7°	56'	♄ ^s	{	♀	6°	57'	♄ ^s
	x	27	15	♅ ^w		♄	4	00	γ
	♄	25	11	♆		♂	16	24	II
	♂	6	00	γ		♂	12	45	III

The ♅ is always opposite to ♄.

Now for the right placing of the Planets into the Scheme, observe this Rule, *viz.* If the Planet's place be less than the Cusp of the House, he is to be placed in; Then place him before the Cusp thereof, but if his Degrees be more than the Cusp of the House, then place him behind, as in the foregoing Scheme.

Note, that when the Hour answering the Sun's place in the Xth House, and Hours, or time after noon added, make more than 24 Hours, then Subtract 24 hours, and the remainder is the number to be made use of.

CHAP. XVI.

The Use of the Lines of Diameters, Circumferences, Areas, and Square-Roots.

PROB. I.

By having the Diameter of a Circle, to find the Circumference.

Find the Diameter upon the line of Diameters, marked with the Letter D. against which on the line C. is the Circumference answering the given Diameter.

EXAMPLE.

Suppose the Diameter be 28, which find in the line of Diameters, and against it in the line of Circumferences Stands 88.0 for the Circumference.

PROB.

P R O B. II.

By having the Circumference, to find the Diameter.

E X A M P L E.

Let us suppose the Circumference to be 88.0, which find in in the line of Circumferences, and against it in the line of Diameters stands, 28.0, for the Diameter, Answering to that Circumference.

And here let it be observed, that when either the Diameter or Circumference is given, the other answers thereto in the line thereof, and likewise doth the Circles of Areas, and Square-Roots, answer the Circles of the same Diameters and Circumferences, but because these two lines of Areas and Square-Roots, doe not joyn to the lines of Diameters and Circumferences, 'tis but moving the Bead upon the String to the Diameter or Circumference given, and then carrying it over to the lines of Areas, and Square-Roots, where the said Bead falls on both the Area, in the line of Areas, and Square-Root, in the line of Square-Roots, agreeing to both the Diameter and Circumference, the Bead was set to.

P R O B. III.

To find the Area of a Circle.

The Diameter or Circumference of a Circle, or both being given, to find the Area of the Circle Corresponding, 'tis but moving the Bead to the given Diameter or Circumference in their respective lines; Then transfer the Bead to the Scale of Areas of Circles, marked with A, so doth the Bead there fall on the Area, or Superficial content of that Circle, agreeing to the said Diameter and Circumference.

E X A M P L E.

Suppose the Diameter given 28.0, or Circumference 88.0, to which fix the Bead, in their respective lines; which done, transfer it to the line of Areas, and there it falls upon 616.00, for the Area, or Superficial content of that Circle.

P R O B. IV.

The Use of the Line of Square-Roots.

By having the Area of a Circle, to find the Square equal, or true Square that Circle will bear.

E X A M P L E.

Admit the Area of a Circle to be 400, which find in the line of Areas, against which in the line of Squares, marked with S, stands, 20.0, for the true Square that Circle will bear.

P R O B. V.

By having the Diameter, or Circumference of any Circle, to find what Square that Circle will bear.

E X A M P L E.

Suppose the Circumference of a Circle or Timber-Stick be 120.0, and its Diameter 38.2, to which, place the Bead in the respective line, or lines, then carry it over the line of Squares, and it there falls upon 33.85, for the true Square of such Circle or Timber-Stick.

Note, that the Thread that supplies the Foreside, coming thro' the Centre, may be extended to the Limb on the Backside, having a Bead put upon it, as the other side hath, but no Plummet.

C H A P. XVII.

*The Explanation and Use of the
A L M A N A C K.*

I. **U**nder the Title *Years*, is placed as many Years as the Table will bear, viz. from 1697, to 1758, in all 62 Years, on the top of which is plac'd the Seven Dominical Letters, which are fitted to the Years underneath them.

II. Under the Title *Sundays*, is first placed Figures gradually from 1 to 31, representing the several Sundays in each Month and Year, shewing what day of the Month each Sunday in any Month and Year will fall upon.

III. The Capital Letters placed in the Squares below, are Dominical Letters fitted to those Years, and Serve to direct to the day of the Month.

IV. The Months of the Year are placed against the Dominical Letters, for further Directions to what follows.

P R O B.

P R O B. I.

The Year of our Lord being given, to find the day of the Month.

I. First, find the Year you desire under the Title *Years*, and in the top of the same Column stands the Dominical Letter, answering to that Year.

II. Secondly, Seek the Month you desire against the Letter before found, over which in the same Column stands all the Sundays in that Month.

E X A M P L E. I.

Suppose it be required to find what day of the Month is the first Monday in *May*, 1700.

Find 1700 under the Title *Years*, and over it you will find F, then amongst the Months find *May*, from thence direct your Eye to F, in the same line, and over it you have all the Sundays in that Month, viz. the 5, 12, 19, and 26th day of *May*, are all the Sundays in that Month, so that Monday is the 6th day.

E X A M P L E. II.

Let it be required to know what day of the Month is the first Monday in *July*, 1715.

First, over the Year is found B, then against *July* over B, is found 3, 10, 17, 24, 31, that is the 3d day of *July*, is the first Sunday in that Month, for that Year, the 10th day is the Second Sunday &c. so that the first Monday in *July*, 1715, is the 4th day.

P R O. B. II.

Let it be required to know what day of the Week, any fixed Feast falls on.

This is in effect the same with the former, as we shall hereafter prove.

E X A M P L E.

Let it be required to know what day of the Week St. *James* falls on, 1700, it being always the 25th day of *July*.

I. Over the Year is found F. under the Title *Years*.

II. Under the Title *Sundays* against the Month *July*, and over F stands these Numbers. 7, 14, 21, 28, being the days of the Month, the Sundays happen; then observing the third Sunday is the 21st, by counting on, Thursday is found the 25th day, for the day of the Week St. *James* this Year falls on.

P R O B. III.

The Year of our Lord being known, to find what day of the Week is any day of the Month.

This is nothing but the Converse of the former, though altogether as useful.

E X A M P L E.

Let it be required to know what day of the Week is the 3d day of *July*, 1700, over which Year you will find F, then against *July* and over F, you'll find the first Sunday to be the 7th day, hence by counting backwards, Saturday 6, Friday 5, Thursday, 4, Wednesday 3.

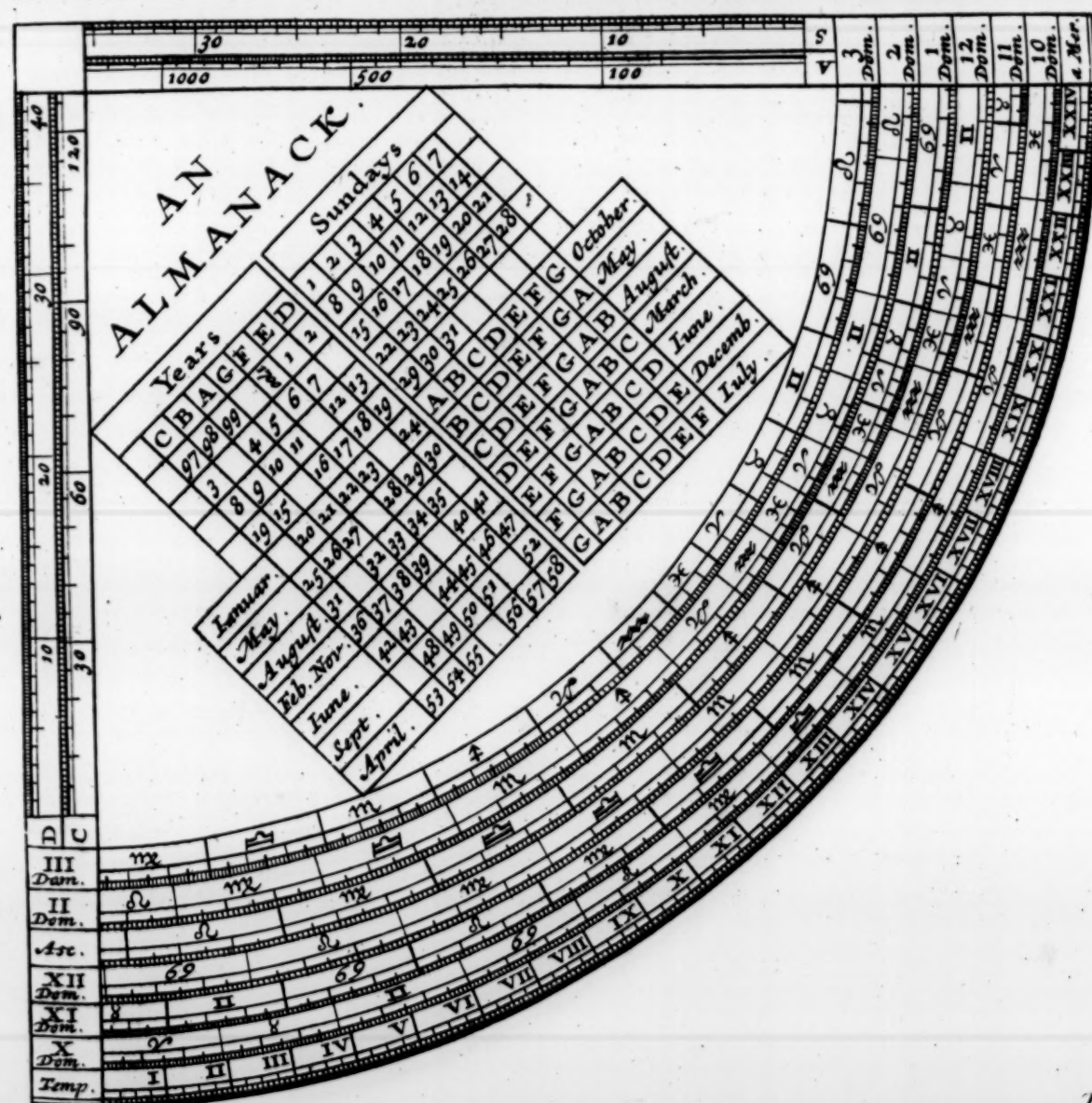
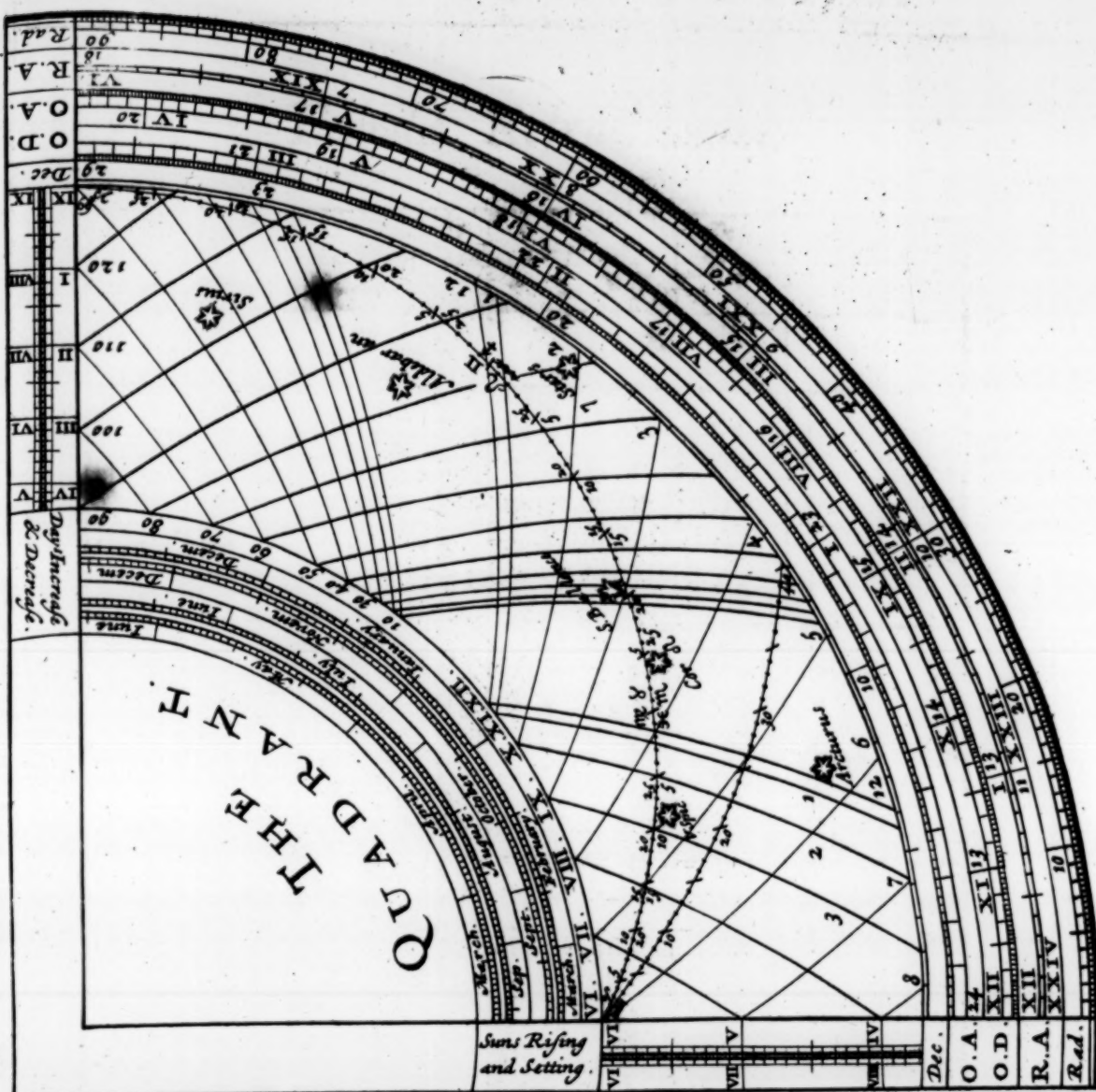
P R O B. IV.

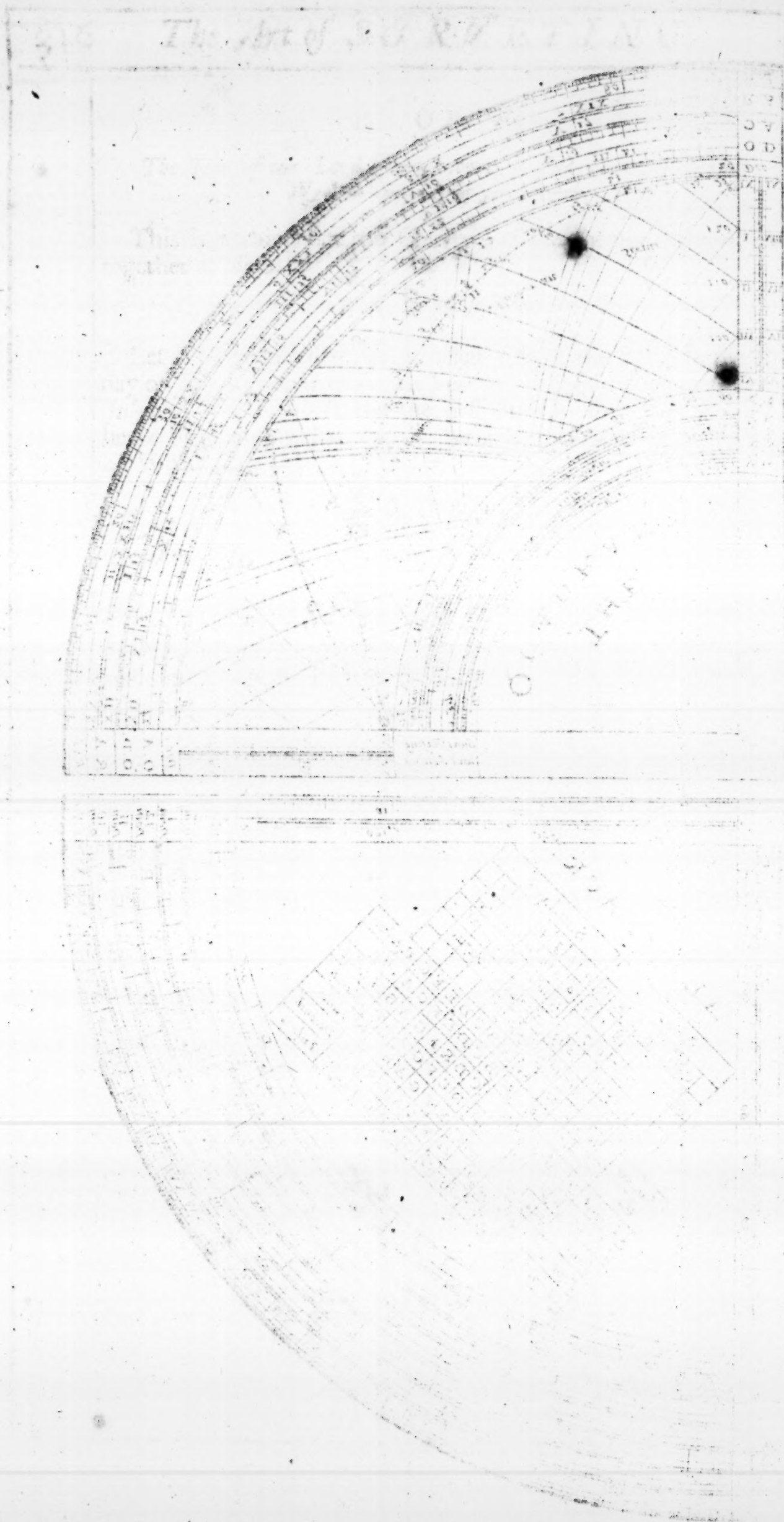
The Year of our Lord being given, to find the Dominical Letter for that Year.

Let it be required to know what the Dominical Letter is for the Year of our Lord 1701; seek the Year under the Title *Years* and over it is E the Dominical Letter for that Year.

*Here follows the Figure of the Quadrant,
Adjusted to the Latitude of 52 Deg.*

Tabula





Tabula Refractionum.

<i>Dist. à Vert.</i>	<i>Refract.</i>		<i>Dist. à Vert.</i>	<i>Refract.</i>		<i>Dist. à Vert.</i>	<i>Refract.</i>	
D.	'	"	D.	'	"	D.	'	"
1	0	1	31	0	30	61	1	27
2	0	2	32	0	31	62	1	31
3	0	2	33	0	32	63	1	36
4	0	3	34	0	33	64	1	40
5	0	4	35	0	34	65	1	45
6	0	5	36	0	35	66	1	50
7	0	6	37	0	36	67	1	55
8	0	6	38	0	37	68	2	1
9	0	7	39	0	39	69	2	7
10	0	8	40	0	41	70	2	14
11	0	9	41	0	42	71	2	22
12	0	10	42	0	44	72	2	31
13	0	11	43	0	46	73	2	40
14	0	12	44	0	47	74	2	50
15	0	13	45	0	49	75	3	3
16	0	14	46	0	51	76	3	16
17	0	15	47	0	53	77	3	32
18	0	16	48	0	55	78	3	48
19	0	17	49	0	57	79	4	9
20	0	18	50	0	59	80	4	35
21	0	19	51	1	0	81	5	5
22	0	20	52	1	2	82	5	42
23	0	21	53	1	5	83	6	30
24	0	22	54	1	8	84	7	32
25	0	23	55	1	10	85	8	55
26	0	24	56	1	12	86	10	53
27	0	26	57	1	15	87	13	55
28	0	27	58	1	18	88	18	24
29	0	28	59	1	21	89	25	12
30	0	29	60	1	24	90	30	0


A Table

A Table of Equation of time, shewing what a Pendulum-Clock or Watch ought to differ from a Sun-Dial.

	Jan.		Feb.		Mar.		April.		May.		June.	
D.	M.	S.	M.	S.	M.	S.	M.	S.	M.	S.	M.	S.
1	9	0	14	49	10	8	0	49	4	9	1	5
2	9	22	14	48	9	51	0	32	4	11	0	53
3	9	44	14	46	9	34	0	16	4	12	0	40
4	10	6	14	43	9	17	0	1	4	13	0	28
5	10	27	14	39	8	59	0	14	4	12	0	16
6	10	46	14	34	8	42	0	29	4	11	0	3
7	11	5	14	29	8	24	0	44	4	10	0	10
8	11	24	14	24	8	5	0	58	4	8	0	23
9	11	41	14	17	7	47	1	12	4	6	0	36
10	11	58	14	10	7	29	1	26	4	4	0	49
11	12	15	14	2	7	10	1	38	4	1	1	1
12	12	31	13	53	6	52	1	51	3	57	1	14
13	12	45	13	44	6	33	2	3	3	52	1	27
14	12	59	13	35	6	15	2	14	3	47	1	40
15	13	13	13	24	5	56	2	24	3	41	1	53
16	13	25	13	13	5	37	2	35	3	35	2	5
17	13	35	13	2	5	18	2	46	3	29	2	17
18	13	46	12	50	5	0	2	56	3	23	2	29
19	13	57	12	37	4	41	3	4	3	15	2	41
20	14	6	12	25	4	22	3	12	3	7	2	53
21	14	14	12	12	4	3	3	20	2	58	3	4
22	14	21	11	57	3	44	3	28	2	50	3	16
23	14	28	11	43	3	26	3	35	2	41	3	27
24	14	33	11	28	3	8	3	42	2	31	3	38
25	14	38	11	13	2	49	3	47	2	21	3	48
26	14	42	10	58	2	31	3	52	2	11	3	59
27	14	45	10	42	2	13	3	56	2	1	4	9
28	14	48	10	25	1	55	4	0	1	51	4	18
29	14	49			1	38	4	3	1	40	4	27
30	14	50			1	22	4	6	1	28	4	35
31	14	50			1	5			1	17		

A Table of Equation of Time, shewing what a Pendulum-Clock or Watch ought to differ from a Sun-Dial.

	July.		Aug.		Sep.		Octob.		Nov.		Dec.	
D.	M.	S.	M.	S.	M.	S.	M.	S.	M.	S.	M.	S.
1	4	43	4	30	3	48	13	14	15	23	5	42
2	4	gains. 51	4	gains. 20	4	loses. 9	13	loses. 28	15	loses. 15	5	loses. 13
3	4	gains. 58	4	gains. 10	4	loses. 29	13	loses. 42	15	loses. 5	4	loses. 45
4	5	5	4	0	4	50	13	56	14	55	4	loses. 16
5	5	11	3	49	5	10	14	8	14	45	3	47
6	5	17	3	37	5	31	14	20	14	33	3	17
7	5	gains. 23	3	gains. 24	5	loses. 51	14	loses. 31	14	loses. 29	2	loses. 47
8	5	gains. 28	3	gains. 11	6	loses. 12	14	loses. 41	14	loses. 6	2	loses. 17
9	5	32	2	58	6	33	14	51	13	52	1	loses. 48
10	5	35	2	44	6	53	15	1	13	38	1	18
11	5	38	2	30	7	14	15	11	13	21	0	* 48
12	5	gains. 41	2	gains. 16	7	loses. 34	15	loses. 20	13	loses. 4	0	* Gains. 18
13	5	gains. 43	2	gains. 2	7	loses. 54	15	loses. 26	12	loses. 47	0	loses. 12
14	5	45	1	46	8	14	15	32	12	28	0	loses. 42
15	5	46	1	30	8	33	15	38	12	9	1	12
16	5	46	1	13	8	53	15	44	11	50	1	41
17	5	gains. 45	0	gains. 56	9	loses. 13	15	loses. 49	11	loses. 30	2	gains. 10
18	5	gains. 44	0	gains. 39	9	loses. 32	15	loses. 52	11	loses. 9	2	gains. 39
19	5	42	0	21	9	52	15	55	10	47	3	loses. 08
20	5	40	0	3	10	11	15	56	10	25	3	37
21	5	38	0	14	10	30	15	58	10	2	4	05
22	5	gains. 35	0	* Loses. 31	10	loses. 48	15	loses. 59	9	loses. 38	4	gains. 32
23	5	gains. 31	0	loses. 50	11	loses. 6	16	loses. 0	9	loses. 14	5	gains. 00
24	5	27	1	9	11	24	15	59	8	49	5	27
25	5	22	1	29	11	41	15	57	8	23	5	55
26	5	16	1	49	11	58	15	55	7	57	6	21
27	5	10	2	7	12	14	15	52	7	31	6	loses. 48
28	5	3	2	27	12	loses. 29	15	loses. 48	7	loses. 5	7	gains. 14
29	4	56	2	47	12	45	15	43	6	38	7	loses. 39
30	4	48	3	8	13	0	15	37	6	10	8	4
31	4	39	3	28			15	31			8	27

 The Table of Refractions I had from that unparallel'd Artist Mr. John Flamsted, by whose Observations (in a little time) we hope to see Astronomy more gloriously array'd.

The Use of the Table of Refractions.

This Table is to be enter'd with the distance of the Sun, Moon, or Stars, from the *Vertex*, or *Zenith*, which is no more than the Complement of the Altitude to 90 Degrees.

E X A M P L E.

Suppose the Altitude of the Sun by Observation be 28 Deg. as page 289. its complement to 90 is 62 Deg. which is the distance from the *Vertex*, with which, enter the Table of Refractions, under the Title *Dist. à Vert.* Against which and under the Title *Refract.* is 1' 31" the Refraction Required, which taken from 28 Deg. the observed Altitude, there remains 27° 58' 29" for the correct Altitude of the Sun at the time of Observation.

The End of the Sixth B O O K.

THE
ART
OF
SURVEYING,
BOOK VII.

In Three PARTS.

CONTAINING,

- I. Several Problemes in Geography, and Spherical Trigonometry.
 - II. Astronomical Problemes.
 - III. A Practical Tract of the Art of Dialling.
-

Formerly Publish'd by

Mr *VINCENT WING*;

Now much Augmented and Enlarg'd by his NEPHEW,

JOHN WING, Math.

Whereunto are Added by the same Hand,

TABLES of Right and Oblique Ascensions in
Time, to five Degrees of North and South-
Latitude.

L O N D O N,

Printed, for *Awnsham and John Churchill*, at the *Black Swan*
in *Pater-Noster-Row*, MDCXCIX.

THE
Art of Surveying.
BOOK VII.

PART. I.

INTRODUCTION.

Although we have not hitherto treated of Sphærical Triangles (as being of little or no Use in the former parts of this Book) yet because the distance of Places upon the Terrestrial Globe, cannot precisely be Surveyed and determined without some knowledge therein, we shall here lay down some compendious Problems performed thereby, which no doubt will be very requisite and necessary for my Surveyor to make use of: For by the help and assistance thereof, He may both speedily and exactly, find the distance of any Cities and Places situate upon the Superficies of the Earth, as they are to be reckoned in a Sphærical line, which I have here added, in regard that in the former Books I have already shewed how the distance of any Places that lye under the Eye, may be discover'd, and truly found out by the solution of Right-lined Triangles; so that now there is not a place either near, or far remote, but (if the Longitude and Latitude be truly known) its bearing and distance may also be known and computed (and that with much celerity and exactness) as we shall demonstrate in the ensuing Problems, which no doubt will yield abundance of delight and recreation to all, though more especially to such, as have not yet tasted of things of this nature, wherein I shall in as plain a Method as may be, (though with some brevity) deliver what I intend upon this Subject, and refer such as are more curious, and delight in varieties, to my *Astronomia Britannica*. But first it will not be unfit, to shew what the Longitude and Latitude of a place is, and how the distance of one place from another, is represented to the Eye, according to the projection of the Sphere.

I. The Longitude of a place is the distance thereof from the Fortunate Islands beyond *Portugal*, which is called the Primary Meridian, from whence the Longitude of all places upon the Earth, are numbered in the Equinoctial, towards the *East*.

II. The Latitude of a place is the distance thereof, from the Equinoctial Circle, which is numbered in the Meridian, towards one of the Poles.

III. The distance of two places is an Arch of a great Circle, passing through both the said places, and is the shortest space between them, upon the Earth's superficies.

Although the Longitude of a place may be had, and found out several ways, yet the most exact of all other is by the Moon's Eclipse. As suppose the Moon's Eclipse should begin at *London*, at 8 a Clock and 55 Min. at Night, and the same Evening it is observed to begin at *Rome*, at 9 a Clock and 46 Min. the difference will be 51 Min. or 12 Deg. and 45 Min. which added to the Longitude of *London* 24 Deg. 20 Min. pointeth out the Longitude of *Rome*, 37 Deg. and 5 Min.

The Latitude of a place may be taken any Day in the Year, by the height of the Sun at Noon, and by the help of his Declination; for if the Sun have *South* Declination, add to the same his Altitude observed by a Quadrant, being corrected by Parallax and Refraction; or if he have *North* Declination, Subtract the same from his Altitude observed, and you shall have the complement of the Elevation of the Pole.

E X A M P L E.

The 10th Day of *April* 1661, the Sun at Noon, (according to my *Ephemerides*) was in 0 Degrees. 52 Minutes. *Taurus*, having *North* Declination 11 Deg. and 49 Min. at which time, his true Meridian Altitude was observed here at *Luffenham* to be 49 Deg. and 9 Min. therefore, according to the Rule, because he hath *North* Declination, I Subtract the Declination out of the Altitude, and there remains 37 Deg. 20 Min. which is the complement of the Pole's Elevation.

But because there are already extant, particular Catalogues of the Longitude and Latitude of most Cities and places in the World, we shall not further insist upon this Business, but shall in the following Problems, shew how to investigate exactly the itinerary distance of any two places, upon the Globe of the Earth.

P R O B. I.

Two Places differing only in Longitude, to find their Distance.

FOR Explanation, observe that in the adjunct Diagram, the outermost Circle marked with the Letters P C M L, represents the primary Meridian of the Earth, C D B L, the Earth's Equinoctial, P the *North* Pole thereof, M the *South* Pole &c.

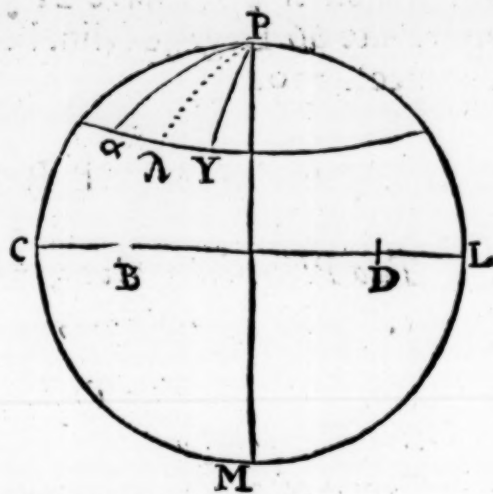
In

In this Problem are two Cases.

I. If both the places are under the Equinoctial, then the difference of their Longitude is the distance required.

E X A M P L E.

Suppose B to be the Island of *St. Thomas*, which hath Longitude 33 Degrees. and 10 Minutes. and D the Island of *Sumatra*, whose Longitude is 137 Deg. 10 Min. therefore the difference of their Longitude 104 Deg. converted into English Miles, by allowing 60 to one Deg. giveth 6240 for their distance.



II. If the two Places given are not situate under the Equinoctial, but lie under some parallel between the Equinoctial and one of the Poles, then take this Example.

In this Diagram, let α represent the City of *Compostella* in *Spain*, whose Latitude is 43 Deg. and γ the City of *Constantinople*, which hath the same Latitude, but differs in Longitude 44 Deg. wherefore to find their distance $\alpha \gamma$, take the half difference of their Longitude $\alpha \lambda$, or $\lambda \gamma$ 22 Deg. Then, in the Rectangled Triangle $\alpha \lambda P$, we have known (1.) αP , the Complement of the Pole's Elevation, 47 Deg. (2.) the Angle $\alpha P \lambda$, the half difference of the Longitude of the said Cities, 22 Deg. (3.) $P \lambda \alpha$, a right Angle 90 Deg. hence to find $\alpha \lambda$, I say,

As the Radius 90 Deg.	10.00000
To the the sine of the Angle $\alpha P \lambda$, 22 Deg.	9.57357
So the sine of $P \alpha$, 47 Deg.	9.86413
To the sine of $\alpha \lambda$, 15 Deg. 54 Min.	9.43770

Which doubled giveth their distance 31 Deg. 48 Min. which maketh 1908 English Miles.

P R O B II.

Two Places differing only in Latitude, to find their Distance.

In this Problem are also two Cases.

I. IF the two places propounded, do differ only in Latitude, and lye both of them on one side of the Equinoctial, you must Subtract the lesser Latitude from the greater, and the residue is the distance required.

Suppose therefore that one place have Latitude 22 Deg. 30 Min. *North*, and the other place 45 Deg. 50 Min. Now the difference is 23 Deg. 20 Min. which being converted into Miles, giveth the distance of the said two places 1400 Miles.

II. But

II. But if the two places propounded lye, the one on the *North* side the Equinoctial, and the other on the *South* side, then you are to add the two Latitudes together, and the Sum will give their true distance

E X A M P L E.

Suppose one place have 45 Deg. 50 Min. *North* Latitude, and the other place have 21 Deg. *South* Latitude, therefore their aggregate 66 Deg. 50 Min. being converted into Miles, gives their distance 4010.

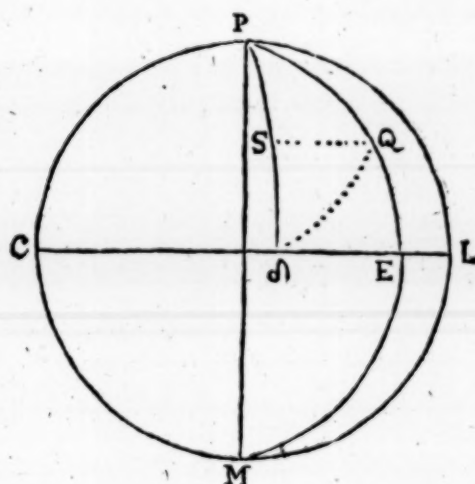
P R O B. III.

Two Places being given, which differ both in Longitude and Latitude, to find their Distance.

In this Problem are also two Cases.

I. IF one of the Places is situate under the Equinoctial, and the other toward one of the Poles, then take this Example.

Let δ represent the City of *Arim* (which of the *Arabian Astrologers* is called the Middle of the World) whose Longitude is 109 Deg. 5 Min. and is situate right under the Equinoctial. And let Q represent the City of *Quinsai*, which hath Longitude 152 Deg. 20. Min. and *North* Latitude 40 Deg. the distance of which two places is shewed by the Arch δQ . Wherefore in the Rectangled Triangle $\delta E Q$ are given (1.) δE the difference of their Longitude, 43 Deg. 15 Min. (2.) $E Q$ the Latitude of *Quinsai*, 40 Deg. (3.) $\delta E Q$ 90 Deg. Hence their distance δQ is inquired.



As the Radius 90 Deg.

To the Cofin. of $E Q$ 40 Deg.

So the Cofin. of δE 43 Deg. 15 Min

To the Cofin. of δQ 56 Deg. 5 Min.

10.00000

9.88425

9.86235

9.74660

Now the Arch δQ being reduced into miles, maketh 3365 *Italian* miles, which is the distance between *Quinsai* and *Arim*.

II. But if both the places are situate without the Equinoctial, their distance is to be sought by the solution of a Sphærical Triangle Obliquangle, as we shall demonstrate in the two following Examples.

E X A M-

the Promontory of Good-hope, 35 Deg. and P R 90 Deg. (3)
 the Included Angle α P θ 34 Deg. which is the difference of the
 Longitudes of the said two places. Hence their distance $\alpha\theta$ may
 be found as before.

(1)

As the Radius 90 Deg.	10.00000
To the Tangent of P α 47 Deg.	10.03034
So the Cofin. of the Angle α P θ 34 Deg.	9.91857
To the Tangent of P K 41 Deg. 38 Min.	9.94891

	deg.	Min.
From the Arch P θ	125	00
Subtract P K	41	38
Refts K θ	83	22

(2)

As the Cofin. of P K 41 Deg. 38 Min.	9.87353
To the Cofin. of P α 47 Deg. 0 Min.	9.83378
So the Cofin. of K θ 83 Deg. 22 Min.	9.06295

To the Cofin. of $\alpha\theta$ 83 Deg. 57 Min.	18.89673
	9.02320

Whereunto answereth 5037 *Italian* Miles, which is the distance
 required.

The End of the first Part.

The

THE
Art of Surveying.
BOOK. VIII.

PART II.

INTRODUCTION.

WE have already delivered such *Problems Geometrical*, as are most necessary for every Surveyor to understand and Practice. And now to the end he may elevate and raise his Eyes (from off the Earth) to the contemplation of those glorious Bodies, the *Sun, Moon, and Stars*, I shall here, in the last place, give him a brief Survey (as it were) of the first *Rudiments of Astronomy*, whereby he may (in his vacant Hours) get a competent Knowledge of such conclusions, as are most meet and requisite for his use and purpose. And first of all (that I may proceed in an orderly method) I shall give you a Brief and succinct Explanation of the several Circles of the Sphere, and then shew how to resolve and perform Artificially, all the most useful and common Problems thereof.

An Explanation of the Circles of the Sphere.

First, I shall begin with the Equinoctial, otherwise called the Equator, which is the chief and principal Circle in the Sphere dividing the Heavens in the Middle between the two Poles: to which when the Sun cometh, he maketh the Days and Nights of an equal length throughout the World.

2. The Meridian is a great Circle passing through the *Poles* of the *World* and the *Zenith* of the place, unto which when the *Sun* cometh, it is Noon: The number of Meridians are as many as
H h h there

there can be imagin'd Vertical Points, from the *West* to the *East*, whereof *Ptolomy* and other *Cosmographers* have described 180.

3. The *Vertical Point* or *Zenith*, is the Point directly over head, and is the Centre or Pole of the *Horizon*.

4. the *Nadir* is the opposite Point.

5. The *Horizon* is a great Circle dividing the visible part of the Heavens from the invisible; namely the superiour *Hemisphere* from the inferiour.

6. The *Zodiac* is a great Circle broad and fopewise, described upon its proper Poles, bearing the XII. Signs, and divideth the Equator into two equal parts, in the middle whereof is a line called the *Ecliptick*, or the way of the *Sun*; from which the Latitude of the Planets are numbered both *Northward* and *Southward*: The Circumference of this Circle contains 360 Degrees; which is divided into 12 equal Parts called Signs, every one representing some living Creature, either in Shape or Property: Again, every Sign containeth 30 Degrees, every Degree 60 Minutes, every Minute 60 Seconds, and every Second 60 Thirds, &c.

7. The *Solstitial Colure* is a great Circle drawn through the Poles of the World, the Poles of the *Zodiack*, and the Solstitial points of *Cancer* and *Capricorn*.

8. The *Equinoctial Colure* is a Circle passing by the Poles of the World, and the Equinoctial points, which intersects the Colure of the Solstices at right Angles in the Poles of the World.

9. The *Tropick of Cancer* is a lesser Circle of the Sphere equally distant from the Equinoctial *Northward*, 23 Degrees 31 Minutes 30 Seconds, wherein when the Sun is, he is entring *Cancer*, making his greatest *Northern* declination.

10. The *Tropick of Capricorn* is also a lesser Circle of the Sphere, equally distant from the Equinoctial *Southward*, 23 degrees, 31 minutes, 30 seconds, to which when the Sun cometh (which is about the tenth of *December*) he maketh his greatest *Southern* Declination.

11. The *Circle Artick* is so far distant from the *North Pole* of the World, as the *Tropick of Cancer* is from the Equinoctial, to which it is parallel; and so much are the Poles of the *Zodiac* distant from the Poles of the World.

12. The *Circle Antartick* is also parallel to the Equinoctial, and is distant from the *South Pole*, as much as the *Circle Artick* is from the *North Pole*, viz. 23 degrees, 31 minutes, 30 seconds.

13. *Azimuth*, or *Verticle Circles* pass through the *Zenith*, and intersect the *Horizon* with right Angles, wherein the distance of the Stars, from any part of the Meridian are accounted, which is call'd the *Azimuth*.

14. *Circles of Altitude* (called the *Almicantherat*) are Circles parallel to the *Horizon*, and intersect the vertical Circles with right Angles, which are greatest in the *Horizon*, and meet together in the *Zenith* of the place; In which Circles, the Altitude of the Stars above the *Horizon*, are accounted.

15. *Circles of Position* pass by the common Sections of the Meridian and *Horizon*, and by the Centre of the Star.

16. *Circles*

16. *Circles of the Cælestial Houses*, are such as divide the Heavens into twelve equal Parts.

17. *Circles of Declination* are drawn through the Poles of the World, and Points of the Equator.

18. *Circles of Latitude* are those that pass through the Poles of the Ecliptick, and the Body of the Star.

19. The *Axis* (or Axel-tree) of the World, is a supposed streight line drawn from the *North Pole* to the *South Pole*, about which the Motions of the Stars and Planets are performed.

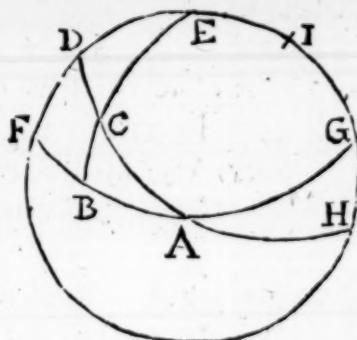
20. The *Elevation of the Pole* is the height thereof above the Horizon, which is equal to the *Zenith* and the *Equinoſtial*, whose complement is equal to the distance of the *Zenith* from the *North Pole*, or to the *Elevation of the Equator* above the *Horizon*.

Theſe Circles which are of moſt uſe, I here thought good to inſert, for if theſe be not perfectly known my Reader cannot well underſtand the following Problems of the Sphere that depend thereupon.

P R O B. I.

The Sun's place and greateſt Declination being given, to find the Declination of any Point required.

IN this Diagram let D F H G represent the ſolſtitial Colure, F A G the Equinoſtial, D A H the Ecliptick, A the point of the vernal Equinox, E C B a Meridian line paſſing through E the Pole of the Equator by the Centre of the Sun at C, and falling upon the Equator G A F at Right Angles in the Point B. Alſo let the Angle D A F be the Sun's greateſt Declination 23 Deg. 31 Min. A C the diſtance of the Sun from the begining of *Aries*, 30 Deg. and B C the declination of the Point ſought Wherefore in the rectangled Sphærical. Triangle A B C, we have given (1) the Hypothenuſe A C 30 Deg. (2) the Angle B A C 23 Deg. 31 Min. Hence to find B C, I ſay



As the Radius 90 Deg.

To the ſine of the Angle B A C 23 Deg. 31'

So the ſine of A C 30 Deg.

To the ſine of B C 11 Deg. 30'

Which is the Sun's Declination required.

10.00000

9.60099

9.69879

9.29996

P R O B. II.

The Sun's greatest Declination and his distance from the next Equinoctial point being given, to find his right Ascension.

IN the Triangle A B C we have given (as before) (1) The Angle of the Sun's greatest Declination B A C 23 Deg. 31 Min. (2) The Longitude of the Sun from the next Equinoctial point *Aries*, viz. A C 30 Deg. Hence, to find the right Ascension of the Sun A B, the Analogue is.

As the Radius 90 Deg.	10.00000
To the Tangent of A C 30 Deg.	9.76144
So the Cofin. of B A C 23 Deg. 31 Min.	9.96233
To the Tangent of A B 27 Deg. 53 Min	9.72377

Which 27 Deg. and 53 Min. is the Sun's right Ascension in 0 Deg. of *Taurus*: But here you are to observe, that if the right Ascension of the point sought, be in the Second Quadrant, $\approx \Omega$, then you are to take the complement of the Arch found to 180 Deg. if it be in the third Quadrant $\approx \pi$, add a Semicircle to the Arch found; but in the last Quadrant, Subtract the Arch found from the Circle 360 Deg. and you shall have the right Ascension desired.

II. Suppose the Sun in \approx 60 Deg. from the Equinoctial point \approx .

As the Radius 90 Deg.	10.00000
To the Tangent of 60 Deg.	10.23856
So the Cofin. of 23 Deg. 31 Min.	9.96233
To the Tangent of 57 Deg. 48 Min.	10.20089

Now the Complement hereof to 180 Deg. is 122 Deg. 12 Min. which is the Sun's right Ascension in 0 Deg. \approx .

III. Suppose the Sun in π 30 Deg. from the Equinoctial point \approx .

The work is the same as in the first Example, therefore to the Arch found 27 Deg. 53 Min. I add a Semicircle or 180 Deg. and the Sum 207 Deg. 53 Min. is the right Ascension of the Sun sought, in the first point of *Scorpio*.

IV. Suppose the Sun in \approx , 60 Deg. from the Equinoctial point. γ .

The Operation is the same with the Second Example, wherefore Subtract the Arch found 57 Deg. 48 Min. from the whole Circle 360 Degrees, and there will remain 302 Deg. 12 Min. which is the Sun's right Ascension in the first point of *Aquarie*.

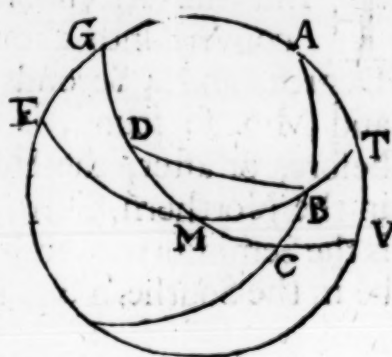
P R O B.

P R O B. III.

The Elevation of the Pole and Declination of the Sun being given, to find the Ascensional difference.

THE Ascensional difference is the quantity or difference between the Ascension of any point of the *Ecliptic* in a right Sphere, and the Ascension of the same point in an oblique Sphere.

In this Diagram, let A G E V represent the Meridian, E M Sth Horizon, G M V the Equator, A T the Pole's Elevation, B C the Sun's Declination, B D an Arch of the Ecliptic, D C the right Ascension, M B the Amplitude of his Rising and Setting, M C the Ascensional difference. Wherefore in the rectangled Spherical Triangle B C M are known, (1.) The Angle B M C the Complement of the Pole's Elevation, 37 deg. 30 min. (2.) The Sun's Declination B C 11 deg. 30 min. Hence to find the Ascensional difference M C, I say,



As the Radius, 90 Deg.	10.00000
To the Contangent of B M C, 37 Deg. 30 Min.	10.11502
So the Tangent of B C, 11 Deg. 30 Min.	9.30846
To the Sine of M C, 15 Deg. 22 Min.	9.42348

P R O B. IV.

The Sun's Right Ascension, and his Ascensional difference being given, to find his oblique Ascension and Descension.

TO perform this, you must observe the two following Rules.

1. If the Sun's Declination be North, you must Subtract the Ascensional difference from the right Ascension, and the residue will be the oblique Ascension, but if you add them together, the sum will be the oblique Descension.

2. If his Declination be South, add the Ascensional difference and right Ascension together, the sum will be the oblique Ascension; but if you make Subtraction, the Remainder will be the oblique Descension.

E X A M P L E.

Suppose the Sun be in the first point of *Taurus*, his right Ascension (by the second Problem) is 27 Deg. 53 Min. and his Ascensional difference (by the third) is 15 Deg. 22 Min. Therefore (according to the first Rule, because his Declination is North) the

the difference of them, 12 Deg. 31 Min. is the Sun's oblique Ascension, and the sum of them 43 Deg. 15 Min. is his oblique Defension.

P R O B. V.

To find the Time of the Sun's Rising and Setting, with the length of the Day and Night.

Find the Ascensional difference by the 3d Problem, which convert into Time, allowing 4 Min. of an Hour for every Degree, and 4 Seconds for every Minute, and the sum of Hours and Min. so found, is the difference of his Rising or Setting, before, or after, the Hour of Six. Therefore when the Sun is in the Northern Signs, add the same to Six, and the Aggregate is the Semidiurnal Arch, or Time of the Sun's Setting; but if he be in the Southern Signs, make Subtraction.

Thus in the former Example :

The Sun being in 0 Deg. of *Taurus*, having 11 Deg. 30 Min. North Declination, his Ascensional difference is found by the 3d Problem, 15 Deg. 22 Min. which converted into time, (as is above shewed) maketh 1 Hour, 1 Min. 28 Sec. and because the Sun is in a Northern Sign, I add the same to Six Hours, and the sum 7 Hours, 1 Min. 28 Sec. is the time of the Sun's Setting, when he enters *Taurus*, in the Latitude of 52 Degrees and an half; whence it follows, that he riseth at 4 a Clock, 58 Min. and 32 Sec. that the length of the day is 14 Hours, 2 Min. 56 Sec. and the length of the Night 9 Hours, 57 Min. 4 Sec.

P R O B. VI.

The Elevation of the Pole, and Declination of the Sun being given, to find his Amplitude of Rising and Setting.

IN the right Angled Spherical Triangle B C M of the 3d Problem, having the Angle B M C the height of the Equator, 37 Deg. 30 Min. and B C the Sun's Declination in 0 Deg. of 8, 11 Deg. 30 Min. his Amplitude M B may be thus found :

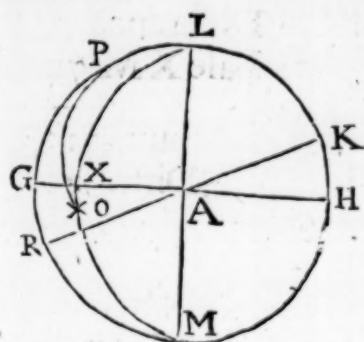
As the Sine of B M C, 37 Deg. 30 Min.	9.78445
To the Radius, 90 Deg.	10.00000
So the Sine of B C, 11 Deg. 30 Min.	9.29996
To the Sine of M B, 19 Deg. 8 Min.	9.51551

P R O B.

P R O B. VII.

The Elevation of the Pole, and Declination of the Sun being given, to find the just quantity of Twilight.

IN this Diagram, let L G M K represent the Meridian, G A H the Horizon, L the Zenith of the Place, M the Nadir, R A K the Equator, P the North Pole, O the Sun's Place in the Summer, X O the Depression of the Sun under the Horizon, 18 Deg. when the day-light is first of all said to break forth.



Now let us suppose, in the Latitude of 52 Deg. and an half, the Sun to be in 0 Deg. 8', having North Declination 11 Deg. 30 Min. we shall then have in the Triangle O P L all the sides given, to find the Angle L P O, therefore, work thus :

Sides	{ P O 78° 30' Com. of ☉ Decl. S. 9.991192	} Add.
	{ P L 37 30 Com. of the Elev. S. 2.784455	

Difference 41 0	19.77564---	1
Base L O 180 0	20.00000---	2

Sum 149 0	Semifum 74° 30'	9.983912	} Add.
Diff. 67 0	Semidiff. 73 30'	9.741895	

19.72580---

Arch Correspondent 70 Deg. 46 Min. 19.95016---

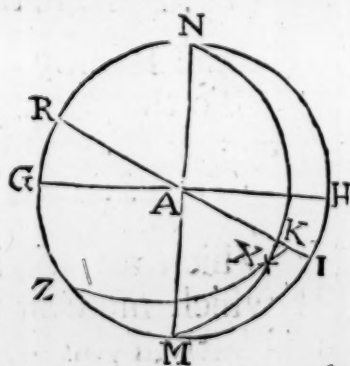
The half 9.97508

Whose double 141. 32 is the Angle L P O, which converted into Time, maketh 9 Hours, 26 Min. 8 Sec. which is the time of Twilight, or Day-light ending, when the Sun enters *Taurus*, in the North Latitude of 52 Degrees and an half.

But if it be required to find the time of Twilight, when the Sun hath South Declination, then Subtract the quantity of the Sun's Depression under the Horizon, 18 Deg. from the Quadrant 90 Deg. and there will remain the distance of the Sun from the Nadir 72 Deg. which done, the Operation will (in a manner) be the same as before.

E X A M P L E.

Let us suppose the Sun be in the opposite point to the former, viz. in 0 Deg. 30 Min. wherefore in the Triangle Z X M we have given, (1.) Z X the Complement of the Sun's Declination 78 Deg. 30 Min. (2.) X M the distance of the Sun from the Nadir, 72 Deg. (3.) Z M



the

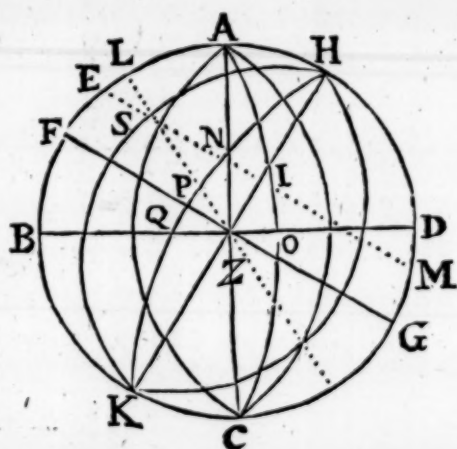
the Complement of the Elevation, 37 Deg. 30 Min. hence to find the Angle, X Z M the work will stand thus :

Sides	{ Z X	78° 30'	Com. ° Decl. S.	9.991192	} Add.
	{ Z M	37 30	Com. Elevat. S.	9.784455	
Difference	41	0		19.77564	---1
Base X M	72	0		20.00000	---2
Sum	113	0	Semi. 56° 30'	9.921102	} Add.
Diffe.	31	0	Semi. 15 30	9.426905	
				19.34800	---3
				19.57236	---4
The Corresp. Arch,	37° 40'.	The half		9.78618	

Whose Double 75 Deg. 20 Min. is the Angle M Z X, which in Time is 5 Hours, 1 Min. 20 Sec. for the Time of Day-break, when the Sun enters π , in the Latitude of 52 Deg. and an half.

P R O B. VIII.

The Latitude of the Place, and the Sun's Declination being given, to find the Time when he will be East or West.



IN this Diagram, let A B C D represent the Meridian, F G the Equinoctial, B D the Horizon, H N K an Arch of the Sun's Meridian, A Z C the vertical Circle of the East and West Points, E N M a Parallel of Declination; and lastly, the Angle A H N, an Arch of the Equinoctial; F P is the term desired.

Let us suppose the Sun in \circ Gemini, having North Declination, 20 Deg. 13 Min. and it's required to find the time when he will be due East or West in the Latitude of 52 Deg. and an half.

Therefore in the right Angled Sphærical Triangle A H N are given, (1.) A H the Complement of the Pole's Elevation, 37 Deg. 30 Min. (2.) H N the Complement of the Sun's Declination, 69 Deg. 47 Min. then I say,

As the Radius	10.00000
To the Cotangent of H N 69 Deg. 47 Min.	9.56615
So the Tangent of A H 37 Deg. 30 Min.	9.88498
To the Sine of A H N 73 Deg. 35 Min.	9.45113

Which reduced into Time, giveth 4 Hours 54 Min. 20 Sec. at which moment in the Afternoon, the Sun will be due West; and lastly, if you substract the Hours and Min. thus found from 12, there

there remaineth 7 Hours, 5 Min. 40 Sec. for the Time in the Morning when he is due East.

P R O B. IX.

The Elevation of the Pole, and Declination of the Sun being given, to find the Sun's Altitude when he cometh to be due-East or West.

IN the former Diagram, the Sun's Altitude when he is due-East or West, is shewed by the Arch N Z, wherefore in the Triangle Z Q N we have given, (1.) The Sun's Declination in \circ II, 20 Deg. 13 Min. (2.) The Angle of the Pole's Elevation, N Z Q, 52 Deg. 30 Min. hence to find his Altitude Z N, I say,

As the Sine of the Angle Q Z N, 52 Deg. 30 Min.	9.89946
To the Radius, 90 Deg.	10.00000
So the Sine of the \odot Decl. QN, 20 Deg. 13 Min.	9.53854
To the Sine of his Altitude Z N, 25 Deg. 49 Min.	9.63908

P R O B. X.

The Elevation of the Pole, and Declination of the Sun being given, to find the Sun's Altitude at the Hour of Six.

IN the Diagram of the 8th Problem, we have known, in the Triangle A I H, (1.) The Complement of the Pole's Elevation A H 37 Deg. 30 Min. (2.) The Complement of the Sun's Declination H I 69 Deg. 47 Min. Hence the Hypothenufe A I is inquired, therefore I say,

As the Radius, 90 Deg.	10.00000
To the Cosine of H I, 69 Deg. 47 Min.	9.53854
So the Cosine of A H, 37 Deg. 30 Min.	9.89945
To the Cosine of A I, 74 Deg. 5 Min.	9.43800

Whose Complement I O, 15 Deg. 55 Min. is the Sun's Altitude at the Hour of Six, when he enters *Gemini*, in the Latitude of 52 Deg. and an half.

P R O B. XI.

The Latitude of the Place, and Declination of the Sun being given, to find the Sun's Azimuth at the Hour of Six.

IN the right Angled Spherical Triangle A H I of the last Diagram, we have known, (1.) A H the Complement of the Pole's Elevation 37 Deg. 30 Min. (2.) H I the Complement of the Sun's Declination 69 Deg. 47 Min. Hence to find the Azimuth of the Sun at the Hour of Six, represented by the Angle H A I, I say,

As the Radius, 90 Deg.	10.00000
To the Sine of A H, 37 Deg. 30 Min.	9.78445
So the Cotangent of H I, 69 Deg. 47 Min.	9.56615
To the Cotangent of H A I, 77 Deg. 22 Min.	9.35060

Which is the Azimuth of the Sun from the North part of the Meridian, at the Hour of Six, when he enters *Gemini*, in the North Latitude of 52 Degrees and an half.

P R O B. XII.

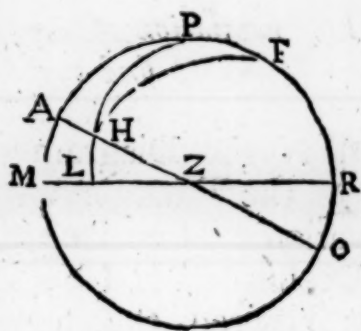
The Elevation of the Pole, the Declination of the Sun, and his Distance from the Meridian being given, to find the Sun's Altitude at any time assigned.

In this Problem are Three Cases.

First, *If the Sun be in the first Point of Aries or Libra.*

IN this Diagram, let P M R represent the Meridian, A Z O the Equator, M Z R the Horizon, H the place of the Sun, A H his distance from the Meridian, which (*for Example sake*) let us here suppose to be two Hours, or 30 Degrees.

Wherefore in the Triangle P A H, we have given, (1.) A P the distance of the Zenith from the Equator, equal to the Pole's Elevation, 52 Deg. 30 Minutes. (2.) A H the distance of the Sun from the Meridian, 30 Deg. Hence to find the Sun's Altitude L H, I say,



As the Radius, 90 Deg.	10.00000
To the Cosine of A H, 30 Deg.	9.93753
So the Cosine of A P, 52 Deg. 30 Min.	9.78445
To the Cosine of P H, 58 Deg. 11 Min.	9.72198

Whose Complement L H, 31 Deg. 49 Min. is the Sun's Altitude required.

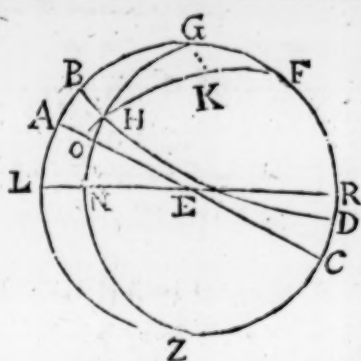
Secondly, *When the Sun is in the North Signs, γ , δ , Π , \ominus , Ω , π .*

In the Diagram annexed, let G L Z R represent the Meridian, A E C the Equinoctial, F the North Pole of the World, L E R the Horizon, G the Zenith, B H D a Parallel of the Sun's Declination, F H O the Meridian of the Sun, B H B F H the distance of the Sun from the Meridian of the place, O H the

the Sun's Declination North, G F the Complement of the Pole's Elevation.

Let it be required to find the Sun's Altitude at 9 of the Clock before Noon, when he enters *Gemini*, in the North Latitude of 52 Deg. 30 Min. wherefore in the Triangle F G H we have known, (1.) G F the Complement of the Pole's Elevation, 37 Deg. 30 Min.

(2.) F H the Complement of the Sun's Declination, 69 Deg. 47 Min. (3.) The comprehended Angle G F H, the distance of the Sun from the Meridian 30 Deg. Hence to find G H, and consequently the Sun's Altitude N H, I say,



(1.)

As the Radius, 90 Deg.

10.00000

To the Tangent of F G, 37 Deg. 30 Min.

9.88498

So the Cosine of the Angle G F H, 30 Deg.

9.93753

To the Tangent of F K, 33 Deg. 36 Min.

9.82251

From the Complement of the Sun's Declination F H, 69 Deg. 47 Min. Subtract F K, 33 Deg. 36 Min. there remains K H, 36 Deg. 11 Min.

(2.)

As the Cosine of F K, 33 Deg. 36 Min.

9.92060

To the Cosine of G F, 37 Deg. 30 Min.

9.89946

So the Cosine of K H, 36 Deg. 11 Min.

9.90694

19.80640

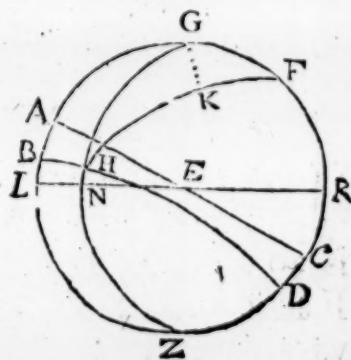
To the Cosine of G H, 39 Deg. 45 Min.

9.88580

Whose Complement N H, 50 Deg. 15 Min. is the Sun's Altitude above the Horizon, at 10 a Clock in the Morning, or at 2 in the Afternoon, when he enters *Gemini*, in the Latitude of 52 Deg. and an half, North.

Thirdly, When the Sun is in the Southern Signs, ♊, ♋, ♌, ♍, ♎, ♏.

Suppose the Sun in the Winter Season be in the opposite Point to the former, having Southern Declination, 20 Deg. 13 Min. and be also distant from the Meridian 30 Deg. therefore in this Diagram, we have given, in the oblique-angled Triangle G F H (1.) F G as before, 37 Deg. 30 Min. (2.) F H 110 Deg. 13 Min. the sum of the Quadrant added to the Sun's Declination, (3.) The Angle G F H, 30 Deg. Hence to find the Sun's Altitude N H, I say, as before.



I i i 2

(1.) As

(1.)

As the Radius, 90 Deg.	10.00000
To the Tangent of F G, 37 Deg. 30 Min.	9.88495
So the Cofine of the Angle G F H, 30 Deg.	9.93753
To the Tangent of F K, 33 Deg. 36 Min. as before	9.82251

From the Arch F H, 110 Deg. 13 Min. subtract the Arch F K, 33 Deg. 36 Min. and there rests K H, 76 Deg. 37 Min.

(2.)

As the Cofine of F K, 33 Deg. 36 Min.	9.92060
To the Cofine of G F, 37 Deg. 30 Min.	9.89946
So the Cofine of K H, 76 Deg. 37 Min.	9.36448

To the Cofine of G H, 77 Deg. 16 Min.	19.26394
	9.43343

Now the Complement of G H is N H, 12 Deg. 44 Min. which is the Sun's Altitude required.

P R O B. XIII.

The Sun's Altitude, his Distance from the Meridian, and Declination being given, to find his Azimuth.

IN the oblique-angled Sphaerical Triangle G F H of the 2d Diagram of the last Problem, we have known, (1.) G H the Complement of the Sun's Altitude, 39 Deg. 45 Min. (2.) The Angle G F H the distance of the Sun from the Meridian, 30 Deg. (3.) F H the Complement of the Sun's Declination, 69 Deg. 47 Min. Then to find the Sun's Azimuth, I work thus:

As the Sine of G H, 39 Deg. 45 Min.	9.80580
To the Sine of the Angle G F H, 30 Deg.	9.69897
So the Sine of F H, 69 Deg. 47 Min.	9.97238

To the Sine of F G H, the Sun's Azimuth, 47 D. 12 M.	19.67135
	9.86555

P R O B. XIV.

The Pole's Elevation, with the Sun's Altitude and Declination given, to find the Sun's Azimuth.

IN the oblique-angled Triangle G H F of the 12th Problem, Second Example, the Complement of the Sun's Altitude G H is 39 Deg. 45 Min. the Complement of the Sun's Declination F H 69 Deg. 47 Min. and the Complement of the Pole's Elevation G F, 37 Deg. 30 Min. which known you may frame your Operation thus:

Sides

Sides	{	GH	39	Deg.	45	Min.		9.805802	} Add
	{	GF	37		30			9.784455	
Difference			2		15			19.59025	-----1
Base FH			69		47			20.00000	-----2
Sum			72		2	Semi.	36° 1'	9.769392	} Add
Difference			67		32	Semi.	33 46	9.744935	
								19.51432	-----3
								19.92407	-----4
								9.96203	

The Corresp, Arch 66° to half 24'

The Corresp, Arch 66° to half 24'

Whose double 132 Deg. 48. Min. is the Angle F G H, now the Complement thereof 47 Deg. 12 Min is the Angle B G H, which is the Sun's Azimuth as before.

The End of the Second Part.

THE

T H E
Art of Surveying.
B O O K. VII.

P A R T III.

I N T R O D U C T I O N.

WE now proceed to give our Surveyor some *Problems* of *Horologigraphy*, shewing how to Calculate and Describe the *Horizontal*, and all sorts of *Mural Sun-Dials*, whether *Direct* or *Declining*: And (though it is not our intention in this place to Treat of the whole Art of *Dialling*, yet) we shall shew him, how he may describe the most usual sorts, which are the *Horizontal*, the direct North and South, and the East and West Plans, together with the erect North and South Plans, declining East and West to any Declination given, according to the Projection of the Sphere.

P R O B. I.

To Describe the Horizontal Dial.

First we shall begin with the *Horizontal*, which is such a Plane, as is Parallel to the *Horizontal Circle* of the Sphere, whose Poles lie directly in the *Zenith* and *Nadir* of the place of your Habitation.

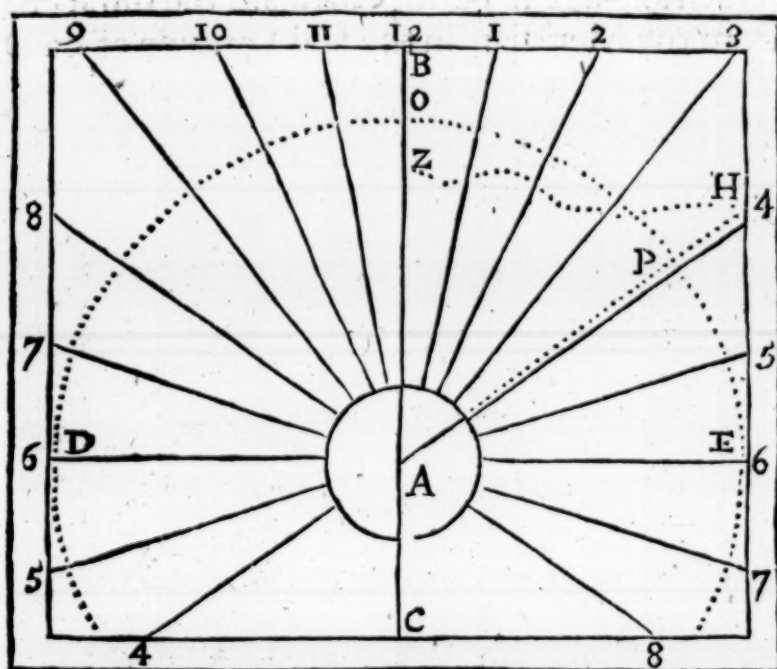
Before we come to the Calculation of the Hour-distances, draw the Meridian Line C A B, and cross the same with the Line D E, at right Angles, in the Point A, which Intersection must be the Centre of your Dial, and the Line so drawn, viz. D E is the Six a Clock-Line, then to draw the other Hour-Lines, say,

As

As the Radius, is to the Sine of the Pole's Elevation ;
 So is the Tangent of the Hour-Lines at the Pole,
 To the Tangent of the distance of the Hour from the Meridian.
 Let the Question be to Supputate the distance of the Eleven,
 or One a Clock Hour from the Meridian in the Latitude of 52
 Deg. and 30 Min. therefore according to the former Analogy, it
 may thus be Resolved.

Radius 90 Deg.	10.00000
Sine of the Pole's Elevation, 52 Deg. 30 Min.	9.89946
Tangent of the Equinoctial distance of One Hour from the Meridian 15 Deg.	9.42805
Tangent of the Hour from the Meridian, 12 deg.	9.32751

After this manner may you find the distance of 2 and 10 of
 the Clock, and of 3 and 9 of the Clock, and so of the rest ;
 only you are to remember, that the Equinoctial distance of 1 a
 Clock is 15 Deg. of 2 a Clock 30 Deg. of 3 a Clock 45 Deg.
 of 4 a Clock 60 Deg. of 5 a Clock 75 Deg. as in the following
 Table.



The distance of the Hour-Lines from the Meridian being now
 found, you may project them into the former Scheme thus.

Take with your Compasses 60
 Deg. from a Line of Chords, and
 with the same Extent, setting one
 Foot in the Centre A, with the
 other describe the Circle D O E,
 which done, take from the same
 Scale of Chords, all the Hour-di-
 stances, and placing one foot of
 your Compasses in O, (where the
 Circle Intersects the Meridian)
 with the other set out the Hour
 distances before found by Calcula-

Hours	Equin. distanc.	Hour Arches.
12	0 0	0 0
11	15 0	12 0
10	30 0	24 37
9	45 0	38 26
8	60 0	53 57
7	75 0	71 20
6	90 0	90 0

tion

tion, both ways upon the Circle D O E, then drawing streight Lines from the Center A, to those Pricks in the Circle, you shall have the true Hour-lines desired.

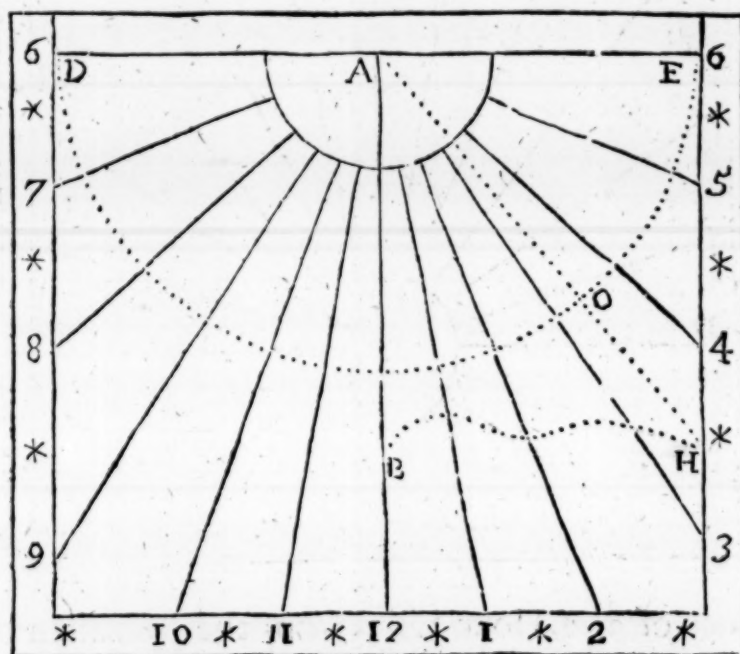
Lastly, From the said Line of Chords, take the Pole's Elevation, 52 Deg. 30 Min. and set it from O to P, drawing the Prickt Line A P H, which shall represent the upper edge, or height of the Style; so will Z A H be the true Pattern of the Cock, or Gnomon of your Dial, which erect at right Angles over the 12 a Clock Line, and so is your Dial finished.

P R O B. II.

To describe the Erect, Direct North or South Dial.

THe making of this differs very little from the Horizontal, only there in the Calculative part, you took the Pole's Elevation, but here you must take its Complement, and insert only 12 Hours, as will appear by the following Figure.

Let the Question again be to Calculate the distance of 11, or 1 a Clock from the Meridian, in the said Latitude of 52 D. 30 Min.



The Calculation.

As the Radius, 90 Deg.

10.00000

To the Cosine of the Pole's Elevation, 52° 30'

9.78445

So the Tangent of the distance of one Hour from the Meridian, 15 Deg.

9.42805

To the Tang. of the Hour Arch from 12, 9° 16'

9.21250

According to the like Order are the rest of the Hour Arches found, as in the Table.

The

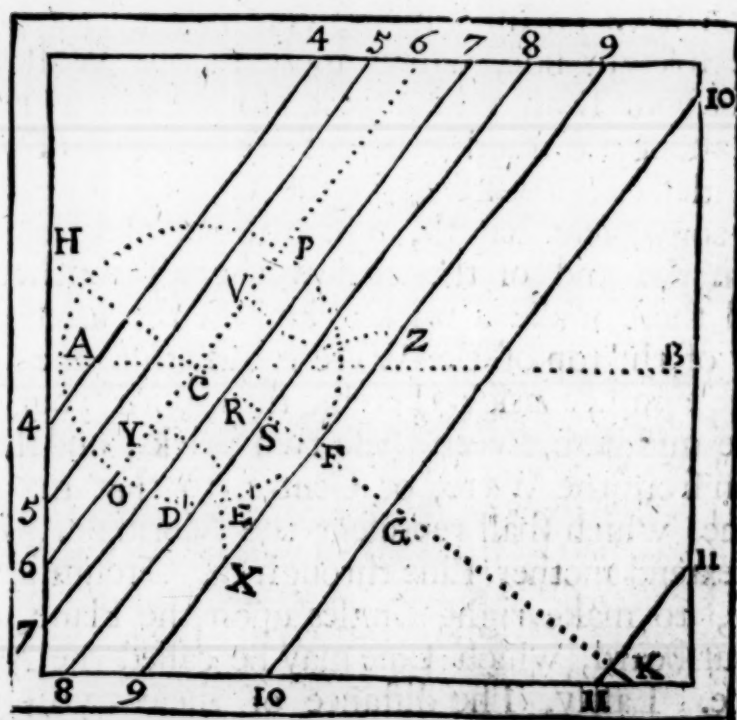
The distance of the Hour-Lines from the 12 a Clock Line being now found, you must Project them into the Dial after the same manner, as we shewed in the Horizontal, only for the height of the Style, you are to take the Complement of the Pole's Elevation, 37 Deg. 30 Min. and then work as before, as you may see by the Diagram.

Hours		Equin. distanc.	Hour Arches.
12		05 0	0 0
11	1	15 0	9 16
10	2	30 0	19 22
9	3	45 0	31 20
8	4	60 0	46 31
7	5	75 0	66 15
6	6	90 0	90 0

P R O B. III.

To Describe the direct East or West Dial.

First draw the Horizontal Line of the Plane A B, and this Dial may most exactly be projected by a Line of Natural Tangents, but we shall here give you that way which is more easie, and fitting all Capacities.



Let the Substylar Line (which stands in the Line of 6) make an Angle therewith, equal to the Latitude of the Place, as 6 C B, so that it may point exactly to the Pole of the World; then from the point C, draw the Line H C K, at right Angles to the 6 a Clock Line. Next upon C, as a Centre, describe a Circle, whose Radius shall be equal to the height of the Style G F, which prick off from O to E, from F to D, from E to G, and from G twice K k k to

to K. Lastly, Lay a Rular from P to D, and it will Intersect the Line H K in the point R, where make a prick for the 7 a Clock Line. Again, Lay the Rular from P to E, and you shall find it to cut the Line H K in S for the 8 a Clock Line. The 9 a Clock Line is at the point F, the 10 a Clock Line at the point G, and the 11 a Clock Line at the point K; then from every of the said points draw Lines parallel to the substyle, or Hour-Line of 6, and you shall have six of the Hour-Lines inserted. Lastly, Make the Hour-Lines of 5 and 4 in the morning, as far distant from the Substyle towards the Left-Hand, as the Lines of 7 and 8 are towards the Right, and then is your Dial compleatly finished; only remember to set your Gnomon erect over the Line O P.

P R O B. IV.

To find the Declination of a Plane.

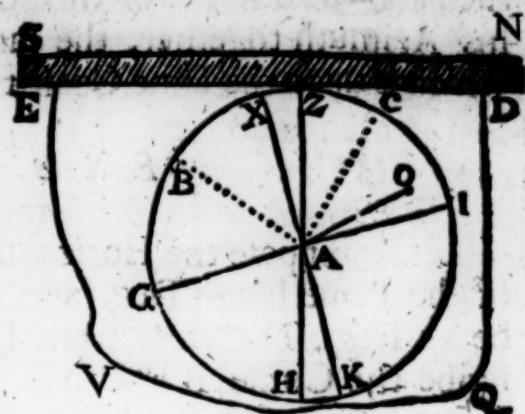
IF the Plane whereon you are to make your Dial, behold neither the East, West, North or South Points of the World, but Decline therefrom, then it will be necessary to shew how to find the Declination thereof, which may be obtained several ways, both by the assistance of Instruments, and other ways. First, If you have no Instrument, you may take a plain Board, having one streight side, which apply to the Wall where you intend to set your Dial, where fix it Horizontal, as near as you can; then about the middle thereof set one foot of your Compasses, and describe a Circle, in the Centre whereof erect a Wyre of a convenient length, which done, observe in the forenoon, when the end of the shadow thereof toucheth the said Circle, and there make a prick; and in the afternoon, when the shadow of the top of the Wyre returneth to the same Circle again, make another prick therein, then with your Compasses measure the middle between these two pricks, and there make a mark; then from the Wyre, or Centre, to that mark, draw a streight Line, which shall represent the Meridian. Next from the Wyre extend another Line through the Circumference of the said Circle, to make right Angles upon the Plane, or streight edge of your board, which Line may be called the Axis or Pole of the Plane. Lastly, The distance of these two pricks in the Circumference of the Circle, is the true Declination of the Plane, which you may know at first sight, whether it be North or South, by ocular Inspection only.

E X A M P L E.

Let S N D E represent the face of the Plane, whereon I am to make my Dial, to which I apply the streight edge of the board

board D E, as in this Figure.

Then about the middle of the board D E V Q, viz. at A, I set one foot of my Compasses, and with the other (opened to 60 Deg. upon my Line of Chords) I describe the Circle Z B H C, in the Centre whereof A, I erect a Wyre, as A O, which done, I find by Observation, that the shadow of the top of the Wyre,



toucheth the Circle in the Forenoon, at the point B, where I make a little mark. Likewise I observe in the Afternoon, that it toucheth the said Circle in the point C, then I measure their distance with my Compasses, and set the half thereof from B or C to X, and drawing a Line with my Ruler from A to X, we shall have the Meridian Line K A X exactly described.

Lastly, Opening my Compasses, I take the distance Z X, which I apply to my Scale of Chords, and find the Arch thereof 18 Deg. 10 Min. and so much is the Declination of the Plane E D N S, which you may see by the Meridian Line K X, is towards the West. This then is a South Plane declining West, 18 Deg. 10 Min.

Although this way of finding the Declination of a Plane, is most easie, yet because it requires Observation both in the forenoon and afternoon, so that it cannot be effected without some considerable time, I shall now shew you another way or two, how to perform the same at one Observation.

Otherwise.

You may find the Declination of any Plane by the Sun's Azimuth; for, take his Altitude with a Quadrant, and by the last Problem of the former Part, calculate his Azimuth; at the same instant, apply one edge of the Quadrant to the Plane, that the Limb thereof may be towards the Sun, then placing the Quadrant as near level as you can, hold up a Thread and a Plummets, in such wise, that the shadow of the Thread may fall upon the Centre and Limb of the Quadrant, then will the shadow shew upon the Limb how many Degrees the Sun is distant from that side of the Quadrant which represents the Axis, or Pole of the Plane, which may be called the distance of the Sun from the Pole of the Plane.

Again, At the same instant observe the Sun's Altitude by your Quadrant, by which you may get his Azimuth from the South point, as is said before. Then to find the Declination, observe the two following Rules.

1. If the shadow fall between the South, and the Perpendicular side of the Quadrant, that represents the Axis of the Plane,

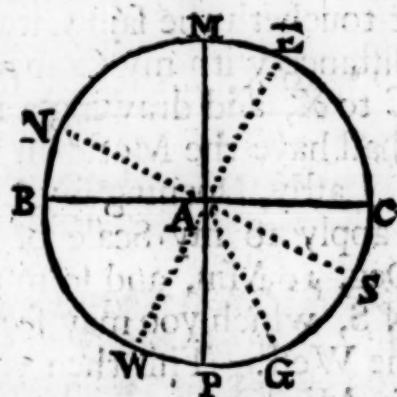
K k k 2

then

then add the distance of the Sun from the Pole of the Plane, and his Azimuth together, the sum is the Declination of the Plane, which is upon the same Coast the Azimuth is, as for Example.

EXAMPLE I.

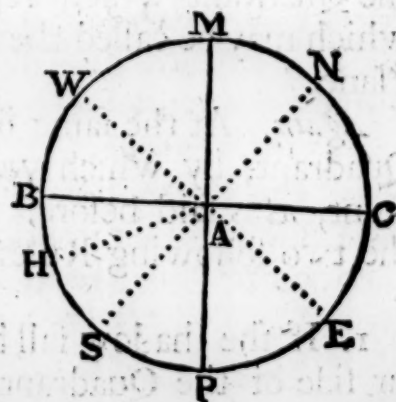
Let us suppose the Horizontal distance of the Sun from the Pole of the Plane be 20 Deg. and the Sun's Azimuth from the South be 42 Deg. Therefore from hence to find the Declination, I describe the Circle B P C M, whereupon I draw the Diameter B A C, representing the Horizontal Line of the Plane, and cross it at right Angles in the Centre A, with the Diameter M A P, which represents the Pole of the Plane. Then with my Compasses, I take from the Scale of Chords, the Horizontal distance, or distance of the Sun from the Pole of the Plane, 20 Deg. and set it from P to G, and then from G to S set off the Sun's Azimuth, 42 Deg. which done, draw the Diameter S N, and cross it at right Angles with the Diameter E A W, so will S represent the South, N the North, E the East, and W the West. Now forasmuch as the Line of the shadow of the Thread G A, falleth between P the Pole of the Plain, and S the South point; therefore according to the former Rule, I add P G the Sun's distance from the Pole of the Plane 20 Deg. to G S the Sun's Azimuth, 42 Deg. and the sum P S 62 Deg. is the Declination required, which is towards the West, as the Figure it self sheweth.



2. If the shadow fall not between the South and the Axis of the Plane, then the difference of the distance and Azimuth is the Declination of the Plane; and if the Azimuth be the greater of the two, the Plane declines to the same coast whereon the Azimuth is; but if it be the lesser, then the Plane declineth to the contrary Coast to that whereon the Azimuth is, as you may see by this Example.

EXAMPLE II.

Admit the Sun's distance from the Pole of the Plane be taken in the afternoon 70 Deg. and the Sun's Azimuth from the South be then given, 44 Deg. Therefore, as before, I draw the Circle M C P B, and from P to H, I set off the Sun's distance from the Pole of the Plane 70 Deg. and from H to S the Sun's Azimuth 44 Deg. now because the South point doth fall between



P the

P the Pole of the Plane, and H the distance of the Sun from the Pole of the Plane; therefore (according to the Rule) I subtract the Sun's Azimuth H S, 44 Deg. from H P the distance of the Sun from the Pole of the Plane, and there remaineth S P 26 Deg. the Declination desired; which is towards the East, as you may perceive by the Figure. So that this is a South Plane declining East 26 Degrees.

E X A M P L E III.

Although the two former ways are exact, if they are but warily performed, yet in regard they cannot be effected without the help of the Sun, I shall therefore shew how you may speedily find the Declination of any Plane by the Needle, whether the Air be clear or not.

Apply the North side of the Instrument, wherein the Needle is placed unto the Wall, and hold it Horizontally, as near as you can, that the Needle may have free liberty to play to and fro, and when it stands, observe upon the Limb of the Chard, over which it moves, upon what Degree the Needle stands, for that is the Declination reckoned from the South. And if you would know the Coast, observe that if the Needle stand upon the East side the Meridian Line, then is the Declination of the Plane West, but if it stand on the West side the Meridian Line, the Declination is East, according to the quantity thereof.

P R O B. V.

To describe the North and South erect Declining Dial, according to its Declination East or West.

First the Declination of the Plane, whereon you intend your Dial, is to be sought, as was shewed in the last Problem, which being attained, we shall come to the Declination of the Dial it self.

Let us suppose the Elevation of the Pole to be 52 Deg. 40 Min. and the Declination of the Plane whereon I am to make my Dial, be 24 Deg. towards the West, (such was one of the Dials I lately made for the Right Worshipful Sir *Erasmus de la Fountain*, at *Kerby-Bellers* in the County of *Leicester*) therefore, because the Declination is West, the Style must stand on the East side the Meridian, or Hour-Line of 12, (but if the Declination had been East, it should have stood on the West side thereof). But before we can come to the Calculation of the Hour-distances, there are three things to be known, (1.) The Elevation of the Pole above the Plane, commonly called the height of the Style; (2.) The distance of the Substile from the Meridian; (3.) The Inclination of the Meridian of the Plane to the Meridian of the place.

The

The Calculation.

(1.)

As the Radius, 90 Deg.	10.00000
To the Cosine of the Elevation, $52^{\circ} 40'$.	9.78279
So the Cosine of the Declination, 24 Deg.	9.96073
To the Height of the Style, $33^{\circ} 38'$	9.74352

(2.)

As the Radius, 90 Deg.	10.00000
To the Sine of the Declination, 24 Deg.	9.60931
So the Cotangent of the Elevation, $52^{\circ} 40'$	9.88236
To the Tangent of the Substile's distance from the Meridian, $17^{\circ} 14'$	9.49167

(3.)

As the Radius, 90 Deg.	10.00000
To the Sine of the Pole's Elevation, $52^{\circ} 40'$	9.90043
So the Cotangent of the Declination, 24 Deg.	10.35142
To the Cotangent of the Inclination of the Meridian, 29 Deg. 15 Min.	10.25185

These things thus found, we shall next proceed to the Calculation of the Hour-distances: But first we are to consider, That the Angle between the Meridians was found to be 29 Deg. 15 Min. and because the Hour of One is distant from the Meridian 15 Deg. and the Hour of Two 30 Deg. therefore I conclude the Substile will fall between one a Clock and two; and if I Subtract 15 Deg. from 29 Deg. 15 Min. the Remainder will be 14 Deg. 15 Min. the distance of the one a Clock-Line from the Substile.

Again, The distance of two of the Clock from the Meridian, is 30 Deg. from which if I Subtract, 29 Deg. 15 Min. the distance of the two a Clock from the Substile, will be 0 Deg. 45 Min. These things being now known, the rest of the Hours are found by a continual addition of 15 Deg. for every Hour, (and for every half hour 7 Deg. 30 Min. &c.) as by the following Table you may perceive. Lastly, To find the distance of each Hour-Line from the Substile, we shall give an Example for one of the Clock, whose Equinoctial distance from the Substile, is (as in the following Table) 14 Deg. and 15 Min.

The Calculation.

As the Radius, 90 Deg.	10.00000
To the Sine of the Height of the Style, $33^{\circ} 38'$	9.74341
So the Tangent of the distance of one Hour, from the Substile, 14 Deg. 15 Min.	9.40478
To the Tangent of the Hour Arch from the Substile, 8 Deg.	9.14819

After

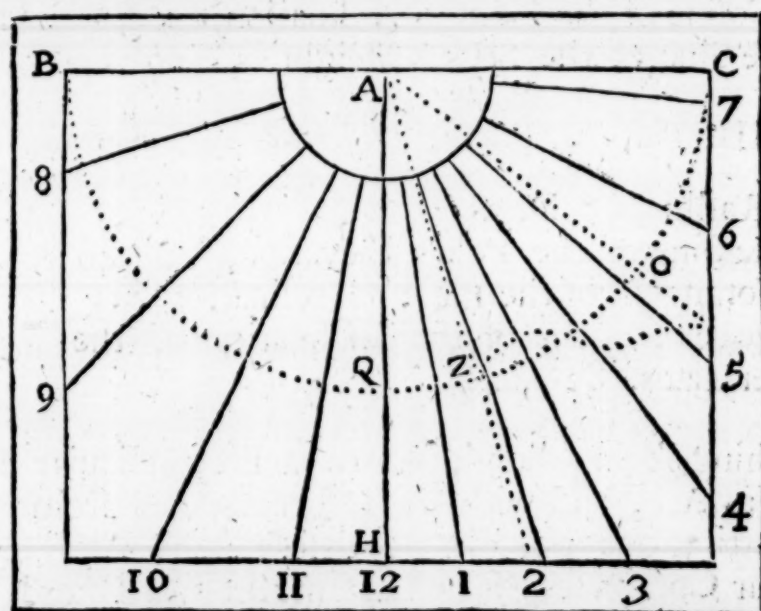
After the same manner we have Calculated the following Table, by which the Dial is most easily projected, as we shall hereunder shew.

First, Draw the Horizontal-Line B C, (as in the following Figure) and from the most convenient place thereof, as A ; let fall the Perpendicular A H, which shall represent the Meridian Line of the Plane. Then take 60 Deg. from a Line of Chords, and making the Centre, draw the Semi-circle, B Z C. In this Circle from Q to Z prick down the distance of the Substyle from the Meridian, which was found before, 17 Deg. 14 Min. and from the Substyle Z, in the same Circle, I set off the height of the Style to O, 33 Deg. 38 Min. so shall Z A O represent the Cock

Hours	Equin. distanc.		Hour Arches.	
8	89	15	88	39
9	74	15	63	1
10	59	15	42	57
11	44	15	28	21
12	29	15	17	14
1	14	15	8	0
	Merid.		Substile	
2	0	45	0	25
3	15	45	8	53
4	30	45	18	14
5	45	45	29	37
6	60	45	44	41
7	75	45	65	22

of the Dial. Then from the same Scale of Chords, take off with your Compasses, the several Hour-distances, as they are ready Calculated in the Table, viz. 8 Deg. 0 Min. for 1 a Clock; 17 Deg. 14 Min. for 12 a Clock; 28 Deg. 21 Min. for 11 a Clock, and

An Erect Dial, Declining from the South, Westward 24 Degrees.



so of the rest, and prick them down from the Substyle, in the Circle B Q C, by help of your Line of Chords. Lastly, Draw streight Lines from the Centre A, to those several Points, and you shall have the true Hour-Lines, which was desired.

P R O B.

P R O B. VI.

The Calculation and Projection of an Erect South Plane, declining Eastward, 81 Degrees.

According to this Method, I shall here take, the Style may be so proportioned, by the Discretion of the Artist, to fill any Plane, by bare Inspection.

The First thing to be found, is, The distance of the Substyle from the Meridian: Secondly, The Elevation of the Pole above the Plane, commonly known by the name of the Style's height: And Thirdly, The Plane's difference of Longitude, or Inclination of Meridians: The Calculation follows:

I. For the Substyle's Distance.

As the Radius, 90 Deg.	10.00000
To the Sine of the Plane's Declination, 81 Deg.	9.99461
So the Cotangent of the Pole's Elevation, 52° 40'	9.88236
To the Tangent of the Substyle's Distance from the Meridian, 37°.	9.87697

II. For the Style's Height.

As the Radius, 90 Deg.	10.00000
To the Cosine of the Pole's Elevation, 52° 40'	9.78279
So the Cosine of the Plane's Declination, 81°,	9.19433
To the Sine of the Style's Height, 5° 27'	8.97712

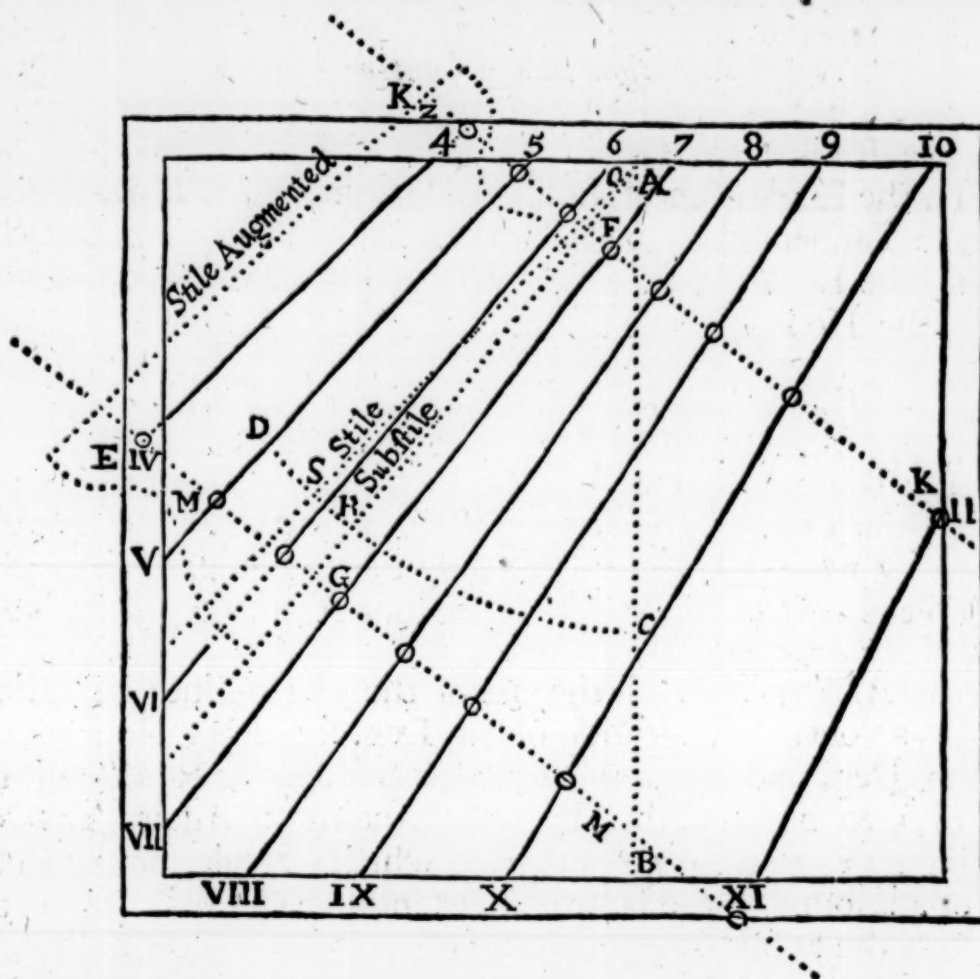
III. For the Plane's Difference of Longitude.

As the Radius, 90 Deg.	10.00000
To the Sine of the Pole's Elevation, 52° 40'	9.90044
So the Cotangent of the Plane's Declination, 81°	9.19971
To the Cotangent of the Inclination of the Meridians, 82° 49'	9.10015

These things being found, Draw a Perpendicular Line upon the Plain, as A B, and with 60 Degrees taken from a Scale of Chords, setting one Foot in A, describe the Arch C D; then take in your Compasses, (from the same Scale of Chords) 37 Deg. the Substyle's Distance, and set it from C to R, and draw the prickt Line A R for the Substyle; this done, Take from the Scale of Chords, 5 Deg. 27 Min. the Style's Height, and set it from the Substyle, where it intersects the Circle, as from R to S, and draw the Line A S for the Stile; then consider the bigness of your Plane, so as you may Augment the Style, that the Hour-Lines may fill the Plane, which in this Example, or Dial, we shall raise 9 Inches, as the Line E Z, parallel to the Line S O,

so

so will the Style be augmented ; then make choice of two Points in the Substyle, as at F and G, and draw the two Contingent Lines, as M M and K K at right Angles with the Substyle ; then



measure the Height of your augmented Style, in both the Contingent Lines, in Inches and Decimal parts, as from G to E, which I find to be 14 Inches, and from F to Z 11 Inches, which two numbers are to be made use of in the Calculation of the several Hour-distances : Next, Considering the Inclination of Meridians was found, 82 D. 49 M. therefore allowing for every Hour 15 Deg. being the Angle at the Pole, so that I find the Substyle will fall between the Hours of 6 and 7 ; for if I Subtract 82 D. 49 M. from 90 Deg. (being 6 hours from the Meridian, for 6 times 15 is 90) the Remainder is 7 D. 11 M. for the Distance of the 6 a Clock-Line from the Substyle, being the Angle at the Pole for that Hour ; so likewise if I Subtract 75 Deg. (the Angle at the Pole for the Hour of 7) from 82 Deg. 49 M. the Remainder is 7 D. 49 M. for the Angle at the Pole for the Hour of 7 ; thus, having these things, we shall proceed to Calculate the several Hour-distances from the Substyle, which are to be set off from the Substyle in both the Contingent Lines, therefore two Arches must be Calculated for each Hour by this Analogy. As the Radius to the Logarithm of the Style's Height in Inches, (in either of the Contingent Lines) so the Tangent of the Angle at the Pole, to the Logarithm in Inches for that Hour-distance from the Substyle, and so for the distance

in Inches and Parts, in the other Contingent Line for the same Hour, as shall here be demonstrated in the 6 a Clock Line, being the first Line on the upper side the Substyle, whose Angle at the Pole was found 7 D. 11 M.

The Calculation in the Contingent K K.

As the Radius, 90 Deg.	10.00000
To the Logarithm of the Style's Height, 11 Inch.	1.04139
So the Tangent of 7° 11' the Angle at the Pole.	9.10048
To the Logarithm of 1, $\frac{39}{100}$ Parts of an Inch, the Hour-Arch.	0.14187

The Calculation in the Contingent M M.

As the Radius, 90 Deg.	10.00000
To the Log. of the Style's Height, 14 Inches.	1.14612
So the Tangent of 7° 11' the Angle at the Pole.	9.10048
To the Log. of 1, $\frac{76}{100}$ Inch. the Hour-Arch.	0.24660

By this Analogy may all the rest of the Hour-Lines be Calculated by a continual Addition of 15 Deg. for every Hour; for if I add 15 Deg. to 7 Deg. 11 Min. the Sum is 22° 11' for the Hour of 5 to be found by the same Analogy: Again, 15 Deg. added to 22° 11', is 37° 11', from which Calculation the Hour-Line of 4 is found, in the same manner must the Hour-Lines on the other side the Substyle be found, by using 7° 49' the Angle at the Pole for the 7 a Clock-Line, which by the former Analogy will give the Hour-Arch for 7 a Clock, to which 7° 49' add 15 Deg. and by the same Proportion find the Hour-Arch for 8, and so by the continual Addition of 15 Deg. used by the same Analogy, may the rest of the Hour-Arches be found, which may most easily be projected into the Dial from the several Calculations, by taking the Hour-Arches in Inches and Parts, and placing them from the Substyle F and G, upon their proper Contingent Lines, through the Plane, the Gnomon, (or Style) set directly over the Substyle, and the Work is finished.

These are all the several sorts of Mural Dials that are properly affixed upon Buildings, which the Surveyor is very often put upon to do, but if he have a desire to make a further progress in this Gnomical Science, I shall wholly recommend him to Mr. *Leybourn's* Dialling in Folio, where the Art is Treated of fully in all its parts, it being the only Piece in that Kind extant.

P R O B. VII.

To find the true Hour of the Day by the shadow of a Staff erected Perpendicularly upon plain level Ground, where the Sun doth shine, the Staff being divided into 10, 100, or 1000 Parts.

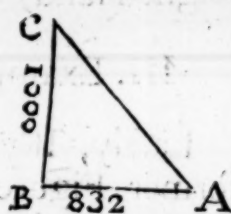
THis Problem may best be effected by the following Table, which is Calculated by the Solution of a Plain Rectangled Triangle, according to the first Problem of the Third Book, for we have given, (1.) The length of the Staff CB 1000. (2.) The Angle of the Sun's Altitude, BAC , to find the Length of the Shadow AB .

Admit the Sun be in the first Point of *Gemini*, and at two a Clock in the Afternoon, it is required to find the length of the Shadow of the Staff. By the 12th Prob. of the 2d Part of this Book, the Sun's Altitude is found, $15^{\circ} 15'$ D. $15^{\circ} 15'$ M. represented by the Angle BAC ; which known, with the length of the Staff BC 1000, to find BA , I say,

As the Radius, 90° Deg.	10.00000
To the Cotang. of the Angle, BAC , $15^{\circ} 15'$	9.91996
So the Length of the Staff, BC 1000.	3.00000
To the Length of the Shadow, 832.	2.91996

According to this Doctrine was the following Table composed, which I shall here Explain.

First, The Staff or Gnomon is here supposed to be divided into 1000 equal Parts, and being set upright, the Table will shew (according to the Sun's Place) how many such Parts, the length of the Shadow thereof is to contain, at any Hour of the Day.



Secondly, If the Staff be divided into 100 Parts, the Figures towards the Left Hand, shew the length of the Shadow; and the last Figure, remaining towards the Right Hand, will tell you how much the Shadow is above so many even Parts, every 100 Part being divided into 10.

Thirdly, But if the Staff be divided into 10 equal Parts, then the former Figure, or Figures towards the Left-Hand, shews how many of those Parts the Shadow of the Staff will yield at each Hour; and the two last Figures, towards the Right-Hand, being distinguished from the former by a prick or Comma, will shew how much the Shadow is above so many even Parts, according to the Partition of every of those 10 even Parts into 100.

But if upon your Staff of 10 equal Parts, you Subdivide each part into 10 more; then will the first Figure of the Fraction, next after the prick or Comma, point out how many of these Subdivided Parts the Shadow shall contain, over and above the whole Parts towards the Left-Hand. But to illustrate, and make this more clear, I shall add the following Examples.

The Use of the following Table.

Seek the place of the Sun in the first or second Column, towards the Left-Hand; and having divided your Staff into 10 equal Parts, (as before was taught) set it upright in some plain level place where the Sun doth shine, and then measure with your Staff, how many parts the shadow thereof contains, which find out in the Table right against the Sun's place, and in the same Column overhead, you have the Hour of the Day.

I. Example, *Where the Staff is divided into 1000 Equal Parts.*

Suppose that upon the 10th of March, when the Sun enters Aries, I erect my Staff upon plain level Ground, and find the shadow thereof to contain 3130 Parts, (that is, three times the length of the Staff, and 130 Parts more) therefore seeking in the Table for the number of the said Parts, against 0 Deg. of γ , I find the same in the seventh Column of the Table, under the Hours of 8 and 4; so that if the Observation had been in the Forenoon, it had been 8 a Clock, but in the Afternoon 4 a Clock.

II. Example, *Where the Staff is divided into 100 Equal Parts.*

But if your Staff be divided but into 100 Parts, and you find the shadow thereof to be 313 of the same Parts in length, seek out the same in the Table, (leaving out the last Figure towards the Right-Hand) and it giveth the Hour of the Day as before.

III. Example, *Where the Staff is divided into 10 Equal Parts.*

Lastly, If your Staff be divided but into 10 equal Parts, then the former Figures distinguished from the other two, towards the Right Hand, shew the length of the shadow, at the same time, to be 31 whole Parts, and 30 Parts of a 100, or 3 Parts of 10; that is, 3 times the length of my Staff, and one whole part, and something above a quarter of a part more.

And if, according to this Example, The same day I should set up my Staff, and find the shadow thereof to contain 62 whole Parts, and 67, which is about $\frac{2}{3}$ of a part; the Table will shew me, that 'tis then 7 a Clock, if the Observation be in the Forenoon, or 5 if it be in the Afternoon.

But I need not add more here to Explain this matter, seeing the Table of it self is so easie, that what is already said, may suffice. And now having shewed my Surveyor, how he may find the just Hour of the day, at all times by the help of the Sun: I shall here also shew him, how to find the true Hour of the Night by the Moon, Planets, and Fixed Stars, when they are seen, after a most concise way. by Tables of Right and Oblique Ascensions in Time, for that purpose.

A TABLE shewing the True Hour of the Day, by a Plain Staff, Divided into 10, 100, or 1000 Equal Parts.

H.	Bef. No.	Aft. No.	12	11 I	10 2	9 3	8 4	7 5	6 6	5 7
☿	0	0	5.54	6.05	7.50	9.88	13.49	19.25	29.97	57.20
	25	5	5.57	6.08	7.54	9.92	13.54	19.34	30.19	57.99
	20	10	5.62	6.13	7.59	9.98	13.65	19.47	30.47	59.02
	15	15	5.75	6.25	7.70	10.12	13.83	19.82	31.24	61.85
	10	20	5.88	6.39	7.86	10.30	14.08	20.20	32.07	65.22
	5	25	6.09	6.60	8.08	10.56	14.41	20.81	33.47	71.15
♈	0	0	6.32	6.83	8.32	10.84	14.81	21.48	35.07	78.61
	25	5	6.61	7.12	8.63	11.21	15.32	22.40	37.34	90.58
	20	10	6.92	7.44	8.98	11.61	15.91	23.42	40.01	107.79
	15	15	7.30	7.82	9.38	12.12	16.63	24.76	43.63	138.38
	10	20	7.71	8.23	9.83	12.67	17.43	26.26	48.08	196.27
	5	25	8.18	8.72	10.36	13.33	18.40	28.16	54.31	358.00
♉	0	0	8.89	9.23	10.93	14.04	19.48	30.35	62.32	864.00
	25	5	9.27	9.83	11.59	14.88	20.78	33.16	74.29	
	20	10	9.88	10.46	12.31	15.80	22.25	36.47	92.18	
	15	15	10.57	11.18	13.12	16.87	24.00	40.74	121.85	
	10	20	11.32	11.96	14.02	18.06	26.05	46.06	181.71	
	5	25	12.14	12.82	15.01	19.43	28.45	53.13	363.69	
♊	0	0	13.03	13.75	16.12	20.96	31.30	62.67		
	25	5	14.01	14.78	17.35	22.73	34.72	76.30		
	20	10	15.09	15.92	18.73	24.75	38.95	97.32		
	15	15	16.26	17.18	20.26	27.08	44.11	113.00		
	10	20	17.57	18.56	21.09	29.80	50.81	209.46		
	5	25	18.95	20.06	23.88	32.90	59.23			
♋	0	0	20.52	21.74	26.07	36.64	70.85			
	25	5	22.15	23.52	28.40	40.81	86.21			
	20	10	23.96	25.52	31.11	45.99	109.88			
	15	15	25.84	27.57	33.94	51.78	145.13			
	10	20	27.95	29.89	37.13	58.91	208.15			
	5	25	30.05	32.14	40.50	66.78	343.68			
♌	0	0	32.10	34.61	44.04	76.00	828.43			
	25	5	34.08	36.81	47.62	86.32				
	20	10	36.00	39.14	51.09	97.18				
	15	15	37.63	40.87	54.18	107.97				
	10	20	39.09	42.52	56.58	117.25				
	5	25	39.71	43.26	58.25	123.84				
♍	0	0	40.11	43.72	59.00	126.36				

P R O B. VIII.

How to find the exact Time of the Planets and Fixed Stars, Rising, Southing, and Setting, by the following Tables; And First,

Of their Southing.

THe Estimate Time of a Planet or Fixed Stars, Rising, Southing or Setting may be nearly known by their distance from the Sun, which known, get the place of the Moon or Star to that time, with Latitude, and also the place of the Sun for that time also, then enter the Table of Right Ascensions, with the Longitude of the Planet or Star under its Latitude, (if it have any) and in the Angle of Meeting is the R A in Time, which write down, and likewise enter the said Table with the Sun's place, under o Latitude, (for the Sun is always in the Ecliptick Line) and take out his R A also, which Subtract from the R A of the Star or Planet, (which increased by 24 Hours, if need require) and the Remainder is the Hour and Minute of the Planet or Stars Culminating, or coming to the South.

E X A M P L E

March 1. 1696. It is required to find the Time of *Jupiter's* coming to the South for the Night following, (we take their Places for Midnight, because they are nearly in opposition) the Longit. of ♃ is $22^{\circ} 00'$, ♃ with $10^{\circ} 15'$ N. Lat. and the Sun in $22^{\circ} 30'$ ♋, Hence

	H.	M.
R A of ♃ in time, 24 hours added) is	35	33
R A of ☉ in time, (Subtract	23	32
♃ South, at 1 Minute after Midnight	12	01

This being both so plain and easie, that more Examples are needless, for the same Method is to be observed, in finding the Southing of the Moon and Fixed Stars.

Of the Rising of the Planets and Fixed Stars.

Enter the Table of Oblique Ascensions, with the Sign and Degree of the Star or Planet's place in respect of Latitude, and take out his Oblique Ascension agreeing thereto; enter the Table also with the Sign and Degree of the Sun's place, and take out his Oblique Ascension also, which Subtracted from the Oblique Ascension of the Star, and to the Remainder, add the time of Sun Rising for that Day, the sum (Subtracting 12 Hours if it exceed 12) is the true time of his Rising that Night.

E X A M P L E.

EXAMPLE I.

Of *Jupiter's* Rising the first day of *March* 1696. as followeth.

	H.	M.
The O A of ♃ in Time, (24 Hours add.)	35	09
The O A of ☉ in Time, Subtract.	23	48
	<hr/>	
Remainder	11	21
Time of Sun Rising, Add	6	19
	<hr/>	
Sum	17	40
Subtract	12	00
	<hr/>	
Hence ♃ Rises, 40' past 5 that Night.	5	40

Otherways by the same Tables: From the O A of the Planet or Star, Subtract the Sun's R A, and if the Remainder exceed six Hours, Subtract six Hours from it; and if it happen to be less than 6 Hours, add thereunto 9 Hours; this Sum or Difference is the true time of the Star or Planet's Rising required, as in the last Example.

EXAMPLE II.

	H.	M.
The O A of ♃ in Time, (24 hours add.)	35	09
R A of ☉ in time, Subtract.	23	29
	<hr/>	
Difference	11	40
Subtract	6	40
	<hr/>	
Time of <i>Jupiter's</i> Rising as before.	5	40

Thus is the Work abbreviated, and made both easie and practicable, observe the same Method in computing the Rising of the Moon, Fixed Stars, and other Planets.

Of the Setting of the Planets and Fixed Stars.

To find the Time of the Moon, Planets, and Fixed Stars Setting, the Oblique Descension is required, which is obtained by Entering the Table of Oblique Ascensions, with the opposite Sign and Degree, and under the Latitude of a contrary Denomination, and in the Angle of meeting is the O D of the Star or Planet; enter the Table also with the opposite Sign and Degree of the Sun's place, which gives his O D also under ☉ Latitude, which Subtracted from the O D of the Star or Planet, and the Remainder added to the time of the Sun's Setting for the same day, the Sum is the true time of the Star or Planet's Setting; as we shall Exemplifie here in *Jupiter* also, the same day that is before Exemplified both in his Southing and Rising, viz. The first of *March* 1696.

EXAM-

EXAMPLE I.

The O D of γ in Time.
The O D of \odot in Time.

H.	M.
23	56
11	18

Time of Sun Setting, Add

Remains	12	38
	5	44

Sum	18	22
Subtract	12	00

Hence, γ sets, 22' past 6 next morning

6	22
---	----

We shall (as in the Rising) Exemplifie this, an easier and readier way from the Tables, as followeth.

EXAMPLE II.

The O D of γ in Time.
The R A of \odot in Time.

H.	M.
23	56
11	34

Remains	12	22
Subtract	6	00

Time of *Jupiter's* Setting as before.

6	22
---	----

Observe the same Method in Calculating the Setting of the D , and Fixed Stars: And for the obtaining the true Places of the Fixed Stars both in Longitude and Latitude, I have here Exhibited a Table of some eminent fixed Stars that are near the Ecliptick,

A TABLE of Ten of the Fixed Star's Places both in Longitude and Latitude, Rectified to the Year 1693.

<i>Nomina Stellarum.</i>	Longitude.			Latitude.		
	S	o	'	o	'	
The Pleiades, or Seven Stars.	γ	25	42	4	0	N
Aldebaran, or the Bull's Eye.	Π	5	30	5	31	S
Precepe.	Ω	3	4	1	14	N
North Afellus.	Ω	3	15	3	8	N
South Afellus.	Ω	4	26	0	4	N
Cor Leonis.	Ω	25	35	0	26	N
Virgin's Spic.	\approx	19	34	1	59	S
South Ballance.	\mathfrak{M}	10	49	0	26	N
Cor \mathfrak{M} , Antares.	\mathfrak{f}	5	31	4	27	S
Auftrales.	\mathfrak{v}	29	50	4	41	N

and Rectified their places to the year 1693. which may serve for this next Century, without sensible Errour.

A TABLE

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

Degr.	North Latitude. γ .						South Latitude. γ .					
	5	4	3	2	1	0	1	2	3	4	5	
	h	'	h	'	h	'	h	'	h	'	h	'
00	8	0	6	0	5	0	3	0	23	58	23	57
10	12	0	10	0	8	0	7	0	5	0	4	0
20	15	0	14	0	12	0	10	0	9	0	7	0
30	19	0	17	0	16	0	14	0	13	0	11	0
40	23	0	21	0	19	0	18	0	16	0	13	0
50	26	0	25	0	23	0	21	0	20	0	18	0
60	30	0	28	0	27	0	25	0	24	0	22	0
70	34	0	32	0	30	0	29	0	27	0	26	0
80	37	0	36	0	34	0	33	0	31	0	29	0
90	41	0	39	0	38	0	36	0	35	0	33	0
100	45	0	43	0	42	0	40	0	38	0	37	0
110	48	0	47	0	45	0	44	0	42	0	40	0
120	52	0	51	0	49	0	47	0	46	0	44	0
130	56	0	54	0	53	0	51	0	49	0	48	0
140	59	0	58	0	56	0	55	0	53	0	52	0
150	1	3	1	1	0	0	58	0	57	0	55	0
160	7	1	5	1	4	1	2	1	0	0	59	0
170	10	1	9	1	7	1	6	1	4	1	3	1
180	14	1	12	1	11	1	9	1	8	1	6	1
190	18	1	16	1	15	1	13	1	12	1	10	1
200	21	1	20	1	18	1	17	1	15	1	14	1
210	25	1	24	1	22	1	20	1	19	1	18	1
220	29	1	27	1	26	1	24	1	23	1	21	1
230	32	1	31	1	30	1	28	1	27	1	26	1
240	36	1	35	1	33	1	32	1	30	1	29	1
250	40	1	39	1	37	1	36	1	34	1	33	1
260	44	1	42	1	41	1	39	1	38	1	36	1
270	47	1	46	1	45	1	43	1	42	1	40	1
280	51	1	50	1	48	1	47	1	45	1	44	1
290	55	1	53	1	52	1	51	1	49	1	48	1
300	59	1	57	1	56	1	55	1	53	1	52	1

M m m

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

Degr.	North Latitude. II.						South Latitude. II.					
	5	4	3	2	1	0	1	2	3	4	5	
	h	h	h	h	h	h	h	h	h	h	h	
03	463	473	483	493	503	513	523	533	543	553	36	
13	523	523	533	533	543	553	563	573	583	594	0	
23	553	563	573	583	594	04	04	14	24	34	4	
33	594	04	14	24	34	44	54	54	64	74	8	
44	44	54	54	64	74	84	94	104	104	114	12	
54	84	94	104	104	114	124	134	144	144	154	16	
64	124	134	144	154	154	164	174	184	194	194	20	
74	174	184	184	194	204	214	214	224	234	244	24	
84	214	224	234	234	244	254	254	264	274	284	28	
94	264	264	274	284	284	294	304	304	314	324	32	
104	304	314	314	324	324	334	344	354	354	364	36	
114	344	354	364	364	364	385	384	394	394	404	41	
124	394	404	404	404	414	424	434	434	444	444	45	
134	434	444	454	454	454	464	474	474	484	484	49	
144	484	484	494	494	504	514	514	524	524	534	53	
154	524	524	534	544	544	554	554	564	564	574	57	
164	574	574	584	584	584	595	05	05	05	15	1	
175	15	25	25	25	25	35	45	45	55	55	6	
185	65	65	65	65	75	85	85	95	95	95	10	
195	105	105	115	115	125	125	125	135	135	145	14	
205	155	155	155	155	155	165	175	175	175	185	18	
215	195	195	195	195	205	215	215	215	225	225	22	
225	235	245	245	245	245	255	255	265	265	265	26	
235	285	285	285	285	285	295	295	305	305	305	31	
245	325	335	335	335	335	345	345	345	345	355	35	
255	375	375	375	375	375	385	385	385	395	395	40	
265	415	425	425	425	425	435	435	435	435	435	43	
275	455	465	465	465	465	475	475	475	475	475	48	
285	505	505	505	505	505	515	525	525	525	535	53	
295	545	545	545	545	555	565	565	565	565	565	56	
306	06	06	06	06	06	06	06	06	06	06	0	

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

	North Latitude. α .						South Latitude. α .															
Degr.	5		4		3		2		1		0		1		2		3		4		5	
	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'
0	8	13	8	12	8	11	8	11	8	10	8	9	8	8	8	7	8	6	8	5	8	4
1	8	18	8	17	8	16	8	15	8	14	8	13	8	12	8	11	8	10	8	9	8	8
2	8	22	8	21	8	20	8	19	8	18	8	17	8	16	8	15	8	14	8	13	8	12
3	8	26	8	25	8	24	8	23	8	22	8	21	8	20	8	19	8	18	8	17	8	16
4	8	30	8	29	8	28	8	27	8	26	8	25	8	24	8	23	8	22	8	21	8	20
5	8	35	8	34	8	33	8	32	8	31	8	29	8	28	8	27	8	26	8	25	8	24
6	8	39	8	38	8	37	8	36	8	35	8	34	8	33	8	31	8	30	8	29	8	28
7	8	43	8	42	8	41	8	40	8	39	8	38	8	37	8	36	8	34	8	33	8	32
8	8	47	8	46	8	45	8	44	8	43	8	42	8	41	8	40	8	38	8	37	8	36
9	8	52	8	50	8	49	8	48	8	47	8	46	8	45	8	44	8	42	8	41	8	40
10	8	56	8	54	8	53	8	52	8	51	8	50	8	49	8	48	8	46	8	45	8	44
11	9	0	8	59	8	57	8	56	8	55	8	54	8	53	8	52	8	50	8	49	8	48
12	9	4	8	3	9	1	9	0	8	59	8	58	8	57	8	56	8	54	8	53	8	52
13	9	8	9	7	9	5	9	4	9	3	9	2	9	1	9	0	8	58	8	57	8	56
14	9	12	9	11	9	10	9	8	9	7	9	6	9	5	9	4	9	2	9	1	9	0
15	9	16	9	15	9	14	9	12	9	11	9	10	9	9	9	7	9	6	9	5	9	4
16	9	20	9	19	9	18	9	16	9	15	9	14	9	13	9	11	9	10	9	9	9	8
17	9	24	9	23	9	22	9	20	9	19	9	18	9	17	9	15	9	14	9	13	9	12
18	9	28	9	27	9	26	9	24	9	23	9	22	9	21	9	19	9	18	9	17	9	16
19	9	32	9	31	9	30	9	28	9	27	9	26	9	24	9	23	9	22	9	21	9	20
20	9	36	9	35	9	34	9	32	9	31	9	30	9	28	9	27	9	26	9	25	9	23
21	9	40	9	39	9	38	9	36	9	35	9	34	9	32	9	31	9	30	9	29	9	27
22	9	44	9	43	9	42	9	40	9	39	9	38	9	36	9	35	9	34	9	32	9	31
23	9	48	9	47	9	46	9	44	9	43	9	41	9	40	9	39	9	37	9	36	9	35
24	9	52	9	51	9	49	9	48	9	47	9	45	9	44	9	43	9	41	9	40	9	39
25	9	56	9	55	9	53	9	52	9	51	9	49	9	48	9	46	9	45	9	44	9	42
26	10	0	9	59	9	57	9	56	9	54	9	53	9	52	9	50	9	49	9	48	9	46
27	10	4	10	3	10	1	10	0	9	58	9	57	9	56	9	54	9	53	9	51	9	50
28	10	8	10	6	10	5	10	4	10	2	10	1	9	59	9	58	9	57	9	55	9	54
29	10	12	10	10	10	9	10	7	10	6	10	5	10	3	10	2	10	0	9	59	9	57
30	10	16	10	14	10	13	10	11	10	10	10	8	10	7	10	6	10	4	10	3	10	1

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

Degr.	North Latitude. μ .						South Latitude. μ .					
	5	4	3	2	1	0	1	2	3	4	5	
	h	h	h	h	h	h	h	h	h	h	h	
0	10 16	10 14	10 13	10 11	10 10	10 8	10 7	10 6	10 4	10 3	10 1	
1	10 20	10 18	10 17	10 15	10 14	10 12	10 11	10 9	10 8	10 7	10 5	
2	10 23	10 22	10 20	10 19	10 18	10 16	10 14	10 13	10 12	10 10	10 9	
3	10 27	10 26	10 24	10 23	10 21	10 20	10 18	10 17	10 15	10 14	10 13	
4	10 31	10 30	10 28	10 27	10 25	10 24	10 22	10 21	10 19	10 18	10 16	
5	10 35	10 33	10 32	10 30	10 29	10 27	10 26	10 24	10 23	10 21	10 20	
6	10 39	10 37	10 36	10 34	10 33	10 31	10 30	10 28	10 27	10 25	10 24	
7	10 43	10 41	10 39	10 38	10 36	10 35	10 33	10 32	10 30	10 29	10 27	
8	10 46	10 45	10 43	10 42	10 40	10 39	10 37	10 36	10 34	10 33	10 31	
9	10 50	10 49	10 47	10 45	10 44	10 42	10 41	10 39	10 38	10 36	10 35	
10	10 54	10 52	10 51	10 49	10 48	10 46	10 45	10 43	10 42	10 40	10 39	
11	10 58	10 56	10 55	10 53	10 51	10 50	10 48	10 47	10 45	10 44	10 42	
12	11 1	11 0	10 58	10 57	10 55	10 54	10 52	10 51	10 49	10 48	10 46	
13	11 5	11 4	11 2	11 1	10 59	10 57	10 56	10 54	10 53	10 51	10 50	
14	11 9	11 7	11 6	11 4	11 3	11 1	11 0	10 58	10 56	10 55	10 53	
15	11 13	11 11	11 9	11 8	11 6	11 5	11 3	11 2	11 0	10 59	10 57	
16	11 16	11 15	11 13	11 12	11 10	11 8	11 7	11 5	11 4	11 2	11 1	
17	11 20	11 18	11 17	11 15	11 14	11 12	11 11	11 9	11 7	11 6	11 4	
18	11 24	11 22	11 21	11 18	11 17	11 16	11 14	11 13	11 11	11 10	11 8	
19	11 28	11 26	11 24	11 23	11 21	11 20	11 18	11 16	11 15	11 13	11 12	
20	11 32	11 30	11 28	11 27	11 25	11 23	11 22	11 20	11 19	11 17	11 16	
21	11 35	11 33	11 32	11 30	11 29	11 27	11 25	11 24	11 22	11 21	11 19	
22	11 39	11 37	11 35	11 34	11 32	11 31	11 29	11 27	11 26	11 24	11 23	
23	11 42	11 41	11 39	11 37	11 36	11 34	11 33	11 31	11 29	11 28	11 26	
24	11 46	11 44	11 43	11 41	11 40	11 38	11 36	11 35	11 33	11 32	11 30	
25	11 50	11 48	11 47	11 45	11 43	11 42	11 40	11 39	11 37	11 35	11 34	
26	11 53	11 52	11 50	11 48	11 47	11 46	11 44	11 42	11 41	11 39	11 37	
27	11 57	11 55	11 54	11 52	11 51	11 49	11 47	11 46	11 44	11 43	11 41	
28	11 1	11 59	11 57	11 56	11 54	11 53	11 51	11 49	11 48	11 46	11 45	
29	11 4	12 3	11 59	11 58	11 56	11 55	11 53	11 52	11 50	11 48	11 47	
30	11 8	12 6	12 5	12 3	12 1	12 0	11 58	11 57	11 55	11 54	11 52	

A TABLE of Right Ascensions in Time, to Five Degrees
of North and South Latitude.

North Latitude. =.							South Latitude. =.				
Degr.	5	4	3	2	1	0	1	2	3	4	5
	h	h	h	h	h	h	h	h	h	h	h
0	12 8	12 6	12 5	12 3	12 2	12 0	11 58	11 57	11 55	11 54	11 52
1	12 12	12 10	12 8	12 7	12 5	12 4	12 2	12 1	11 59	11 57	11 56
2	12 15	12 14	12 12	12 10	12 9	12 7	12 6	12 4	12 3	12 1	11 59
3	12 19	12 17	12 16	12 14	12 13	12 11	12 9	12 8	12 6	12 5	12 3
4	12 23	12 21	12 19	12 18	12 16	12 15	12 13	12 12	12 10	12 8	12 7
5	12 26	12 25	12 23	12 21	12 20	12 18	12 17	12 15	12 14	12 12	12 10
6	12 30	12 28	12 27	12 25	12 24	12 22	12 20	12 19	12 17	12 16	12 14
7	12 34	12 32	12 30	12 29	12 27	12 26	12 24	12 23	12 21	12 19	12 18
8	12 37	12 36	12 34	12 33	12 31	12 29	12 28	12 26	12 25	12 23	12 21
9	12 41	12 39	12 38	12 36	12 35	12 33	12 31	12 30	12 28	12 27	12 25
10	12 45	12 43	12 42	12 40	12 38	12 37	12 35	12 34	12 32	12 30	12 29
11	12 48	12 47	12 45	12 44	12 42	12 40	12 39	12 37	12 36	12 34	12 32
12	12 52	12 51	12 49	12 47	12 46	12 44	12 43	12 41	12 39	12 38	12 36
13	12 56	12 54	12 53	12 51	12 49	12 48	12 46	12 44	12 43	12 41	12 40
14	12 59	12 58	12 56	12 55	12 53	12 52	12 50	12 48	12 47	12 45	12 44
15	13 3	13 1	13 0	12 58	12 57	12 55	12 54	12 52	12 51	12 49	12 48
16	13 7	13 5	13 4	13 2	13 0	12 59	12 57	12 56	12 54	12 53	12 52
17	13 10	13 9	13 7	13 6	13 4	13 3	13 1	13 0	12 58	12 56	12 55
18	13 14	13 12	13 11	13 9	13 8	13 6	13 5	13 3	13 2	13 0	12 59
19	13 18	13 16	13 15	13 13	13 12	13 10	13 9	13 7	13 5	13 4	13 2
20	13 21	13 20	13 18	13 17	13 15	13 14	13 12	13 11	13 9	13 8	13 6
21	13 25	13 24	13 22	13 20	13 19	13 18	13 16	13 14	13 13	13 11	13 10
22	13 29	13 27	13 26	13 24	13 23	13 21	13 20	13 18	13 17	13 15	13 14
23	13 32	13 31	13 30	13 28	13 27	13 26	13 24	13 23	13 21	13 19	13 17
24	13 36	13 35	13 33	13 32	13 30	13 29	13 27	13 26	13 24	13 23	13 21
25	13 40	13 39	13 37	13 36	13 34	13 33	13 32	13 30	13 28	13 27	13 25
26	13 44	13 42	13 41	13 39	13 38	13 36	13 35	13 33	13 32	13 30	13 29
27	13 47	13 46	13 45	13 43	13 42	13 40	13 39	13 37	13 36	13 34	13 33
28	13 51	13 50	13 48	13 47	13 45	13 44	13 43	13 41	13 40	13 38	13

North Latitude. m.						South Latitude. m.					
Degr.	5	4	3	2	1	0	1	2	3	4	5
	h	h	h	h	h	h	h	h	h	h	h
0	13 59	13 57	13 56	13 55	13 53	13 52	13 50	13 49	13 47	13 46	13 44
1	14 2	14 1	13 59	13 58	13 56	13 55	13 54	13 53	13 51	13 50	13 48
2	14 6	14 5	14 3	14 2	14 0	13 59	13 58	13 56	13 55	13 54	13 52
3	14 10	14 9	14 7	14 6	14 4	14 3	14 2	14 0	13 59	13 58	13 56
4	14 14	14 12	14 11	14 10	14 8	14 7	14 6	14 4	14 3	14 1	14 0
5	14 18	14 16	14 15	14 14	14 12	14 11	14 9	14 8	14 7	14 5	14 4
6	14 21	14 20	14 19	14 17	14 16	14 15	14 13	14 12	14 11	14 9	14 8
7	14 25	14 24	14 23	14 21	14 20	14 19	14 17	14 16	14 14	14 13	14 12
8	14 29	14 28	14 26	14 25	14 24	14 23	14 21	14 20	14 18	14 17	14 16
9	14 33	14 32	14 30	14 29	14 28	14 26	14 25	14 24	14 22	14 21	14 20
10	14 37	14 35	14 34	14 33	14 32	14 30	14 29	14 28	14 26	14 25	14 24
11	14 41	14 39	14 38	14 37	14 35	14 34	14 33	14 32	14 30	14 29	14 28
12	14 44	14 43	14 42	14 41	14 39	14 38	14 37	14 36	14 34	14 33	14 32
13	14 48	14 47	14 46	14 45	14 43	14 42	14 41	14 40	14 38	14 37	14 36
14	14 52	14 51	14 50	14 49	14 47	14 46	14 45	14 44	14 42	14 41	14 40
15	14 56	14 55	14 54	14 53	14 51	14 50	14 49	14 48	14 46	14 45	14 44
16	15 0	14 59	14 58	14 56	14 55	14 54	14 52	14 52	14 50	14 49	14 48
17	15 4	15 3	15 2	15 0	14 59	14 58	14 57	14 56	14 54	14 53	14 52
18	15 8	15 7	15 6	15 4	15 3	15 2	15 1	15 0	14 59	14 57	14 56
19	15 12	15 11	15 10	15 8	15 7	15 6	15 5	15 4	15 3	15 1	15 0
20	15 16	15 15	15 14	15 12	15 12	15 10	15 9	15 8	15 7	15 6	15 4
21	15 20	15 19	15 18	15 16	15 15	15 14	15 13	15 12	15 11	15 10	15 8
22	15 24	15 23	15 22	15 20	15 19	15 18	15 17	15 16	15 15	15 14	15 13
23	15 28	15 27	15 26	15 24	15 23	15 22	15 21	15 20	15 19	15 18	15 17
24	15 32	15 31	15 30	15 28	15 27	15 26	15 25	15 24	15 23	15 22	15 21
25	15 36	15 35	15 34	15 33	15 31	15 30	15 29	15 28	15 27	15 26	15 25
26	15 40	15 39	15 38	15 37	15 35	15 35	15 34	15 33	15 32	15 31	15 29
27	15 44	15 43	15 42	15 41	15 40	15 39	15 38	15 37	15 36	15 35	15 34
28	15 48	15 47	15 46	15 45	15 44	15 43	15 42	15 41	15 40	15 39	15 38
29	15 52	15 51	15 50	15 49	15 48	15 47	15 46	15 45	15 44	15 43	15 42
30	15 56	15 55	15 54	15 53	15 52	15 51	15 50	15 49	15 48	15 47	15 46

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

Degr.	North Latitude. †.						South Latitude. †.					
	5	4	3	2	1	0	1	2	3	4	5	
	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	h ' "	
0	15 56	15 55	15 54	15 53	15 52	15 51	15 50	15 49	15 48	15 47	15 46	
1	16 0	15 59	15 58	15 57	15 56	15 55	15 54	15 53	15 53	15 52	15 52	
2	16 4	16 3	16 2	16 1	16 0	16 0	15 59	15 58	15 57	15 56	15 55	
3	16 8	16 7	16 6	16 5	16 4	16 4	16 3	16 2	16 1	16 0	15 59	
4	16 12	16 11	16 10	16 10	16 9	16 8	16 7	16 6	16 5	16 4	16 4	
5	16 16	16 15	16 14	16 14	16 13	16 12	16 11	16 10	16 10	16 9	16 8	
6	16 20	16 19	16 19	16 18	16 17	16 16	16 15	16 15	16 14	16 13	16 12	
7	16 24	16 24	16 23	16 22	16 21	16 21	16 20	16 19	16 18	16 18	16 17	
8	16 28	16 28	16 27	16 26	16 25	16 25	16 24	16 23	16 23	16 22	16 21	
9	16 32	16 32	16 31	16 30	16 30	16 29	16 28	16 28	16 27	16 26	16 26	
10	16 36	16 36	16 35	16 35	16 34	16 33	16 32	16 32	16 31	16 31	16 30	
11	16 41	16 40	16 39	16 39	16 38	16 38	16 37	16 36	16 36	16 35	16 34	
12	16 45	16 44	16 44	16 43	16 43	16 42	16 41	16 40	16 40	16 39	16 39	
13	16 49	16 48	16 48	16 47	16 47	16 46	16 45	16 45	16 45	16 44	16 43	
14	16 53	16 52	16 52	16 52	16 51	16 51	16 50	16 49	16 49	16 48	16 48	
15	16 57	16 57	16 56	16 56	16 55	16 55	16 54	16 54	16 53	16 53	16 52	
16	17 1	17 1	17 0	17 0	17 0	16 59	16 58	16 58	16 58	16 57	16 57	
17	17 6	17 5	17 5	17 4	17 4	17 3	17 3	17 2	17 2	17 2	17 1	
18	17 10	17 9	17 9	17 9	17 8	17 8	17 8	17 7	17 7	17 6	17 6	
19	17 14	17 14	17 13	17 13	17 12	17 12	17 12	17 11	17 11	17 11	17 10	
20	17 18	17 18	17 17	17 17	17 17	17 16	17 16	17 15	17 15	17 15	17 15	
21	17 22	17 22	17 22	17 21	17 21	17 21	17 20	17 19	17 19	17 19	17 19	
22	17 26	17 26	17 26	17 26	17 25	17 25	17 24	17 24	17 24	17 24	17 23	
23	17 31	17 30	17 30	17 30	17 30	17 29	17 28	17 28	17 28	17 28	17 28	
24	17 35	17 35	17 34	17 34	17 34	17 34	17 33	17 33	17 33	17 33	17 32	
25	17 40	17 39	17 39	17 38	17 38	17 38	17 37	17 37	17 37	17 37	17 37	
26	17 43	17 43	17 43	17 43	17 43	17 43	17 42	17 42	17 42	17 42	17 41	
27	17 48	17 47	17 47	17 47	17 47	17 47	17 46	17 46	17 46	17 46	17 45	
28	17 53	17 53	17 52	17 52	17 52	17 51	17 50	17 50	17 50	17 50	17 50	
29	17 56	17 56	17 56	17 56	17 56	17 56	17 55	17 54	17 54	17 54	17 54	
30	18 0	18 0	18 0	18 0	18 0	18 0	18 0	18 0	18 0	18 0	18 0	

A TABLE of Right Ascensions in Time, to Five Degrees of North and South Latitude.

Degr.	North Latitude. \approx .						South Latitude. \approx .					
	5	4	3	2	1	0	1	2	3	4	5	
0	20 4	20 5	20 6	20 7	20 8	20 9	20 10	20 11	20 11	20 12	20 13	
1	20 8	20 9	20 10	20 11	20 12	20 13	20 14	20 15	20 16	20 17	20 18	
2	20 12	20 13	20 14	20 15	20 16	20 17	20 18	20 19	20 20	20 21	20 22	
3	20 16	20 17	20 18	20 19	20 20	20 21	20 22	20 23	20 24	20 25	20 26	
4	20 20	20 21	20 22	20 23	20 24	20 25	20 26	20 27	20 28	20 29	20 30	
5	20 24	20 25	20 26	20 27	20 28	20 29	20 31	20 32	20 33	20 34	20 35	
6	20 28	20 29	20 30	20 31	20 33	20 34	20 35	20 36	20 37	20 38	20 39	
7	20 32	20 33	20 34	20 36	20 37	20 38	20 39	20 40	20 41	20 42	20 43	
8	20 36	20 37	20 38	20 40	20 41	20 42	20 43	20 44	20 45	20 46	20 47	
9	20 40	20 41	20 42	20 44	20 45	20 46	20 47	20 48	20 49	20 50	20 52	
10	20 44	20 45	20 46	20 48	20 49	20 50	20 51	20 52	20 53	20 54	20 56	
11	20 48	20 49	20 50	20 52	20 53	20 54	20 55	20 56	20 57	20 59	21 0	
12	20 52	20 53	20 54	20 56	20 57	20 58	20 59	21 0	21 1	21 3	21 4	
13	20 56	20 57	20 58	21 0	21 1	21 2	21 3	21 4	21 5	21 7	21 8	
14	21 0	21 1	21 2	21 4	21 5	21 6	21 7	21 8	21 10	21 11	21 12	
15	21 4	21 5	21 6	21 7	21 9	21 10	21 11	21 12	21 14	21 15	21 16	
16	21 8	21 9	21 10	21 11	21 13	21 14	21 15	21 16	21 18	21 19	21 20	
17	21 12	21 13	21 14	21 15	21 17	21 18	21 19	21 20	21 22	21 23	21 24	
18	21 16	21 17	21 18	21 19	21 21	21 22	21 23	21 24	21 26	21 27	21 28	
19	21 19	21 21	21 22	21 23	21 24	21 26	21 27	21 28	21 30	21 31	21 32	
20	21 23	21 25	21 26	21 27	21 28	21 30	21 31	21 32	21 34	21 35	21 36	
21	21 27	21 29	21 30	21 31	21 32	21 34	21 35	21 36	21 38	21 39	21 40	
22	21 31	21 32	21 34	21 35	21 36	21 38	21 39	21 40	21 42	21 43	21 44	
23	21 35	21 36	21 37	21 39	21 40	21 41	21 43	21 44	21 46	21 47	21 48	
24	21 39	21 40	21 41	21 43	21 44	21 45	21 47	21 48	21 49	21 51	21 52	
25	21 42	21 44	21 45	21 46	21 48	21 49	21 51	21 52	21 53	21 55	21 56	
26	21 46	21 48	21 49	21 50	21 52	21 53	21 54	21 56	21 57	21 59	22 0	
27	21 50	21 52	21 53	21 54	21 56	21 57	21 58	22 0	22 1	22 3	22 4	
28	21 54	21 55	21 57	21 58	21 59	22 1	22 2	22 4	22 5	22 6	22 8	
29	21 57	21 59	22 0	22 2	22 3	22 5	22 6	22 7	22 9	22 10	22 12	
30	22 1	22 3	22 4	22 6	22 7	22 8	22 10	22 11	22 13	22 14	22 16	

North Latitude. κ .										South Latitude. κ .												
Degt.	5		4		3		2		1		0		1		2		3		4		5	
	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'	h	'
0	22	1	22	3	22	4	22	6	22	7	22	8	22	10	22	11	22	13	22	14	22	16
1	22	5	22	7	22	8	22	9	22	11	22	12	22	14	22	15	22	17	22	18	22	20
2	22	9	22	10	22	12	22	13	22	14	22	16	22	18	22	19	22	20	22	22	22	23
3	22	13	22	14	22	15	22	17	22	18	22	20	22	21	22	23	22	24	22	26	22	27
4	32	16	22	18	22	19	22	21	22	22	22	24	22	25	22	27	22	28	22	30	22	31
5	22	20	22	21	22	23	22	24	22	26	22	27	22	29	22	30	22	32	22	33	22	35
6	22	24	22	25	22	27	22	28	22	30	22	31	22	33	22	34	22	36	22	37	22	39
7	22	27	22	29	22	30	22	32	22	33	22	35	22	36	22	38	22	39	22	41	22	41
8	22	31	22	33	22	34	22	36	22	37	22	39	22	40	22	42	22	43	22	45	22	46
9	22	35	22	36	22	38	22	39	22	41	22	42	22	44	22	45	22	47	22	49	22	50
10	22	39	22	40	22	42	22	43	22	45	22	46	22	48	22	49	22	51	22	52	22	54
11	22	42	22	44	22	45	22	47	22	49	22	50	22	51	22	53	22	55	22	56	22	58
12	22	46	22	48	22	49	22	51	22	52	22	54	22	55	22	57	22	58	23	0	23	1
13	22	50	22	51	22	53	22	54	22	56	22	57	22	59	23	1	23	2	23	3	23	5
14	22	53	22	55	22	56	22	58	23	0	23	1	23	3	23	4	23	6	23	7	23	9
15	22	57	22	59	23	0	23	2	23	3	23	5	23	6	23	8	23	9	23	11	23	13
16	23	1	23	2	23	4	23	5	23	7	23	8	23	10	23	12	23	13	23	15	23	16
17	23	4	23	6	23	7	23	9	23	11	23	12	23	14	23	15	23	17	23	18	23	20
18	23	8	23	10	23	11	23	13	23	14	23	16	23	18	23	19	23	21	23	22	23	24
19	23	12	23	13	23	15	23	16	23	18	23	20	23	21	23	23	23	24	23	26	23	28
20	23	16	23	17	23	19	23	20	23	22	23	23	23	25	23	27	23	28	23	30	23	32
21	23	19	23	21	23	22	23	24	23	25	23	27	23	29	23	30	23	32	23	33	23	35
22	23	23	23	24	23	26	23	27	23	29	23	31	23	32	23	34	23	35	23	37	23	

North Latitude. γ .										South Latitude. γ .													
Degt.	5		4		3		2		1		0		1		2		3		4		5		
	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	
0	23	27	23	34	23	40	23	47	23	53	0	0	0	6	0	13	0	19	0	26	0	32	
1	23	29	23	36	23	42	23	48	23	55	0	1	0	8	0	14	0	21	0	27	0	34	
2	23	30	23	37	23	44	23	50	23	57	0	3	0	9	0	16	0	22	0	29	0	35	
3	23	32	23	39	23	45	23	52	23	58	0	4	0	11	0	17	0	24	0	30	0	37	
4	23	33	23	40	23	47	23	53	24	0	0	6	0	12	0	19	0	26	0	32	0	39	
5	23	35	23	42	23	48	23	55	0	1	0	8	0	14	0	21	0	27	0	33	0	40	
6	23	36	23	43	23	50	23	56	0	3	0	9	0	16	0	22	0	29	0	35	0	42	
7	23	38	23	45	23	51	23	58	0	4	0	11	0	17	0	24	0	30	0	37	0	43	
8	23	39	23	46	23	53	23	59	0	6	0	12	0	19	0	25	0	32	0	38	0	45	
9	23	41	23	48	23	54	0	1	0	7	0	14	0	20	0	27	0	33	0	40	0	47	
10	23	43	23	49	23	56	0	2	0	9	0	15	0	22	0	28	0	35	0	41	0	48	
11	23	44	23	51	23	57	0	4	0	11	0	17	0	23	0	30	0	37	0	43	0	50	
12	23	46	23	52	23	59	0	5	0	22	0	19	0	25	0	32	0	38	0	45	0	51	
13	23	47	23	54	0	2	0	7	0	14	0	20	0	27	0	33	0	40	0	46	0	53	
14	23	49	23	55	0	4	0	9	0	15	0	22	0	28	0	35	0	42	0	48	0	54	
15	2	35	0	23	57	0	5	0	10	0	17	0	23	0	30	0	37	0	43	0	50	0	56
16	23	52	23	58	0	7	0	12	0	19	0	25	0	32	0	38	0	45	0	51	0	58	
17	23	53	0	0	0	8	0	13	0	20	0	27	0	33	0	40	0	46	0	53	0	59	
18	23	55	0	2	0	10	0	15	0	22	0	28	0	35	0	41	0	48	0	54	1	1	
19	23	56	0	3	0	12	0	17	0	23	0	30	0	36	0	43	0	50	0	56	1	2	
20	23	58	0	5	0	13	0	18	0	25	0	32	0	38	0	45	0	51	0	58	1	4	
21	23	59	0	6	0	15	0	20	0	27	0	33	0	40	0	47	0	53	1	0	1	6	
22	0	1	0	8	0	16	0	21	0	28	0	35	0	42	0	48	0	55	1	1	1	8	
23	0	2	0	9	0	18	0	23	0	30	0	37	0	43	0	50	0	56	1	3	1	9	
24	0	4																					

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

North Latitude. 8.							South Latitude. 8.				
Degr.	5	4	3	2	1	0	1	2	3	4	5
	h	h	h	h	h	h	h	h	h	h	h
00	140	210	280	350	420	500	561	21	91	161	22
10	150	230	300	370	440	510	581	41	111	181	24
20	170	240	320	390	460	520	591	61	131	191	26
30	190	260	330	400	470	541	11	81	151	211	28
40	200	280	350	420	490	561	31	101	171	231	30
50	220	300	370	440	510	581	51	121	191	251	32
60	240	310	390	460	531	01	71	141	211	271	34
70	260	330	410	480	551	21	91	161	231	291	36
80	270	350	420	500	571	41	111	181	251	311	38
90	290	370	440	520	591	61	131	201	271	331	40
100	310	390	460	541	11	81	151	221	291	351	42
110	330	410	480	561	31	101	171	241	311	371	44
120	340	420	500	581	51	121	191	261	331	401	46
130	360	440	521	01	71	141	211	281	351	421	49
140	380	460	541	21	91	161	231	301	371	441	51
150	400	480	591	41	111	181	251	331	391	461	53
160	420	500	581	61	131	201	281	351	421	491	55
170	440	521	01	81	151	231	301	371	441	511	58
180	460	541	21	101	181	251	321	391	461	532	0
190	480	561	41	121	201	271	341	411	491	552	2
200	500	581	71	141	221	291	371	441	511	582	5
210	521	11	91	161	241	321	391	461	532	02	7
220	541	31	111	191	261	341	411	491	562	32	9
230	571	51	131	211	291	361	441	511	582	52	12
240	591	71	151	231	311	381	461	532	12	72	14
251	11	101	181	261	341	411	491	562	32	102	17
261	31	121	201	281	361	441	511	592	62	132	20
271	61	141	231	301	391	461	542	12	82	152	22
281	81	171	251	331	411	491	572	42	112	182	25
291	101	191	281	361	441	521	592	72	142	212	28
301	131	221	301	391	461	542	22	92	172	242	30

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

Degr.	North Latitude. II.						South Latitude. II.					
	5	4	3	2	I	0	I	2	3	4	5	
0	I 13	I 22	I 30	I 39	I 47	I 54	2 22	4 2	16 2	24 2	30	
1	I 15	I 24	I 33	I 41	I 49	I 57	2 5	12 2	19 2	26 2	33	
2	I 18	I 27	I 35	I 44	I 52	2 0	2 7	15 2	22 2	29 2	36	
3	I 21	I 30	I 38	I 46	I 55	2 3	10 2	18 2	25 2	32 2	39	
4	I 23	I 32	I 41	I 49	I 58	2 6	13 2	21 2	28 2	35 2	42	
5	I 26	I 35	I 44	I 52	2 1	2 8	16 2	24 2	31 2	38 2	45	
6	I 29	I 38	I 47	I 55	2 3	11 2	19 2	26 2	34 2	41 2	48	
7	I 32	I 41	I 50	I 58	2 6	14 2	22 2	24 2	37 2	44 2	51	
8	I 34	I 44	I 53	2 1	2 9	17 2	25 2	33 2	40 2	47 2	54	
9	I 37	I 47	I 56	2 4	12 2	21 2	28 2	36 2	43 2	50 2	57	
10	I 40	I 50	I 59	2 7	16 2	24 2	31 2	39 2	46 2	53 3	0	
11	I 43	I 53	2 2	11 2	19 2	27 2	34 2	42 2	49 2	57 3	4	
12	I 47	I 56	2 5	14 2	22 2	30 2	38 2	45 2	53 3	0 3	7	
13	I 50	I 59	2 8	17 2	25 2	33 2	41 2	49 2	56 3	3 3	10	
14	I 53	2 3	12 2	20 2	29 2	37 2	45 2	52 3	0 3	7 3	14	
15	I 56	2 6	15 2	24 2	32 2	40 2	48 2	56 3	3 3	10 3	17	
16	2 0	10 2	19 2	27 2	36 2	44 2	52 2	59 3	7 3	14 3	21	
17	2 3	13 2	22 2	31 2	39 2	47 2	55 3	3 3	10 3	17 3	24	
18	2 7	17 2	26 2	34 2	43 2	51 2	59 3	6 3	14 3	21 3	28	
19	2 11	20 2	29 2	38 2	47 2	55 3	3 3	10 3	17 3	24 3	31	
20	2 14	24 2	33 2	42 2	50 2	58 3	6 3	14 3	21 3	28 3	35	
21	2 18	28 2	37 2	46 2	54 3	2 3	10 3	17 3	25 3	32 3	39	
22	2 22	32 2	41 2	49 2	58 3	6 3	14 3	21 3	28 3	36 3	42	
23	2 26	36 2	45 2	53 3	2 3	10 3	18 3	25 3	32 3	39 3	46	
24	2 30	40 2	49 2	57 3	6 3	14 3	22 3	29 3	36 3	43 3	50	
25	2 34	44 2	53 3	2 3	10 3	18 3	26 3	33 3	40 3	47 3	54	
26	2 38	48 2	57 3	6 3	14 3	22 3	30 3	37 3	44 3	51 3	58	
27	2 42	52 3	1 3	10 3	18 3	26 3	34 3	41 3	48 3	55 4	2	
28	2 47	56 3	6 3	14 3	22 3	30 3	38 3	45 3	53 3	59 4	6	
29	2 51	1 3	10 3	19 3	27 3	35 3	42 3	49 3	57 4	4 4	10	
30	2 56	5 3	14 3	23 3	31 3	39 3	47 3	53 4	1 4	8 4	15	

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

North Latitude. S.												South Latitude. S.											
Degr.	5		4		3		2		1		0		1		2		3		4		5		
	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	
0	2	56	3	0	5	3	14	3	23	3	31	3	39	3	47	3	54	4	1	4	8	4	15
1	3	0	3	0	10	3	19	3	27	3	36	3	43	3	51	3	58	4	5	4	12	4	19
2	3	0	5	3	14	3	23	3	32	3	40	3	48	3	55	4	3	4	10	4	17	4	23
3	3	0	9	3	19	3	28	3	37	3	45	3	52	4	0	4	7	4	14	4	21	4	27
4	3	1	4	3	24	3	33	3	41	3	49	3	57	4	4	4	12	4	19	4	25	4	32
5	3	1	9	3	29	3	38	3	46	3	54	4	2	4	9	4	16	4	23	4	30	4	36
6	3	2	4	3	34	3	42	3	51	3	59	4	6	4	14	4	21	4	28	4	34	4	41
7	3	2	9	3	39	3	47	3	55	4	3	4	11	4	18	4	25	4	32	4	39	4	45
8	3	3	4	3	44	3	52	4	0	4	8	4	16	4	23	4	30	4	37	4	43	4	50
9	3	3	9	3	48	3	57	4	5	4	13	4	21	4	28	4	35	4	41	4	48	4	54
10	3	4	5	3	54	4	2	4	10	4	18	4	25	4	33	4	40	4	46	4	53	4	59
11	3	5	0	3	59	4	7	4	15	4	23	4	30	4	38	4	44	4	51	4	57	5	4
12	3	5	5	4	4	4	13	4	20	4	28	4	35	4	42	4	49	4	56	5	2	5	8
13	4	1	4	4	10	4	18	4	26	4	33	4	40	4	48	4	54	5	1	5	7	5	13
14	4	1	6	4	15	4	23	4	31	4	38	4	45	4	52	4	59	5	6	5	12	5	18
15	4	1	2	4	20	4	28	4	36	4	44	4	51	4	57	5	4	5	10	5	17	5	23
16	4	1	7	4	26	4	34	4	41	4	49	4	56	5	2	5	9	5	15	5	22	5	28
17	4	2	3	4	31	4	39	4	47	4	54	5	1	5	8	5	14	5	20	5	27	5	33
18	4	2	9	4	37	4	45	4	52	4	59	5	6	5	13	5	19	5	25	5	32	5	37
19	4	3	4	4	43	4	50	4	58	5	5	5	12	5	18	5	24	5	31	5	37	5	42
20	4	4	0	4	48	4	56	5	3	5	10	5	17	5	23	5	30	5	36	5	42	5	47
21	4	4	6	4	54	5	1	5	9	5	16	5	22	5	29	5	35	5	41	5	47	5	52
22	4	5	2	5	0	5	7	5	14	5	21	5	28	5	34	5	40	5	46	5	52	5	57
23	4	5	8	5	5	5	13	5	20	5	27	5	33	5	39	5	45	5	51	5	57	6	3
24	5	4	5	5	11	5	18	5	25	5	32	5	39	5	45	5	51	5	56	6	2	6	8
25	5	10	5	5	17	5	24	5	31	5	38	5	44	5	50	5	56	6	2	6	7	6	13
26	5	16	5	5	23	5	30	5	37	5	43	5	49	5	56	6	1	6	7	6	13	6	18
27	5	22	5	5	29	5	36	5	42	5	49	5	55	6	1	6	7	6	13	6	18	6	23
28	5	28	5	5	35	5	42	5	48	5	54	6	1	6	7	6	12	6	18	6	23	6	28
29	5	34	5	5	41	5	48	5	54	6	0	6	6	6	12	6	18	6	23	6	29	6	33
30	5	40	5	5	47	5	53	6	0	6	6	6	12	6	18	6	23	6	29	6	34	6	38

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

Degr.	North Latitude. α .						South Latitude. α .					
	5	4	3	2	1	0	1	2	3	4	5	
	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	h ' h	
05	405	475	536	06	66	126	186	236	296	346	37	
15	465	535	596	66	126	186	236	296	346	396	44	
25	525	596	5	116	176	236	296	346	396	456	50	
35	586	56	116	176	236	296	346	406	456	506	55	
46	46	116	176	236	296	356	406	466	516	567	1	
56	116	176	236	296	356	406	466	516	567	17	6	
66	176	236	296	356	416	466	516	577	27	67	11	
76	226	296	356	416	466	526	577	27	77	127	17	
86	296	356	416	476	526	577	37	87	137	177	22	
96	356	416	476	536	587	37	87	137	187	237	28	
106	426	476	536	597	47	97	147	197	247	297	33	
116	486	546	597	47	107	157	207	257	297	347	39	
126	547	07	57	117	167	217	267	307	357	407	44	
137	07	67	117	167	227	267	317	357	417	457	50	
147	67	127	177	227	277	327	377	417	467	517	55	
157	137	187	237	287	337	387	437	477	527	568	1	
167	197	247	297	347	397	447	497	537	588	28	6	
177	257	307	357	407	457	507	547	598	38	88	12	
187	317	377	417	467	517	568	08	48	98	138	17	
197	387	437	487	527	578	18	68	108	158	198	23	
207	447	497	547	588	38	78	128	168	208	248	29	
217	507	558	08	48	98	138	178	228	268	308	34	
227	568	18	68	108	158	198	238	278	328	368	40	
238	28	78	128	168	218	258	298	338	378	418	45	
248	88	138	188	228	268	318	358	388	438	478	51	
258	148	198	248	288	328	378	418	458	498	538	57	
268	218	258	308	348	388	428	468	518	558	589	2	
278	278	318	368	408	448	488	528	569	09	49	8	
288	338	378	428	468	508	548	589	29	69	109	13	
298	398	438	488	528	569	09	49	89	129	159	19	
308	458	498	548	589	29	69	109	139	179	219	25	

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

Degr.	North Latitude. \approx .						South Latitude. \approx .					
	5	4	3	2	1	0	1	2	3	4	5	
	h	h	h	h	h	h	h	h	h	h	h	
0	11 43	11 47	11 50	11 53	11 57	12 0	12 3	12 7	12 10	12 13	12 17	
1	11 49	11 53	11 56	11 59	12 3	12 6	12 9	12 12	12 16	12 19	12 22	
2	11 55	11 58	12 2	12 5	12 8	12 11	12 15	12 18	12 21	12 25	12 28	
3	12 1	12 4	12 8	12 11	12 14	12 17	12 21	12 24	12 27	12 31	12 34	
4	12 7	12 10	12 13	12 16	12 20	12 23	12 26	12 30	12 33	12 36	12 40	
5	12 12	12 16	12 19	12 22	12 26	12 29	12 32	12 36	12 39	12 42	12 46	
6	12 18	12 22	12 25	12 28	12 31	12 35	12 38	12 41	12 45	12 48	12 51	
7	12 24	12 27	12 31	12 35	12 37	12 40	12 44	12 47	12 50	21 54	12 57	
8	12 30	12 33	12 36	12 40	12 43	12 46	12 50	12 53	12 56	13 0	13 3	
9	12 35	12 39	12 42	12 45	12 49	12 52	12 56	12 59	13 2	13 6	13 9	
10	12 41	12 45	12 48	12 51	12 55	12 58	13 1	13 5	13 8	13 11	13 15	
11	12 47	12 50	12 54	12 57	13 0	13 4	13 7	13 10	13 14	13 18	13 21	
12	12 53	12 56	12 59	13 3	13 6	13 10	13 13	13 16	13 20	13 23	13 27	
13	12 59	13 2	13 5	13 8	13 12	13 15	13 19	13 21	13 26	13 29	13 33	
14	13 4	13 8	13 11	13 14	13 18	13 21	13 25	13 28	13 31	13 35	13 39	
15	13 10	13 13	13 17	13 20	13 23	13 27	13 30	13 34	13 37	13 41	13 44	
16	13 16	13 19	13 22	13 26	13 29	13 33	13 36	13 40	13 43	13 47	13 50	
17	13 21	13 25	13 28	13 32	13 35	13 38	13 42	13 45	13 49	13 53	13 56	
18	13 27	13 30	13 34	13 37	13 41	13 44	13 48	13 50	13 55	13 59	14 2	
19	13 33	13 36	13 40	13 43	13 47	13 50	13 54	13 57	14 1	14 5	14 8	
20	13 38	13 42	13 45	13 49	13 52	13 56	13 59	14 3	14 7	14 10	14 14	
21	13 44	13 48	13 51	13 55	13 58	14 2	14 5	14 9	14 13	14 16	14 20	
22	13 50	13 53	13 57	14 0	14 4	14 8	14 11	14 15	14 19	14 22	14 26	
23	13 56	13 59	14 3	14 6	14 10	14 13	14 17	14 21	14 25	14 28	14 32	
24	14 1	14 5	14 8	14 12	14 16	14 19	14 23	14 27	14 31	14 34	14 38	
25	14 7	14 11	14 14	14 18	14 21	14 25	14 29	14 33	14 36	14 40	14 44	
26	14 13	14 16	14 20	14 24	14 27	14 32	14 35	14 39	14 42	14 46	14 50	
27	14 18	14 22	14 26	14 29	14 33	14 37	14 41	14 45	14 48	14 52	14 57	
28	14 24	14 28	14 31	14 35	14 39	14 43	14 47	14 50	14 54	14 58	15 3	
29	14 30	14 33	14 37	14 41	14 45	14 48	14 52	14 56	15 0	15 5	15 9	
30	14 35	14 39	14 43	14 47	14 50	14 54	14 59	15 2	15 6	15 11	15 15	

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

	North Latitude. φ .					South Latitude. φ .					
Degr.	5	4	3	2	1	0	1	2	3	4	5
	h	h	h	h	h	h	h	h	h	h	h
0	19 45	19 52	19 59	20 6	20 13	20 21	20 29	20 37	20 46	20 55	21 4
1	19 50	19 56	20 3	20 11	20 18	20 25	20 33	20 41	20 50	20 59	21 9
2	19 54	20 1	20 7	20 15	20 22	20 30	20 38	20 46	20 54	21 4	21 13
3	19 58	20 5	20 12	20 19	20 26	20 34	20 42	20 50	20 59	21 8	21 18
4	20 2	20 9	20 16	20 23	20 30	20 38	20 46	20 54	21 3	21 12	21 32
5	20 6	00 13	20 20	20 27	20 34	20 42	20 50	20 58	21 7	21 16	21 26
6	20 10	20 17	20 24	20 31	20 38	20 46	20 54	21 3	21 11	21 20	21 30
7	20 14	20 21	20 28	20 35	20 42	20 50	20 58	21 7	21 15	21 24	21 34
8	20 18	20 24	20 32	20 39	20 46	20 54	21 2	21 11	21 19	21 28	21 38
9	20 21	20 28	20 35	20 43	20 50	20 58	21 6	21 14	21 23	21 32	21 42
10	20 25	20 32	20 39	20 46	20 54	21 2	21 10	21 18	21 27	21 36	21 46
11	20 29	20 36	20 43	20 50	20 57	21 5	21 13	21 22	21 31	21 40	21 49
12	20 33	20 39	20 46	20 54	21 1	21 9	21 17	21 26	21 34	21 43	21 53
13	20 36	20 43	20 50	20 57	21 5	21 13	21 21	21 29	21 38	21 47	21 57
14	20 39	20 46	20 53	21 1	21 8	21 16	21 24	21 33	21 41	21 50	22 0
15	20 43	20 50	20 57	21 4	21 12	21 20	21 28	21 36	21 45	21 54	22 4
16	20 46	20 53	21 0	21 8	21 15	21 23	21 31	21 40	21 48	21 57	22 7
17	20 50	20 57	21 4	21 11	21 19	21 27	21 35	21 43	21 52	22 1	22 10
18	20 53	21 0	21 7	21 15	21 22	21 30	21 38	21 46	21 55	22 4	22 13
19	20 56	21 3	21 11	21 18	21 26	21 33	21 41	21 49	21 58	22 7	22 17
20	21 0	21 7	21 14	21 22	21 29	21 36	21 44	21 53	22 1	22 10	22 20
21	21 3	21 10	21 17	21 24	21 32	21 39	21 48	21 56	22 4	22 13	22 23
22	21 6	21 13	21 20	21 27	21 35	21 43	21 51	21 59	22 7	22 16	22 26
23	21 9	21 16	21 23	21 31	21 38	21 46	21 54	22 2	22 10	22 19	22 29
24	21 12	21 19	21 26	21 34	21 41	21 49	21 57	22 5	22 13	22 22	22 31
25	21 15	21 22	21 29	21 36	21 44	21 52	21 59	22 8	22 16	22 25	22 34
26	21 18	21 25	21 32	21 39	21 47	21 54	22 2	22 11	22 19	22 27	22 37
27	21 21	21 28	21 35	21 42	21 50	21 57	22 5	22 14	22 22	22 30	22 39
28	21 24	21 31	21 38	21 45	21 53	22 0	22 8	22 16	22 25	22 33	22 42
29	21 27	21 34	21 41	21 48	21 55	22 3	22 11	22 19	22 27	22 36	22 45
30	21 30	21 36	21 44	21 51	21 58	22 6	22 13	22 21	22 30	22 38	22 48

A TABLE of Oblique Ascensions in Time, for the Latitude of 53 Deg. And to Five Degrees of North and South Latitude.

Degr.	North Latitude. x.						South Latitude. x.					
	5	4	3	2	1	0	1	2	3	4	5	
0	22 38	22 44	22 51	22 58	23 4	23 11	23 18	23 25	23 32	23 39	23 46	
1	22 40	22 46	22 53	22 59	23 6	23 13	23 20	23 27	23 34	23 41	23 48	
2	22 42	22 48	22 55	23 1	23 8	23 15	23 22	23 28	23 35	23 42	23 50	
3	22 44	22 50	22 56	23 3	23 10	23 17	23 23	23 30	23 37	23 44	23 51	
4	22 45	22 52	22 58	23 5	23 11	23 18	23 25	23 32	23 39	23 46	23 53	
5	22 47	22 53	23 0	23 7	23 13	23 20	23 27	23 34	23 40	23 47	23 54	
6	22 49	22 55	23 2	23 8	23 15	23 22	23 28	23 35	23 42	23 49	23 56	
7	22 51	22 57	23 4	23 10	23 17	23 23	23 30	23 37	23 44	23 51	23 58	
8	22 52	22 59	23 5	23 12	23 18	23 25	23 32	23 39	23 45	23 52	23 59	
9	22 54	23 0	23 7	23 13	23 20	23 27	23 33	23 40	23 47	23 54	0 1	
10	22 56	23 2	23 9	23 15	23 22	23 28	23 35	23 42	23 48	23 55	0 2	
11	22 58	23 4	23 10	23 17	23 24	23 30	23 37	23 43	23 50	23 57	0 4	
12	22 59	23 6	23 12	23 19	23 25	23 32	23 38	23 45	23 52	23 58	0 5	
13	23 1	23 7	23 14	23 20	23 27	23 33	23 40	23 47	23 53	0 0	0 7	
14	23 2	23 9	23 15	23 22	23 28	23 35	23 41	23 48	23 55	0 20	0 8	
15	23 4	23 10	23 17	23 23	23 30	23 37	23 43	23 50	23 56	0 30	0 10	
16	23 6	23 12	23 18	23 25	23 32	23 38	23 45	23 51	23 58	0 50	0 11	
17	23 7	23 14	23 20	23 27	23 33	23 40	23 46	23 53	0 0	0 60	0 13	
18	23 9	23 15	23 22	23 28	23 35	23 41	23 48	23 55	0 10	0 80	0 14	
19	23 10	23 17	23 23	23 30	23 37	23 43	23 49	23 56	0 30	0 90	0 16	
20	23 12	23 19	23 25	23 32	23 38	23 45	23 51	23 58	0 40	0 110	0 17	
21	23 13	23 20	23 27	23 33	23 40	23 46	23 53	23 59	0 60	0 120	0 19	
22	23 15	23 22	23 28	23 35	23 41	23 48	23 54	0 10	0 70	0 140	0 21	
23	23 17	23 23	23 30	23 36	23 43	23 49	23 56	0 20	0 90	0 150	0 22	
24	23 18	23 25	23 31	23 38	23 44	23 51	23 57	0 40	0 100	0 170	0 24	
25	23 20	23 27	23 33	23 39	23 46	23 52	23 59	0 50	0 120	0 180	0 25	
26	23 21	23 28	23 34	23 41	23 48	23 54	24 00	0 70	0 130	0 200	0 27	
27	23 23	23 30	23 36	23 43	23 49	23 56	0 20	0 80	0 150	0 210	0 28	
28	23 25	23 31	23 38	23 44	23 51	23 57	0 30	0 100	0 160	0 230	0 30	
29	23 26	23 33	23 39	23 46	23 52	23 59	0 50	0 120	0 180	0 240	0 31	
30	23 28	23 34	23 41	23 47	23 53	24 00	0 60	0 130	0 190	0 260	0 33	

FINIS.

SCIENTIA STELLARUM:

OR, THE

Starry Science

Expofed in the Calculation of the

Planets Places,

BOTH IN

LONGITUDE and LATITUDE,

For any Time,

Past, Present, or to Come :

AS ALSO,

The Doctrine of Eclipses and Places of the Fixed Stars:

All Performed from

New and Accurate TABLES,

Which are Grounded upon the Best and moſt Rational Observations of former Ages ; And more particularly Adjusted to the moſt Correct Observations of this Preſent Age : And are ſo Ordered and Diſpoſed , That the Planets Places are thereby Obtain'd with much leſs Time and Pains than by any yet Extant ; and are Exhibited in a moſt Plain and Practicable Method, for the Benefit of Young CALCULATORS, as well as Others :

Being Added, As a

S U P P L E M E N T

To the Preceding

BOOK of SURVEYING.

By JOHN WING, *Math.*

L O N D O N,

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SCIENTIA STELLARUM:

O R, T H E

Starry Science,

Exposed in the Calculation of the

Planets Places, &c.

C H A P. I.

Of the Equation of Time for the Difference of Meridians.

THE Radices of the Middle Motions in these Tables are accommodated to the last Day of the *Julian* Year, under the Meridian of the Ancient and Famous City of *LONDON*, the Metropolis of *Great Britain*, whose Longitude is 24 Degrees, 20 Minutes; That therefore these Tables may Serve all Parts of the Earth, I have added a Catalogue of most of the chiefest Cities in the World, whereby the Latitude and Difference of Meridians of any Place may be had from that of *London*, which is the Primary Meridian of these Tables.

I. Therefore if it be Required to Reduce the Time given under the Meridian of *London*, to some other Meridian, seek the place desired in the Catalogue of Cities, and the Difference of Time there found, Add to, or Subtract from, the Time of *London*, according as the Titles of Addition direct, for so will the Time be reduced to the Meridian of the other Place, as was required.

E X A M P L E. I.

Suppose the Time given of the Middle of the Moon's Eclipse at *London*, be at 10 hours P. M. and it is required to Reduce the same to the Meridian of *Uraniburg*; Therefore I seek *Uraniburg* in the Catalogue, against which I find 52 Min. with the Letter A; therefore I conclude, that the middle of the said Eclipse was seen at *Uraniburg* at 10 Hours 52 Min. P.M.

II. If the Time given be under some other Meridian, it is then requisite (that the middle Motions may aright be obtain'd) to reduce the same to the Meridian of *London*; Therefore seek the Place given in the Catalogue, and the Difference of Time there found, contrary to the Title, is to be Added or Subtracted from the Time there given.

E X A M P L E. II.

Suppose the Middle of the same Eclipse had been observed at *Uraniburg*, at 10 Hours, 52 Min. Now against *Uraniburg*, (as before) I find 52 Min. A. Therefore contrary to the Title, Subtract 52 Min. and the Residue 10 Hours is the middle of the Eclipse in the Meridian of *London*.

C H A P. II.

The Use of the Table of Logistical Logarithms in Astronomical Proportions.

MULTIPLICATION is perform'd by adding the Logistical Logarithms of the two Numbers, for the Sum is the Logistical Logarithm of the Product.

Division is done by Subtracting the Logistical Logarithm of the Divisor, from the Logistical Logarithm of the Dividend, and the Remainder is the Logistical Logarithm of the Quotient.

But in these Tables, a simple Multiplication or Division is seldom required, but as it concerns the Rule of Proportion; hence for the most part we use a tacit Addition, or Subduction, of the Logarithm of an Integer, which is 1000000, which is the Radius, the Result being the Fourth Proportional.

I. E X A M.

I. Example of Division.

If 27 M. 36 S. give 1 D. or 60 M. what will 7 M. 20 S. give.

Divide $\left\{ \begin{array}{l} 7' \text{----} 20'' \text{----} \text{LL} \text{----} 9087152 \\ 27 \text{----} 36 \text{----} \text{LL} \text{----} 966276 \end{array} \right\}$ Subtract.

Quot. 15----57----LL----942439 Difference.

II. Example of Multiplication.

If 1 D. or 60 M. give 5 M. 29 S. what will 19 M. 50 S. give.

Multiply $\left\{ \begin{array}{l} 5' \text{----} 29'' \text{----} \text{LL} \text{----} 8960892 \\ 19 \text{----} 50 \text{----} \text{LL} \text{----} 951924 \end{array} \right\}$ Add.

Product 1----49----LL----848013 Sum.

The like may be used in Time also by using the Figures of Time in the Top of the Table, standing against T. H. But to make all plain, I have added Examples in all the material Cases, as followeth.

By the Logistical Logarithms.

I. To Reduce the Planets Places to any Hour and Minute of the Day, and to find the time of any Aspect, as also their Ingresses into any of the Signs.

Let it be required to find the Sun's entrance into the first Point of *Aries* 1693.

The Sun enter'd γ that year sometime on the 9th day; Hence,

The place of \odot the 9th day at Noon, is--29^o 36' 58" \times
The place of \odot the 10th day at Noon, is-- 0 36 22 γ

LL---999563----Sun's Diurnal Motion--- 0 59 24
LL---958420-----Diurnal Excess.----- 0 23 2

LL---957983 --- Sun entred γ , Mar. 9. 9 h. 7' 15" P. M.

Note, That the Diurnal Excess is found by Subtracting the Sun's place the 9th Day, from 00^o 00' 00" γ .

II. To Reduce the place of a Planet to any Hour and Minute of the Day.

Let it be required, to find the place of *Mars* the first Day of *June* for the past year 1693. at 10 h. 25 min. P. M.

The

The Determination.

Place of δ the 2d day at Noon.	4° 46' 00" 28
Place of δ the 1st day at Noon.	4 2 00 3
Diurnal Motion of δ	0 44 00-986530
Time Afternoon, 10 h. 25'.	963751
Gives 19' 6" to be added to δ 's place the 1st Day.	950281

Hence the place of δ the 1st day, at 10 h. 25' P. M. is 4° 21' 6" 8.

III. Let it be required to find the Time of any Aspect, as on the 1st day of June 1693. there happened \square of γ and γ , to find the true time thereof observe the following Work.

	γ	γ	
Jupiter and γ 1 Day-	22 7	0 19	γ pl. 1st d. at N. 22 7
Moon's Place 2 Day-	6 12	0 32	γ pl. 1st d. at N. 0 19
Moon's Diur. Motion	14 5	0 13	Diff. γ a γ fr. \square 8 12
Jupiter's Diur. Moti.	0 13		
Diurnal Excess - -	13 52		

Then by the Logistical Logarithms.

Distance Moon from the \square of γ is 8° 12'	913566
Diurnal Excess 13 52	936382
True time γ and γ 's \square is at 14 h. 11' P. M.	977184

IV. To find the Prosthaphæresis of the Sun or other Planet in the Ellipsis by the Table of Logistical Logarithms.

IV. Suppose the Anomaly be 1 S. 10° 20' 15" and the Prosthaphæresis be required, then take the Prosthaphæresis.

To { 1 S. 10° 20' 15" }	which is { 1° 16' 49"
{ 1 11 }	{ 1 18 26 }
Difference	1 37

Then by the Logistical Logarithms.

LL- - - 1' 37" - - -	-843047
LL- - - 20 15 - - -	952827
LL- - - 0 33 - - -	795874
Prosthaphæresis cor. to 1 S. 10° is	1° 16' 49".
Add	0 33
Prosthaphæresis cor. to 1 S. 10° 20' 15". is	1 87 22

V. If

V. If the Sun in One Day move 58 M. 56 S. How much moves he in 17 H. 54 M.

The Solution.

LL- - -17 H. 54'	00" - - -	-987264
LL- - - 0 58	56 - - -	-999221
LL- - - 0 43	57 - - -	-986485

By Adding the two given Logarithms, makes the Logarithm of 986485, which is the Logist. Log. of 43 M. 57 S. and so much doth the Sun move in 17 H. 54 Min.

VI. How to find the Log. of a Planet's Curt Distance from the Sun, which I shall Illustrate in the Example of *Mars*.

Anomaly of *Mars*, is - - - 9 S. 28° 12' 33"

To { 9 S. 29 D. } answers the L. of δ , { 520436
 { 9 28 } { 520382

54. Had this Number exceeded 60, I should have taken the next lesser Number to it in the second Column on the top of the Table of LL, and the Remainder on the Left Hand, and in the Angle of Meeting had been the LL sought: But because this number is under 60, I find it in the Left Hand Column, against which 54, stands the LL of 817909, to which add the LL of 12 M. 33 S. viz. 932049, and the Sum is 749658. Find this LL in the Table, and observe what Number stands over it in the second Column on the Top, and in the Column of Motion on the Left Hand, which is 0 on the Top, and 11 in the Left Hand Column; which 11 added to 520382, (the LL answering to 9 S. 28 D.) and the Sum is 520393, the Curt Distance of δ from \odot as was required.

See the Example.

LL of 54 is - - -	-817609
LL of 12' 33" - - -	-932049
LL of - - 11 } Add.	749658
520382 }	

520393 Log. Curt. Dist. δ from \odot .

There are a great many other Examples might be produced from these Logistical Logarithms; however, what other Use I shall make of them will be better done in the proper Places, especially in the Calculation of Eclipses, where they shall be further Exemplified.

C H A P. III.

*Of the Refraction and Parallax of the Sun,
Moon, and Stars.*

BEfore we come to Treat of the Use of our Tables, I shall take Notice of that gross Error in all Authors relating to the Parallax and Refraction of the Sun, Moon, and Stars.

First then ; the Refraction limited by *Ticho*, is greater in the Sun and Moon than in the Stars, which is quite Repugnant to Reason, for the Affections of the Air is doubtless the same in all of them ; and tho' the best Limitation that can be made here, and in the Regions Conterminate, is about 30 M. in the Horizon, yet the Rarity or Condensation of the Air makes them more or less, which depends upon the Cressitude thereof ; and in those Countries that are more Remote from the Sun, the Vapours of the Air must needs be more Condensed, so consequently augments the Refraction : so that the difference which *Tycho* Defined betwixt the Refraction of the Sun and Stars, arises from the Parallax of the Sun, which he made 3 M. which appears according to the Limitation here made, to be but 30 S. For he supposing the Sun to be lower then really it was, by making of it so great a Parallax, which he was forced to raise by Refraction above the Stars that have no Parallax ; and this is the reason that he makes the Horizontal Refraction of the Sun and Moon to be 33 or 34 M. and the Stars 30 M. Hence it appears, That the Sun by a Refracted Ray is seen wholly above the Horizon, when really its upper Edge doth but just touch it, neither are the Sun, Moon, and Stars free from Refraction at 45 D. Elevation, (as the Correct Observations of the Indefatigable Mr. *Flamsteed* demonstrates, from whom I received the Table of Refractions) as all or most Authors supposed, being at that height Refracted near a Minute, which none are free from, because the Refraction is not quite extinct till it approach the Vertex.

C H A P.

C H A P. IV.

To calculate the true Place of the Sun from these Tables.

THE Observations I not only make use of, but have depended upon for the framing of these New Tables, are of a different Nature from *Tycho's*; and tho' I am sure of the Sun's Meridional Distance from the *Vertex* to $\frac{1}{4}$ of a Minute or $15''$, yet I trust not to that, since an Errour of $24''$, either in the Height, or assum'd Refraction, will make a whole Minute's Errour in his Place; and therefore I make use of the times of the Transits of his Centre, and some fixed Star near the same Parallel over the Meridian, and the Star's Return; whereby the Star's Right Ascension being known, the Sun's is given, and consequently his Place, without consideration of Refraction, Parallax, or the Latitude of the Place: The Stars Places being not the same with *Tycho's*, whose Observations were faulty, by reason he wanted Glasses to apply to his Instruments, which were not found out till about 8 Years after his Decease.

Here follows an Observation, by which I shall examine these new Solar Tables, made by Mr. *Flamsteed*, at his Majesty's Observatory at *Greenwich*.

	D.	H.	'	"	
Anno 1690, March	13	0	3	51	☉ Centre Transit. the Merid.
	14	0	3	14	☉ Centre Transit. the Merid.
Procyon	14	7	9	22 $\frac{1}{2}$	Transited the Meridian.
Regulus	14	9	37	40	Transited the Meridian.
Regulus	15	9	33	26	Transited the Meridian.
Difference			4	14	

Which subtracted from 24 Hours, (a Day natural) leaveth the Length of the Syderal Day, $23\text{ h. } 55' 46''$, the Pendulum Clock told the same, and for further Confirmation was found the same the Night following. Hence the Sun's Right Ascension in the Meridian, on the 14th Day of *March*, 1690, was $3\text{ gr. } 55' 42''$, and his Place, $4\text{ gr. } 16' 56'' \text{ } \gamma$, which how our Tables agree to, we shall here examine.

First then, From the Tables of the Sun's middle Motion, collect the mean Motion and Anomaly, answering to the Year, Month, Day, Hour, Minute, and Second, (if occasion be) which Sums added, is the mean Motion and Anomaly required.

Secondly, With the Sun's Anomaly, enter the Table of his *Prosthaphæresis*, with the Sign on the Head, and the Degree descending on the Left-hand, if the Number thereof be under six Signs; But if it exceed six Signs, enter with the Sign at the Bottom, and the Degree Ascending on the Right-hand, and in the common

common Angle is the *Prosthaphæresis* and Logarithmic Number thereto, only you must remember to take the proportional part, if need require, as is shewed in Chap. II. Rule IV.

Anno 1690 March 14 Day at 0 Ho. 3' 51" in the Meridian of London, the Sun was observed in 4° 16' 56" 7.

<i>Tempus datum.</i>	Longit. S. o. ' "	☉	Anom. S. o. ' "	☉
Anno 1690	9 20 23	9	6 13 8	11
March 14 day	2 11 57	8	2 11 56	56
Min. 3		7		7
Sec. 51		2		2
The Sun's mean Motion.	0 2 20 26		8 25 5 16	
<i>Prosthaphæresis</i> Add.	1 57 18		Logar.	
			499951	
The Sun's true place.	7 4 17 44			

Diff. from
Observat.
0' 48"

The middle motion in these Tables is stated from the best Observations of all Ages, wherein Observations were made, compared with this present Age: But the *Prosthaph.* of the Sun, there being little to be grounded on from former Observations, I have only limited from the Accurate Observations of this Age, which proves the Sun's greatest Equation to be 1gr. 57' 30"

C H A P. V.

To Calculate the true place of the Moon, from these Tables.

TO the time given find the Sun's true place as is taught in the last Chapter.

2. Collect the mean motion of the Moon, her *Anomaly* and *Node*, as in the Sun.

3. With the mean *Anomaly*, enter the Table Intituled *Prosthaphæresis* in *Ellipsi*, and the Equation there found (according to the Title) being added, or Subtracted, to or from the mean *Anomaly* and the place of the Moon, giveth her true *Anomaly* and place Equated.

4. From the Equated place of the Moon, Subtract the Sun's true place, and the residue is the distance of the Moon from the Sun, which (in *Tabula Reflection.* &c.) gives the *Logarithm* of the Chord of Evection, and entering the same with their double distance, you have the *Reflection* which is to be applied to the Equated *Anomaly*, that it may be correct.

5. To find the *Synodical Anomaly* Observe, that from the Conjunction and Opposition of the Sun and Moon to the Quadrature, the

the complement of their distance to a Quadrant, is to be added to the correct *Anomaly*. But from their Quadrature to Conjunction or Opposition, the Excess of their distance above a Quadrant, is to be Subtracted from the correct *Anomaly*, and the sum or difference is the *Synodical Anomaly*.

6. From the *Logarithm* of the Chord of Evection, Subtract the *Logar.* of the Moon's distance, and the residue is the *Logarithmic* Number, with which enter the Table entitled (*Tabula Evectionis Luna*) finding the *Log.* number on the head, and the *Synodical Anomaly* in the first Column on the Left-hand, if it be less than six Signs, or on the Right-hand if more, and in the common Angle you have the Evection with its title.

7. If the Reflection and Evection be both of one denomination, their Sum, (otherwise their difference) is the absolute Secondary Equation; which being apply'd to the place of the Moon first Equated, gives her true *Longitude* in her *Orb*.

E X A M P L E.

Anno 1690, February 19th Day at 17 Hours 3' 55" Mr. *Flamsteed* Observed the Moon's Central place to be in $2^{\circ} 23' 36''$ with $4^{\circ} 46' 10''$ South Latitude, and because the Observation was made at the Observatory at *Greenwich* (it being in the same Meridian with *London*) no other time need be inquired after.

<i>Tempus datum</i>	Longit. S ° ' ''	Anomal. S ° ' ''	Node S ° ' ''
Anno 1690	9 22 33 00	1 11 20 00	0 0 8 00
February 19	9 28 49 00	9 23 15 00	0 2 38 00
Ho. 17	0 9 20 00	0 9 15 16	2 15
Min. 3	1 39	1 38	
Sec. 55	30	30	0 2 40 15
Middle Motion >	8 00 44	9 11 13 52 24	11 27 27 45
<i>Prosthaph.</i> Add	1 20 6	1 20 6	> Node
Motion > Equat.	8 2 4 15	11 15 12 30	Anom. Equat.
Sun's place	11 12 8 12	13 56	Reflect. Add
Distance > ☉	8 19 56 3	11 15 26 26	Anom. Corr.
Double distance	5 9 52 6	10 3 52	Distance Add
2d. Equation Add	24 36	11 25 30 18	Synod. Anom.
Moon in her Orb	8 2 28 51		
Node > Substr.	11 26 56 6	Logar. Chord. Ev. 223632	
Argument. Latit.	8 5 32 45	Logar. Distant. 362507	
		Numerus Logar. 861125	
Reduction Sub.	4 49	Reflect. Add 0° 13' 56''	
Ecliptic place >	8 2 24 2	Evect. Add 0 10 40	
Latit. > South	3 47 59	2d Equat. Add 0 24 36	

The Moon's Latitude, and Reduction from her Orb to the Ecliptick, is found as followeth.

With the distance of the Moon from the Sun $8^s\ 19^{\circ}\ 56'\ 3''$, I enter the Table entit'led (*Tabula Scrup. proportionalium & Equationes Nodorum*) where I find the proportional Scruples $58'\ 11''$ and the Equation of Nodes $31'\ 39''$ Subtract, which according to the Title, being Subtracted from the equal Motion of the Node $11^s\ 27'\ 27''\ 45''$ leaveth the true place $11^s\ 26^{\circ}\ 56'\ 6''$, which Subtracted from the Moon's place in her Orb $8^s\ 2^{\circ}\ 28'\ 51''$, leaveth the Argument of Latitude $8^s\ 5^{\circ}\ 32'\ 45''$, which (in *Tabula Latitudinis Lune*) gives the Moon's Latitude $4^{\circ}\ 33'\ 00''$, with the excess $15'\ 28''$ of which the proportional part is $14'\ 59''$, which added to the Latitude before found, produceth the Moon's true Latitude $4^{\circ}\ 47'\ 59''$ South.

By the Argument of Latitude is found the Reduction $4'\ 59''$ to be Subtracted, and therefore the true place of the Moon in the Ecliptic is $8^s\ 2^{\circ}\ 24'\ 2''$, agreeing to $26''$ in Longit. and $1'\ 49''$ Latitude.

CHAP VI.

To Calculate the Geocentric place of any of the Primary Planets both in Longitude, and Latitude.

First, To find the Longitude of any of the Primary Planets, get first the Planet's Place from the Sun, in his *Ellipsis*, (as before directed in the Sun) which I here call his Ecliptic place) remembring to collect the *Node* and *Logarithm* of the Planet also.

2. Subtract the *Node* of the Planet (First placing the Planet's Ecliptic place under the *Node*) from the Ecliptic place of the Planet, and the remainder is the Argument of Latitude.

3. In the superiour Planets ι , π , δ , Subtract their Helio-centric, or Ecliptic place, from the place of the Sun, and the Remainder is the *Anomaly* of Commutation: but in the inferiour Planets γ and ν , Subtract the Sun's place from theirs, and the remainder is the *Anomaly* of Commutation.

4. To find the *Parallax* of the Earth's Orb, place the Log. of the Planet and Log. of the Sun one under another, subtracting the greater Log. from the less (the Radius being first added) the remainder will be the Tangent of an Arch, to which must be added 45 Degrees, and to the Co-Tangent of the Sum, add the Tangent of half the *Anomaly* of the Orb, the Sum (subtracting the Radius) is the Tang. of an Arch, which in the Superiour

perior Planets must be added to the said half *Anomaly* of Commutation; but in the Inferiour Planets, subtracted from it, the sum or difference is the Planet's *Elongation* from the Sun, then subtracting the half Difference from the half *Anomaly* of Commutation, or *Orb*, the difference is the *Parallax* of the Earth's *Orb*.

5. If the *Anomaly* of Commutation be less than six Signs, the *Parallax* of the *Orb* is to be added to the Heliocentric Longitude or Ecliptic place of \hbar , π , δ , but in φ and ψ it is to be added to the place of the Sun: But if the Commutation be more than six Signs, the *Parallax* of the *Orb* is to be subtracted from the Ecliptic place of \hbar , π , δ , and in φ and ψ Subtracted from the Sun's place, and the Sum or difference is the true Geocentric Longitude of the Planet.

For the Latitude.

First with the Argument of Latitude, take out the *Orb* of the Planet from the Plane of the Ecliptic, in its respective Table, then to that number affix its Co-Tang. to which set down the Arith. Comp. of the Sine of Elongation, and also the Sine of the *Anomaly* of Commutation: These three numbers added into one sum (Subtracting the Radius) is the Co-Tang. of the Lat. of the Planet.

E X A M P L E I.

Of π both in Longitude and Latitude.

Anno, 1690. May 11 Day, at 20 Hours 13 Min. P. M. Mr. John Flamsteed Observed π in $2^{\circ}-29'-6''$ γ with $1^{\circ}-9'-30''$ S. Lat.

<i>Tempus datum</i>	Longit. π	Anomal. π	Node π	
	S. 0 1 "	S. 0 1 "	S. 0 1 "	π
Anno, 1690	11 13 1 00	5 3 12 00	3 7 15 00	Node
May 11 Day	10 54 00	10 54 00	11 22 24 22	Ecl.P.
Ho. 20	4 9	4 9	8 15 9 22	A.Lat
Min. 13	3	3		
			569698. Logar. π	
Mean Motion π	11 23 59 12	5 14 10 12	500624. Logar. \odot	
Prosthaph. Sub.	1 34 50			
		Tang. 930926	11°-31'-10" Ad. 45°	
Eclipt. place π	11 22 24 22	Co-T. 982046	56--31--10 Sum	
Sun's place	2 1 29 44	Tang. 983786	34--32--41 A. $\frac{1}{2}$ Orb.	
Anomal Com.	2 9 5 22	Tang. 965832	24--28--51 $\frac{1}{2}$ Diff.	
Par. Orb. Add	10 3 50			
		Elongat. π à \odot	59--1--32 Elongat.	
Longitude π	γ 2 28 12	Parallax. Add	10--3--50 P.E. Orb.	

For

For the Latitude of π .

Elongation π à \odot	59	1	32	---A. C.	---006680
Anomaly of Commutation	69	5	22	---S.	---997041
Inclination Ecliptic.	1	19	10	---c. t.	---1163765
Latitude π So. Ascend.	1	12	40	---c. t.	---1167486

Differ. in Longit. 0' 54"

Differ. in Latit. 3 10

EXAMPLE II.

in φ .

Anno 1631, October 28th Day at 7 Ho. 58' *Manè*, Gassendus at Paris, Observed (by a Telescope) φ in the Sun's Disc, being towards the North-East part of the Sun's Body and the distance of their Centers Observed 4' 15". The time Reduced to the Meridian of London, is 7 Ho. 50' *Manè*.

Tempus datum	Longit. φ S. o ' "	Anomal. φ S. o ' "	Node φ S. o ' "	φ
Anno 1631	8 22 51 00	0 11 54 00	1 13 18 00	Node
Octob. 27 Day	4 27 43 00	4 27 42 00	1 14 39 12	Ecl.P.
19 Ho. 56'	3 22 55	3 22 55	1 21 12	A.Lat
Mean Motion φ	1 23 56 55	5 12 58 55	1499511	L. \odot R. Add
Prosthaph. Sub.	9 17 43		449190	Logar. φ
Eclipt. place φ	1 14 39 12	Tan. 1050321	72°-34'-24"	Ad. 45°
Sun's place	7 14 40 48	Tan. 971783	27°-34'-24"	Sum
Anomal. Com.	5 29 58 24	Tan. 636454	0---0-48½	Co. Orb.
Parallax Add	24	Tang. 608237	0---0-24	Substr.
		Elongation or	0---0-24	Parallax
	7 14 41 12			

For the Latitude of φ .

Elongation φ à \odot	0°	0'	24"---A. C.	392538
Comp. Anom. Orb.	0	1	36---S.	666269
Inclination	0	9	30---c. t.	1255854
Latitude φ North	0	2	34-----	1314661

Agreeing to the Observation of Gassendus.

C H A P. VII.

To find the time of the true Conjunction or Opposition of the Sun and Moon.

First find out (by the Epact) the Day of the New or full Moon for the Year and Month proposed.

II. At the Noonside of the day thus found, compute the true places of the Sun and Moon, (as is taught in the 4th and 5th Chapter) and divide their distance from Conjunction or Opposition, by the true Hourly Motion of the Moon from the Sun, and the Quotient Add or Subtract (according as you find the Moon wanting or past \odot or \oslash) and you shall have the time of the \odot or \oslash near the truth. At this time thus corrected, Calculate the true places of the Sun and Moon; and if they agree you have the equal time of the Conjunction or Opposition in respect of the Moon's Orb, but if there be some difference, divide the same again by the true Hourly Motion of the \odot or \oslash , as before, and so proceed till you find a concurrence.

E X A M P L E.

In the Year 1693, I would know what time in *January* the full Moon was, therefore to the Epact 22, I add the number of Months from *March*, which is 11 Inclusive, and the sum is 33, from which taking 30, the remainder is 3, which subtract from 30 and there remains 27 for the day of the New Moon in *December*, to which add the half *Syzygia* 14 Days 18 Ho. 22', and the Sum (abating 30) is 11 Days 18 Ho. 22' for the time of the Mean \oslash in *January* 1693, to which time I compute the places of the Sun and Moon, finding the Sun in $3^{\circ} 5' 40''$; and the Moon in $4^{\circ} 19' 38''$, their distance from \oslash $1^{\circ} 13' 58''$, which I divide by $32' 47''$ the Hourly Motion of the \odot or \oslash , and the Quotient is 2 Ho. 15' 22'', which being subtracted from 11 Days 18 Ho. 22' (the time before given, because the Moon's place is greater then the Sun's) leaveth 11 Days 16 Ho. 6' 38'', to which time I compute their places, finding their distance from \oslash $2' 58''$ which I again divide by the Hourly Motion \odot or \oslash , and the Quotient is 5' 25'' to be Subtracted (because the Moon's place is yet greater than the Sun's) from 11 Days 16 Ho. 6' 38'', and there remains 11 Days 16 Ho. 1' 13'', to which time I again compute the places of the Luminaries, finding their distance from \oslash $9''$, which divide as before, and the Quotient is 16'' to be Subtracted from 11 Days 16 H. 1' 13'' and the Remainder is 11^d 6^b 0' 57'', which is the middle time of the true \oslash respecting the Moon's Orb, at which time the Sun is in $\approx 2^{\circ} 59' 40''$, and the Moon in $\approx 2^{\circ} 59' 40''$.

III. For

III. For this time I find out the Anomaly of the Moon's Latitude, and thereby the Reduction, which divide by the Hourly Motion, and the Quotient (contrary to the Title of Reduction) apply to the time before found, so have you the true δ in respect of the Ecliptic.

E X A M P L E.

	S.	o	'	"
True place of the Moon	4	2	59	40
North Node Subtract	10	1	28	50
Argument of Latitude	6	1	30	50
Reduction Subtract				22
Time of Reduction Add				40
True δ respecting the Ecliptic.	11 ^d	16 ^b	1	37

IV. To the time here given apply the Equation to make it apparent.

	D.	H	'	"
Time given	11	16	1	37
Æquation of time Subtract			9	14
Apparent time of the true δ	11	15	52	23

C H A P. VIII.

To Calculate the Eclipse of the Moon.

First to know when the Moon will be Eclipsed, and when not; Therefore observe at the true δ : If the true motion of Latitude be within 12 Degrees backward or forward of 6 or 12 Signs, there is a possibility of an Eclipse, otherways not.

Otherways, if at the time of the true δ , the Moon's Latitude be less than the sum of the Semidiameters of the Moon and Earth's Shadow, there must be an Eclipse, else not.

E X A M P L E. I.

At the time of the true δ in *January* 1693, the true Motion of Latitude is only $1^{\circ} 30' 50''$ above 6 Signs, which shews the necessity of an Eclipse.

E X A M-

EXAMPLE II.

At the time of the true δ , the sum of the Semidiameters is $58' 11''$, and the Latitude of the Moon $7' 52''$; thus because the Moon's Latitude is less than the said sum, it shews there will be an Eclipse.

II. At the time of the true δ (with the mean *Anomalys* of the Sun and Moon) enter the Table entitled (*Tabula Horariorum Motum Semid. &c.*) and under the Titles *Semid. ☉ Semid. ☾, Hor. Mot. &c.* You have their apparent Semidiameters, Parallax of the ☾ , &c. Then from the sum of their Horizontal Parallaxes (the Sun's Parallax in the Horizon being ever $30''$) Subtract the Sun's Semidiameter, and the residue is the apparent Semidiameter of the Earth's Shadow, in respect of the Moon's Transit.

EXAMPLE.

Sum of the Horizontal Parallaxes ☉ and ☾	58'	34''
Semidiameter of the Sun Sub.	16	29
Apparent Semidiameter Earth's Shadow	42	5

III. Add together the Semidiameters of ☾ and Earth's Shadow; and from their sum, Subtract the Moon's Latitude; the Remainder is the parts deficient.

EXAMPLE.

Semidiameter of the Moon	16'	6''
Semidiameter of the Shadow	42	5
<hr/>		
Their Sum		58 11
Latitude ☾ Subtract		7 52
<hr/>		
Parts or Scruples deficient	53	19

IV. You may speedily convert the Scruples deficient into Digits thus: From the Logist. Logarithm of the Scruples deficient, Sub. the Logistical Log. of the double of the Moon's Diameter, the remainder is the Logist. Log. of the Digits Eclipsed.

EXAMPLE.

Scruples deficient	0° 50' 19''	LL---992356
Double ☾'s Diameter	1 4 24	LL-1003073
Digits Eclipsed	19 45 10	LL--989283

C c c c

Here

Here is to be *Noted* that Lunar Eclipses are of three sorts.

1. *Partial*, when the *Scruples Deficient* are less than the Moon's Diameter.

2. *Total without Continuance*, when they are equal.

3. *Total with Continuance*, when the *Scruples deficient* are greater than the Moon's Diameter, and in these, the *Digits Eclipsed* are more than 12, which shews how far the Eclipse is over the body of the Moon.

V. Take the Logarithms of the sum and difference of the Semidiameters and Latitude of the Moon, and the half Sum of the two Logarithms shall be the Logarithm of the *Scruples of Incidence* or half duration.

EXAMPLE.

Sum of the Semidiameter in Seconds	3491"
Latitude of the Moon in Seconds	472
	<hr/>
Sum	3963
Difference	3019
	<hr/>
Sum	7.07788
Scruples of Incidence 3459" or 57' 39"	Sum 3.53894

VI. As the true hourly Motion of the ☾ a ☉, to 1 Hour or 60'; so the *Scruples of Incidence*, to the time of Incidence, which subtracted from, and added to the time of the greatest Obscuration, gives the Beginning and End of the Eclipse.

EXAMPLE.

LL--of 57' 39" Rad. Add	1998265
LL--of 32 42	973040
LL--of 1 ho. 52' 40"	1024625

Or dividing the *Scruples of Incidence* by the Hourly Motion, ☾ a ☉, gives the same.

With the Moon's true Latitude at the time of the true ☿, enter the Table entitled (*Distantia Vera ☿ & ☿ a Maxima Observatione*) and the distance there found, divide by the hourly Motion ☾ a ☉; the Quotient being apply'd to the apparent time of the true ☿, gives the time of the greatest Obscuration or middle of the Eclipse.

E X A M.

E X A M P L E.

"The Latitude of the Moon $7^{\circ} 52''$, gives in the Table $47''$, which divided by the hourly Motion, produceth $1^{\circ} 27''$ in time, to be Subtracted.

	H	'	"
Apparent time of the true \odot respecting the Ecliptic	15	52	23
Interval Subtracted		1	27
Middle of the Eclipse, or greatest Obscuration	15	50	56
Time of Incidence Sub. and Add	1	52	40
Beginning of the Eclipse	13	58	16
The End of the Eclipse	17	43	36
Total Duration.	3	45	20

VIII. To know the continuence of total Darknes, take the difference of the Semidiameters instead of the Sum, and then work as before.

Hence the continuence of Total Darknes is found to be $48^{\circ} 52''$

	H	'	"
Hence { The Beginning of the Eclipse	13	58	16
{ The Beginning of Total Darknes	15	26	30
{ The Total Obscuration or Middle	15	50	56
{ The End of Total Darknes	16	15	22
{ The End, or full recovery of Light	17	43	36

IX. To find the Latitude of the Moon in the beginning and end of the Eclipse: Add the Motion of the Sun, agreeing to the time of Incidence to the Scruples of Incidence, the sum whereof Subtracted from the Argument of Latitude, at the beginning of the Eclipse, gives the Argument of the Latitude at the end thereof, by which you may find the true Latitude as before was taught.

EXAMPLE

Motion of ☉ agreeing to the time of Incidence 0 0 41 38
 Scruples of Incidence 57 49

Sum
 Argument of ☾ Latitude at the Middle 0 1 2 17
 6 1 30 50

Argument of Latitude at Beginning 6 0 28 33

Argument of Latitude at End 6 2 33 7

Hence { Latitude ☾ at the Beginning So. Afc. 2 22
 { Latitude ☾ at the End So. Afc. 13 20

CHAP. IX.

To Calculate the Eclipse of the Sun.

First find out the true ☉ as was taught in the Moon's Eclipse, at which time add the Sum of the Semidiameters of the Sun and Moon, to the difference of their Horizontal Parallaxes, and if the Sum thereof exceed the true Latitude of the Moon, at that Instant, it shews the Sun will be Eclipsed in some part of the Earth, otherways not.

EXAMPLE.

At the time of the true ☉ June 12th Day in the Afternoon,
 Anno 1694.

Sum of Semidiameters of ☉ and ☾ is 0 30 55
 Differ. Horizontal Parallaxes ☉ and ☾ Add 0 52 40

Sum
 True Latitude of the ☾ at that time. 1 23 35
 14 6

Hence the Sum of the Semidiameters added to the Difference of their Horizontal Parallaxes, exceeds the true Latitude of the Moon; which shews the necessity of an Eclipse.

II. If at the time of the Visible ☉ the apparent Latitude of the Moon, shall be less than the Sum of the two Semidiameters, the Sun will suffer an Eclipse in that Place, else not.

EXAMPLE

EXAMPLE.

At the before mentioned Time, the

Sum of the Semidiameters is	0	'	"
Visible Latitude is	0	30	55
	0	24	55

Which proves the Sun's Eclipse in these parts of the World.

This being known proceed to the Calculation after this manner.

I. Find out the Midheaven, its Altitude, and Meridian Angle as followeth.

	S	D	'	"
	d.	h.		
The true time of the ☿ 1694, June	12	3	54	31
the true place of the Sun	☿	1	26	17
Excentric place of the Moon	☾	1	26	17
Mean Anomaly of the Sun	☿	23	54	41
Mean Anomaly of the Moon	☾	21	0	40
Argument of the Moon's Latitude	5	27	18	48
True Latitude of the Moon North			14	6
Hourly Motion of the Sun			2	23
Hourly Motion of the Moon			29	52
Hourly Motion ☾ ☿			27	29
Reduction Add				38
Time of Reduction Subtract			1	23
The true Ecliptic Conjunction June	12	3	55	54
Equation of time Subtract				29
Apparent time of the true ☿ June	12	3	55	25
Horizontal Parallax ☾ ☿			52	40

II. Find out the Midheaven, its Altitude, and the Meridian Angle, at the Apparent time of the true ☿, 1694, June 12th Day 3 Ho. 55' 25".

EXAMPLE.

The Sun's place is	S.	o.	'
Time in Degrees	☿	1	26
Sun's Right Ascension		58	51
R. A. of the Medium Caeli.		91	34
M. C. in the Ecliptic		150	25
Meridian Angle	☿	28	23
Declination of M. C.		69	40
Altitude Equator at London		12	5 North.
Altitude of the M. C.		38	28
		50	30

III. Add

III. Add the Sine of the Meridian Angle to the Co-sine of the Altitude of the *M. C.* the Sum is the Co-sine of the Altitude of the *Nonagesime* Degree.

EXAMPLE.

The Meridian Angle	69	40--s--9.97205
Altitude of <i>M. C.</i>	50	33--cs--9.80305
Altitude of <i>Nonages. gr.</i>	53	26--cs--9.77510

IV. Add the Co-sine of the Meridian Angle, to the Cotangent of the Altitude of the *Medium Cæli*; the sum is the Tangent of the distance of the *Nonagesime* Degree from the *Medium Cæli*, which add to the *M. C.* from *Capricorn* to *Cancer*, and Subtract from *Cancer* to *Capricorn*, and you have the *Nonagesime* Degree.

EXAMPLE.

The Meridian Angle	69	40--cs--9.54093
Altitude of the <i>M. C.</i>	50	33--ct--9.91533
Dist. <i>M. C.</i> from <i>Nonages. gr.</i>	15	57--t--9.45626

The Midheaven	4	28	23	00
Distance Subtract	0	15	57	00

<i>Nonages. gr.</i> viz. $12^{\circ} 26' \Omega$	4	12	26	00
The Sun's place	3	11	26	17

Dist. $\alpha \odot$, from <i>Nonages. gr.</i> to the <i>West</i>	1	10	59	43
--	---	----	----	----

V. Add together the Logistical Logarithm of the Horizontal Parallax of the Moon from the Sun, the Sine of the Altitude of the *Nonagesime* Degree, and the Sine of the distance of the Sun from the *Nonagesime* Degree; the Sum, Subtracting the double Radius, is the Logistical Logar. of the Parallax in Longitude.

EXAMPLE.

Horizontal Parallax $\alpha \odot$	52	40--LL--9.94338
Altitude <i>Nonages. gr.</i>	53	26--S---9.90480
Dist. $\odot \alpha$ <i>Nonages. gr.</i>	40	59--S---9.81689
Parallax of Longitude	27	45--LL--9.66507

Here

Here Note, That if the Sun's place be less than the *Nonagesime*, the Luminarie appears more *West* than the truth, but if his place be greater, then the Luminarie seems more *East*, according to the quantity of the Parallax of Latitude.

VI. Add the Logistical Logarithm of the Horizontal Parallax of \odot & \circ , to the Co-sine of the Altitude of the *Nonagesime* Degree, the Sum is the Logistical Logarithm of the Parallax of Latitude.

E X A M P L E

Horizontal Parallax \odot & \circ	52	40--LL--	9.94338
Altitude <i>Nonages. gr.</i>	53	26	00--cs--
Parallax of Latitude	31	22--LL--	9.71845

In the next place we shall shew how to find the visible Hourly Motion of the Moon from the Sun, to which end I shall deliver these following Rules.

VII. If the Eclipse happen in the Oriental Quadrant of the Signifier, and the Parallax of Longitude decrease, Subtract the difference of the Parallax of Longitude in one hour (or any other time) from the true Motion of the Moon from the Sun, but if the Parallax of Longitude increase, add the said Difference.

VIII. If the Eclipse happen in the Occidental Quadrant, and the Parallax of Longitude decrease, add the difference of Parallaxes to the true Motion of the Moon from the Sun; otherways Subtract the same, if the Parallax of Longitude Increase.

IX. If the Eclipse happen in the *Nonagesime* Degree, so that the former part fall in the Oriental Quadrant, and the latter in the Occidental, Subtract the difference from the true Motion of the Moon from the Sun, and you shall have the visible Motion of the Moon from the Sun.

Note, That whensoever the Sun's place is greater than the *Nonagesime* Degree, the Eclipse happens in the Oriental Quadrant, but if less, in the Occidental.

As in our Example the Sun is in $1^{\circ} 26' 17'' \text{ } \ominus$, and the *Nonagesime* Degree $12^{\circ} 26' \text{ } \text{ } \circ$, therefore the Sun is in the Occidental Quadrant distant as before $40^{\circ} 59' 43''$.

	H	'	"
To 1 hour following the true \circ , viz.	4	55	25
Parallax of Longit. according to the former doctrine		31	5
True hourly Motion \odot & \circ		27	29
Difference Parallax Longitude Substr.		3	20
Visible hourly Motion \odot & \circ		24	9
By which dividing the Parallax of Longitude,			
at the time of the true \circ , giveth the Interval	1	8	56
of the true and visible \circ to be added			
Hence the visible \circ is June 12 day at	5	4	21
			At

At which time the Parallax of Longit. is	31	26
Distance of the Sun and Moon at that time	31	26
Parallax of Latitude South	34	59
True Latitude > No. Descending	10	46
Visible Latitude of the Moon South	24	13
Semidiameter of the Sun	16	11
Semidiameter of the Moon	14	54
Sum of the Semidiameters	30	55
From which taking the visible Latitude } leaveth the Scruples deficient.	6	42
Which converted into Digits as (in the } Moon's Eclipse, by using the Double of } the Sun's Diameter) makes	2	30 26

X. For the Scruples of Incidence, Subtract the Logistical Logar. of the sum of the Semidiameters of the Sun and Moon, from the Logistical Logarithm of the Visible Latitude of the Moon from the Sun, the Remainder seek in the Table of Sines, and to its Co-sine Add the Logistical Logarithm of the Sum of the Semidiameters; the sum shall be the Logistical Logar. of the Scruples of Incidence.

EXAMPLE.

Visible Latitude > a ⊙	24	13--LL--9.60596
Sum of the Semidiameters	30	55--LL--9.71204
		<hr/>
		s---9.89392
		cs---9.79354
Sum of the Semidiameters	30	55--LL--9.71204
		<hr/>
Scruples of Incidence	18	19--LL--9.50558.

XI. To 1 hour before the visible σ , viz. $4^b 4' 21''$ we shall find (according to the former Doctrine) the Parallax of Longitude is $28' 21''$, so that the hourly difference of the Parallax of Longitude is $3' 5''$, which Subtracted from the hourly Motion > a ⊙ $27' 29''$, leaveth the visible hourly Motion $24' 24''$, by which dividing the Scruples of Incidence $19' 13''$, it gives the time of Incidence $47' 15''$.

Again, to 1 hour after the visible σ , viz. $6^b 4' 21''$, the Parallax of Longitude is $32' 19''$ so that the hourly difference of Parallax is $0' 53''$, which Subtract from the true hourly Motion $27' 29''$; and it leaves $26' 36''$, for the visible hourly Motion, by which dividing the Scruples of Incidence $19' 13''$, produceth the time of Repletion $43' 20''$; hence the duration of the Eclipse is $1^b 30' 35''$.

XII. In

XII. In the Table of the difference of the ϕ or δ from the Mid-Eclipse or greatest Obscuration, the visible Latitude at the time of the visible ϕ , giveth the Interval $2' 7''$, which divide by the visible hourly Motion, following the visible ϕ , giveth the Interval $4' 46''$ to be Subtracted; so that the greatest Obscuration is at $4^h 59' 35''$ P. M.

Hence,

	H	
The Beginning at London is at	4 12 20	
The Middle or greatest Obscuration	4 59 35	P. M.
The Visible Conjunction	5 4 21	
The End of the Eclipse	5 42 55	

XIII. To find the visible Latitude of \odot , at the Beginning and End of this Solar Eclipse. First, for the Beginning, add to the Minutes of Incidence, the Motion of the Sun agreeing to the time of Incidence, and the Sum subtract from the true Motion of Latitude at the true time of the visible Conjunction; so have you the true Motion of Latitude at the Beginning, by which find the true Latitude, and at the same time find the Parallax of Latitude; by these (observing the former directions) is had the visible Latitude.

EXAMPLE.

	S. o.	
The Scruples of Incidence	19	13
Motion of the \odot to the time of Incidence	1	55
Sum Subtract	21	8
Motion of Latitude at the visible ϕ	5 27 54	20
Motion of Latitude at the Beginning	5 27 33	12
Moon's true Latitude North Sub.	12	49
Parallax of Latitude	32	13
Visible Latitude at the Beginning South	19	24

XIV. For the end, add to the Minutes of Incidence the Motion of the Sun agreeing to the time of Repletion, and the Sum add to the true Motion of Latitude at the time of the visible ϕ , so have you the true motion of Latitude at the end, by which proceed, as before, to find the visible Latitude.

D d d d

EXAM

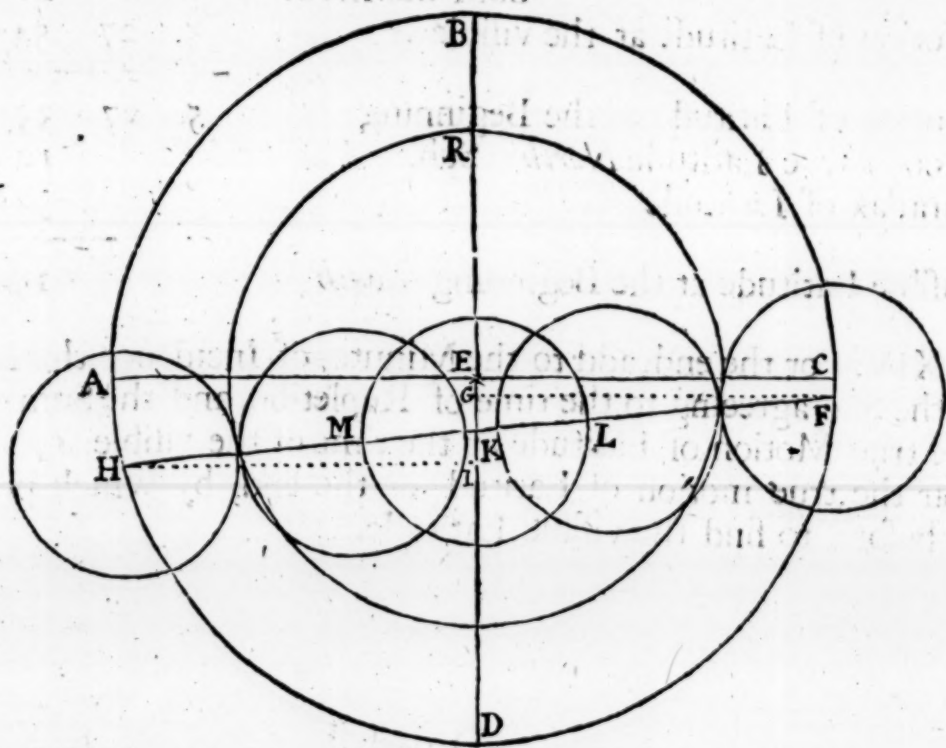
EXAMPLE.

E X A M P L E.			
The Scruples of Incidence		19	13
Motion of ☉ to the time of Repletion		1	46
	Sum Add	20	59
Motion of Latitude at the Visible ☿	5	27	54
Motion of Latitude at the End	5	28	15
Moon's true Latitude North Sub.		9	9
Parallax of Latitude		37	11
Visible Latitude South		28	2

CHAPTER. X.

To Delineate the Eclipses of the Sun and Moon.

I. **F**OR the Moon, draw the lines A C and B D to intersect one another at Right Angles in E, which point of Intersection is the Plane of the Ecliptic, where the Eclipse happens: upon which, as a Centre, draw the Peripherie A B C D, of the quantity of the sum of the Semidiameters of the Moon and Earth's Shadow (which may be done by a Scale of equal Parts) also to



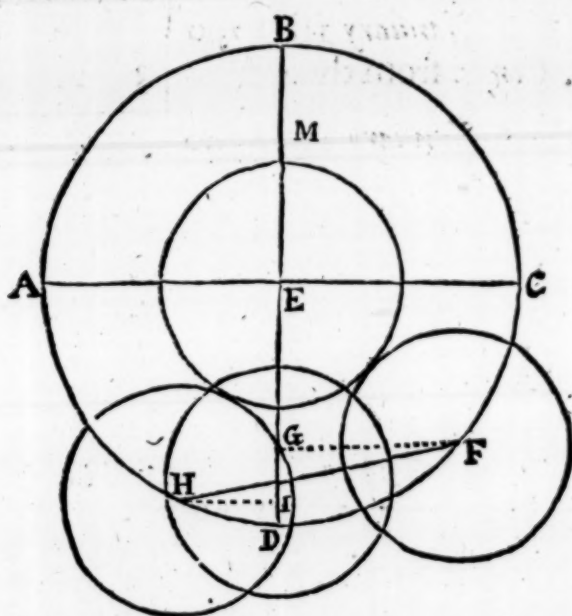
the quantity of the Semidiameter of the Earth's Shadow, draw upon the same Centre another Peripherie, then because the Moon's Eclipse begins on the East part of her Body, you must upon the West

West side of your Plane Note down the Latitude of the Moon, in the Arch B C D, which here represents the West part, which may thus be done. From E upon the line B D, prick off the Latitude at the beginning towards D, which terminates at G, from which draw a Parallel line to A C, as G F. For the End of the Eclipse proceed in like manner on the other side, and set off the Latitude from E to I, whose Parallel falls at H, then draw a line between F and H, which respects the way of the Moon during the Eclipse: Then draw the five equal Circles, having for the Radius the Semidiameter of the Moon. Then F shews the place of the Moon at the beginning of the Eclipse, L her place when she begins to be Totally darkned, K her place at the Middle, M her place when she begins to recover her light, and H the end of the Eclipse.

E X A M P L E.

Sum of the Semidiameters	E B	58	11
Semidiameter of the Shadow	E R	42	5
Initial Latitude of the Moon	E G	2	22
Final Latitude of the Moon	E I	13	20
Semidiameter of the Moon	R B	16	6

II. For the Eclipse of the Sun, which differs in nothing at all from this of the Moon, but only that instead of the Semidiamete-



ter of the Shadow of the Earth, you use the Semidiameter of the Sun, and the visible Latitude instead of the true: see what follows from the foregoing Eclipse, by way of

E X A M P L E.

Sum of the Semidiameters	E B	30	55
Semidiameter of the Sun	E M	16	1
Initial visible Latitude	E G	19	24 South
Final visible Latitude	E I	28	2
Semidiameter of the Moon	M B	14	54

D d d d 2

CHAP.

C H A P. XI.

*To find the place of the Fixed Stars for
any time given.*

First, gather the Recession of the Equinoctial (which is equal to the distance of the first Star in the Catalogue from the first point of γ) to which add the distance of the Star, whose Longitude is sought: the distance of the said Star is found by Subtracting the place of the first $*$ in the Catalogue, from the place of the proposed Star there found; the sum is the place of the Star required.

E X A M P L E.

I desire to know the place of *Cor Leonis* the of 1st *January* 1700, to which end I gather the Recession of the Equinoctial after this following manner.

	S	o	'	"
Epocha 1681		28	44	00
Years add 19			15	59
Place 1st $*$ γ <i>January</i> 1st 1700		28	59	59
Add Dist. <i>Cor</i> α from the 1st $*$ γ	3	26	40	00
Place of <i>Cor</i> α <i>January</i> 1st. 1700	α	25	39	59

A CATA-

A CATALOGUE of some of the most Eminent Cities and Towns in the *World*, with their Latitude, and difference of Meridians from *London*.

Names of the Cities.	Diff. Merid.			Alt. Po.	
	H			o	'
<i>Alberdeen</i> in <i>Scotland</i>	0	7	S	58	4
<i>Alexandria</i> in <i>Egypt</i>	2	20	A	30	58
<i>Amsterdam</i> in <i>Holland</i>	0	20	A	52	25
<i>Antwerp</i> in <i>Brabant</i>	0	17	A	51	12
<i>Aracta</i> in <i>Syria</i>	3	20	A	36	0
<i>Athens</i> in <i>Greece</i>	1	54	A	37	42
<i>Babylon</i> in <i>Chaldea</i>	3	10	A	35	0
<i>Bedford</i> in <i>England</i>	0	2	S	52	12
<i>Berwick</i> in <i>England</i>	0	6	S	55	50
<i>Bethlem</i> in <i>Judea</i>	2	48	A	31	50
<i>Bononia</i> in <i>Italy</i>	0	45	A	43	49
<i>Bristol</i> in <i>England</i>	0	12	S	51	28
<i>Calis</i> in <i>France</i>	0	10	A	50	52
<i>Calecut</i> in <i>E. India</i>	5	52	A	11	30
<i>Cambridge</i> in <i>England</i>	0	1	A	52	17
<i>Canterbury</i> in <i>England</i>	0	4	A	51	25
<i>Cassells</i> in <i>Hessia</i>	0	39	A	51	19
<i>Compostella</i> in <i>Spain</i>	0	36	S	43	0
<i>Conimbria</i> in <i>Portugal</i>	0	33	S	40	15
<i>Coventry</i> in <i>England</i>	0	6	S	52	30
<i>Derby</i> in <i>England</i>	0	6	S	53	3
<i>Dantzick</i> in <i>Prussia</i>	1	14	A	54	23
<i>Dublin</i> in <i>Ireland</i>	0	27	S	53	11
<i>Edenburgh</i> in <i>Scotland</i>	0	10	S	57	6
<i>Frankford</i> upon <i>Meene</i>	0	35	A	50	2
<i>Fruenburg</i> in <i>Prussia</i>	1	28	A	54	22
<i>Glocester</i> in <i>England</i>	0	9	S	51	58
<i>Ghent</i> in <i>Flanders</i>	0	18	A	51	4
<i>Haphnia</i> in <i>Denmark</i>	0	52	A	55	43
<i>Huntingdon</i> in <i>England</i>	0	1	S	52	24
<i>Hierusalem</i>	3	2	A	32	10
<i>Knockfergus</i> in <i>Ireland</i>	0	29	S	54	40
<i>Leyden</i> in <i>Holland</i>	0	21	A	52	7
<i>Lisbon</i> in <i>Portugal</i>	0	34	S	38	45
<i>Leicester</i> in <i>England</i>	0	4	S	52	41
<i>Lincoln</i> in <i>England</i>	0	1	S	53	15
<i>L O N D O N.</i>	0	0		51	32
<i>Middleburg</i> in <i>Zeland</i>	0	18	A	51	30
<i>Madrid</i> in <i>Spain</i>	0	9	S	40	45

A CATALOGUE of some of the most Eminent Cities and Towns in the World, with their Latitude, and difference of Meridians from London.

Names of the Cities.	Diff. Merid.			Alt. Po.	
	H			o	'
Naples in Italy	1	0	A	40	42
Northampton in England	0	3	S	52	18
Norwich in England	0	5	A	52	46
Norimberg in Germany	0	48	A	49	26
Nottingham in England	0	4	S	53	0
Ostend in Flanders	0	16	A	51	10
Oxford in England	0	5	S	51	45
Pickworth Sedes Authoris	0	2	S	52	40
Paris in France	0	8	A	48	39
Prague in Bohemia	0	58	A	50	6
Pembroke in England	0	19	S	51	54
Peterborough in England	0	1	S	52	38
Quinsai in China	8	32	A	40	0
Ratisbone in Bavaria	0	51	A	49	9
Richmond in England	0	7	S	54	26
Rochel in Aquitain	0	4	S	45	49
Rome in Italy	0	51	A	42	2
Rotterdam in Holland	0	15	A	51	55
Sarum in England	0	7	S	51	12
Sardis in Lydia	2	24	A	38	34
Salamanca in Spain	0	20	S	41	12
Salisburgh in Bavaria	0	56	A	47	42
Stafford in England	0	9	S	52	54
Spires in Germany	0	37	A	49	24
Stockholm in Sweden	1	3	A	58	50
Stamford in England	0	2	S	52	41
Theſſalonica	1	47	A	41	32
Toledo in Spain	0	24	S	40	10
Tubinga in Sweden	0	40	A	48	34
Valentia in Spain	0	7	S	39	55
Venice	0	50	A	45	15
Vienna in Austria	1	8	A	48	22
Ulm in Sweden	0	44	A	48	24
Uraniburg in Denmark	0	52	A	55	55
Warwick in England	0	6	S	52	25
Witteberg in Saxony	0	54	A	51	52
Winchester in England	0	8	S	51	13
Worms in Germany	0	31	A	50	25
Worcester in England	0	9	S	52	18

A TABLE

A TABLE of the SUN's Mean Motion.

Years.	Longit. \odot .	Anomal. \odot .	Years.	Longit. \odot .	Anomal. \odot .
aft. Ch S	o ' " S o ' "	o ' " S o ' "	Years.	S o ' " S o ' "	S o ' " S o ' "
0 I	9 7 59 57	6 29 39 48	1	II 29 45 40	II 29 44 38
10 I	9 8 44 50	6 28 41 58	2	II 29 31 20	II 29 29 16
20 I	9 9 29 42	6 27 44 18	3	II 29 16 59	II 29 13 54
30 I	9 10 14 35	6 26 46 18	B 4	0 0 1 48	II 29 57 41
40 I	9 10 59 28	6 25 48 28	5	II 29 47 28	II 29 42 20
50 I	9 11 44 20	6 24 50 37	6	II 29 33 7	II 29 26 58
60 I	9 12 29 13	6 23 52 47	7	II 29 18 47	II 29 11 35
70 I	9 13 14 6	6 22 54 57	B 8	0 0 3 35	II 29 55 22
80 I	9 13 58 58	6 21 57 7	9	II 29 49 15	II 29 40 1
90 I	9 14 43 51	6 20 59 17	10	II 29 34 55	II 29 24 39
100 I	9 15 28 44	6 20 1 27	11	II 29 20 35	II 29 9 17
110 I	9 16 13 37	6 19 3 37	B 12	0 0 5 23	II 29 53 3
120 I	9 16 58 29	6 18 5 47	13	II 29 51 3	II 29 37 42
130 I	9 17 43 22	6 17 7 57	14	II 29 36 43	II 29 22 20
140 I	9 18 28 15	6 16 10 7	15	II 29 22 23	II 29 6 58
150 I	9 19 13 7	6 15 12 16	B 16	0 0 7 11	II 29 50 45
160 I	9 19 58 0	6 14 14 26	17	II 29 52 51	II 29 35 23
170 I	9 20 42 53	6 13 16 36	18	II 29 38 31	II 29 20 12
180 I	9 21 27 45	6 12 18 46	19	II 29 24 10	II 29 4 39
190 I	9 22 12 38	6 11 20 56	B 20	0 0 8 59	II 29 48 26
200 I	9 22 57 31	6 10 23 6	Years from 1690.		
Middle Motion of the Sun in the intermediate Years.			1690	9 20 23 9	6 13 8 11
			1691	9 20 8 49	6 12 52 44
			B 1692	9 19 54 28	6 12 37 27
			1693	9 20 39 17	6 13 21 13
			1694	9 20 24 57	6 13 5 52
			1695	9 20 10 36	6 12 50 30
			B 1696	9 19 56 16	6 12 35 8
			1697	9 20 41 5	6 13 18 55
			1698	9 20 26 45	6 13 3 39

A TABLE of the SUN's Mean Motion

Years.	Longit. \odot .	Anomal. \odot .	Years.	Longit. \odot .	Anomal. \odot .
S	$^{\circ}$ ' "	S	$^{\circ}$ ' "	S	$^{\circ}$ ' "
1699	9 20 12 24	6 12 48 12	1729	9 20 55 37	6 13 10 24
BI700	9 19 58 14	6 12 32 49	1730	9 20 41 17	6 12 45 3
1701	9 20 42 53	6 13 16 36	1731	9 20 26 56	6 12 29 41
1702	9 20 28 33	6 13 1 15	BI732	9 20 12 36	6 12 14 19
1703	9 20 14 12	6 12 45 52	1733	9 20 57 25	6 12 58 5
BI704	9 19 59 52	6 12 30 30	1734	9 20 43 4	6 12 42 44
1705	9 20 44 41	6 13 14 17	1735	9 20 28 44	6 12 27 22
1706	9 20 30 21	6 12 58 56	BI736	9 20 14 23	6 12 12 0
1707	9 20 16 0	6 12 43 33	1737	9 20 59 12	6 12 55 47
BI708	9 20 1 40	6 12 28 11	1738	9 20 44 52	6 12 40 25
1709	9 20 46 29	6 13 11 58	1739	9 20 30 31	6 12 25 4
1710	9 20 32 9	6 12 56 37	BI740	9 20 16 11	6 12 9 41
1711	9 20 17 48	6 12 41 15	1741	9 21 0 50	6 12 53 28
BI712	9 20 3 28	6 12 25 53	1742	9 20 46 30	6 12 38 7
1713	9 20 48 17	6 13 9 39	1743	9 20 32 9	6 12 22 44
1714	9 20 33 57	6 12 54 18	BI744	9 20 17 49	6 12 7 22
1715	9 20 29 36	6 12 38 56	1745	9 21 2 38	6 12 51 9
BI716	9 20 5 16	6 12 23 34	1746	9 20 48 18	6 12 35 48
1717	9 20 50 5	6 13 7 21	1747	9 20 33 57	6 12 20 25
1718	9 20 35 45	6 12 51 59	BI748	9 20 19 37	6 12 5 3
1719	9 20 21 24	6 12 36 38	1749	9 21 4 26	6 12 48 50
BI720	9 20 7 3	6 12 21 15	1750	9 20 50 5	6 12 33 29
1721	9 20 51 52	6 13 5 2	1751	9 20 35 44	6 12 18 7
1722	9 20 37 32	6 12 49 41	BI752	9 20 21 24	6 12 2 45
1723	9 20 23 11	6 12 34 18	1753	9 21 6 13	6 12 46 31
BI724	9 20 8 51	6 12 18 56	1754	9 20 51 52	6 12 31 10
1725	9 20 53 40	6 13 2 43	1755	9 20 37 31	6 12 15 48
1726	9 20 39 19	6 12 47 22	BI756	9 20 23 11	6 12 0 26
1727	9 20 25 9	6 12 31 59	1757	9 21 8 0	6 12 44 13
BI728	9 20 10 48	6 12 16 37	1758	9 20 53 39	6 12 28 51

A TABLE of the SUN's Mean Motion.

Years.	Longit. ☉.				Anomal. ☉.				Years.	Longit. ☉.				Anomal. ☉.			
	S	o	'	"	S	o	'	"		S	o	'	"	S	o	'	"
1759	9	20	39	19	6	12	13	29	1789	9	21	22	22	6	12	25	42
Bi760	9	20	24	58	6	11	58	7	1790	9	21	8	2	6	12	10	21
1761	9	21	9	48	6	12	41	54	1791	9	20	53	41	6	11	54	59
1762	9	20	55	27	6	12	26	33	Bi792	9	20	39	20	6	11	39	37
1763	9	20	41	7	6	12	11	10	1793	9	21	24	9	6	12	23	23
Bi764	9	20	26	46	6	11	55	48	1794	9	21	9	49	6	12	8	2
1765	9	21	11	25	6	12	39	35	1795	9	20	55	28	6	11	52	40
1766	9	20	57	5	6	12	24	14	Bi796	9	20	41	7	6	11	37	18
1767	9	20	42	49	6	12	8	51	1797	9	21	25	57	6	12	21	5
Bi768	9	20	28	28	6	11	53	29	1798	9	21	11	36	6	12	5	43
1769	9	21	13	17	6	12	37	16	1799	9	20	57	16	6	11	50	21
1770	9	20	58	57	6	12	21	35	Bi800	9	20	42	55	6	11	34	59
1771	9	20	44	36	6	12	6	33	1801	9	21	27	44	6	12	18	46
Bi772	9	20	30	15	6	11	51	11	1802	9	21	13	24	6	12	3	25
1773	9	21	15	4	6	12	34	57	1803	9	20	59	3	6	11	48	2
1774	9	20	0	44	6	12	19	36	Bi804	9	20	44	42	6	11	32	40
1775	9	20	46	23	6	12	4	14	1805	9	21	29	31	6	12	16	27
Bi776	9	20	32	2	6	11	48	52	1806	9	21	15	11	6	12	1	6
1777	9	21	16	51	6	12	32	39	1807	9	21	0	50	6	11	45	43
1778	9	21	2	31	6	12	17	17	Bi808	9	20	46	30	6	11	30	21
1779	9	20	48	10	6	12	1	54	1809	9	21	31	19	6	12	14	8
Bi780	9	20	33	59	6	11	46	33	1810	9	21	16	59	6	11	58	47
1781	9	21	18	48	6	12	30	20	1811	9	21	2	40	6	11	43	25
1782	9	21	4	27	6	12	14	59	Bi812	9	20	48	20	6	11	28	3
1783	9	20	50	6	6	11	59	36	1813	9	20	33	9	6	12	11	49
Bi784	9	20	35	46	6	11	44	14	1814	9	21	18	49	6	11	56	28
1785	9	21	20	35	6	12	28	1	1815	9	21	4	28	6	11	41	6
1786	9	21	6	14	6	12	12	40	Bi816	9	20	50	7	6	11	25	44
1787	9	20	51	54	6	11	57	17	1817	9	21	34	56	6	12	9	31
Bi788	9	20	37	33	6	11	41	55	1818	9	21	20	36	6	11	54	9

A TABLE of the SUN's Mean Motion.

Years.	Longit. ☉.				Anomal. ☉			
	S	°	'	"	S	°	'	"
1819	9	21	6	15	6	11	38	48
B1820	9	20	51	54	6	11	23	25
1821	9	21	36	44	6	12	7	12
1822	9	21	22	23	6	11	51	50
1823	9	21	8	3	6	11	36	28
B1824	9	20	53	42	6	11	21	6

The Præcession of the Æquinoctial.

Christ years.	Præf. Æqu.				Year Chr.	° ' "			
	S	°	'	"		Chr.	Præc. Æq.		
1000	5	10	56		1000	14	1	7	
1581	10	27	19	53		1	0	0	50
1601	10	27	36	43		2	0	1	41
1621	10	27	53	32		3	0	2	31
1641	10	28	10	21		4	0	3	22
1661	10	28	27	11		5	0	4	12
1681	10	28	44	0		6	0	5	3
1701	10	29	0	49		7	0	5	53
2000	0	16	49			8	0	6	44
4000	0	33	39			9	0	7	34
6000	0	50	28			10	0	8	25
8000	1	7	18			11	0	9	15
10000	1	24	7			12	0	10	6
20000	2	48	13			13	0	10	56
30000	4	12	20			14	0	11	46
40000	5	36	27			15	0	12	37
50000	7	0	33			16	0	13	27
60000	8	24	40			17	0	14	18
70000	9	48	47			18	0	15	8
80000	11	12	53			19	0	15	59
90000	12	37	0			20	0	16	49

The Middle Motions of the Planets may be continued by the yearly Motions, as followeth.

SUN. S ° ' "				
Longitude.-----	11	29	45	40
Anomaly.-----	11	29	44	38
Præf. Æqui.---	0	0	0	50

SATURN. S ° ' "				
Longitude.-----	0	12	13	35
Anomaly.-----	0	12	12	15
Node.-----	0	0	0	36

JUPITER. S ° ' "				
Longitude.-----	1	0	20	32
Anomaly.-----	1	0	19	12
Node.-----	0	0	0	13

MARS. S ° ' "				
Longitude.-----	6	11	17	8
Anomaly.-----	6	11	15	55
Node.-----	0	0	0	43

VENUS. S ° ' "				
Longitude.-----	7	14	47	29
Anomaly.-----	7	14	46	1
Node.-----	0	0	0	37

MERCURY. S ° ' "				
Longitude.-----	1	23	43	16
Anomaly.-----	1	23	41	34
Node.-----	0	0	1	36

MOON. S ° ' "				
Longitude.-----	4	9	23	2
Anomaly.-----	2	28	43	8
Node.-----	0	19	19	43

The SUN's Mean Motion in Months and Days.

Com. Years	Pra. Eq. 1/2	J A N U A R Y.						F E B R U A R Y.						Pra. Eq. 1/2	Bissextile.				
		Longit. ☉.				Anomal. ☉.		Longit. ☉.				Anomal. ☉.							
		S	o	'	"	S	o	'	"	S	o	'	"			S	o	'	"
1	0	0	0	59	8	0	0	59	8	I	I	32	26	I	I	32	21	4	0
2	0	0	1	58	17	0	1	58	17	I	2	31	35	I	2	31	30	4	1
3	0	0	2	57	25	0	2	57	25	I	3	30	43	I	3	30	38	5	2
4	I	0	3	56	33	0	3	56	32	I	4	29	51	I	4	29	45	5	3
5	I	0	4	55	42	0	4	55	41	I	5	29	0	I	5	28	54	5	4
6	I	0	5	54	50	0	5	54	49	I	6	28	8	I	6	28	2	5	5
7	I	0	6	53	58	0	6	53	57	I	7	27	16	I	7	27	10	5	6
8	I	0	7	53	7	0	7	53	6	I	8	26	25	I	8	26	19	5	7
9	I	0	8	52	15	0	8	52	14	I	9	25	33	I	9	25	27	5	8
10	I	0	9	51	23	0	9	51	21	I	10	24	41	I	10	24	34	5	9
11	2	0	10	50	31	0	10	50	29	I	11	23	49	I	11	23	42	6	10
12	2	0	11	49	40	0	11	49	38	I	12	22	58	I	12	22	51	6	11
13	2	0	12	48	48	0	12	48	46	I	13	22	6	I	13	21	59	6	12
14	2	0	13	47	57	0	13	47	55	I	14	21	15	I	14	21	8	6	13
15	2	0	14	47	5	0	14	47	3	I	15	20	23	I	15	20	16	6	14
16	2	0	15	46	13	0	15	46	10	I	16	19	31	I	16	19	23	6	15
17	2	0	16	45	22	0	16	45	19	I	17	18	40	I	17	18	32	6	16
18	2	0	17	44	30	0	17	44	27	I	18	17	48	I	18	17	40	6	17
19	3	0	18	43	38	0	18	43	35	I	19	16	56	I	19	16	48	6	18
20	3	0	19	42	47	0	19	42	44	I	20	16	5	I	20	15	57	7	19
21	3	0	20	41	55	0	20	41	52	I	21	15	13	I	21	15	5	7	20
22	3	0	21	41	3	0	21	40	59	I	22	14	21	I	22	14	12	7	21
23	3	0	22	40	12	0	22	40	8	I	23	13	30	I	23	13	21	7	22
24	3	0	23	39	20	0	23	39	16	I	24	12	38	I	24	12	29	7	23
25	3	0	24	38	28	0	24	38	24	I	25	11	46	I	25	11	37	7	24
26	4	0	25	37	37	0	25	37	33	I	26	10	55	I	26	10	46	7	25
27	4	0	26	36	45	0	26	36	41	I	27	10	3	I	27	9	54	8	26
28	4	0	27	35	53	0	27	35	48	I	28	9	11	I	28	9	1	8	27
29	4	0	28	35	2	0	28	34	57	I	29	8	20	I	29	8	10	8	28
30	4	0	29	34	10	0	29	34	5	0	0	0	0	0	0	0	0	0	29
31	4	I	0	33	18	I	0	33	13	0	0	0	0	0	0	0	0	0	30

The SUN's Mean Motion in Months and Days.

Com. Years	Pre. Eq. j.	M A R C H.						A P R I L.						Pre. Eq. j.	Billecrite				
		Longit. ☉.			Anomal. ☉.			Longit. ☉.			Anomal. ☉.								
		S	o	' "	S	o	' "	S	o	' "	S	o	' "						
1	8	1	29	8	20	1	29	8	10	2	29	41	38	2	29	41	23	12	0
2	8	2	0	7	28	2	0	7	18	3	0	40	47	3	0	40	32	12	1
3	8	2	1	6	36	2	1	6	26	3	1	39	55	3	1	39	40	12	2
4	9	2	2	5	44	2	2	5	33	3	2	39	3	3	2	38	47	13	3
5	9	2	3	4	53	2	3	4	42	3	3	38	12	3	3	37	56	13	4
6	9	2	4	4	1	2	4	3	50	3	4	37	20	3	4	37	4	13	5
7	9	2	5	3	9	2	5	2	58	3	5	36	28	3	5	36	12	13	6
8	9	2	6	2	18	2	6	2	7	3	6	35	37	3	6	35	21	13	7
9	9	2	7	1	26	2	7	1	15	3	7	34	45	3	7	34	29	13	8
10	9	2	8	0	34	2	8	0	22	3	8	33	53	3	8	33	36	13	9
11	10	2	8	59	42	2	8	59	30	3	9	33	1	3	9	32	44	14	10
12	10	2	9	58	51	2	9	58	39	3	10	32	10	3	10	31	53	14	11
13	10	2	10	57	59	2	10	57	47	3	11	31	18	3	11	31	1	14	12
14	10	2	11	57	8	2	11	56	56	3	12	30	27	3	12	30	10	14	13
15	10	2	12	56	16	2	12	56	4	3	13	29	35	3	13	29	18	14	14
16	10	2	13	55	24	2	13	55	11	3	14	28	43	3	14	28	25	14	15
17	10	2	14	54	33	2	14	54	20	3	15	27	52	3	15	27	34	14	16
18	10	2	15	53	41	2	15	53	28	3	16	27	0	3	16	26	42	15	17
19	11	2	16	52	49	2	16	52	36	3	17	26	8	3	17	25	50	15	18
20	11	2	17	51	58	2	17	51	45	3	18	25	17	3	18	24	59	15	19
21	11	2	18	51	6	2	18	50	53	3	19	24	25	3	19	24	7	15	20
22	11	2	19	50	14	2	19	50	0	3	20	23	33	3	20	23	14	15	21
23	11	2	20	49	23	2	20	49	9	3	21	22	42	3	21	22	23	15	22
24	11	2	21	48	31	2	21	48	17	3	22	21	50	3	22	21	31	15	23
25	11	2	22	47	39	2	22	47	25	3	23	20	58	3	23	20	39	15	24
26	11	2	23	46	48	2	23	46	34	3	24	20	7	3	24	19	48	16	25
27	12	2	24	45	56	2	24	45	42	3	25	19	15	3	25	18	56	16	26
28	12	2	25	45	4	2	25	44	49	3	26	18	23	3	26	18	4	16	27
29	12	2	26	44	13	2	26	43	58	3	27	17	32	3	27	17	12	16	28
30	12	2	27	43	21	2	27	43	6	3	28	16	40	3	28	16	20	16	29
31	12	2	28	42	29	2	28	42	15	3	29	15	48	3	29	15	28	17	30

The SUN's Mean Motion in Months and Days.

Com. Years	Præ. Eq. 1"	M A Y.								J U N E.								Præ. Eq. 1"	Biflexile.
		Longit. ☉.				Anomal. ☉.				Longit. ☉.				Anomal. ☉.					
		S	o	'	"	S	o	'	"	S	o	'	"	S	o	'	"		
1	17	3	29	15	48	3	29	15	28	4	29	49	0	4	29	48	41	21	0
2	17	4	0	14	56	4	0	14	36	5	0	48	5	5	0	47	50	21	1
3	17	4	1	14	4	4	1	13	44	5	1	47	23	5	1	46	58	21	2
4	17	4	2	13	12	4	2	12	51	5	2	46	31	5	2	46	5	21	3
5	17	4	3	12	21	4	3	12	0	5	3	45	40	5	3	45	14	21	4
6	17	4	4	11	29	4	4	11	8	5	4	44	48	5	4	44	22	22	5
7	18	4	5	10	37	4	5	10	16	5	5	43	56	5	5	43	30	22	6
8	18	4	6	9	46	4	6	9	25	5	6	43	5	5	6	42	39	22	7
9	18	4	7	8	54	4	7	8	33	5	7	42	13	5	7	41	47	22	8
10	18	4	8	8	2	4	8	7	40	5	8	41	21	5	8	40	54	22	9
11	18	4	9	7	10	4	9	6	48	5	9	40	29	5	9	40	2	22	10
12	18	4	10	6	19	4	10	5	57	5	10	39	38	5	10	39	11	22	11
13	18	4	11	5	27	4	11	5	5	5	11	38	46	5	11	38	19	22	12
14	19	4	12	4	36	4	12	4	14	5	12	37	55	5	12	37	28	23	13
15	19	4	13	3	44	4	13	3	22	5	13	37	3	5	13	36	36	23	14
16	19	4	14	2	52	4	14	2	29	5	14	36	11	5	14	35	43	23	15
17	19	4	15	2	1	4	15	1	38	5	15	35	20	5	15	34	52	23	16
18	19	4	16	1	9	4	16	0	46	5	16	34	28	5	16	34	0	23	17
19	19	4	17	0	17	4	16	59	54	5	17	33	36	5	17	33	8	23	18
20	19	4	17	59	26	4	17	59	3	5	18	32	45	5	18	32	17	23	19
21	20	4	18	58	34	4	18	58	11	5	19	31	53	5	19	31	25	24	20
22	20	4	19	57	42	4	19	57	18	5	20	31	1	5	20	30	32	24	21
23	20	4	20	56	51	4	20	56	27	5	21	30	10	5	21	29	41	24	22
24	20	4	21	55	59	4	21	55	35	5	22	29	18	5	22	28	49	24	23
25	20	4	22	55	7	4	22	54	43	5	23	28	26	5	23	27	57	24	24
26	20	4	23	54	16	4	23	53	52	5	24	27	35	5	24	27	6	24	25
27	20	4	24	53	24	4	24	53	0	5	25	26	43	5	25	26	14	24	26
28	20	4	25	52	32	4	25	52	7	5	26	25	51	5	26	25	21	24	27
29	21	4	26	51	41	4	26	51	16	5	27	25	0	5	27	24	30	25	28
30	21	4	27	50	49	4	27	50	24	5	28	24	8	5	28	23	38	25	29
31	21	4	28	49	57	4	28	49	32	5	29	23	16	5	29	22	46	25	30

The SUN's Mean Motion in Months and Days.

Com. Years	Pra. Eq. 1/2	J U L Y.				A U G U S T.				Pra. Eq. 1/2	Bif. Ex. 1/2
		Longit. ☉.		Anomal. ☉.		Longit. ☉.		Anomal. ☉.			
		S	O	'	"	S	O	'	"		
1	25	5	29	23	16	5	29	22	46	29	0
2	25	6	0	22	24	6	0	21	53	29	1
3	25	6	1	21	32	6	1	21	1	29	2
4	26	6	2	20	40	6	2	20	8	30	3
5	26	6	3	19	49	6	3	19	17	30	4
6	26	6	4	18	57	6	4	18	25	30	5
7	26	6	5	18	5	6	5	17	23	30	6
8	26	6	6	17	14	6	6	16	42	30	7
9	26	6	7	16	22	6	7	15	50	30	8
10	26	6	8	15	30	6	8	14	57	30	9
11	26	6	9	14	38	6	9	14	5	31	10
12	27	6	10	13	47	6	10	13	14	31	11
13	27	6	11	12	55	6	11	12	22	31	12
14	27	6	12	12	4	6	12	11	31	31	13
15	27	6	13	11	12	6	13	10	39	31	14
16	27	6	14	10	20	6	14	9	46	31	15
17	27	6	15	9	29	6	15	8	55	31	16
18	27	6	16	8	37	6	16	8	3	31	17
19	27	6	17	7	45	6	17	7	11	32	18
20	27	6	18	6	54	6	18	6	20	32	19
21	28	6	19	6	2	6	19	5	28	32	20
22	28	6	20	5	10	6	20	4	35	32	21
23	28	6	21	4	19	6	21	3	44	32	22
24	28	6	22	3	27	6	22	2	52	33	23
25	28	6	23	2	35	6	23	2	0	33	24
26	28	6	24	1	44	6	24	1	9	33	25
27	28	6	25	0	52	6	25	0	17	33	26
28	29	6	26	0	00	6	25	59	24	33	27
29	29	6	26	59	9	6	26	58	33	33	28
30	29	6	27	58	17	6	27	57	41	34	29
31	29	6	28	57	25	6	28	56	49	34	30
						7	29	30	43	7	29

The SUN's Mean Motion in Months and Days.

Com. Years	Pra. Eq. 1/2	S E P T E M B E R.				O C T O B E R.				Pra. Eq. 1/2	Bissextile.
		Longit. ☉.		Anomal. ☉.		Longit. ☿.		Anomal. ☉.			
		S	o ' "	S	o ' "	S	o ' "	S	o ' "		
1	34	8	0 29 52	8	0 29 18	9	0 4 2	9	0 3 22	38	0
2	34	8	1 29 1	8	1 28 27	9	1 3 11	9	1 2 29	38	1
3	34	8	2 28 9	8	2 27 35	9	2 2 19	9	2 1 36	39	2
4	34	8	3 27 17	8	3 26 42	9	3 1 27	9	3 0 43	39	3
5	34	8	4 26 26	8	4 25 51	9	4 0 36	9	3 59 50	39	4
6	35	8	5 25 34	8	5 24 59	9	4 59 44	9	4 58 58	39	5
7	35	8	6 24 42	8	6 24 7	9	5 58 52	9	5 58 5	39	6
8	35	8	7 23 51	8	7 23 16	9	6 58 1	9	6 57 13	39	7
9	35	8	8 22 59	8	8 22 24	9	7 57 9	9	7 56 21	39	8
10	35	8	9 22 7	8	9 21 31	9	8 56 17	9	8 55 28	40	9
11	35	8	10 21 15	8	10 20 39	9	9 55 25	9	9 54 36	40	10
12	36	8	11 20 24	8	11 19 48	9	10 54 34	9	10 53 45	40	11
13	36	8	12 19 32	8	12 18 56	9	11 53 42	9	11 52 53	40	12
14	36	8	13 18 39	8	13 18 5	9	12 52 49	9	12 52 2	40	13
15	36	8	14 17 48	8	14 17 13	9	13 51 58	9	13 51 10	40	14
16	36	8	15 16 57	8	15 16 20	9	14 51 7	9	14 50 17	40	15
17	36	8	16 16 6	8	16 15 29	9	15 50 16	9	15 49 26	40	16
18	36	8	17 15 14	8	17 14 37	9	16 49 24	9	16 48 34	41	17
19	36	8	18 14 22	8	18 13 45	9	17 48 32	9	17 47 42	41	18
20	37	8	19 13 31	8	19 12 54	9	18 47 41	9	18 46 51	41	19
21	37	8	20 12 39	8	20 12 2	9	19 46 49	9	19 45 59	41	20
22	37	8	21 11 47	8	21 11 9	9	20 45 57	9	20 45 6	41	21
23	37	8	22 10 56	8	22 10 18	9	21 45 6	9	21 44 15	41	22
24	37	8	23 10 4	8	23 9 26	9	22 44 14	9	22 43 23	41	23
25	37	8	24 9 12	8	24 8 34	9	23 43 22	9	23 42 31	42	24
26	37	8	25 8 21	8	25 7 43	9	24 42 31	9	24 41 40	42	25
27	38	8	26 7 29	8	26 6 51	9	25 41 39	9	25 40 48	42	26
28	38	8	27 6 37	8	27 5 58	9	26 40 47	9	26 39 56	42	27
29	38	8	28 5 46	8	28 5 7	9	27 39 56	9	27 39 4	42	28
30	38	8	29 4 54	8	29 4 15	9	28 39 4	9	28 38 12	42	29
31	38	9	0 4 2	9	0 3 22	9	29 38 12	9	29 37 20	42	30

The SUN's Mean Motion in Months and Days.

Com. Years	Præ. Eq. 1	N O V E M B E R.				D E C E M B E R.				Præ. Eq. 2	Biflexile
		Longit. ☉.		Anomal. ☉.		Longit. ☉.		Anomal. ☉.			
		S	o ' "	S	o ' "	S	o ' "	S	o ' "		
1	42	10	0 37 20	10	0 36 27	II	0 II 30	II	0 IO 32	46	0
2	42	10	1 36 29	10	1 35 36	II	I IO 39	II	I 9 40	46	I
3	43	10	2 35 37	10	2 34 44	II	2 9 47	II	2 8 48	47	2
4	43	10	3 34 45	10	3 33 52	II	3 8 55	II	3 7 55	47	3
5	43	10	4 33 54	10	4 33 0	II	4 8 4	II	4 7 4	47	4
6	43	10	5 33 2	10	5 32 8	II	5 7 12	II	5 6 12	47	5
7	43	10	6 32 10	10	6 31 16	II	6 6 20	II	6 5 20	47	6
8	43	10	7 31 19	10	7 30 25	II	7 5 29	II	7 4 29	47	7
9	43	10	8 30 27	10	8 29 33	II	8 4 37	II	8 3 37	47	8
10	43	10	9 29 35	10	9 28 40	II	9 3 45	II	9 2 44	47	9
11	44	10	10 28 43	10	10 27 48	II	10 2 53	II	10 1 52	48	10
12	44	10	11 27 52	10	11 26 57	II	11 2 2	II	11 1 1	48	11
13	44	10	12 27 0	10	12 26 5	II	12 1 10	II	12 0 9	48	12
14	44	10	13 26 9	10	13 25 14	II	13 0 19	II	12 59 18	48	13
15	44	10	14 25 17	10	14 24 22	II	13 59 27	II	13 58 26	48	14
16	44	10	15 24 25	10	15 23 29	II	14 58 35	II	14 57 33	48	15
17	44	10	16 23 34	10	16 22 38	II	15 57 44	II	15 56 42	48	16
18	45	10	17 22 42	10	17 21 46	II	16 56 52	II	16 55 50	49	17
19	45	10	18 21 50	10	18 20 54	II	17 56 0	II	17 54 58	49	18
20	45	10	19 20 59	10	19 20 3	II	18 55 9	II	18 54 7	49	19
21	45	10	20 20 7	10	20 19 11	II	19 54 17	II	19 53 15	49	20
22	45	10	21 19 15	10	21 18 18	II	20 53 25	II	20 52 22	49	21
23	45	10	22 18 24	10	22 17 27	II	21 52 34	II	21 51 31	49	22
24	45	10	23 17 32	10	23 16 35	II	22 51 42	II	22 50 39	49	23
25	45	10	24 16 40	10	24 15 43	II	23 50 50	II	23 49 47	50	24
26	46	10	25 15 49	10	25 14 52	II	24 49 59	II	24 48 56	50	25
27	46	10	26 14 57	10	26 14 0	II	25 49 7	II	25 48 4	50	26
28	46	10	27 14 5	10	27 13 7	II	26 48 15	II	26 47 11	50	27
29	46	10	28 13 14	10	28 12 16	II	27 47 24	II	27 46 20	50	28
30	46	10	29 12 22	10	29 11 24	II	28 46 32	II	28 45 28	50	29
31	46	II	0 II 30	II	0 IO 32	II	29 45 40	II	29 44 36	50	30

The SUN'S Mean Motion in Ho. Min. and Sec.

H	Longit. ☉	Anom. ☉	H	Longit. ☉	Anom. ☉
	° ' "	° ' "		° ' "	° ' "
1	0 2 28	0 2 28	31	1 16 23	1 16 23
2	0 4 56	0 4 56	32	1 18 51	1 18 51
3	0 7 24	0 7 24	33	1 21 19	1 21 19
4	0 9 51	0 9 51	34	1 23 47	1 23 47
5	0 12 19	0 12 19	35	1 26 15	1 26 15
6	0 14 47	0 14 47	36	1 28 43	1 28 43
7	0 17 15	0 17 15	37	1 31 11	1 31 11
8	0 19 43	0 19 43	38	1 33 39	1 33 39
9	0 22 11	0 22 11	39	1 36 6	1 36 6
10	0 24 38	0 24 38	40	1 38 34	1 38 34
11	0 27 6	0 27 6	41	1 41 2	1 41 2
12	0 29 34	0 29 34	42	1 43 30	1 43 30
13	0 32 2	0 32 2	43	1 45 58	1 45 58
14	0 34 30	0 34 30	44	1 48 25	1 48 25
15	0 36 58	0 36 58	45	1 50 53	1 50 53
16	0 39 25	0 39 25	46	1 53 21	1 53 21
17	0 41 53	0 41 53	47	1 55 49	1 55 49
18	0 44 21	0 44 21	48	1 58 17	1 58 17
19	0 46 49	0 46 49	49	2 0 44	2 0 44
20	0 49 17	0 49 17	50	2 3 12	2 3 12
21	0 51 45	0 51 45	51	2 5 40	2 5 40
22	0 54 13	0 54 13	52	2 8 8	2 8 8
23	0 56 40	0 56 40	53	2 10 36	2 10 36
24	0 59 8	0 59 8	54	2 13 3	2 13 3
25	1 1 36	1 1 36	55	2 15 31	2 15 31
26	1 4 4	1 4 4	56	2 17 59	2 17 59
27	1 6 32	1 6 32	57	2 20 27	2 20 27
28	1 9 0	1 9 0	58	2 22 55	2 22 55
29	1 11 27	1 11 27	59	2 25 23	2 25 23
30	1 13 55	1 13 55	60	2 27 51	2 27 51
"	" " "	" " "	"	" " "	" " "

A TABLE of the SUN's Equation.

Degrees.	Sig. 9.		Logar.	Sig. 1.		Logar.	Sig. 2.		Logar.	Degrees.
	Equa.	Sub.		Equa.	Sub.		Equa.	Sub.		
0	0	0	500773	0	57	51	1	40	55	30
1	0	1	500773	0	59	36	1	41	57	29
2	0	3	500772	1	1	20	1	42	56	28
3	0	5	500772	1	3	4	1	43	55	27
4	0	7	500771	1	4	45	1	44	51	26
5	0	9	500770	1	6	27	1	45	45	25
6	0	11	500769	1	8	6	1	46	38	24
7	0	13	500767	1	9	44	1	47	28	23
8	0	15	500765	1	11	21	1	48	17	22
9	0	17	500763	1	12	57	1	49	3	21
10	0	19	500761	1	14	32	1	49	48	20
11	0	21	500759	1	16	5	1	50	31	19
12	0	23	500757	1	17	37	1	51	11	18
13	0	25	500754	1	19	8	1	51	50	17
14	0	27	500751	1	20	37	1	52	27	16
15	0	29	500748	1	22	5	1	53	1	15
16	0	31	500744	1	23	32	1	53	34	14
17	0	33	500740	1	24	58	1	54	4	13
18	0	35	500736	1	26	20	1	54	33	12
19	0	37	500732	1	27	41	1	54	59	11
20	0	39	500728	1	29	2	1	55	27	10
21	0	41	500723	1	30	21	1	55	45	9
22	0	43	500719	1	31	38	1	56	5	8
23	0	45	500714	1	32	53	1	56	23	7
24	0	47	500709	1	34	7	1	56	39	6
25	0	48	500704	1	35	19	1	56	52	5
26	0	50	500698	1	36	30	1	57	4	4
27	0	52	500693	1	37	39	1	57	13	3
28	0	54	500687	1	38	46	1	57	20	2
29	0	56	500681	1	39	51	1	57	25	1
30	0	57	500674	1	40	55	1	57	28	0
Add.				Add.			Add.			
Sig. 11.				Sig. 10.			Sig. 9.			

A TABLE of the SUN's Equation.

Degrees.	Sig. 3.		Sig. 4.		Sig. 5.		Degrees.
	Equa. Sub.	Logar.	Equa. Sub.	Logar.	Equa. Sub.	Logar.	
0	1 57 28	500017	1 43 8	499624	1 0 4	499329	30
1	1 57 30	500003	1 42 7	499613	0 58 15	499322	29
2	1 57 29	499989	1 41 4	499601	0 56 25	499316	28
3	1 57 27	499976	1 39 59	499589	0 54 33	499309	27
4	1 57 24	499963	1 38 52	499577	0 52 41	499302	26
5	1 57 18	499949	1 37 44	499565	0 50 48	499296	25
6	1 57 10	499938	1 36 33	499554	0 48 54	499290	24
7	1 57 0	499923	1 35 20	499543	0 46 58	499285	23
8	1 56 47	499909	1 34 6	499532	0 45 2	499279	22
9	1 56 32	499896	1 32 51	499521	0 43 5	499274	21
10	1 56 15	499883	1 31 33	499516	0 41 8	499269	20
11	1 55 56	499868	1 30 14	499499	0 39 9	499264	19
12	1 55 35	499855	1 28 52	499488	0 37 9	499260	18
13	1 55 11	499842	1 27 29	499478	0 35 9	499256	17
14	1 54 45	499828	1 26 5	499468	0 33 8	499252	16
15	1 54 18	499815	1 24 38	499458	0 31 7	499248	15
16	1 53 48	499802	1 23 10	499447	0 29 5	499245	14
17	1 53 15	499789	1 21 41	499437	0 27 2	499241	13
18	1 52 41	499776	1 20 19	499428	0 24 59	499238	12
19	1 52 5	499763	1 18 37	499419	0 22 55	499235	11
20	1 51 26	499750	1 17 3	499410	0 20 51	499233	10
21	1 50 46	499737	1 15 27	499401	0 18 46	499230	9
22	1 50 3	499724	1 13 50	499392	0 16 41	499228	8
23	1 49 18	499711	1 12 11	499384	0 14 36	499226	7
24	1 48 31	499698	1 10 31	499375	0 12 30	499225	6
25	1 47 43	499686	1 8 50	499367	0 10 24	499223	5
26	1 46 52	499673	2 7 7	499359	0 8 18	499222	4
27	1 45 59	499661	1 5 23	499351	0 6 12	499221	3
28	1 45 5	499648	1 3 38	499344	0 4 6	499220	2
29	1 44 7	499636	1 1 42	499336	0 2 0	499220	1
30	1 43 8	499624	1 0 4	499329	0 0 0	499220	0
Add.			Add.		Add.		
Sig. 8.			Sig. 7.		Sig. 6.		

TABLE of the SUMS Expended.

The Epocha or Radices.										Moon's Mean Motion to 20 Years									
Anni	Longit. ☾			Anom. ☾			Node ☾			Years.	Longit. ☾			Anom. ☾			Node ☾		
Christi	S	o	'	S	o	'	S	o	'		S	o	'	S	o	'	S	o	'
14	2	32	6	21	42	8	28	31		14	9	23	2	28	43	0	19	20	
101	2	10	21	1	10	13	4	14	20	28	18	46	5	27	26	1	8	39	
201	0	18	9	7	28	43	0	0	8	30	28	9	8	26	9	1	27	59	
301	10	25	58	2	17	14	7	15	58	B	45	20	43	0	7	56	2	17	22
401	9	3	47	9	5	45	3	1	47	510	0	6	3	6	40	3	6	42	
501	7	11	35	3	24	16	10	17	35	62	9	29	6	5	23	3	26	1	
601	5	19	24	10	12	47	6	3	24	76	18	52	9	4	6	4	15	21	
701	3	27	12	5	1	18	1	19	13	B	811	11	25	0	15	53	5	4	44
801	2	5	1	11	19	49	9	5	1	93	20	49	3	24	36	5	24	4	
901	0	12	50	6	8	20	4	20	50	108	0	12	6	13	19	6	13	24	
1001	10	20	38	0	26	50	0	6	39	110	9	35	9	12	27		2	43	
1101	8	28	27	7	15	21	7	22	28	B	125	2	8	0	23	49	7	22	6
1201	7	6	16	2	3	52	3	8	17	139	11	31	3	22	32	8	11	26	
1301	5	14	4	8	22	23	10	24	6	141	20	54	6	21	16	9	0	46	
1401	3	21	53	3	10	54	6	9	55	156	0	17	9	19	59	9	20	5	
1501	1	29	41	9	29	25	1	25	46	B	1610	22	51	1	1	46	10	9	28
1601	0	7	30	4	17	55	9	11	33	173	2	14	4	0	29	10	28	48	
1701	10	15	19	11	6	26	4	27	22	187	11	37	6	29	12	11	18	8	
1801	8	23	7	5	24	57	0	13	11	1911	21	0	9	27	55	5	7	27	
1901	7	0	56	0	13	28	7	28	59	B	204	13	34	1	9	42	0	26	50
2001	5	8	44	7	1	59	3	14	48	Years from 1690.									
The Moon's Mean Motion exceeding 20 Years.										1690	9	22	33	1	11	20	0	0	8
										1691	2	1	56	4	9	57	11	10	49
										1692	6	11	20	7	8	46	10	21	29
										1693	11	3	53	10	20	34	10	2	6
										1694	3	13	16	1	19	17	9	12	46
										1695	7	22	39	4	18	0	8	23	23
										1696	0	2	27	7	16	43	8	4	7
										1697	4	24	36	10	28	30	7	14	44
										1698	9	3	59	1	27	13	6	25	24

A TABLE of the MOON'S Mean Motion

Years.	Longit.	Anom.	Node	Years.	Longit.	Anom.	Node
S	o	'S	o	'S	o	'S	o
1699	I	13 22	4 25 56	6 6 5	1729	2 10 18	I 2 1 10 25 48
BI700	5	22 45	7 24 39	5 16 45	1730	6 19 41	4 0 55 10 6 28
1701	10	15 19	11 6 26	4 27 22	1731	10 29 4	6 29 28 9 17 8
1702	2	24 42	2 5 9	4 8 2	BI732	3 8 27	9 28 11 8 27 48
1703	7	4 5	5 3 53	3 18 43	1733	8 1 11	9 58 8 8 26
BI704	11	13 28	8 2 36	2 29 23	1734	0 10 24	4 8 41 7 19 6
1705	4	6 1	11 14 23	2 10 0	1735	4 19 47	7 7 24 6 29 46
1706	8	15 24	2 13 6	1 20 40	BI736	8 29 10	10 6 7 6 10 26
1707	0	24 47	5 11 49	1 1 20	1737	1 21 43	1 17 54 5 21 4
BI708	5	4 10	8 10 32	0 12 1	1738	6 1 6	4 16 37 5 1 44
1709	9	26 44	11 22 19	11 22 38	1739	10 10 29	7 15 21 4 12 24
1710	2	6 7	2 21 2	11 3 18	BI740	2 19 52	10 14 4 3 23 4
1711	6	15 30	5 19 45	10 13 58	1741	7 12 26	2 25 51 3 3 42
BI712	10	24 53	8 18 29	9 24 39	1742	11 21 49	4 24 34 2 14 22
1713	3	17 37	0 0 16	9 5 16	1743	4 1 12	7 23 17 1 25 2
1714	7	26 50	2 28 59	8 15 56	BI744	8 10 35	10 22 0 1 5 42
1715	0	6 13	6 5 42	7 26 36	1745	1 3 9	2 3 47 0 16 19
BI716	4	15 36	8 26 25	7 7 17	1746	5 12 32	5 2 30 11 27 0
1717	9	8 10	0 8 12	6 17 54	1747	9 21 55	8 1 13 11 7 40
1718	1	17 33	3 6 55	5 28 34	BI748	2 1 18	10 29 57 10 18 20
1719	5	26 56	6 5 37	5 9 14	1749	6 23 52	2 11 44 9 28 57
BI720	10	6 19	9 4 21	4 19 54	1750	11 3 15	5 10 27 9 9 38
1721	2	28 52	0 16 9	4 0 32	1751	3 12 38	8 9 10 8 20 18
1722	7	8 15	3 14 52	3 11 12	BI752	7 22 1	11 7 53 8 0 58
1723	11	17 38	6 13 35	2 21 52	1753	0 14 34	2 19 40 7 11 35
BI724	7	27 19	12 18 2	2 2 33	1754	4 23 57	5 18 23 6 22 16
1725	3	19 35	0 24 5	1 13 10	1755	9 3 20	9 17 16 6 2 56
1726	0	28 58	3 22 48	0 23 50	BI756	1 12 43	11 15 49 5 13 36
1727	5	8 21	6 21 32	0 4 30	1757	0 5 17	2 27 36 4 24 13
BI728	9	17 44	9 29 14	11 15 11	1758	10 14 40	5 26 20 4 4 54

A TABLE of the MOON'S Mean Motion.

Years.	Longit.	Anom.	Node	Years.	Longit.	Anom.	Node
S	o	'	S	S	o	'	S
1759	21 24 23	8 25 03	3 15 34	1789	3 0 20 38	5 24 17	5 17
B1760	7 1 3 26	11 23 46	2 26 14	1790	8 7 00 22	7 29 51	15 57
1761	11 26 00	3 0 5 33	2 6 51	1791	0 4 09 45	10 28 35	6 26 37
1762	4 8 15 23	6 0 4 16	1 17 32	B1792	4 4 19 28	1 27 18	6 7 18
1763	8 8 34 46	9 1 3 10	0 28 12	1793	9 8 11 41	5 29 45	17 55
B1764	0 24 09	0 1 42	0 8 52	1794	1 2 21 24	8 0 7 47	4 28 35
1765	5 0 16 43	3 13 29	11 19 29	1795	6 0 00 27	11 16 30	4 9 15
1766	9 0 26 06	6 12 12	11 0 10	B1796	10 9 50	2 25 13	3 19 56
1767	2 7 5 29	9 10 56	10 10 50	1797	3 2 24	5 17 13	0 0 33
B1768	6 2 34 52	0 9 40	9 21 30	1798	7 11 47	8 15 44	2 11 13
1769	11 17 25	3 21 26	9 2 7	1799	11 21 10	11 14 23	1 21 53
1770	3 8 16 48	6 20 09	8 12 47	B1800	4 0 33	2 13 10	1 2 44
1771	7 26 11	9 18 52	7 23 27	1801	8 23 07	5 24 57	0 13 11
B1772	0 5 34	0 17 35	7 4 8	1802	1 2 30	8 23 40	11 23 51
1773	4 28 8	3 39 22	6 14 45	1803	5 11 53	11 22 23	11 4 32
1774	9 1 7 31	6 28 05	5 25 25	B1804	9 21 16	2 21 06	10 15 12
1775	1 16 54	9 26 48	5 6 6	1805	2 13 50	6 2 54	9 25 49
B1776	5 26 17	0 25 24	16 46	1806	6 23 13	9 1 37	9 6 29
1777	10 18 51	4 7 19	3 27 23	1807	11 2 36	0 0 20	8 17 10
1778	2 28 14	7 6 23	8 3	B1808	3 11 59	2 29 37	27 50
1779	7 7 37	10 4 45	2 18 44	1809	8 4 32	6 10 49	7 8 27
B1780	11 17 01	1 3 28	1 29 24	1810	0 13 56	9 9 42	6 19 7
1781	4 8 9 33	4 15 15	1 10 1	1811	4 23 19	0 8 17	5 29 48
1782	8 18 56	7 13 58	0 20 41	B1812	9 2 49	3 7 05	10 28
1783	0 28 19	10 12 41	0 1 22	1813	1 25 15	6 18 46	4 21 5
B1784	5 7 42	1 11 24	11 12 2	1814	6 4 38	9 17 29	4 1 45
1785	10 0 16	4 23 12	10 22 49	1815	10 14 10	16 12 3	12 25
1786	2 9 39	7 21 55	10 3 19	B1816	2 23 24	3 14 55	2 23 6
1787	6 19 21	10 20 38	9 14 0	1817	7 15 58	6 26 43	2 3 43
B1788	10 28 25	1 19 21	8 24 40	1818	11 25 21	9 25 26	1 14 27

A TABLE of the MOON'S Mean Motion

Com. Years	JANUARY.			FEBRUARY.			Biflexile.
	Longit. ☾	Anom. ☾	Node.	Longit. ☾	Anom. ☾	Node.	
	S o '	S o '	o '	S o '	S o '	o '	
1	0 13 11	0 13 4	0 3	2 1 39	1 28 5	1 41	0
2	0 26 21	0 26 8	0 6	2 14 49	2 11 9	1 44	1
3	1 9 32	1 9 12	0 10	2 28 0	2 24 13	1 48	2
4	1 22 42	1 22 15	0 13	3 11 10	3 7 16	1 51	3
5	2 5 53	2 5 19	0 16	3 24 21	3 20 20	1 54	4
6	2 19 4	2 18 23	0 19	4 7 32	4 3 24	1 57	5
7	3 2 14	3 1 27	0 22	4 20 42	4 16 28	2 0	6
8	3 15 24	3 14 31	0 25	5 3 52	4 29 32	2 3	7
9	3 28 35	3 27 35	0 29	5 17 3	5 12 36	2 7	8
10	4 11 46	4 10 39	0 32	6 0 14	5 25 40	2 10	9
11	4 24 56	4 23 43	0 35	6 13 24	6 8 44	2 13	10
12	5 8 7	5 6 47	0 38	6 26 35	6 21 48	2 16	11
13	5 21 18	5 19 51	0 41	7 9 46	7 4 52	2 19	12
14	6 4 28	6 2 55	0 44	7 22 56	7 17 56	2 22	13
15	6 17 39	6 15 59	0 47	8 6 7	8 1 0	2 25	14
16	7 0 49	6 29 2	0 51	8 19 17	8 14 3	2 28	15
17	7 14 0	7 12 6	0 54	9 2 28	8 27 7	2 32	16
18	7 27 10	7 25 10	0 57	9 15 38	9 10 11	2 35	17
19	8 10 21	8 8 14	1 0	9 28 49	9 23 15	2 38	18
20	8 23 32	8 21 18	1 4	10 12 0	10 6 19	2 42	19
21	9 6 42	9 4 22	1 7	10 25 10	10 19 23	2 45	20
22	9 19 53	9 17 26	1 10	11 8 21	11 2 27	2 48	21
23	10 3 3	10 0 30	1 13	11 21 31	11 15 31	2 51	22
24	10 16 14	10 13 34	1 16	0 4 42	11 28 35	2 54	23
25	10 29 25	10 26 38	1 19	0 17 53	0 11 39	2 57	24
26	11 12 35	11 9 42	1 23	1 1 3	0 24 43	3 1	25
27	11 25 46	11 22 46	1 26	1 14 14	1 7 47	3 4	26
28	0 8 56	0 5 49	1 29	1 27 24	1 20 50	3 7	27
29	0 22 7	0 18 53	1 32	2 10 34	2 3 54	3 10	28
30	1 5 18	1 1 57	1 35	0 0 0	0 0 0	0 0	29
31	1 18 28	1 15 1	1 38	0 0 0	0 0 0	0 0	30

A TABLE of the MOON'S Mean Motion

Com. Years	M A R C H.			A P R I L.			Biflexile.
	Longit. ☾	Anom. ☾	Node.	Longit. ☾	Anom. ☾	Node.	
	S o '	S o ' o ' ,	o ' ,	S o ' S o ' o ' ,	S o ' S o ' o ' ,	o ' ,	
1	2 15 35	2 5 54	3 10	3 26 3	3 18 55	4 49	0
2	2 23 45	2 16 58	3 13	4 12 14	4 1 59	4 52	1
3	3 6 56	3 0 2	3 17	4 25 25	4 15 3	4 56	2
4	3 20 6	3 13 5	3 20	5 8 35	4 28 6	4 59	3
5	4 5 17	3 26 9	3 23	5 21 46	5 11 10	5 2	4
6	4 16 28	4 9 14	3 26	6 4 57	5 24 14	5 5	5
7	4 29 38	4 22 17	3 29	6 18 7	6 7 18	5 8	6
8	5 12 49	5 5 21	3 32	7 1 18	6 20 22	5 11	7
9	5 25 59	5 18 25	3 36	7 14 28	7 3 26	5 15	8
10	6 9 10	6 1 29	3 39	7 27 39	7 16 30	5 18	9
11	6 22 20	6 14 33	3 42	8 10 49	7 29 34	5 21	10
12	7 5 31	6 27 37	3 45	8 24 0	8 12 38	5 24	11
13	7 18 42	7 10 41	3 48	9 7 11	8 25 42	5 27	12
14	8 1 52	7 23 45	3 51	9 20 21	9 8 46	5 30	13
15	8 15 3	8 6 49	3 54	10 3 32	9 21 50	5 33	14
16	8 28 13	8 19 52	3 58	10 16 42	10 4 53	5 37	15
17	9 11 24	9 2 56	4 1	10 29 53	10 17 57	5 40	16
18	9 24 34	9 16 0	4 4	11 13 3	11 1 1	5 43	17
19	10 7 45	9 29 4	4 7	11 26 14	11 14 5	5 46	18
20	10 20 56	10 12 8	4 11	0 9 25	11 27 9	5 50	19
21	11 4 6	10 25 12	4 14	0 22 35	0 10 13	5 53	20
22	11 17 17	11 8 16	4 17	1 5 46	0 23 17	5 56	21
23	0 0 27	11 21 20	4 20	1 18 56	1 6 21	5 59	22
24	0 13 38	0 4 24	4 23	2 2 7	1 19 25	6 2	23
25	0 26 49	0 17 28	4 26	2 15 18	2 2 29	6 5	24
26	1 9 59	1 0 32	4 30	2 28 28	2 15 33	6 9	25
27	1 23 10	1 13 36	4 33	3 11 37	2 28 37	6 12	26
28	2 6 20	1 26 39	4 36	3 24 49	3 11 40	6 15	27
29	2 19 31	2 9 43	4 39	4 8 0	3 24 44	6 18	28
30	3 2 42	2 22 47	4 42	4 21 10	4 7 48	6 21	29
31	3 15 52	3 5 51	4 45	0 0 0	0 0 0	0 0	30

Com. Years	M A Y.			J U N E.			Biflexile
	Longit. ☾.	Anom. ☾.	Node.	Longit. ☾.	Anom. ☾.	Node.	
	S o '	S o '	o '	S o '	S o '	o '	
1	5 4 21	4 20 52	6 24	6 22 49	6 5 53	8 3	0
2	5 17 31	5 3 56	6 27	7 5 59	6 18 57	8 6	1
3	6 0 42	5 17 0	6 31	7 19 10	7 2 1	8 10	2
4	6 13 52	6 0 3	6 34	8 2 20	7 15 4	8 13	3
5	6 27 3	6 13 7	6 37	8 15 31	7 28 8	8 16	4
6	7 10 14	6 26 11	6 40	8 28 42	8 11 12	8 19	5
7	7 23 24	7 9 15	6 43	9 11 52	8 24 16	8 22	6
8	8 6 35	7 22 19	6 46	9 25 2	9 7 20	8 25	7
9	8 19 45	8 5 23	6 50	10 8 13	9 20 24	8 29	8
10	9 2 56	8 18 27	6 53	10 21 24	10 3 28	8 32	9
11	9 16 6	9 1 31	6 56	11 4 34	10 16 32	8 35	10
12	9 29 17	9 14 35	6 59	11 17 45	10 29 36	8 38	11
13	10 12 28	9 27 39	7 2	0 0 56	11 12 40	8 41	12
14	10 25 38	10 10 43	7 5	0 14 6	11 25 44	8 44	13
15	11 8 49	10 23 47	7 8	0 27 17	0 8 48	8 47	14
16	11 21 59	11 6 50	7 12	1 10 27	0 21 51	8 51	15
17	0 5 10	11 19 54	7 15	1 23 38	1 4 55	8 54	16
18	0 18 20	0 2 58	7 18	2 6 48	1 17 59	8 57	17
19	1 1 31	0 16 2	7 21	2 19 59	2 1 3	9 0	18
20	1 14 42	0 29 6	7 25	3 3 10	2 14 7	9 4	19
21	1 27 52	1 12 10	7 28	3 16 20	2 27 11	9 7	20
22	2 11 3	1 25 14	7 31	3 29 31	3 10 15	9 10	21
23	2 24 13	2 8 18	7 34	4 12 41	3 23 19	9 13	22
24	3 7 24	2 21 22	7 37	4 25 52	4 6 23	9 16	23
25	3 20 35	3 4 26	7 40	5 9 3	4 19 27	9 19	24
26	4 3 45	3 17 30	7 44	5 22 13	5 2 31	9 23	25
27	4 16 56	4 0 34	7 47	6 5 24	5 15 35	9 26	26
28	5 0 6	4 13 37	7 50	6 18 34	5 28 38	9 29	27
29	5 13 17	4 26 41	7 53	7 1 45	6 11 42	9 32	28
30	5 26 28	5 9 45	7 56	7 14 56	6 24 46	9 34	29
31	6 9 38	5 22 49	8 0	7 28 7	7 7 50	9 38	30

The MOON's Mean Motion.

Com. Years	S E P T E M B E R.			O C T O B E R.			Diff. x 10 ⁴
	Longit. λ	Anom. λ	Node	Longit. λ	Anom. λ	Node	
	S o ' "	S o ' "	o ' "	S o ' "	S o ' "	o ' "	
1	11 5 2	10 17 51	12 55	0 10 20	11 09 48	14 30	0
2	11 18 12	10 20 55	12 58	0 23 30	11 22 52	14 33	1
3	10 1 23	11 3 59	13 2	1 6 41	0 5 56	14 37	2
4	0 14 33	11 17 2	13 5	1 19 51	0 18 59	14 40	3
5	0 27 44	0 0 6	13 8	2 3 2	1 2 3	14 43	4
6	0 10 55	0 13 10	13 11	2 16 13	1 15 7	14 46	5
7	1 24 5	0 26 14	13 14	2 29 23	1 28 11	14 49	6
8	2 7 16	1 9 18	13 17	3 12 34	2 11 15	14 52	7
9	2 20 26	1 22 22	13 21	3 25 44	2 24 19	14 56	8
10	3 3 37	2 5 26	13 24	4 8 55	3 7 23	14 59	9
11	3 16 47	2 18 30	13 27	4 22 5	3 20 27	15 2	10
12	3 29 58	3 1 34	13 30	5 5 16	4 3 31	15 5	11
13	4 13 9	3 14 38	13 33	5 18 27	4 16 35	15 8	12
14	4 26 19	3 27 42	13 36	6 1 37	4 29 39	15 11	13
15	5 9 30	4 10 46	13 39	6 14 48	5 12 43	15 14	14
16	5 22 40	4 23 49	13 43	6 27 58	5 25 46	15 18	15
17	6 5 51	5 16 5	13 46	7 11 9	6 8 50	15 21	16
18	6 19 1	5 29 9	13 49	7 24 19	6 21 54	15 24	17
19	7 2 12	6 3 1	13 52	8 7 30	7 4 58	15 27	18
20	7 15 23	6 16 5	13 56	8 20 41	7 18 2	15 31	19
21	7 28 33	6 29 9	13 59	9 3 51	8 1 6	15 34	20
22	8 11 44	7 12 13	14 2	9 17 2	8 14 10	15 37	21
23	8 24 54	7 25 17	14 5	10 0 12	8 27 14	15 40	22
24	9 8 5	8 8 21	14 8	10 13 23	9 10 18	15 43	23
25	9 21 16	8 21 25	14 11	10 26 34	9 23 22	15 46	24
26	10 4 26	9 4 29	14 15	11 9 44	10 6 26	15 50	25
27	10 17 37	9 17 33	14 18	11 22 55	10 19 30	15 53	26
28	11 0 47	10 0 36	14 21	0 6 5	11 2 33	15 56	27
29	11 13 58	10 13 40	14 24	0 19 16	11 15 37	15 59	28
30	11 27 9	10 26 44	14 27	1 2 27	11 28 41	16 2	29
31	0 10 20	11 9 48	14 30	1 15 37	0 11 45	16 6	30

The MOON's Mean Motion in Months and Days.

Com. Years	N O V E M B E R.			D E C E M B E R.			Ephemeris
	Longit. λ .	Anom. λ .	Node.	Longit. λ .	Anom. λ .	Node.	
	S o ' "	S o ' "	o ' "	S o ' "	S o ' "	o ' "	
1	1 28 48	0 24 49	16 9	3 4 6	1 26 46	17 44	0
2	2 11 58	1 7 53	16 12	3 17 16	2 9 50	17 47	1
3	2 25 9	1 20 57	16 16	4 0 27	2 22 54	17 52	2
4	3 8 19	2 4 0	16 19	4 13 37	3 5 57	17 54	3
5	3 21 30	2 17 4	16 22	4 26 48	3 19 1	17 57	4
6	4 4 41	3 0 8	16 25	5 9 59	4 2 5	18 0	5
7	4 17 51	3 13 12	16 28	5 23 9	4 15 9	18 3	6
8	5 1 1	3 26 16	16 31	6 6 20	4 28 13	18 6	7
9	5 14 12	4 9 20	16 35	6 19 30	5 11 17	18 10	8
10	5 27 23	4 22 24	16 38	7 2 41	5 24 21	18 13	9
11	6 10 33	5 5 28	16 41	7 15 51	6 7 25	18 16	10
12	6 23 44	5 18 32	16 44	7 29 2	6 20 39	18 19	11
13	7 6 55	6 1 36	16 47	8 12 13	7 3 33	18 22	12
14	7 20 5	6 14 40	16 50	8 25 23	7 16 37	18 25	13
15	8 3 16	6 27 44	16 53	9 8 34	7 29 41	18 28	14
16	8 16 26	7 10 47	16 57	9 21 44	8 12 44	18 32	15
17	8 29 37	7 23 51	17 0	10 4 55	8 25 48	18 35	16
18	9 12 47	8 6 55	17 3	10 18 5	9 8 52	18 38	17
19	9 25 58	8 19 59	17 6	11 1 16	9 21 56	18 41	18
20	10 9 9	9 3 3	17 10	11 14 27	10 5 0	18 45	19
21	10 22 19	9 16 7	17 13	11 27 37	10 18 4	18 48	20
22	11 5 30	9 29 11	17 16	0 10 48	11 1 8	18 51	21
23	11 18 40	10 12 15	17 19	0 23 58	11 14 12	18 54	22
24	0 1 51	10 25 19	17 22	1 7 9	11 27 16	18 57	23
25	0 15 2	11 8 23	17 25	1 20 20	0 10 20	19 0	24
26	0 28 12	11 21 27	17 29	2 3 30	0 23 24	19 4	25
27	1 11 23	0 4 31	17 32	2 16 41	1 6 28	19 7	26
28	1 24 33	0 17 34	17 35	2 29 51	1 19 31	19 10	27
29	2 7 44	1 0 38	17 38	3 13 2	2 2 35	19 13	28
30	2 20 55	1 13 42	17 41	3 26 13	2 15 39	19 16	29
31	3 4 6	1 26 46	17 44	4 9 23	2 28 43	19 19	30

The Moon's Mean Motion, in Hours, Minutes, and Seconds.

H.	Longit. ☾	Anom. ☾	Node.	H.	Longit. ☾	Anom. ☾	Node.
	° ' "	° ' "	' "		° ' "	° ' "	' "
1	0 32 56	0 32 39	0 8	31	17 1 10	16 52 32	4 6
2	1 5 53	1 5 20	0 16	32	17 34 7	17 25 13	4 14
3	1 38 49	1 37 59	0 24	33	18 7 3	17 57 52	4 22
4	2 11 46	2 10 39	0 32	34	18 39 59	18 30 31	4 30
5	2 44 42	2 43 18	0 40	35	19 12 55	19 3 11	4 38
6	3 17 39	3 15 59	0 48	36	19 45 52	19 35 50	4 46
7	3 50 35	3 48 38	0 56	37	20 18 48	20 8 29	4 54
8	4 23 32	4 21 18	1 4	38	20 51 45	20 41 9	5 2
9	4 56 28	4 53 58	1 12	39	21 24 41	21 13 59	5 10
10	5 29 25	5 26 38	1 19	40	21 57 38	21 46 30	5 18
11	6 2 21	5 59 17	1 27	41	22 30 34	22 19 9	5 26
12	6 35 18	6 31 57	1 35	42	23 3 31	22 51 49	5 34
13	7 8 14	7 4 47	1 43	43	23 36 27	23 24 28	5 42
14	7 41 10	7 37 16	1 51	44	24 9 24	23 57 8	5 50
15	8 14 7	8 9 56	1 59	45	24 42 20	24 29 48	5 58
16	8 47 3	8 42 36	2 7	46	25 15 17	25 2 29	6 6
17	9 20 0	9 15 16	2 15	47	25 48 13	25 25 6	6 14
18	9 52 56	9 47 55	2 23	48	26 21 10	26 7 48	6 22
19	10 25 53	10 20 35	2 31	49	26 54 6	26 40 27	6 30
20	10 58 49	10 53 15	2 39	50	27 27 3	27 13 7	6 38
21	11 31 46	11 25 55	2 47	51	27 59 59	27 45 46	6 46
22	12 4 42	11 58 34	2 55	52	28 32 56	28 18 26	6 54
23	12 37 39	12 31 15	3 3	53	29 5 52	28 51 6	7 1
24	13 10 35	13 3 54	3 11	54	29 38 49	29 23 47	7 8
25	13 43 32	13 36 34	3 19	55	30 11 45	29 56 26	7 16
26	14 16 28	14 9 13	3 27	56	30 44 42	30 29 6	7 24
27	14 49 25	14 41 54	3 34	57	31 17 38	31 1 45	7 32
28	15 22 21	15 14 33	3 42	58	31 50 34	31 34 24	7 40
29	15 55 17	15 47 12	3 50	59	32 23 31	32 7 5	7 48
30	16 28 14	16 19 15	3 58	60	32 56 27	32 39 44	7 56
31	' " "	' " "	" "	"	' " "	' " "	" "

A TABLE of the MOON'S Equation.

Degrees.	Sig. 0.			Equa. Sub.	Logar.	Sig. 1.			Equa. Sub.	Logar.	Sig. 2.			Equa. Sub.	Logar.	Degrees.
	o	'	"			o	'	"			o	'	"			
0	0	0	0	362572		2	24	35	362349		4	13	16	361720		30
1	0	5	2	362572		2	28	59	362334		4	15	55	361694		29
2	0	10	4	362571		2	33	20	362319		4	18	29	361661		28
3	0	15	5	362570		2	37	38	362303		4	20	58	361639		27
4	0	20	6	362568		2	41	54	362287		4	23	22	361612		26
5	0	25	7	362566		2	46	7	362270		4	25	42	361584		25
6	0	30	7	362564		2	50	17	362252		4	27	58	361556		24
7	0	35	6	362561		2	54	25	362235		4	30	9	361528		23
8	0	40	5	362557		2	58	29	362216		4	32	15	361499		22
9	0	45	4	362552		3	2	36	362198		4	34	15	361470		21
10	0	50	2	362546		3	6	28	362180		4	36	10	361440		20
11	0	54	59	362541		3	10	23	362161		4	38	2	361410		19
12	0	59	55	362536		3	14	16	362142		4	39	49	361380		18
13	1	4	50	362530		3	18	5	362121		4	41	31	361350		17
14	1	9	44	362523		3	21	50	362101		4	43	7	361320		16
15	1	14	37	362516		3	25	31	362080		4	44	38	361290		15
16	1	19	29	362508		3	29	8	362059		4	46	4	361259		14
17	1	24	20	362500		3	32	42	362037		4	47	25	361228		13
18	1	29	9	362491		3	36	13	362015		4	48	40	361197		12
19	1	33	56	362481		3	39	40	361992		4	49	51	361166		11
20	1	38	41	362472		3	43	3	361969		4	50	57	361135		10
21	1	43	24	362462		3	46	23	361946		4	51	58	361104		9
22	1	48	6	362452		3	49	39	361923		4	52	53	361072		8
23	1	52	47	362441		3	52	51	361898		4	53	44	361040		7
24	1	57	27	362429		3	50	59	361874		4	54	30	361008		6
25	2	2	4	362417		3	59	2	361849		4	55	9	360976		5
26	2	6	38	362404		4	2	1	361824		4	55	43	360944		4
27	2	11	11	362391		4	4	56	361799		4	56	11	360911		3
28	2	15	41	362377		4	7	46	361774		4	56	34	360878		2
29	2	20	9	362363		4	10	32	361747		4	56	51	360846		1
30	2	24	35	362349		4	13	16	361720		4	57	3	360813		0
Add.				Add.				Add.				Add.				
Sig. 11.				Sig. 10.				Sig. 9.								

A TABLE of the MOON's Equation.

Degrees.	Sig. 3.		Sig. 4.		Sig. 5.		Degrees.
	Equa. Sub. o ' "	Logar.	Equa. Sub. o ' "	Logar.	Equa. Sub. o ' "	Logar.	
0	4 57 3	360813	4 21 26	359847	2 32 48	359098	30
1	4 57 12	360780	4 18 52	359817	2 28 13	359081	29
2	4 57 14	360748	4 16 13	359788	2 23 35	359064	28
3	4 57 11	860715	4 13 31	359758	2 18 53	359047	27
4	4 57 1	360685	4 10 45	359729	2 14 8	359031	26
5	4 56 45	360650	4 7 53	359700	2 9 20	359016	25
6	4 56 24	360617	4 4 56	359672	2 4 30	359001	24
7	4 55 58	360584	4 1 54	359643	1 59 38	359086	23
8	4 55 28	360551	3 58 48	359615	1 54 43	359072	22
9	4 54 52	360518	3 55 37	359587	1 49 46	358958	21
10	4 54 10	360485	3 52 21	359559	1 44 46	358945	20
11	4 53 23	360453	3 49 0	359532	1 39 44	358932	19
12	4 52 30	360420	3 45 35	359506	1 34 41	358920	18
13	4 51 31	360387	3 42 6	359479	1 29 36	358901	17
14	4 50 27	360354	3 38 34	359453	1 24 29	358898	16
15	4 49 19	360321	3 34 57	359427	1 19 21	358888	15
16	4 48 5	360289	3 31 15	359402	1 14 12	358879	14
17	4 46 45	360256	3 27 29	359378	1 9 0	358870	13
18	4 45 20	360224	3 23 39	359353	1 3 47	358862	12
19	4 43 50	360191	3 19 45	359329	0 58 33	358855	11
20	4 42 15	360159	3 15 46	359306	0 53 18	358848	10
21	4 40 33	360127	3 11 43	359283	0 48 1	358842	9
22	4 38 46	360095	3 7 37	359261	0 42 43	358837	8
23	4 36 54	360063	3 3 28	359239	0 37 24	358832	7
24	4 34 57	360032	2 59 15	359218	0 32 5	358828	6
25	4 32 55	360001	2 54 59	359197	0 26 45	358825	5
26	4 30 48	359970	2 50 40	359176	0 21 25	358822	4
27	4 28 35	359939	2 46 17	359156	0 16 4	358820	3
28	4 26 17	359908	2 41 50	359136	0 10 42	358818	2
29	4 23 53	359877	2 37 20	359117	0 5 21	358817	1
30	4 21 26	359847	2 32 48	359098	0 0 0	358816	0
Add.			Add.		Add.		
Sig. 8.			Sig. 7.		Sig. 6.		

A TABLE of the MOON'S Reflection,
and Logarithm of the Chord of Evection.

Degrees.	Sig. 0.		Add.	Sig. 1.	Add.		Sig. 2.	Add.		Degrees.		
	Sig. 6.		Substr.		Sig. 7.			Substr.	Sig. 8.		Substr.	
	Reflecti.	"	Log.Ch. Evection		Reflecti.	"	Log. Ch. Evection		Reflecti.	"	Log. Ch. Evection	
0	0	0	000000	20	15		194201	35	4		218017	30
1	0	43	048489	20	51		195487	35	25		218485	29
2	1	26	078586	21	27		196724	35	45		218898	28
3	2	8	096184	22	3		197914	36	5		219272	27
4	2	50	108662	22	38		199060	36	24		219670	26
5	3	32	118333	23	13		200163	36	42		220031	25
6	4	14	126224	23	48		201225	37	0		220377	24
7	4	56	132893	24	22		202250	37	17		220706	23
8	5	38	138659	24	56		203238	37	33		221020	22
9	6	20	143737	25	29		204191	37	48		221319	21
10	6	53	148271	26	2		205110	38	3		221602	20
11	7	44	152363	26	34		205998	38	17		221871	19
12	8	26	156091	27	6		206855	38	30		222124	18
13	9	7	159512	27	39		207682	38	42		222363	17
14	9	48	162671	28	8		208481	38	55		222588	16
15	10	29	165604	28	38		209252	39	7		222798	15
16	11	10	168337	29	8		209997	39	18		222994	14
17	11	51	170897	29	37		210716	39	28		223176	13
18	12	31	173302	30	6		211411	39	37		223344	12
19	13	11	175568	30	34		212081	39	45		223498	11
20	13	51	177709	31	1		212729	39	53		223639	10
21	14	31	179736	31	28		213354	40	0		223765	9
22	15	10	181662	31	55		213957	40	6		223879	8
23	15	49	183491	32	21		214538	40	12		223979	7
24	16	28	185235	32	46		215099	40	17		224065	6
25	17	7	186899	33	11		215640	40	21		224138	5
26	17	45	188488	33	35		216161	40	25		224198	4
27	18	23	190009	33	58		216663	40	27		224244	3
28	19	1	191465	34	21		217146	40	28		224277	2
29	19	38	192861	34	43		217610	40	29		224297	1
30	20	15	194201	35	4		218057	40	30		224304	0
	Sig. 5. Add.			Sig. 4. Add.			Sig. 3. Add.					
	Sig. 11. Substr.			Sig. 10. Substr.			Sig. 9. Substr.					

Add H h h h

Synodical Anomaly.		A TABLE of the Moon's Evection. Substract										Synodical Anomaly.	
		Numerus Logarithmicus.											
		720000	730000	740000	750000	760000	770000	780000	790000	800000			
S. G.	o	'	o	'	o	'	o	'	o	'	o	G. S.	
0.	00	00	00	00	00	00	00	00	00	00	00	0. 12	
	50	00	10	10	10	10	10	20	20	20	3	25	
	100	10	10	10	10	20	20	30	40	50	6	20	
	150	10	20	20	30	30	40	60	70	70	9	15	
	200	20	20	30	40	50	60	70	90	90	12	10	
	250	20	30	40	50	60	70	90	110	110	14	5	
1.	00	30	30	40	50	70	90	110	130	130	17	0. 11	
	50	30	40	50	60	80	100	120	150	150	19	25	
	100	30	40	60	70	90	110	140	170	170	22	20	
	150	40	50	60	80	100	120	150	190	190	24	15	
	200	40	50	70	80	100	130	160	210	210	26	10	
	250	40	60	70	90	110	140	180	220	220	28	5	
2.	00	50	60	70	90	120	150	190	240	240	30	0. 10	
	50	50	60	80	100	120	160	200	250	250	31	25	
	100	50	60	80	100	130	160	200	260	260	32	20	
	150	50	70	80	100	130	170	210	260	260	33	15	
	200	50	70	80	110	130	170	210	270	270	34	10	
	250	50	70	90	110	140	170	220	270	270	34	5	
3.	00	50	70	90	110	140	170	220	270	270	34	0. 9	
	50	50	70	90	110	140	170	220	270	270	34	25	
	100	50	70	80	110	130	170	210	270	270	34	20	
	150	50	70	80	100	130	170	210	260	260	33	15	
	200	50	60	80	100	130	160	200	260	260	32	10	
	250	50	60	80	100	120	160	200	250	250	31	5	
4.	00	50	60	70	90	120	150	190	240	240	30	0. 8	
	50	40	60	70	90	110	140	180	220	220	28	25	
	100	40	50	70	80	100	130	170	210	210	26	20	
	150	40	50	60	80	100	120	150	190	190	24	15	
	200	30	40	60	70	90	110	140	180	180	22	10	
	250	30	40	50	60	80	100	120	160	160	20	5	
5.	00	30	30	40	50	70	90	110	140	140	17	0. 7	
	50	20	30	40	50	60	70	90	120	120	15	25	
	100	20	20	30	40	50	60	70	100	100	12	20	
	150	10	20	20	30	40	40	60	80	80	9	15	
	200	10	10	10	20	20	30	40	50	50	6	10	
	250	00	10	10	10	10	10	20	20	20	3	5	
6.	00	00	00	00	00	00	00	00	00	00	00	0. 6	
Add													

Add

Synodical Anomaly.		A TABLE of the Moon's Evection. Subtract										Synodical Anomaly.	
		Numerus Logarithmicus.											
		819000	820000	821000	822000	823000	824000	825000	826000	827000	828000		
S. G.	o	'	o	'	o	'	o	'	o	'	o	'	G. S.
0.	00	00	00	00	00	00	00	00	00	00	00	00	0. 12
	50	50	50	50	50	50	50	50	50	50	60	60	25
	100	90	90	90	100	100	100	100	110	110	110	110	20
	150	130	140	140	140	150	150	150	160	160	170	170	15
	200	180	180	190	190	200	200	200	210	210	220	220	10
	250	220	230	230	240	240	250	250	260	260	270	270	5
1.	00	260	270	270	280	290	290	300	310	310	320	320	0. 11
	50	300	310	310	320	330	340	350	350	360	370	370	25
	100	340	350	350	360	370	380	390	400	410	410	410	20
	150	370	380	390	400	410	420	430	440	450	460	460	15
	200	400	410	420	430	440	450	460	470	490	500	500	10
	250	430	440	450	460	470	480	490	510	520	530	530	5
2.	00	460	470	480	490	500	510	520	540	550	560	560	0. 10
	50	480	490	500	510	530	540	550	560	580	590	590	25
	100	500	510	520	530	550	560	570	580	600	610	610	20
	150	510	520	530	550	560	580	590	600	620	630	630	15
	200	520	530	540	560	570	590	600	610	630	640	640	10
	250	530	540	550	570	580	590	610	620	640	650	650	5
3.	00	530	540	560	570	580	600	610	620	640	650	650	0. 9
	50	530	540	550	570	580	590	610	620	640	650	650	25
	100	530	540	550	560	580	590	600	620	630	650	650	20
	150	520	530	540	550	570	580	590	610	620	640	640	15
	200	500	510	530	540	550	560	580	590	610	620	620	10
	250	480	490	510	520	530	540	560	570	580	600	600	5
4.	00	460	470	490	500	510	520	530	550	560	570	570	0. 8
	50	440	450	460	470	480	490	500	520	530	540	540	25
	100	410	420	430	440	450	460	470	480	500	510	510	20
	150	380	390	400	410	420	430	440	450	460	470	470	15
	200	350	350	360	370	380	390	400	410	420	430	430	10
	250	310	320	320	330	340	350	360	360	370	380	380	5
5.	00	270	280	280	290	300	300	310	320	320	330	330	0. 7
	50	230	230	240	240	250	260	260	270	270	280	280	25
	100	180	190	190	200	200	210	210	220	220	230	230	20
	150	140	140	150	150	150	160	160	160	170	170	170	15
	200	90	100	100	100	100	110	110	110	110	120	120	10
	250	50	50	50	50	50	50	50	60	60	60	60	5
6.	00	00	00	00	00	00	00	00	00	00	00	00	0. 6
Add													

Add

Add

A TABLE of the Moon's Evection. Subtract											Synodical Anomaly.
Numerus Logarithmicus.											
	848000	849000	850000	851000	852000	853000	854000	855000	856000		
S. G.	'	'	'	'	'	'	'	'	'	'	G. S.
0.	00	00	00	00	00	00	00	00	00	00	0. 12
50	90	90	90	90	100	100	100	100	100	100	25
100	170	180	180	190	190	190	200	200	200	210	20
150	260	270	270	280	280	290	300	300	300	310	15
200	340	350	360	370	380	390	390	400	400	410	10
250	430	440	450	460	470	480	490	500	500	510	5
1.	00	510	520	530	540	550	570	580	590	00	0. 11
50	580	590	11	21	31	51	61	81	9	25	
100	51	71	81	101	111	131	151	161	18	20	
150	121	131	151	171	191	201	221	241	26	15	
200	181	201	221	231	251	271	291	311	33	10	
250	231	251	271	291	311	331	361	381	40	5	
2.	01	281	301	331	351	371	391	411	441	46	0. 10
50	331	351	371	391	421	441	461	491	51	25	
100	361	391	411	431	461	481	511	521	56	20	
150	391	421	441	461	491	511	541	571	59	15	
200	421	441	461	481	511	541	571	592	2	10	
250	431	451	481	501	531	561	582	12	4	5	
3.	01	441	461	491	511	541	561	592	22	50.	9
50	441	461	491	511	541	561	592	22	5	25	
100	431	451	481	501	531	551	582	12	4	20	
150	411	421	461	481	511	531	561	592	2	15	
200	381	411	431	451	481	501	531	561	59	10	
250	351	371	401	421	451	471	501	521	55	5	
4.	01	311	331	361	381	401	431	451	471	500.	8
50	261	281	311	331	351	371	391	421	44	25	
100	211	231	251	271	291	311	331	361	38	20	
150	151	171	191	201	221	241	261	281	30	15	
200	81	101	121	131	151	171	191	201	22	10	
250	11	21	41	51	71	91	101	121	13	5	
5.	00	530	550	560	570	590	01	11	31	40.	7
50	450	460	470	480	500	510	520	530	54	25	
100	360	370	380	390	400	410	420	430	44	20	
150	270	280	290	300	300	310	320	330	33	15	
200	180	190	190	200	200	210	210	220	22	10	

A TABLE of the Moon's Evection. Substraet

Numerus Logarithmicus.

Synodical Anomaly.	857000	858000	859000	860000	861000	862000	863000	864000	865000	866000	Synodical Anomaly.
S. G. 0'	0	0	0	0	0	0	0	0	0	0	S. G.
0. 00	00	00	00	00	00	00	00	00	00	00	00. 12
50	110	110	110	110	110	120	120	120	120	130	1325
100	210	220	220	220	230	230	240	240	250	250	2620
150	320	330	330	340	350	360	360	370	380	390	3915
200	420	430	440	450	460	470	480	490	500	510	5210
250	520	530	450	560	570	581	01	11	21	45	
1. 01	21	31	51	61	81	91	111	121	141	160	0. 11
51	111	131	141	161	181	191	211	231	251	2725	
101	101	221	231	251	271	291	311	331	351	3720	
151	281	301	321	341	361	381	411	431	451	4715	
201	351	381	401	421	441	471	491	521	541	5710	
251	421	451	471	501	521	551	572	02	32	55	
2. 01	491	511	541	561	592	22	42	72	102	130	0. 10
51	541	571	592	22	52	82	102	132	172	2025	
101	582	12	42	72	102	132	162	192	222	2520	
152	22	52	82	112	142	172	202	232	272	3015	
202	52	82	112	142	172	202	232	272	302	3310	
252	72	102	132	162	192	222	252	292	322	365	
3. 02	82	112	142	172	202	232	262	302	342	370	0. 9
52	82	112	142	172	202	232	262	302	332	3725	
102	72	92	122	162	192	222	252	292	322	3620	
152	52	72	102	132	172	202	232	262	302	3315	
202	22	42	72	102	132	162	202	232	262	3010	
251	582	02	32	62	92	122	152	182	222	255	
4. 01	531	551	582	12	42	72	102	132	162	190	0. 8
51	471	491	521	551	572	02	32	62	92	1225	
101	401	431	451	471	501	531	551	582	12	420	
151	331	351	371	391	421	441	471	491	521	5515	
201	241	261	281	311	321	351	371	401	421	4510	
251	161	171	191	211	231	251	271	291	311	345	
5. 01	61	71	91	111	121	141	161	181	201	220	0. 7
50	560	570	591	01	11	31	41	61	81	925	
100	450	460	470	490	500	510	520	530	550	5620	
150	340	350	360	370	380	390	400	400	410	4215	
200	230	240	240	250	250	260	270	270	280	2810	
250	110	120	120	120	130	130	130	140	140	145	
6. 00	00	00	00	00	00	00	00	00	00	00	0. 6

A Table of the MOON's Latitude.

Degr.	Sig. 0 North Sig. 6 South				Sig. 1 North Sig. 7 South				Sig. 2 North Sig. 8 South				Degr.	
	Latitude		Excess		Latitude		Excess		Latitude		Excess			
	0	'	"	'	0	'	"	'	0	'	"	'		
0	0	0	0	0	0	2	29	52	8	30	4	14	43	30
1	0	5	14	0	18	2	34	22	8	45	4	22	18	29
2	0	10	27	0	36	2	38	50	9	0	4	24	49	28
3	0	15	41	0	54	2	43	15	9	15	4	27	14	27
4	0	20	54	1	12	2	47	37	9	30	4	29	34	26
5	0	26	7	1	29	2	51	56	9	45	4	31	50	25
6	0	31	19	1	55	2	56	11	10	0	4	34	0	24
7	0	36	31	2	5	3	0	24	10	14	4	36	6	23
8	0	41	42	2	22	3	4	33	10	28	4	38	6	22
9	0	46	52	2	40	3	8	39	10	42	4	40	2	21
10	0	52	2	2	57	3	12	42	10	56	4	41	52	20
11	0	57	10	3	15	3	16	41	11	9	4	43	37	19
12	1	2	18	3	32	3	20	36	11	22	4	45	17	18
13	1	7	24	3	49	3	24	28	11	35	4	46	52	17
14	1	12	29	4	7	3	28	16	11	48	4	48	21	16
15	1	17	33	4	24	3	32	6	12	1	4	49	45	15
16	1	22	36	4	41	3	35	40	12	13	4	51	4	14
17	1	27	37	4	58	3	39	17	12	25	4	52	17	13
18	1	32	36	5	15	3	42	49	12	37	4	53	26	12
19	1	37	42	5	32	3	46	17	12	49	4	54	29	11
20	1	42	30	5	49	3	49	42	13	1	4	55	26	10
21	1	47	24	6	5	3	53	2	13	12	4	56	18	9
22	1	52	16	6	22	3	56	17	13	23	4	57	4	8
23	1	57	6	6	38	3	59	29	13	34	4	57	45	7
24	2	1	54	6	55	4	2	36	13	45	4	58	21	6
25	2	6	39	7	11	4	5	38	13	55	4	58	51	5
26	2	11	23	7	27	4	8	37	14	5	4	59	16	4
27	2	16	4	7	43	4	11	30	14	14	4	59	35	3
28	2	20	42	7	58	4	14	19	14	24	4	59	49	2
29	2	25	18	8	14	4	17	4	14	33	4	59	57	1
30	2	29	52	8	30	4	19	43	14	43	5	0	0	0
Sig. 11 North Sig. 5 South					Sig. 10 North Sig. 4 South					Sig. 9 South Sig. 3 North				

A Table of the MOON'S Latitude in Eclipses.

Sig. 0 Latitude North Sig. 6 Latitude South	Sig. 0 Latitude North Sig. 6 Latitude South	Sig. 0 Latitude North Sig. 6 Latitude South
0 0 0 0 0 30 10 0 0 52 50 20 0 1 44 40 30 0 2 37 30 40 0 3 29 20 50 0 4 21 10 1 0 0 5 14 0 29 10 0 6 6 50 20 0 6 58 40 30 0 7 50 30 40 0 8 43 20 50 0 9 35 10 2 0 0 10 27 0 28 10 0 11 20 50 20 0 12 12 40 30 0 13 4 30 40 0 13 56 20 50 0 14 49 10 3 0 0 15 41 0 27 10 0 16 33 50 20 0 17 25 40 30 0 18 18 30 40 0 19 10 20 50 0 20 2 10 4 0 0 20 54 0 26 10 0 21 46 50 20 0 22 39 40 30 0 23 31 30 40 0 24 23 20 50 0 25 15 10 5 0 0 26 7 0 25	5 0 0 26 7 0 25 10 0 26 59 50 20 0 27 51 40 30 0 28 43 30 40 0 29 37 20 50 0 30 27 10 6 0 0 31 19 0 24 10 0 32 11 50 20 0 33 3 40 30 0 33 55 30 40 0 34 47 20 50 0 35 39 10 7 0 0 36 31 0 23 10 0 37 23 50 20 0 38 15 40 30 0 39 7 30 40 0 39 58 20 50 0 40 50 10 8 0 0 41 42 0 22 10 0 42 34 50 20 0 43 25 40 30 0 44 17 30 40 0 45 9 20 50 0 46 1 10 9 0 0 46 54 0 21 10 0 47 44 50 20 0 48 35 40 30 0 49 27 30 40 0 50 18 20 50 0 51 10 10 10 0 0 52 1 0 20	10 0 0 52 1 0 20 10 0 52 53 50 20 0 53 44 40 30 0 54 36 31 40 0 55 27 20 50 0 56 19 10 11 0 0 57 10 0 19 10 0 58 2 50 20 0 58 53 40 30 0 59 44 30 40 1 0 36 20 50 1 1 27 10 12 0 1 2 18 0 18 10 1 3 9 50 20 1 4 0 40 30 1 4 51 30 40 1 5 42 20 50 1 6 33 10 13 0 1 7 24 0 17 10 1 8 15 50 20 1 9 6 40 30 1 9 57 30 40 1 10 48 20 50 1 11 38 10 14 0 1 12 29 0 16 10 1 13 20 50 20 1 14 10 40 30 1 15 1 30 40 1 15 52 20 50 1 16 42 10 15 0 1 17 33 0 15
Sig. 5 Latitude North Sig. 11 Latitude South	Sig. 5 Latitude North Sig. 11 Latitude South	Sig. 5 Latitude North Sig. 11 Latitude South

A TABLE of the MOON'S Latitude in Eclipses.

Sig. 0 Latitude North Sig. 6 Latitude South				Sig. 0 Latitude North Sig. 6 Latitude South			
0	1	2	3	0	1	2	3
15 0	I	17	33	0 15	I	42	30
10	I	18	23	50	I	43	19
20	I	19	14	40	I	44	8
30	I	20	4	30	I	44	57
40	I	20	55	20	I	45	46
50	I	21	45	10	I	46	35
16 0	I	22	36	0 14	I	47	24
10	I	23	26	50	I	48	13
20	I	24	16	40	I	49	1
30	I	25	6	30	I	49	50
40	I	25	57	20	I	50	39
50	I	26	47	10	I	51	27
17 0	I	27	37	0 13	I	52	16
10	I	28	27	50	I	53	4
20	I	29	17	40	I	53	53
30	I	30	6	30	I	54	41
40	I	30	56	20	I	55	29
50	I	31	46	10	I	56	18
18 0	I	32	36	0 12	I	57	6
10	I	33	25	50	I	57	54
20	I	34	15	40	I	58	42
30	I	35	5	30	I	59	30
40	I	35	54	20	2	0	18
50	I	36	44	10	2	1	6
19 0	I	37	34	0 11	2	1	54
10	I	38	23	50	2	2	42
20	I	39	13	40	2	3	29
30	I	40	2	30	2	4	17
40	I	40	51	20	2	5	4
50	I	41	41	10	2	5	52
20 0	I	42	30	0 10	2	6	39
Sig. 5 Latitude North Sig. 11 Latitude South				Sig. 5 Latitude North Sig. 11 Latitude South			
20 0	I	42	30	0 10	2	6	39
Sig. 5 Latitude North Sig. 11 Latitude South				Sig. 5 Latitude North Sig. 11 Latitude South			
20 0	I	42	30	0 10	2	6	39

A TABLE Respecting the MOON's Orb, and Eclipses.

A Table of the Reduction of the
MOON from her proper Orb, to the
Ecliptic, and the Contrary

Anomaly, Moon's Latitude from α .

Degr.	Sig. 6	Sub.	Sig. 1	Sub.	Sig. 2	Sub.	Degr.
0	0	0	0	0	0	0	0
1	0	14	0	5	0	5	29
2	0	28	0	5	0	5	28
3	0	42	0	5	0	5	27
4	0	55	0	5	0	5	26
5	1	7	0	5	0	4	25
6	1	20	0	5	0	4	24
7	1	34	0	6	0	4	23
8	1	47	0	6	0	4	22
9	2	0	0	6	0	4	21
10	2	12	0	6	0	4	20
11	2	25	0	6	0	3	19
12	2	38	0	6	0	3	18
13	2	51	0	6	0	3	17
14	3	3	0	6	0	3	16
15	3	14	0	6	0	3	15
16	3	25	0	6	0	3	14
17	3	36	0	6	0	2	13
18	3	47	0	6	0	2	12
19	3	57	0	6	0	2	11
20	4	6	0	6	0	2	10
21	4	16	0	6	0	2	9
22	4	26	0	6	0	1	8
23	4	35	0	6	0	1	7
24	4	45	0	6	0	1	6
25	4	52	0	5	0	1	5
26	5	0	0	5	0	0	4
27	5	8	0	5	0	0	3
28	5	16	0	5	0	0	2
29	5	24	0	5	0	0	1
30	5	30	0	5	0	0	0
Degr.	Sig. 11	Add.	Sig. 10	Add.	Sig. 9	Add.	Degr.
	Sig. 5		Sig. 4		Sig. 3		

A Table of the
Distance of the
true Conjunction
or Opposition from
the greatest Obscu-
ration.

Lar. Δ .	Distance.
0	0
0	5
0	10
0	15
0	20
0	25
0	30
0	35
0	40
0	45
0	50
0	55
1	0
1	5
1	10
1	15
1	20
1	25
1	30
1	35
1	40

No. Ascend. }
So. Ascend. } .qns

No. Descend. }
So. Descend. } Add.

A Table of the Horizontal Parallax of the MOON, with the Hourly Motions, and Semidiameters of the SUN and MOON.

Middle Anom. ☉ & ☾	Semi- diam. ☉	Hourly Motion ☉	Horiz. Parall. ☾	Semi- diam. ☾	Hourly Motion ☾	Middle Anom. ☉ & ☾
S 0	16 0	2 23	53 0	14 50	29 40	0 12
6	16 1	2 23	53 1	14 51	29 41	24
12	16 1	2 23	53 3	14 52	29 43	18
18	16 2	2 23	53 7	14 53	29 48	12
24	16 2	2 23	53 14	14 54	29 56	6
I 0	16 3	2 23	53 22	14 56	30 6	0 11
6	16 3	2 24	53 33	14 59	30 18	24
12	16 3	2 24	53 45	15 2	30 32	18
18	16 4	2 24	54 0	15 6	30 49	12
24	16 6	2 25	54 17	15 10	31 9	6
2 0	16 8	2 25	54 34	15 15	31 31	0 10
6	16 9	2 25	54 54	15 20	31 53	24
12	16 10	2 26	55 15	15 25	32 16	18
18	16 11	2 26	55 37	15 31	32 40	12
24	16 13	2 27	56 1	15 37	33 5	6
3 0	16 15	2 27	56 25	15 43	33 30	0 9
6	16 17	2 28	56 50	15 49	33 57	24
12	16 19	2 28	57 15	15 45	34 24	18
18	16 20	2 29	57 41	16 1	34 50	12
24	16 21	2 30	58 6	16 7	35 16	6
4 0	16 23	2 30	58 30	16 13	35 41	0 8
6	16 25	2 31	58 54	16 18	36 5	24
12	16 26	2 31	59 16	16 22	36 27	18
18	16 27	2 32	59 37	16 26	36 48	12
24	16 28	2 32	59 56	16 31	37 8	6
5 0	16 29	2 32	60 12	16 34	37 25	0 7
6	16 29	2 33	60 26	16 36	37 41	24
12	16 30	2 33	60 37	16 37	37 54	18
18	16 30	2 33	60 45	16 38	38 3	12
24	16 30	2 33	60 48	16 39	38 8	6
6 0	16 30	2 33	60 50	16 40	38 10	0 6

A Table of the MOON's Proportional Scruples,
and Equation of Nodes.

Dif. @ 2)	Proportional Scruples						Equation of Nodes						Dif. @ 2)		
	Sig. 0 Sig. 6		Sig. 1 Sig. 7		Sig. 2 Sig. 8		Sig. 0 Sig. 6		Sig. 1 Sig. 7		Sig. 2 Sig. 8				
	0	1	0	1	0	1	0	1	0	1	0	1			
0	0	0	0	15	17	0	45	18	0	0	0	1	23	10	30
1	0	0	1	16	13	0	46	11	0	3	24	1	24	44	29
2	0	0	4	17	11	0	47	3	0	6	48	1	26	10	28
3	0	0	9	18	9	0	47	52	0	10	11	1	27	30	27
4	0	0	16	19	7	0	48	41	0	13	34	1	28	44	26
5	0	0	26	20	6	0	49	29	0	16	55	1	29	51	25
6	0	0	39	21	5	0	50	17	0	20	14	1	30	50	24
7	0	0	54	22	5	0	51	2	0	23	33	1	31	45	23
8	0	1	11	23	6	0	51	45	0	26	49	1	32	30	22
9	0	1	31	24	7	0	52	26	0	30	3	1	33	10	21
10	0	1	52	25	9	0	53	6	0	33	16	1	33	44	20
11	0	2	14	26	12	0	53	44	0	36	25	1	34	10	19
12	0	2	39	27	15	0	54	21	0	39	32	1	34	28	18
13	0	3	6	28	18	0	54	57	0	42	35	1	34	40	17
14	0	3	35	29	21	0	55	31	0	45	36	1	34	45	16
15	0	4	7	30	24	0	56	4	0	48	32	1	34	42	15
16	0	4	40	31	26	0	56	34	0	51	24	1	34	35	14
17	0	5	15	32	29	0	57	1	0	54	12	1	34	16	13
18	0	5	51	33	31	0	57	26	0	56	57	1	33	54	12
19	0	6	29	34	33	0	57	51	0	59	37	1	33	26	11
20	0	7	9	35	35	0	58	13	1	2	13	1	32	50	10
21	0	7	51	36	37	0	58	34	1	4	43	1	32	6	9
22	0	8	34	37	39	0	58	52	1	7	7	1	31	19	8
23	0	9	20	38	40	0	59	7	1	9	27	1	30	22	7
24	0	10	9	39	40	0	59	20	1	11	42	1	29	19	6
25	0	10	58	40	38	0	59	32	1	13	53	1	28	11	5
26	0	11	47	41	35	0	59	42	1	15	57	1	26	54	4
27	0	12	37	42	32	0	59	50	1	17	54	1	25	33	3
28	0	13	28	43	28	0	59	55	1	19	46	1	24	8	2
29	0	14	22	44	23	0	59	58	1	21	31	1	22	34	1
30	1	15	17	45	18	1	0	0	1	23	10	1	20	54	0
	Sig. 11 Sig. 5		Sig. 10 Sig. 4		Sig. 9 Sig. 3		Sig. 11 Sig. 5		Sig. 10 Sig. 4		Sig. 9 Sig. 3		Add.		

A Table of SATURN'S Mean Motion.

The Epocha or Radices				Years to xx.	Saturn's Mean Motion to 20 Ye.		
Anni	Longit. h	Anom. h	Node. h		Longit. h	Anom. h	Node h
Christ S	o	'S	o		S o	'S o	S o
1	2 15 44	6 22 c	3 4 28		1 0 12 14	0 12 13	0 0 1
101	7 9 2	11 13 16	3 5 28		2 0 24 27	0 24 24	0 0 1
201	0 2 19	4 4 31	3 6 28		3 1 6 41	1 6 37	0 0 2
301	4 25 36	8 25 48	3 7 28	B	4 1 18 56	1 18 51	0 0 2
401	9 18 53	1 17 4	3 8 29		5 2 1 10	2 1 3	0 0 3
501	2 12 10	6 8 19	3 9 29		6 2 13 24	2 13 16	0 0 4
601	7 5 27	10 29 35	3 10 29		7 2 25 37	2 25 28	0 0 4
701	11 28 45	3 20 51	3 11 30	B	8 3 7 53	3 7 42	0 0 5
801	4 22 2	8 12 7	3 12 30		9 3 20 6	3 19 54	0 0 5
901	9 15 19	1 3 23	3 13 30		10 4 2 19	4 2 7	0 0 6
1001	2 8 36	5 24 39	3 14 31		11 4 14 33	4 14 19	0 0 7
1101	7 1 54	10 15 55	3 15 31	B	12 4 26 48	4 26 33	0 0 7
1201	11 25 11	3 7 10	3 16 31		13 5 9 2	5 8 46	0 0 8
1301	4 18 28	7 28 27	3 17 32		14 5 21 15	5 20 57	0 0 8
1401	9 11 45	0 19 43	3 18 32		15 6 3 29	6 3 10	0 0 9
1501	2 5 2	5 10 58	3 19 32	B	16 6 15 45	6 15 25	0 0 9
1601	6 28 20	10 2 14	3 20 33		17 6 27 58	6 27 36	0 0 10
1701	11 21 37	2 23 30	3 21 33		18 7 10 12	7 9 49	0 0 11
1801	4 14 54	7 14 45	3 22 33		19 7 22 25	7 22 1	0 0 11
1901	9 8 12	0 6 2	3 23 34	B	20 8 4 40	8 4 15	0 0 12
2001	2 1 30	4 27 18	3 24 34		Years from 1690.		
Saturn's Mean Motion exceeding 20 Years.				1690	7 7 5	10 9 9	3 21 26
20	8 4 40	8 4 15	0 0 12	1691	7 19 18	10 21 22	3 21 27
40	4 9 20	4 8 30	0 0 24	B1692	8 1 32	11 3 34	3 21 27
60	0 14 0	0 12 46	0 0 36	1993	8 13 47	11 15 48	3 21 28
80	8 18 39	8 17 1	0 0 48	1694	8 26 1	11 28 1	3 21 28
100	4 23 18	4 21 16	0 1 0	1695	9 8 14	0 10 13	3 21 29
1000	11 22 54	11 2 39	0 10 2	B1696	9 20 28	0 22 25	3 21 30
				1697	10 2 44	1 4 40	3 21 30
				1698	10 14 57	1 16 51	3 21 31

A Table of SATURN's Mean Motion.

Years	Longit. h			Anom. h			Node h			Years	Longit. h			Anom. h			Node h		
	S.	o		S.	o		S.	o			S.	o		S.	o		S.	o	
1699	10	27	10	1	29	9	3	21	32	1729	11	4	10	2	5	28	3	21	50
BI700	11	9	23	2	11	1	3	21	32	1730	11	16	23	2	17	40	3	21	50
1701	11	21	37	2	23	30	3	21	33	1731	11	28	37	2	29	52	3	21	51
1702	0	3	51	3	5	43	3	21	34	BI732	0	10	50	3	12	4	3	21	52
1703	0	16	5	3	17	55	3	21	34	1733	0	23	5	3	24	18	3	21	53
BI704	0	28	18	4	0	7	3	21	35	1734	1	5	19	4	6	31	3	21	53
1705	1	10	34	4	12	22	3	21	35	1735	1	17	33	4	18	43	3	21	54
1706	1	22	47	4	24	34	3	21	36	BI736	1	29	46	5	0	55	3	21	54
1707	2	5	1	5	6	46	3	21	37	1737	2	12	1	5	13	9	3	21	55
BI708	2	17	14	5	18	58	3	21	37	1738	2	24	15	5	25	22	3	21	55
1709	2	29	30	6	1	12	3	21	38	1739	3	6	29	6	7	34	3	21	56
1710	3	11	43	6	13	24	3	21	39	BI740	3	18	42	6	19	46	3	21	56
1711	3	23	57	6	25	37	3	21	39	1741	4	0	58	7	2	0	3	21	57
BI712	4	6	10	7	7	49	3	21	40	1742	4	13	11	7	14	13	3	21	57
1713	4	18	25	7	20	3	3	21	40	1743	4	25	24	7	26	25	3	21	58
1714	5	0	39	8	2	15	3	21	41	BI744	5	7	38	8	8	37	3	21	59
1715	5	12	52	8	14	28	3	21	41	1745	5	19	53	8	20	51	3	22	0
BI716	5	25	6	8	26	40	3	21	42	1746	6	2	7	9	3	4	3	22	0
1717	6	7	22	9	8	55	3	21	43	1747	6	14	20	9	15	16	3	22	1
1718	6	19	36	9	21	7	3	21	43	BI748	6	26	34	9	27	28	3	22	1
1719	7	1	44	10	3	19	3	21	44	1749	7	8	49	10	9	42	3	22	2
BI720	7	14	2	10	15	31	3	21	44	1750	7	21	3	10	21	55	3	22	2
1721	7	26	17	10	27	45	3	21	45	1751	8	3	16	11	4	7	3	22	3
1722	8	8	31	11	9	58	3	21	45	BI752	8	15	30	11	16	19	3	22	4
1723	8	20	44	11	22	10	3	21	46	1753	8	27	45	11	28	33	3	22	4
BI724	9	2	58	0	4	22	3	21	47	1754	9	9	58	0	10	46	3	22	5
1725	9	15	13	0	16	36	3	21	47	1755	9	22	12	0	22	58	3	22	5
1726	9	27	27	0	28	49	3	21	48	BI756	10	4	26	1	5	10	3	22	6
1727	10	9	40	1	11	1	3	21	48	1757	10	16	42	1	17	25	3	22	7
BI728	10	10	54	1	23	13	3	21	49	1758	10	28	56	1	29	37	3	22	7

A Table of SATURN'S Mean Motion.

Years	Longit. $^{\circ}$	Anom. $^{\circ}$	Node $^{\circ}$	Years	Longit. $^{\circ}$	Anom. $^{\circ}$	Node $^{\circ}$
	S. o	S. o	S. o		S. o	S. o	S. o
1759	11 11 9	2 11 49	3 22 8	1789	11 18 8	2 18 13	3 22 26
BI760	11 23 22	2 24 1	3 22 8	1790	0 0 21	3 0 25	3 22 26
1761	0 5 37	3 6 15	3 22 9	1791	0 12 35	3 12 38	3 22 27
1762	0 17 50	3 18 28	3 22 10	BI792	0 24 49	3 24 50	3 22 28
1763	1 0 4	4 0 41	3 22 10	1793	1 7 4	4 7 4	3 22 28
BI764	1 12 18	4 12 53	3 22 11	1794	1 19 17	4 19 16	3 22 29
1765	1 24 34	4 25 8	3 22 11	1795	2 1 31	5 1 28	3 22 29
1766	2 6 47	5 7 20	3 22 12	BI796	2 13 45	5 13 41	3 22 30
1767	2 19 0	5 19 32	3 22 13	1797	2 26 0	5 25 55	3 22 31
BI768	3 1 14	6 1 44	3 22 13	1798	3 8 13	6 8 7	3 22 31
1769	3 13 28	6 13 58	3 22 14	1799	3 20 27	6 20 20	3 22 32
1770	3 25 42	6 26 10	3 22 14	BI800	4 2 41	7 2 32	3 22 32
1771	4 7 56	7 8 23	3 22 15	1801	4 14 56	7 14 46	3 22 33
BI772	4 20 10	7 20 35	3 22 16	1802	4 27 9	7 26 58	3 22 34
1773	5 2 25	8 2 49	3 22 16	1803	5 9 22	8 9 10	3 22 34
1774	5 14 38	8 15 1	3 22 17	BI804	5 21 35	8 21 22	3 22 35
1775	5 26 52	8 27 14	3 22 17	1805	6 3 50	9 3 36	3 22 35
BI776	6 9 6	9 9 26	3 22 18	1806	6 16 3	9 15 48	3 22 36
1777	6 21 21	9 21 40	3 22 19	1807	6 28 17	9 28 1	3 22 36
1778	7 3 35	10 3 52	3 22 19	BI808	7 10 31	10 10 13	3 22 37
1779	7 15 48	10 16 4	3 22 20	1809	7 22 46	10 22 27	3 22 38
BI780	7 28 2	10 28 17	3 22 20	1810	8 4 59	11 4 39	3 22 38
1781	8 10 17	11 10 31	3 22 21	1811	8 17 13	11 16 52	3 22 39
1782	8 22 30	11 22 43	3 22 22	BI812	8 29 27	11 29 4	3 22 40
1783	9 4 44	0 4 56	3 22 22	1813	9 11 42	0 11 18	3 22 40
BI784	9 16 57	0 17 8	3 22 23	1814	9 23 55	0 23 30	3 22 41
1785	9 29 12	0 29 21	3 22 23	1815	10 6 9	1 5 43	3 22 41
1786	10 11 25	1 11 33	3 22 24	BI816	10 18 23	1 17 55	3 22 42
1787	10 23 39	1 23 46	3 22 25	1817	11 0 38	2 0 9	3 22 43
BI788	11 5 53	2 5 59	3 22 25	1818	11 12 52	2 12 21	3 22 43

A TABLE of SATURN's Mean Motion.

Com. Years	JANUARY.		FEBRUAR.		MARCH.		Bifextile.
	Lon. h	An. h	Lon. h	An. h	Lon. h	An. h	
	o	o	o	o	o	o	
1	0 2	0 2	1 4	1 4	2 1	2 1	0
2	0 4	0 4	1 6	1 6	2 3	2 3	1
3	0 6	0 6	1 8	1 8	2 5	2 5	2
4	0 8	0 8	1 10	1 10	2 7	2 7	3
5	0 10	0 10	1 12	1 12	2 9	2 9	4
6	0 12	0 12	1 14	1 14	2 11	2 11	5
7	0 14	0 14	1 16	1 16	2 13	2 13	6
8	0 16	0 16	1 18	1 18	2 15	2 15	7
9	0 18	0 18	1 20	1 20	2 17	2 17	8
10	0 20	0 20	1 22	1 22	2 19	2 19	9
11	0 22	0 22	1 24	1 24	2 21	2 21	10
12	0 24	0 24	1 26	1 26	2 23	2 23	11
13	0 26	0 26	1 28	1 28	2 25	2 25	12
14	0 28	0 28	1 30	1 30	2 27	2 27	13
15	0 30	0 30	1 32	1 32	2 29	2 29	14
16	0 32	0 32	1 34	1 34	2 31	2 31	15
17	0 34	0 34	1 36	1 36	2 33	2 33	16
18	0 36	0 36	1 38	1 38	2 35	2 35	17
19	0 38	0 38	1 40	1 40	2 37	2 37	18
20	0 40	0 40	1 42	1 42	2 39	2 39	19
21	0 42	0 42	1 44	1 44	2 41	2 41	20
22	0 44	0 44	1 46	1 46	2 43	2 43	21
23	0 46	0 46	1 48	1 48	2 45	2 45	22
24	0 48	0 48	1 50	1 50	2 47	2 47	23
25	0 50	0 50	1 52	1 52	2 49	2 49	24
26	0 52	0 52	1 55	1 55	2 51	2 51	25
27	0 54	0 54	1 57	1 57	2 53	2 53	26
28	0 56	0 56	1 59	1 59	2 55	2 55	27
29	0 58	0 58	2 1	2 1	2 57	2 57	28
30	1 0	1 0	0 0	0 0	2 59	2 59	29
31	1 2	1 2	0 0	0 0	3 1	3 1	30

A T A B L E of SATURN's Mean Motion.

Com. Years	A P R I L.		M A Y.		J U N E.		Bifextile.
	Lon. h	An. h	Lon. h	An. h	Lon. h	An. h	
	o	o	o	o	o	o	
1	3 3	3 3	4 3	4 3	5 5	5 5	0
2	3 5	3 5	4 5	4 5	5 7	5 7	1
3	3 7	3 7	4 7	4 7	5 9	5 9	2
4	3 9	3 9	4 9	4 9	5 11	5 11	3
5	3 11	3 11	4 11	4 11	5 13	5 13	4
6	3 13	3 13	4 13	4 13	5 15	5 15	5
7	3 15	3 15	4 15	4 15	5 17	5 17	6
8	3 17	3 17	4 17	4 17	5 19	5 19	7
9	3 19	3 19	4 19	4 19	5 21	5 21	8
10	3 21	3 21	4 21	4 21	5 23	5 23	9
11	3 23	3 23	4 23	4 23	5 25	5 25	10
12	3 25	3 25	4 25	4 25	5 27	5 27	11
13	3 27	3 27	4 27	4 27	5 29	5 29	12
14	3 29	3 29	4 29	4 29	5 31	5 31	13
15	3 31	3 31	4 31	4 31	5 33	5 33	14
16	3 33	3 33	4 33	4 33	5 35	5 35	15
17	3 35	3 35	4 35	4 35	5 37	5 37	16
18	3 37	3 37	4 37	4 37	5 39	5 39	17
19	3 39	3 39	4 39	4 39	5 41	5 41	18
20	3 41	3 41	4 41	4 41	5 43	5 43	19
21	3 43	3 43	4 43	4 43	5 45	5 45	20
22	3 45	3 45	4 45	4 45	5 47	5 47	21
23	3 47	3 47	4 47	4 47	5 49	5 49	22
24	3 49	3 49	4 49	4 49	5 51	5 51	23
25	3 51	3 51	4 51	4 51	5 53	5 53	24
26	3 53	3 53	4 53	4 53	5 55	5 55	25
27	3 55	3 55	4 55	4 55	5 57	5 57	26
28	3 57	3 57	4 57	4 57	5 59	5 59	27
29	3 59	3 59	4 59	4 59	6 1	6 1	28
30	4 1	4 1	5 1	5 1	6 3	6 3	29
31	4 3	4 3	5 3	5 3	6 6	6 5	30

A TABLE of SATURN's Mean Motion.

Com. Years	JULY.		AUGUST.		SEPTEMBER.		Biflexile.
	Lon. $\frac{h}{m}$	An. $\frac{h}{m}$	Lon. $\frac{h}{m}$	An. $\frac{h}{m}$	Lon. $\frac{h}{m}$	An. $\frac{h}{m}$	
	o	o	o	o	o	o	
1	6 6	6 5	7 8	7 7	8 10	8 9	0
2	6 8	6 7	7 10	7 9	8 12	8 11	1
3	6 10	6 9	7 12	7 11	8 14	8 13	2
4	6 12	6 11	7 14	7 13	8 16	8 15	3
5	6 14	6 13	7 16	7 15	8 18	8 17	4
6	6 16	6 15	7 18	7 17	8 20	8 19	5
7	6 18	6 17	7 20	7 19	8 22	8 21	6
8	6 20	6 19	7 22	7 21	8 24	8 23	7
9	6 22	6 21	7 24	7 23	8 26	8 25	8
10	6 24	6 23	7 26	7 25	8 28	8 27	9
11	6 26	6 25	7 28	7 27	8 30	8 29	10
12	6 28	6 27	7 30	7 29	8 32	8 31	11
13	6 30	6 29	7 32	7 31	8 34	8 33	12
14	6 32	6 31	7 34	7 33	8 36	8 35	13
15	6 34	6 33	7 36	7 35	8 38	8 37	14
16	6 36	6 35	7 38	7 37	8 40	8 39	15
17	6 38	6 37	7 40	7 39	8 42	8 41	16
18	6 40	6 39	7 42	7 41	8 44	8 43	17
19	6 42	6 41	7 44	7 43	8 46	8 45	18
20	6 44	6 43	7 46	7 45	8 48	8 47	19
21	6 46	6 45	7 48	7 47	8 50	8 49	20
22	6 48	6 47	7 50	7 49	8 52	8 51	21
23	6 50	6 49	7 52	7 51	8 54	8 53	22
24	6 52	6 51	7 54	7 53	8 56	8 55	23
25	6 54	6 53	7 56	7 55	8 58	8 57	24
26	6 56	6 55	7 58	7 57	9 0	8 59	25
27	6 58	6 57	8 0	7 59	9 2	9 1	26
28	7 0	6 59	8 2	8 1	9 4	9 3	27
29	7 2	7 1	8 4	8 3	9 6	9 5	28
30	7 4	7 3	8 6	8 5	9 8	9 7	29
31	7 6	7 5	8 8	8 7	9 11	9 10	30

A T A B L E of SATURN's Mean Motion.

Com. Years	OCTOB.		NOVEM.		DEC.EM.		Bifextile.
	Lon. h	An. h	Lon. h	An. h	Lon. h	An. h	
	o	o	o	o	o	o	
1	9 11	9 10	10 13	10 12	11 13	11 12	0
2	9 13	9 12	10 15	10 14	11 15	11 14	1
3	9 15	9 14	10 17	10 16	11 17	11 16	2
4	9 17	9 16	10 19	10 18	11 19	11 18	3
5	9 19	9 18	10 21	10 20	11 21	11 20	4
6	9 21	9 20	10 23	10 22	11 23	11 22	5
7	9 23	9 22	10 25	10 24	11 25	11 24	6
8	9 25	9 24	10 27	10 26	11 27	11 26	7
9	9 27	9 26	10 29	10 28	11 29	11 28	8
10	9 29	9 28	10 31	10 30	11 31	11 30	9
11	9 31	9 30	10 33	10 32	11 33	11 32	10
12	9 33	9 32	10 35	10 34	11 35	11 34	11
13	9 35	9 34	10 37	10 36	11 37	11 36	12
14	9 37	9 36	10 39	10 38	11 39	11 38	13
15	9 39	9 38	10 41	10 40	11 41	11 40	14
16	9 41	9 40	10 43	10 42	11 43	11 42	15
17	9 43	9 42	10 45	10 44	11 45	11 44	16
18	9 45	9 44	10 47	10 46	11 47	11 46	17
19	9 47	9 46	10 49	10 48	11 49	11 48	18
20	9 49	9 48	10 51	10 50	11 51	11 50	19
21	9 51	9 50	10 53	10 52	11 53	11 52	20
22	9 53	9 52	10 55	10 54	11 55	11 54	21
23	9 55	9 54	10 57	10 56	11 57	11 56	22
24	9 57	9 56	10 59	10 58	11 59	11 58	23
25	9 59	9 58	11 1	11 0	12 1	12 0	24
26	10 1	10 0	11 3	11 2	12 3	12 2	25
27	10 3	10 2	11 5	11 4	12 5	12 4	26
28	10 5	10 4	11 7	11 6	12 7	12 6	27
29	10 7	10 6	11 9	11 8	12 9	12 8	28
30	10 9	10 8	11 11	11 10	12 11	12 10	29
31	10 11	10 10	11 13	11 12	12 13	12 12	30

SATURN'S Mean Motion in Ho. Min. and Sec.

H	Longit. h	Anom. i	H	Longit. h	Anom. h
	o ' "	o ' "		o ' "	o ' "
1	0 0 5	0 0 5	31	0 2 36	0 2 36
2	0 0 10	0 0 10	32	0 2 41	0 2 41
3	0 0 15	0 0 15	33	0 2 46	0 2 46
4	0 0 20	0 0 20	34	0 2 51	0 2 51
5	0 0 25	0 0 25	35	0 2 56	0 2 56
6	0 0 30	0 0 30	36	0 3 1	0 3 1
7	0 0 35	0 0 35	37	0 3 6	0 3 6
8	0 0 40	0 0 40	38	0 3 11	0 3 11
9	0 0 45	0 0 45	39	0 3 16	0 3 16
10	0 0 50	0 0 50	40	0 3 22	0 3 22
11	0 0 55	0 0 55	41	0 3 27	0 3 27
12	0 1 0	0 1 0	42	0 3 32	0 3 32
13	0 1 5	0 1 5	43	0 3 37	0 3 37
14	0 1 10	0 1 10	44	0 3 42	0 3 42
15	0 1 15	0 1 15	45	0 3 47	0 3 47
16	0 1 20	0 1 20	46	0 3 52	0 3 52
17	0 1 25	0 1 25	47	0 3 57	0 3 57
18	0 1 30	0 1 30	48	0 4 2	0 4 2
19	0 1 35	0 1 35	49	0 4 7	0 4 7
20	0 1 40	0 1 40	50	0 4 12	0 4 12
21	0 1 46	0 1 46	51	0 4 17	0 4 17
22	0 1 51	0 1 51	52	0 4 22	0 4 22
23	0 1 56	0 1 56	53	0 4 27	0 4 27
24	0 2 1	0 2 1	54	0 4 32	0 4 32
25	0 2 6	0 2 6	55	0 4 37	0 4 37
26	0 2 11	0 2 11	56	0 4 42	0 4 42
27	0 2 16	0 2 16	57	0 4 48	0 4 48
28	0 2 21	0 2 21	58	0 4 53	0 4 53
29	0 2 26	0 2 26	59	0 4 58	0 4 58
30	0 2 31	0 2 31	60	0 5 3	0 5 3
II	II II III	II II III	II	II II III	II II III

A TABLE of SATURN'S Equation.

Degrees.	Sig. 0.				Logar. Dist. Δ \odot Curt.	Degrees.	Sig. 1.				Logar. Dist. Δ \odot Curt.	Degrees.	Sig. 2.				Logar. Dist. Δ \odot Curt.	Degrees.	
	Equa. Sub.						Equa. Sub.						Equa. Sub.						
	o	'	"				o	'	"				o	'	"				
0	0	0	0		600349	3	7	2		600049	5	31	30		599224	30			
1	0	6	30		600349	3	12	46		600029	5	35	7		599188	29			
2	0	12	58		600347	3	18	27		600009	5	38	38		599153	28			
3	0	19	26		600345	3	24	5		599988	5	42	5		599116	27			
4	0	25	54		600342	3	29	38		599968	5	45	26		599080	26			
5	0	32	22		600339	3	35	5		599946	5	48	41		599043	25			
6	0	38	49		600336	3	40	39		599923	5	51	49		599006	24			
7	0	45	15		600331	3	46	4		599900	5	54	53		598968	23			
8	0	51	41		600326	3	51	25		599877	5	57	50		598931	22			
9	0	58	6		600320	3	56	43		599853	6	0	42		598892	21			
10	1	4	30		600313	4	1	57		599828	6	3	26		598853	20			
11	1	10	53		600305	4	7	7		599802	6	6	5		598814	19			
12	1	17	15		600297	4	12	13		599777	6	8	39		598775	18			
13	1	23	36		600289	4	17	15		599749	6	11	6		598735	17			
14	1	29	55		600280	4	22	13		599723	6	13	26		598696	16			
15	1	36	13		600269	4	27	7		599696	6	15	40		598655	15			
16	1	42	35		600260	4	31	57		599669	6	17	47		598615	14			
17	1	48	46		600249	4	36	43		599642	6	19	48		598573	13			
18	1	55	0		600238	4	41	25		599614	6	21	43		598532	12			
19	2	1	12		600225	4	46	2		599586	6	23	31		598490	11			
20	2	7	22		600212	4	50	34		599558	6	25	13		598449	10			
21	2	13	30		600198	4	55	1		599529	6	26	48		598407	9			
22	2	19	37		600184	4	59	23		599489	6	28	15		598365	8			
23	2	25	42		600169	5	3	41		599457	6	29	35		598323	7			
24	2	31	44		600154	5	7	54		599425	6	30	49		598281	6			
25	2	37	43		600138	5	12	3		599392	6	31	57		598238	5			
26	2	43	40		600122	5	16	7		599360	6	32	58		598195	4			
27	2	49	34		600105	5	20	6		599326	6	33	53		598152	3			
28	2	55	26		600087	5	23	58		599292	6	34	41		998109	2			
29	3	1	15		600068	5	27	46		599258	6	35	22		598066	1			
30	3	7	2		600049	5	31	30		599224	6	35	55		598023	0			
Add						Add						Add.							
Sig. 11.						Sig. 10						Sig. 9.							

A TABLE of SATURN's Equation.

Degrees.	Sig. 3.			Logar. Dist. \hat{a} \odot Curt.	Sig. 4.			Logar. Dist. \hat{a} \odot Curt.	Sig. 5.			Logar. Dist. \hat{a} \odot Curt.	Degrees.
	o	'	"		o	'	"		o	'	"		
0	6	35	55	598023	5	54	50	596741	3	30	28	595730	30
1	6	36	19	597979	5	51	17	596701	3	24	13	595706	29
2	6	36	36	597936	5	48	16	596661	3	17	54	595683	28
3	6	36	44	597892	5	44	46	596622	3	11	29	595659	27
4	6	36	46	597849	5	41	9	596582	3	5	0	595637	26
5	6	36	42	597805	5	37	26	596543	2	58	27	595616	25
6	6	36	31	597763	5	33	37	596504	2	51	51	595595	24
7	6	36	11	597719	5	29	41	596467	2	45	10	595574	23
8	6	35	44	597675	5	25	37	596429	2	38	26	595556	22
9	6	35	9	597632	5	21	26	596392	2	31	39	595537	21
10	6	34	26	597588	5	17	8	596354	2	24	49	595520	20
11	6	33	36	597545	5	12	44	596318	2	17	55	595503	19
12	6	32	40	597502	5	8	14	596282	2	10	58	595488	18
13	6	31	36	597458	5	3	38	596247	2	3	58	595473	17
14	6	30	25	597415	4	58	56	596211	1	55	55	595459	16
15	6	29	7	597372	4	54	7	596177	1	40	49	595445	15
16	6	27	41	597329	4	49	12	596143	1	42	41	595433	14
17	6	26	7	597286	4	44	11	596110	1	35	30	595421	13
18	6	24	26	597243	4	39	3	596077	1	28	19	595411	12
19	6	22	39	597199	4	33	50	596045	1	21	3	595400	11
20	6	20	45	597157	4	28	51	596013	1	13	47	595392	10
21	6	18	42	597114	4	23	6	595982	1	6	29	595385	9
22	6	16	32	597072	4	17	36	595952	0	59	10	595376	8
23	6	14	14	597029	4	12	1	595922	0	51	49	595369	7
24	6	11	49	596988	4	6	20	595893	0	44	27	595364	6
25	6	9	17	596946	4	0	34	595864	0	37	4	595359	5
26	6	6	37	596905	3	54	43	595835	0	29	40	595356	4
27	6	3	52	596863	3	48	46	595808	0	22	16	595353	3
28	6	0	59	596822	3	42	44	595782	0	14	51	595352	2
29	5	57	58	596781	3	36	38	595756	0	7	26	595351	1
30	5	54	50	596741	3	30	28	595730	0	0	0	595350	0
Add.					Add.				Add.				
Sig. 8.					Sig. 7.				Sig. 6.				

For JUPITER in the next Table read SATURN.

A TABLE of JUPITER's Inclination from the Plan of the Ecliptic, with the proportional Scruples of Latitude.

Argument of Latitude.

Degrees.	Sig. 0. North Asc. Sig. 6. South Asc.				Sig. 1. North Asc. Sig. 7. South Asc.				Sig. 2. North Asc. Sig. 8. South Asc.				Degrees.				
	Inclinat.			P. Scr.	Inclinat.			P. Scr.	Inclinat.			P. Scr.					
	0	'	"	'	"	0	'	"	'	"	0	'		"	'	"	
0	0	0	0	0	0	0	1	15	15	30	0	2	10	19	51	57	30
1	0	2	37	1	3	1	17	31	30	54	2	11	37	52	28	29	
2	0	5	15	2	6	1	19	46	31	48	2	12	53	52	58	28	
3	0	7	52	3	8	1	21	59	32	41	2	14	6	53	27	27	
4	0	10	30	4	11	1	24	10	33	33	2	15	16	53	56	26	
5	0	13	6	5	14	1	26	18	34	25	2	16	23	54	23	25	
6	0	15	44	6	17	1	28	26	35	15	2	17	28	54	49	24	
7	0	18	21	7	19	1	30	32	36	6	2	18	31	55	14	23	
8	0	20	57	8	21	1	32	37	36	56	2	19	32	55	38	22	
9	0	23	33	9	23	1	34	41	37	45	2	20	30	56	1	21	
10	0	26	8	10	25	1	36	43	38	34	2	21	25	56	23	20	
11	0	28	42	11	27	1	38	44	39	22	2	22	18	56	44	19	
12	0	31	16	12	29	1	40	42	40	9	2	23	8	57	4	18	
13	0	33	50	13	30	1	42	38	40	55	2	23	55	57	23	17	
14	0	36	23	14	31	1	44	32	41	40	2	24	40	57	40	16	
15	0	38	56	15	32	1	46	24	42	26	2	25	22	57	57	15	
16	0	41	27	16	32	1	48	15	43	10	2	26	1	58	13	14	
17	0	43	59	17	32	1	50	3	43	53	2	26	38	58	28	13	
18	0	46	29	18	32	1	51	49	44	35	2	27	12	58	42	12	
19	0	48	59	19	32	1	53	34	45	16	2	27	44	58	54	11	
20	0	51	27	20	31	1	55	16	45	57	2	28	13	59	5	10	
21	0	53	55	21	30	1	56	56	46	37	2	28	40	59	16	9	
22	0	56	22	22	29	1	58	34	47	16	2	29	3	59	25	8	
23	0	58	48	23	27	2	0	10	47	54	2	29	24	59	33	7	
24	1	1	11	24	24	2	1	44	48	32	2	29	41	59	40	6	
25	1	3	35	25	21	2	3	16	49	9	2	29	55	59	46	5	
26	1	5	57	26	18	2	4	45	49	44	2	30	9	59	52	4	
27	1	8	18	27	14	2	6	13	50	18	2	30	19	59	56	3	
28	1	10	38	28	10	2	7	37	50	52	2	30	26	59	58	2	
29	1	12	57	29	5	2	8	59	51	25	2	30	29	59	59	1	
30	1	15	15	30	0	2	10	19	51	57	2	30	30	60	0	c	
Sig. 11. South Desc. Sig. 5. North Desc.					Sig. 10. South Desc. Sig. 4. North Desc.					Sig. 9. South Desc. Sig. 3. North Desc.							

Argument of Latitude.

A TABLE of JUPITER's Mean Motion.

Anni	Longit. γ	Anom. γ	Node γ	Years	Longit. γ	Anom. γ	Node γ
Chr.	S. o ' "	S. o ' "	S. o ' "	to xx.	S. o ' "	S. o ' "	S. o ' "
I	5 29 55	0 27 47	3 1 9	I	1 0 21	1 0 19	0 0 0
101	11 6 13	6 1 51	3 1 31	2	2 0 41	2 0 38	0 0 0
201	4 12 32	11 5 55	3 1 53	3	3 1 2	3 0 58	0 0 1
301	9 18 49	4 9 59	3 2 14	B 4	4 1 27	4 1 22	0 0 1
401	2 25 7	9 14 3	3 2 36	5	5 1 48	5 1 41	0 0 1
501	8 1 25	2 18 7	3 2 58	6	6 2 8	6 2 0	0 0 1
601	1 7 43	7 22 12	3 3 19	7	7 2 29	7 2 20	0 0 1
701	6 14 1	0 26 16	3 3 41	B 8	8 2 54	8 2 43	0 0 2
801	11 20 19	6 0 20	3 4 3	9	9 3 15	9 3 3	0 0 2
901	4 26 37	11 4 25	3 4 24	10	10 3 35	10 3 22	0 0 2
1001	10 2 55	4 8 29	3 4 46	11	11 3 56	11 3 41	0 0 2
1101	3 9 12	9 12 33	3 5 8	B 12	0 4 21	0 4 5	0 0 3
1201	8 15 30	2 16 37	3 5 29	13	1 4 42	1 4 25	0 0 1
1301	1 21 49	7 20 41	3 5 51	14	2 5 2	2 4 43	0 0 3
1401	6 28 7	0 24 45	3 6 13	15	3 5 23	3 5 3	0 0 3
1501	0 4 25	5 28 40	3 6 34	B 16	4 5 48	4 5 27	0 0 3
1601	5 10 43	11 2 53	3 6 56	17	5 6 9	5 5 46	0 0 4
1701	10 17 1	4 6 58	3 7 18	18	6 6 30	6 6 6	0 0 4
1801	3 23 19	9 11 2	3 7 40	19	7 6 50	7 6 25	0 0 4
1901	8 29 37	2 15 6	3 8 1	B 20	8 7 16	8 6 49	0 0 4
2001	2 5 55	7 19 10	3 8 23	Years from 1690.			
Jupiter's Mean Motion exceeding 20 Years.				1690	11 13 1	5 3 12	3 7 15
20	8 7 16	8 6 40	0 0 4	1691	0 13 21	6 3 31	3 7 15
40	4 14 31	4 13 37	0 0 9	B 1692	1 13 41	7 3 50	3 7 15
60	0 21 47	0 20 27	0 0 13	1693	2 14 6	8 4 14	3 7 16
80	8 29 3	8 27 16	0 0 17	1694	3 14 27	9 4 34	3 7 16
100	5 6 18	5 4 4	0 0 22	1695	4 14 48	10 4 52	3 7 16
1000	4 2 58	3 10 42	0 3 37	B 1696	5 15 8	11 5 12	3 7 16
				1697	6 15 34	0 5 36	3 7 16
				1698	7 15 54	1 5 56	3 7 17

A TABLE of JUPITER's Mean Motion.

Years.	Longit. π	Anom. μ	Node μ	Years.	Longit. π	Anom. μ	Node π
	S o ' "	S o ' "	S o ' "		S o ' "	S o ' "	S o ' "
1699	8 16 15	2 6 15	3 7 17	1729	2 27 11	8 16 31	3 7 24
BI700	9 16 35	3 6 34	3 7 17	1730	3 27 32	9 16 50	3 7 24
1701	10 17 0	4 6 58	3 7 18	1731	4 27 53	10 17 10	3 7 25
1702	11 17 21	5 7 18	3 7 18	BI732	5 28 13	11 17 27	3 7 25
1703	0 17 42	6 7 37	3 7 18	1733	6 28 39	0 17 53	3 7 25
BI704	1 18 2	7 7 55	3 7 18	1734	7 28 59	1 18 12	3 7 25
1705	2 18 28	8 8 20	3 7 19	1735	8 29 20	2 18 31	3 7 26
1706	3 18 48	9 8 39	3 7 19	BI736	9 29 40	3 18 50	3 7 26
1707	4 19 9	10 8 58	3 7 19	1737	11 0 6	4 19 16	3 7 26
BI708	5 19 30	11 9 18	3 7 19	1738	0 0 26	5 19 34	3 7 26
1709	6 19 55	0 9 42	3 7 20	1739	1 0 47	6 19 53	3 7 27
1010	7 20 16	1 10 1	3 7 20	BI740	2 1 7	7 20 12	3 7 27
1711	8 20 37	2 10 21	3 7 20	1741	3 1 33	8 20 36	3 7 27
BI712	9 20 57	3 10 38	3 7 20	1742	4 1 53	9 20 56	3 7 27
1713	10 21 23	4 11 4	3 7 21	1743	5 2 14	10 21 15	3 7 27
1714	11 21 43	5 11 23	3 7 21	BI744	6 2 34	11 21 33	3 7 28
1715	0 22 4	6 11 42	3 7 21	1745	7 2 59	0 21 58	3 7 28
BI716	1 22 24	7 12 1	3 7 21	1746	8 3 20	1 22 17	3 7 28
1717	2 22 49	8 12 26	3 7 21	1747	9 3 41	2 22 36	3 7 28
1718	3 23 10	9 12 42	3 7 22	BI748	10 4 2	3 22 56	3 7 28
1719	4 23 31	10 13 4	3 7 22	1749	11 4 27	4 23 20	3 7 29
BI720	5 23 51	11 13 23	3 7 22	1750	0 4 48	5 23 39	3 7 29
1721	6 24 17	0 13 47	3 7 22	1751	1 5 9	6 23 59	3 7 29
1722	7 24 37	1 14 7	3 7 23	BI752	2 5 30	7 24 18	3 7 29
1723	8 24 58	2 14 26	3 7 23	1753	3 5 55	8 24 42	3 7 30
BI724	9 25 18	3 14 44	3 7 23	1754	4 6 15	9 25 1	3 7 30
1725	10 25 44	4 15 9	3 7 23	1755	5 6 36	10 25 20	3 7 30
1726	11 26 4	5 15 28	3 7 23	BI756	6 6 56	11 25 39	3 7 30
1727	0 26 25	6 15 47	3 7 24	1757	7 7 21	0 26 3	3 7 30
BI728	1 26 46	7 16 7	3 7 24	1758	8 7 42	1 26 22	3 7 31

A TABLE of JUPITER's Mean Motion.

Years.	Longit. 1			Anom. 4			Node 7			Years.	Longit. 2			Anom. 2			Node 2		
	S	o		S	o		S	o			S	o		S	o		S	o	
1759	9	8	3	2	26	42	3	7	31	1789	3	18	59	9	6	58	3	7	37
BI760	10	8	23	3	27	1	3	7	31	1790	4	19	20	10	7	17	3	7	37
1761	11	8	49	4	27	26	3	7	31	1791	5	19	41	11	7	37	3	7	38
1762	0	9	9	5	27	45	3	7	31	BI792	6	20	1	0	7	55	3	7	38
1763	1	9	30	6	28	4	3	7	32	1793	7	20	26	1	8	19	3	7	38
BI764	2	9	51	7	28	23	3	7	32	1794	8	20	47	2	8	39	3	7	38
1765	3	10	16	8	28	47	3	7	32	1795	9	21	1	3	8	58	3	7	39
1766	4	10	39	9	29	6	3	7	32	BI796	10	21	28	4	9	17	3	7	39
1767	5	10	57	10	29	25	3	7	32	1797	11	21	54	5	9	42	3	7	39
BI768	6	11	18	11	29	45	3	7	33	1798	0	22	15	6	10	1	3	7	39
1769	7	11	48	1	0	9	3	7	33	1799	1	22	35	7	10	20	3	7	39
1770	8	12	4	2	0	28	3	7	33	BI800	2	22	55	8	10	38	3	7	40
1771	9	12	25	3	0	48	3	7	33	1801	3	23	19	9	11	2	3	7	40
BI772	10	12	45	4	1	7	3	7	33	1802	4	23	40	10	11	23	3	7	40
1773	11	13	11	5	1	31	3	7	33	1803	5	24	1	11	11	42	3	7	40
1774	0	13	31	6	1	59	3	7	34	BI804	6	24	21	0	12	2	3	7	40
1775	1	13	52	7	2	9	3	7	34	1805	7	24	47	1	12	26	3	7	41
BI776	2	14	12	8	2	28	3	7	34	1806	8	25	7	2	12	45	3	7	41
1777	3	14	38	9	2	58	3	7	34	1807	9	25	28	3	13	4	3	7	41
1778	4	14	58	10	3	12	3	7	34	BI808	10	25	49	4	13	23	3	7	41
1779	5	15	19	11	3	31	3	7	35	1809	11	26	14	5	13	47	3	7	42
BI780	6	15	39	0	3	50	3	7	35	1810	0	26	35	6	14	6	3	7	42
1781	7	16	5	1	4	14	3	7	35	1811	1	26	56	7	14	26	3	7	42
1782	8	16	25	2	4	34	3	7	35	BI812	2	27	16	8	14	43	3	7	42
1783	9	16	46	3	4	53	3	7	36	1813	3	27	42	9	15	8	3	7	43
BI784	10	17	6	4	5	12	3	7	36	1814	4	28	2	10	15	28	3	7	43
1785	11	17	32	5	5	36	3	7	36	1815	5	28	23	11	15	47	3	7	43
1786	0	17	53	6	5	55	3	7	37	BI816	6	28	43	0	16	6	3	7	43
1787	1	18	13	7	6	14	3	7	37	1817	7	29	9	1	16	30	3	7	43
BI788	2	18	14	8	6	34	3	7	37	1818	8	29	29	2	16	49	3	7	44

A TABLE of JUPITER's Mean Motion.

Com. Years	JANUARY.		FEBRUAR.		MARCH.		Bifextile.
	Lon. \times	An. μ	Lon. \times	An. \times	Lon. \times	An. \times	
	o	o	o	o	o	o	
1	o 5	o 5	2 40	2 40	4 59	4 59	o
2	o 10	o 10	2 45	2 45	5 4	5 4	1
3	o 15	o 15	2 50	2 50	5 9	5 9	2
4	o 20	o 20	2 55	2 55	5 14	5 14	3
5	o 25	o 25	3 0	3 0	5 19	5 19	4
6	o 30	o 30	3 5	3 5	5 24	5 24	5
7	o 35	o 35	3 10	3 10	5 29	5 29	6
8	o 40	o 40	3 15	3 15	5 34	5 34	7
9	o 45	o 45	3 20	3 20	5 39	5 39	8
10	o 50	o 50	3 25	3 25	5 44	5 44	9
11	o 55	o 55	3 30	3 30	5 49	5 49	10
12	I 0	I 0	3 35	3 35	5 54	5 54	11
13	I 5	I 5	3 40	3 40	5 59	5 59	12
14	I 10	I 10	3 45	3 45	6 4	6 4	13
15	I 15	I 15	3 50	3 50	6 9	6 9	14
16	I 20	I 20	3 55	3 55	6 14	6 14	15
17	I 25	I 25	4 0	4 0	6 19	6 19	16
18	I 30	I 30	4 5	4 5	6 24	6 24	17
19	I 35	I 35	4 10	4 10	6 29	6 29	18
20	I 40	I 40	4 15	4 15	6 34	6 34	19
21	I 45	I 45	4 20	4 20	6 39	6 39	20
22	I 50	I 50	4 25	4 25	6 44	6 44	21
23	I 55	I 55	4 30	4 30	6 49	6 49	22
24	2 0	2 0	4 35	4 35	6 54	6 54	23
25	2 5	2 5	4 40	4 40	6 59	6 59	24
26	2 10	2 10	4 45	4 45	7 4	7 4	25
27	2 15	2 15	4 50	4 50	7 9	7 9	26
28	2 20	2 20	4 55	4 55	7 14	7 14	27
29	2 25	2 25	4 59	4 59	7 19	7 19	28
30	2 30	2 30	o 0	o 0	7 24	7 24	29
31	2 35	2 35	o 0	o 0	7 29	7 29	30

A TABLE of JUPITER's Mean Motion.

Com. Years	APRIL.		MAY.		JUNE.		Billexile.
	Lon. μ	An. μ	Lon. μ	An. μ	Lon. μ	An. μ	
	o	o	o	o	o	o	
1	7 34	7 34	10 4	10 4	12 38	12 38	0
2	7 39	7 39	10 9	10 9	12 43	12 43	1
3	7 44	7 44	10 14	10 14	12 48	12 48	2
4	7 49	7 49	10 19	10 19	12 53	12 53	3
5	7 54	7 54	10 24	10 24	12 58	12 58	4
6	7 59	7 59	10 29	10 29	13 3	13 3	5
7	8 4	8 4	10 34	10 34	13 8	13 8	6
8	8 9	8 9	10 39	10 39	13 13	13 13	7
9	8 14	8 14	10 44	10 44	13 18	13 18	8
10	8 19	8 19	10 49	10 49	13 23	13 23	9
11	8 24	8 24	10 54	10 54	13 28	13 28	10
12	8 29	8 29	10 59	10 59	13 33	13 33	11
13	8 34	8 34	11 4	11 4	13 38	13 38	12
14	8 39	8 39	11 9	11 9	13 43	13 43	13
15	8 44	8 44	11 14	11 14	13 48	13 48	14
16	8 49	8 49	11 19	11 19	13 53	13 53	15
17	8 54	8 54	11 24	11 24	13 58	13 58	16
18	8 59	8 59	11 29	11 29	14 3	14 3	17
19	9 4	9 4	11 34	11 34	14 8	14 8	18
20	9 9	9 9	11 39	11 39	14 13	14 13	19
21	9 14	9 14	11 44	11 44	14 18	14 18	20
22	9 19	9 19	11 49	11 49	14 23	14 22	21
23	9 24	9 24	11 54	11 54	14 28	14 27	22
24	9 29	9 29	11 59	11 59	14 33	14 32	23
25	9 34	9 34	12 4	12 4	14 38	14 37	24
26	9 39	9 39	12 9	12 9	14 43	14 42	25
27	9 44	9 44	12 14	12 14	14 48	14 47	26
28	9 49	9 49	12 19	12 19	14 53	14 52	27
29	9 54	9 54	12 24	12 24	14 58	14 57	28
30	9 59	9 59	12 29	12 29	15 3	15 2	29
31	10 4	10 4	12 33	12 33	15 8	15 7	30

A TABLE of JUPITER's Mean Motion.

Com. Years	J U L Y.		A U G U S T.		S E P T E M B.		Biflexile.
	Lon. γ	An. γ	Lon. γ	An. γ	Lon. γ	An. γ	
	o	o	o	o	o	o	
1	15 8	15 7	17 42	17 41	20 17	20 16	0
2	15 13	15 12	17 47	17 46	20 22	20 21	1
3	15 18	15 17	17 52	17 51	20 27	20 26	2
4	15 23	15 22	17 57	17 56	20 32	20 31	3
5	15 28	15 27	18 2	18 1	20 37	20 36	4
6	15 33	15 32	18 7	18 6	20 42	20 41	5
7	15 38	15 37	18 12	18 11	20 47	20 46	6
8	15 43	15 42	18 17	18 16	20 52	20 51	7
9	15 48	15 47	18 22	18 21	20 57	20 56	8
10	15 53	15 52	18 27	18 26	21 2	21 1	9
11	15 58	15 57	18 32	18 31	21 7	21 6	10
12	16 3	16 2	18 37	18 36	21 12	21 11	11
13	16 8	16 7	18 42	18 41	21 17	21 16	12
14	16 13	16 12	18 47	18 46	21 22	21 21	13
15	16 18	16 17	18 52	18 51	21 27	21 26	14
16	16 23	16 22	18 57	18 56	21 32	21 31	15
17	16 28	16 27	19 2	19 1	21 37	21 36	16
18	16 33	16 32	19 7	19 6	21 42	21 41	17
19	16 38	16 37	19 12	19 11	21 47	21 46	18
20	16 43	16 42	19 17	19 16	21 52	21 51	19
21	16 48	16 47	19 22	19 21	21 57	21 56	20
22	16 53	16 52	19 27	19 26	22 2	22 1	21
23	16 58	16 57	19 32	19 31	22 7	22 6	22
24	17 3	17 2	19 37	19 36	22 12	22 11	23
25	17 8	17 7	19 42	19 41	22 17	22 16	24
26	17 13	17 12	19 47	19 46	22 22	22 21	25
27	17 18	17 17	19 52	19 51	22 27	22 26	26
28	17 23	17 22	19 57	19 56	22 32	22 31	27
29	17 28	17 27	20 2	20 1	22 37	22 36	28
30	17 33	17 32	20 7	20 6	22 42	22 41	29
31	17 37	17 36	20 12	20 11	22 47	22 46	30

A TABLE of JUPITER's Mean Motion.

Com. Years	OCTOBER.		NOVEMB.		NOVEMB.		Biflexile.
	Lon. φ	An. ψ	Lon. φ	An. ψ	Lon. φ	An. ψ	
	o	o	o	o	o	o	
1	22 47	22 46	25 21	25 20	27 51	27 50	0
2	22 52	22 51	25 26	25 25	27 56	27 55	1
3	22 57	22 56	25 31	25 30	28 1	28 0	2
4	23 2	23 1	25 36	25 35	28 6	28 5	3
5	23 7	23 6	25 41	25 40	28 11	28 10	4
6	23 12	23 11	25 46	25 45	28 16	28 15	5
7	23 17	23 16	25 51	25 50	28 21	28 20	6
8	23 22	23 21	25 56	25 55	28 26	28 25	7
9	23 27	23 26	26 1	26 0	28 31	28 30	8
10	23 32	23 31	26 6	26 5	28 36	28 35	9
11	23 37	23 36	26 11	26 10	28 41	28 40	10
12	23 42	23 41	26 16	26 15	28 46	28 45	11
13	23 47	23 46	26 21	26 20	28 51	28 50	12
14	23 52	23 51	26 26	26 25	28 56	28 55	13
15	23 57	23 56	26 31	26 30	29 1	29 0	14
16	24 2	24 1	26 36	26 35	29 6	29 5	15
17	24 7	24 6	26 41	26 40	29 11	29 10	16
18	24 12	24 11	26 46	26 45	29 16	29 15	17
19	24 17	24 16	26 51	26 50	29 21	29 20	18
20	24 22	24 21	26 56	26 55	29 26	29 25	19
21	24 27	24 26	27 1	27 0	29 31	29 30	20
22	24 32	24 31	27 6	27 5	29 36	29 35	21
23	24 37	24 36	27 11	27 10	29 41	29 40	22
24	24 42	24 41	27 16	27 15	29 46	29 45	23
25	24 46	24 45	27 21	27 20	29 51	29 50	24
26	24 51	24 50	27 26	27 25	29 56	29 55	25
27	24 56	24 55	27 31	27 30	30 1	30 0	26
28	25 1	25 0	27 36	27 35	30 6	30 5	27
29	25 6	25 5	27 41	27 40	30 11	30 10	28
30	25 11	25 10	27 46	27 45	30 16	30 15	29
31	25 16	25 15	27 51	27 50	30 21	30 20	30

M m m m

A TABLE of JUPITER's Mean Motion,
in Hours Minutes and Seconds.

H	Longit. π	Anom. μ		Longit. π	Anom. μ
	o ' "	o ' "	"	o ' "	o ' "
1	0 0 12	0 0 12	31	0 6 27	0 6 27
2	0 0 25	0 0 25	32	0 6 40	0 6 40
3	0 0 35	0 0 37	33	0 6 52	0 6 52
4	0 0 50	0 0 50	34	0 7 5	0 7 5
5	0 1 2	0 1 2	35	0 7 17	0 7 17
6	0 1 15	0 1 15	36	0 7 30	0 7 30
7	0 1 27	0 1 27	37	0 7 42	0 7 42
8	0 1 40	0 1 42	38	0 7 55	0 7 55
9	0 1 52	0 1 52	39	0 8 7	0 8 7
10	0 2 5	0 2 5	40	0 8 20	0 8 20
11	0 2 17	0 2 17	41	0 8 32	0 8 32
12	0 2 30	0 2 30	42	0 8 44	0 8 44
13	0 2 42	0 2 42	43	0 8 57	0 8 57
14	0 2 55	0 2 55	44	0 9 9	0 9 9
15	0 3 7	0 3 7	45	0 9 22	0 9 22
16	0 3 20	0 3 20	46	0 9 34	0 9 34
17	0 3 32	0 3 32	47	0 9 47	0 9 47
18	0 3 44	0 3 44	48	0 9 59	0 9 59
19	0 3 57	0 3 57	49	0 10 12	0 10 12
20	0 4 9	0 4 9	50	0 10 24	0 10 24
21	0 4 22	0 4 22	51	0 10 37	0 10 37
22	0 4 34	0 4 34	52	0 10 50	0 10 50
23	0 4 47	0 4 47	53	0 11 2	0 11 2
24	0 4 59	0 4 59	54	0 11 15	0 11 15
25	0 5 12	0 5 12	55	0 11 27	0 11 27
26	0 5 24	0 5 24	56	0 11 40	0 11 40
27	0 5 37	0 5 37	57	0 11 52	0 11 52
28	0 5 50	0 5 50	58	0 12 5	0 12 5
29	0 6 2	0 6 2	59	0 12 17	0 12 17
30	0 6 15	0 6 15	60	0 12 30	0 12 30
"	" " "	" " "	"	" " "	" " "

A TABLE of JUPITER's Equation.

Degrees.	Sig. 0.		Logar. Dist. à ☉ Curt.	Sig. 1.		Logar. Dist. à ☉ Curt.	Sig. 2.		Logar. Dist. à ☉ Curt.	Degrees.
	Equa.	Sub.		Equa.	Sub.		Equa.	Sub.		
0	0	0	573765	2	37 19	573515	4	37 33	572820	30
1	0	5 26	573765	2	42 7	573499	4	40 31	572791	29
2	0	10 54	573764	2	46 54	573481	4	43 26	572762	28
3	0	16 22	573762	2	51 37	573464	4	46 14	572732	27
4	0	21 49	573759	2	56 15	573446	4	48 57	572701	26
5	0	27 15	573757	3	0 53	573428	4	51 36	572671	25
6	0	32 42	573754	3	5 27	573409	4	54 11	572640	24
7	0	38 7	573750	3	9 59	573389	4	56 42	572608	23
8	0	43 31	573745	3	14 28	573369	4	59 5	572577	22
9	0	48 56	573741	3	18 54	573349	5	1 24	572545	21
10	0	54 19	573735	3	23 16	573329	5	3 39	572513	20
11	0	59 42	573729	3	27 34	573307	5	5 47	572480	19
12	1	5 4	573723	3	31 48	573285	5	7 50	572447	18
13	1	10 25	573716	3	36 0	573263	5	9 49	572414	17
14	1	15 45	573708	3	40 9	573240	5	11 42	572381	16
15	1	21 2	573700	3	44 14	573217	5	13 29	572347	15
16	1	26 19	573692	3	48 14	573194	5	15 5	572314	14
17	1	31 35	573683	3	52 13	573169	5	16 41	572280	13
18	1	36 49	573673	3	56 7	573145	5	18 12	572245	12
19	1	42 2	573663	3	59 56	573120	5	19 44	572211	11
20	1	47 13	573652	4	3 44	573095	5	21 4	572177	10
21	1	52 23	573640	4	7 27	573070	5	22 17	572142	9
22	1	57 31	573628	4	11 4	573044	5	23 26	572107	8
23	2	2 37	573616	4	14 38	573016	5	24 28	572072	7
24	2	7 40	573603	4	18 6	572990	5	25 25	572037	6
25	2	12 41	573590	4	21 30	572963	5	26 15	572000	5
26	2	17 40	573576	4	24 51	572936	5	27 0	571966	4
27	2	22 38	573561	4	28 8	572907	5	27 39	571929	3
28	2	27 32	573546	4	31 20	572878	5	28 12	571893	2
29	2	32 26	573531	4	34 29	572850	5	28 40	571857	1
30	2	37 19	573515	4	37 33	572820	5	29 4	571820	0
	Add.			Add.			Add.			
	Sig. 11.			Sig. 10.			Sig. 9.			

A TABLE of JUPITER's Equation.

Degrees.	Sig. 3.		Logar. Dist. Δ \odot Curt.	Sig. 4.		Logar. Dist. Δ \odot Curt.	Sig. 5.		Logar. Dist. Δ \odot Curt.	Degrees.
	Equa. Sub.			Equa. Sub.			Equa. Sub.			
0	5 29 4		571820	4 52 54		570754	2 52 43		569920	30
1	5 29 19		571784	4 50 8		570720	2 47 33		569901	29
2	5 29 28		571748	4 47 18		570686	2 42 20		569881	28
3	5 29 34		571712	4 44 22		570653	2 37 3		569862	27
4	5 29 30		571676	4 41 20		570621	2 31 44		569853	26
5	5 29 26		571641	4 38 13		570590	2 26 21		569825	25
6	5 29 16		571604	4 35 0		570558	2 20 54		569808	24
7	5 28 46		571568	4 31 40		570526	2 15 26		569791	23
8	5 28 19		571532	4 28 16		570495	2 9 54		569776	22
9	5 27 47		571495	4 24 46		570464	2 4 18		569761	21
10	5 27 9		571458	4 21 10		570434	1 58 39		569747	20
11	5 26 23		571423	4 17 30		570404	1 52 59		569733	19
12	5 25 33		571386	4 13 45		570374	1 47 16		569721	18
13	5 24 36		571349	4 9 54		570345	1 41 32		569708	17
14	5 23 32		571313	4 5 59		570317	1 35 47		569696	16
15	5 22 22		571277	4 2 0		570288	1 29 58		569685	15
16	5 21 6		571242	3 57 55		570260	1 24 7		569674	14
17	5 19 44		571206	3 53 44		570232	1 18 15		569664	13
18	5 18 17		571170	3 49 30		570205	1 12 20		569655	12
19	5 16 39		571134	3 45 9		570178	1 6 24		569647	11
20	5 15 2		571099	3 40 44		570152	1 0 26		569639	10
21	5 13 17		571064	3 36 15		570126	0 54 26		569632	9
22	5 11 27		571029	3 31 40		570101	0 48 26		569626	8
23	5 9 29		570994	3 27 3		570077	0 42 25		569621	7
24	5 7 25		570959	3 22 21		570053	0 36 24		569616	6
25	5 5 14		570925	3 17 38		570029	0 30 22		569612	5
26	5 2 57		570890	3 12 44		570006	0 24 18		569609	4
27	5 0 35		570856	3 7 50		569984	0 18 14		569608	3
28	4 58 1		570822	3 2 51		569962	0 10 10		569606	2
29	4 55 33		570787	2 57 49		569941	0 6 5		569605	1
30	4 52 54		570754	2 52 43		569920	0 0 0		569605	0
	Add.			Add.			Add.			
	Sig. 8.			Sig. 7.			Sig. 6.			

A TABLE of JUPITER's Inclination from the Plan
of the Ecliptic, with the proportional Scruples of Latitude.

Argument of Latitude.

Degrees.	Sig. 0. North Asc. Sig. 6. South Asc.		Sig. 1. North Asc. Sig. 7. South Asc.		Sig. 2. North Asc. Sig. 8. South Asc.		Degrees.
	Inclinat.	P. Scr.	Inclinat.	P. Scr.	Inclinat.	P. Scr.	
	° ' "	' "	° ' "	' "	° ' "	' "	
0	0 0 0	0 0	0 40 58	30 0	1 10 57	51 57	30
1	0 1 26	1 3	0 42 12	30 54	1 11 39	52 28	29
2	0 2 51	2 6	0 43 25	31 47	1 12 20	52 58	28
3	0 4 17	3 8	0 44 38	32 39	1 13 0	23 27	27
4	0 5 42	4 11	0 45 50	33 32	1 13 38	53 56	26
5	0 7 8	5 14	0 47 1	34 24	1 14 15	54 24	25
6	0 8 33	6 17	0 48 10	35 15	1 14 50	54 49	24
7	0 9 59	7 19	0 49 18	36 6	1 15 24	55 14	23
8	0 11 24	8 21	0 50 27	36 56	1 15 57	55 38	22
9	0 12 49	9 23	0 51 34	37 45	1 16 28	56 1	21
10	0 14 14	10 25	0 52 40	38 34	1 16 59	56 23	20
11	0 15 38	11 27	0 53 45	39 21	1 17 28	56 44	19
12	0 17 1	12 29	0 54 50	40 9	1 17 55	57 4	18
13	0 18 25	13 30	0 55 53	40 55	1 18 21	57 23	17
14	0 19 49	14 31	0 56 55	41 41	1 18 45	57 40	16
15	0 21 12	15 32	0 57 58	42 26	1 19 7	57 57	15
16	0 22 35	16 32	0 58 59	43 10	1 19 30	58 13	14
17	0 23 58	17 32	0 59 58	43 53	1 19 50	58 28	13
18	0 25 19	18 32	1 0 55	44 35	1 20 9	58 42	12
19	0 26 41	19 31	1 1 50	45 17	1 20 26	58 54	11
20	0 28 2	20 30	1 2 46	45 58	1 20 41	59 5	10
21	0 29 22	21 29	1 3 41	46 38	1 20 55	59 16	9
22	0 30 41	22 27	1 4 34	47 17	1 21 7	59 25	8
23	0 32 1	23 25	1 5 26	47 55	1 21 18	59 33	7
24	0 33 19	24 23	1 6 17	48 32	1 21 28	59 40	6
25	0 34 37	25 21	1 7 7	49 9	1 21 37	59 46	5
26	0 35 55	26 18	1 7 55	49 45	1 21 44	59 52	4
27	0 37 12	27 14	1 8 42	50 19	1 21 49	59 56	3
28	0 38 29	28 10	1 9 29	50 53	1 21 53	59 58	2
29	0 39 44	29 5	1 10 13	51 25	1 21 55	59 59	1
30	0 40 58	30 0	1 10 57	51 57	1 21 56	60 0	0
	Sig. 11. South Desc. Sig. 5. North Desc.		Sig. 10. South Desc. Sig. 4. North Desc.		Sig. 9. South Desc. Sig. 3. North Desc.		

Argument of Latitude.

A TABLE of MARS's Mean Motion.

Epocha or Radices				Mars's Mean Motion to 20 Years,			
Anni	Longit. δ	Anom. δ	Node δ	Years.	Longit. δ	Anom. δ	Node δ
Christi	S o 'S o 'S o	S o 'S o 'S o	S o 'S o 'S o		S o 'S o 'S o	S o 'S o 'S o	S o 'S o 'S o
1	1 10 13	9 13 36	0 27 21		1 6 11 17	6 11 16	0 0 1
101	3 11 53	11 13 14	0 28 33		2 0 22 34	0 22 32	0 0 1
201	5 13 32	1 12 52	0 29 46		3 7 3 51	7 3 48	0 0 2
301	7 15 12	3 12 31	1 0 59	B	4 1 15 40	1 15 35	0 0 3
401	9 16 51	5 12 8	1 2 11		5 7 26 57	7 26 51	0 0 4
501	11 18 31	7 11 47	1 3 24		6 2 8 14	2 8 7	0 0 4
601	1 20 10	9 11 24	1 4 37		7 8 19 31	8 19 23	5 0 5
701	3 21 50	11 11 3	1 5 49	B	8 3 1 20	3 1 10	6 0 6
801	5 23 29	1 10 41	1 7 2		9 5 12 37	9 12 26	7 0 7
901	7 25 9	3 10 19	1 8 15		10 3 23 54	3 23 42	0 0 7
1001	9 26 48	5 9 57	1 9 27		11 10 5 11	10 4 58	0 0 8
1101	11 28 28	7 9 35	1 10 40	B	12 4 17 0	4 16 45	0 0 9
1201	2 0 7	9 9 13	1 11 52		13 10 28 17	10 28 1	0 0 9
1301	4 1 47	11 8 51	1 13 5		14 5 9 34	5 9 17	0 0 10
1401	6 3 26	1 8 29	1 14 18		15 11 20 51	11 20 33	0 0 11
1501	8 5 6	3 8 7	1 15 31	B	16 6 2 40	6 2 21	0 0 11
1601	10 6 45	5 7 45	1 16 43		17 0 13 57	0 13 36	0 0 12
1701	0 8 25	7 7 23	1 17 56		18 6 25 14	6 24 52	0 0 13
1801	2 10 4	9 7 1	1 19 9		19 1 6 31	1 6 8	0 0 13
1901	4 11 44	11 6 40	1 20 22	B	20 7 18 20	7 17 55	0 0 14
2001	6 13 23	1 6 18	1 21 34				
Mars's Mean Motion exceeding 20 Years.				Years from 1690.			
20	7 18 20	7 17 56	0 0 14	1690	2 2 42	9 1 54	1 17 48
40	3 6 40	3 5 52	0 0 29	1691	8 13 59	3 13 10	1 17 49
60	10 25 0	10 23 47	0 0 44	B1692	2 25 16	9 24 26	1 17 49
80	6 13 20	6 11 43	0 0 58	1693	9 7 5	4 6 13	1 17 50
100	2 1 40	1 29 39	0 1 13	1694	3 18 22	10 17 29	1 17 51
1000	8 16 35	7 26 21	0 12 7	1695	9 29 39	4 28 45	1 17 52
				B1696	4 10 56	11 10 1	1 17 52
				1697	10 22 44	5 21 48	1 17 53
				1698	5 4 2	0 3 4	1 17 54

A TABLE of MARS's Mean Motion.

Years.	Longit. δ	Anom. δ	Node δ	Years.	Longit. δ	Anom. δ	Node δ
	S o	S o	S o		S o	S o	S o
1699	11 15 19	6 14 20	1 17 55	1729	10 28 5	5 26 29	1 18 17
BI700	5 26 36	0 25 36	1 17 56	1730	5 9 22	0 7 45	1 18 18
1701	0 8 25	7 7 23	1 17 56	1731	11 20 39	6 19 2	1 18 19
1702	6 19 42	1 18 39	1 17 57	BI732	6 1 56	1 0 18	1 18 19
1703	1 0 59	7 29 55	1 17 57	1733	0 13 44	7 12 5	1 18 20
BI704	7 12 16	2 11 11	1 17 58	1734	6 25 2	1 23 21	1 18 21
1705	1 24 4	8 22 58	1 17 59	1735	1 6 19	8 4 37	1 18 21
1706	8 5 22	3 4 14	1 18 0	BI736	7 17 36	2 15 58	1 18 22
1707	2 16 39	9 15 30	1 18 0	1737	1 29 24	8 27 40	1 18 23
BI708	8 27 56	3 26 46	1 18 1	1738	8 10 42	3 8 56	1 18 23
1709	3 9 44	10 8 33	1 18 2	1739	2 21 59	9 20 12	1 18 24
1710	9 21 2	7 19 49	1 18 3	BI740	9 3 16	4 1 28	1 18 25
1711	4 2 19	11 1 5	1 18 4	1741	3 15 4	10 13 15	1 18 25
BI712	10 13 36	5 12 21	1 18 4	1742	9 26 22	4 24 31	1 18 26
1713	4 25 24	11 24 8	1 18 5	1743	4 7 39	11 5 47	1 18 27
1714	11 6 42	6 5 24	1 18 6	BI744	10 18 56	5 17 3	1 18 28
1715	5 17 59	0 16 40	1 18 7	1745	0 0 44	11 28 50	1 18 28
BI716	11 29 16	6 27 56	1 18 7	1746	11 12 2	6 10 6	1 18 29
1717	6 11 4	1 9 43	1 18 8	1707	5 23 19	0 21 22	1 18 30
1718	0 22 22	7 20 59	1 18 9	BI708	0 4 36	7 2 38	1 18 31
1719	7 3 39	2 2 15	1 18 10	1709	6 16 24	1 14 25	1 18 31
BI720	1 14 56	8 13 31	1 18 10	1750	0 27 42	7 25 41	1 18 32
1721	7 26 44	2 25 19	1 18 11	1751	7 8 59	2 6 57	1 18 33
1722	2 8 2	9 6 35	1 18 12	BI752	1 20 16	8 18 13	1 18 34
1723	8 19 19	3 17 51	1 18 12	1753	8 2 4	3 0 0	1 18 34
BI724	3 0 36	9 29 7	1 18 13	1754	2 13 22	9 11 16	1 18 35
1725	9 12 24	4 10 54	1 18 14	1755	8 24 39	3 22 32	1 18 36
1726	3 23 42	10 22 11	1 18 15	BI756	3 5 56	10 3 48	1 18 36
1727	10 4 59	5 3 26	1 18 15	1757	9 17 44	4 15 35	1 18 37
BI728	4 16 16	11 14 42	1 18 16	1758	3 29 1	10 26 51	1 18 38

A TABLE of MARS's Mean Motion.

Years.	Longit. δ	Anom. δ	Node δ	Years.	Longit. δ	Anom. δ	Node δ
S o	S o	S o	S o	S o	S o	S o	S o
1759	10 10 19	5 8 7	1 18 39	1789	9 23 4	4 20 16	1 19 0
Bi760	4 21 36	11 19 23	1 18 40	1790	4 4 22	11 1 32	1 19 1
1761	11 3 24	6 1 10	1 18 40	1791	10 15 39	5 12 48	1 19 2
1762	5 14 42	0 12 26	1 18 41	Bi792	4 26 56	11 24 4	1 19 2
1763	11 25 59	6 23 42	1 18 41	1793	11 8 44	6 5 51	1 19 3
Bi764	6 7 16	1 4 58	1 18 42	1794	5 20 2	0 17 7	1 19 4
1765	0 19 4	7 16 45	1 18 43	1795	0 1 19	6 28 23	1 19 5
1766	7 0 22	1 28 2	1 18 44	Bi796	6 12 36	1 9 29	1 19 6
1767	1 11 39	8 9 17	1 18 44	1797	0 24 24	7 21 26	1 19 6
Bi768	7 22 56	2 20 33	1 18 45	1798	7 5 42	2 2 42	1 19 7
1769	2 4 44	9 2 20	1 18 46	1799	1 16 59	8 13 58	1 19 8
1770	8 16 2	3 13 36	1 18 47	Bi800	7 28 16	2 25 14	1 19 8
1771	2 27 19	9 24 52	1 18 48	1801	2 10 4	9 7 1	1 19 9
1772	9 8 36	4 6 8	1 18 48	1802	8 21 22	3 18 17	1 19 10
Bi773	3 20 24	10 17 55	1 18 49	1803	3 2 39	9 29 33	1 19 10
1774	10 1 42	4 29 11	1 18 50	Bi804	9 13 56	4 10 49	1 19 11
1775	4 12 59	11 10 27	1 18 51	1805	3 25 44	10 22 36	1 19 12
Bi776	10 24 16	5 21 43	1 18 51	1806	10 7 2	5 3 53	1 19 13
1777	5 6 4	0 3 30	1 18 52	1807	4 18 19	11 15 8	1 19 13
1778	11 17 22	6 14 46	1 18 52	Bi808	10 29 36	5 26 24	1 19 14
1779	5 28 39	0 26 2	1 18 53	1809	5 11 24	0 8 11	1 19 15
Bi780	0 9 56	7 7 19	1 18 54	1810	11 22 42	6 19 27	1 19 16
1781	6 21 44	1 19 6	1 18 54	1811	6 3 59	1 0 43	1 19 17
1782	1 3 2	8 0 22	1 18 55	Bi812	0 15 16	7 11 59	1 19 17
1783	7 14 19	2 11 38	1 18 56	1813	6 27 4	1 23 46	1 19 18
Bi784	1 25 36	8 22 54	1 18 56	1814	1 8 22	8 5 2	1 19 19
1785	8 7 24	3 4 41	1 18 57	1815	7 19 39	2 16 18	1 19 20
1786	2 18 42	9 15 58	1 18 58	Bi816	2 27 34	8 27 34	1 19 20
1787	8 29 59	3 27 13	1 18 58	1817	8 9 21	3 9 21	1 19 21
Bi788	3 11 16	10 8 29	1 18 59	1818	2 20 37	9 20 37	1 19 22

A TABLE of MAR S's Mean Motion.

Com. Years	JANUARY.		FEBRUARY.		MARCH.		Biflexile.
	Longit. δ	Anom. δ	Longit. δ	Anom. δ	Longit. δ	Anom. δ	
	S o	S o	S o	S o	S o	S o	
1	o o 31	o o 31	o 16 46	o 16 46	I 1 27	I 1 27	o
2	o 1 3	o 1 3	o 17 18	o 17 18	I 1 58	I 1 58	1
3	o 1 34	o 1 34	o 17 49	o 17 49	I 2 29	I 2 29	2
4	o 2 6	o 2 6	o 18 21	o 18 21	I 3 1	I 3 1	3
5	o 2 37	o 2 37	o 18 52	o 18 52	I 3 32	I 3 32	4
6	o 3 9	o 3 9	o 19 24	o 19 24	I 4 4	I 4 4	5
7	o 3 40	o 3 40	o 19 55	o 19 55	I 4 35	I 4 35	6
8	o 4 11	o 4 11	o 20 26	o 20 26	I 5 6	I 5 6	7
9	o 4 43	o 4 43	o 20 58	o 20 58	I 5 38	I 5 38	8
10	o 5 14	o 5 14	o 21 29	o 21 29	I 6 9	I 6 9	9
11	o 5 46	o 5 46	o 22 1	o 22 1	I 6 41	I 6 41	10
12	o 6 17	o 6 17	o 22 32	o 22 32	I 7 12	I 7 12	11
13	o 6 49	o 6 49	o 23 4	o 23 4	I 7 44	I 7 44	12
14	o 7 20	o 7 20	o 23 35	o 23 35	I 8 15	I 8 15	13
15	o 7 52	o 7 52	o 24 7	o 24 7	I 8 47	I 8 47	14
16	o 8 23	o 8 23	o 24 38	o 24 38	I 9 18	I 9 18	15
17	o 8 55	o 8 55	o 25 10	o 25 10	I 9 50	I 9 50	16
18	o 9 26	o 9 26	o 25 41	o 25 41	I 10 21	I 10 21	17
19	o 9 57	o 9 57	o 26 12	o 26 12	I 10 52	I 10 52	18
20	o 10 29	o 10 29	o 26 44	o 26 44	I 11 24	I 11 24	19
21	o 11 0	o 11 0	o 27 15	o 27 15	I 11 55	I 11 55	20
22	o 11 32	o 11 32	o 27 47	o 27 47	I 12 27	I 12 27	21
23	o 12 3	o 12 3	o 28 18	o 28 18	I 12 58	I 12 58	22
24	o 12 35	o 12 35	o 28 50	o 28 50	I 13 30	I 13 30	23
25	o 13 6	o 13 6	o 29 21	o 29 21	I 14 1	I 14 1	24
26	o 13 38	o 13 38	o 29 53	o 29 53	I 14 33	I 14 33	25
27	o 14 9	o 14 9	o 0 24	o 0 24	I 15 4	I 15 4	26
28	o 14 40	o 14 40	o 0 55	o 0 55	I 15 35	2 15 35	27
29	o 15 12	o 15 12	o 1 27	o 1 27	I 16 7	I 16 7	28
30	o 15 43	o 15 43	o 0 0	o 0 0	I 16 38	I 16 38	29
31	o 16 15	o 16 15	o 0 0	o 0 0	I 17 10	I 17 10	30

Com. Years	A P R I L.		M A Y.		J U N E.		Biflextile.
	Longit. ♂	Anom. ♂	Longit. ♂	Anom. ♂	Longit. ♂	Anom. ♂	
	S o	S o	S o	S o	S o	S o	
1	I 17 41	I 17 41	2 3 24	2 3 24	2 19 39	2 19 39	0
2	I 18 13	I 18 13	2 3 56	2 3 56	2 20 11	2 20 11	1
3	I 18 44	I 18 44	2 4 27	2 4 27	2 20 42	2 20 42	2
4	I 19 16	I 19 16	2 4 59	2 4 59	2 21 14	2 21 14	3
5	I 19 47	I 19 47	2 5 30	2 5 30	2 21 45	2 21 45	4
6	I 20 19	I 20 19	2 6 2	2 6 2	2 22 17	2 22 17	5
7	I 20 50	I 20 50	2 6 33	2 6 33	2 22 48	2 22 48	6
8	I 21 21	I 21 21	2 7 4	2 7 4	2 23 19	2 23 19	7
9	I 21 53	I 21 53	2 7 36	2 7 36	2 23 53	2 23 53	8
10	I 22 24	I 22 24	2 8 7	2 8 7	2 24 22	2 24 22	9
11	I 22 56	I 22 56	2 8 39	2 8 39	2 24 54	2 24 54	10
12	I 23 27	I 23 27	2 9 10	2 9 10	2 25 25	2 25 25	11
13	I 23 59	I 23 59	2 9 42	2 9 42	2 25 57	2 25 57	12
14	I 24 30	I 24 30	2 10 13	2 10 13	2 26 28	2 26 28	13
15	I 25 2	I 25 2	2 10 45	2 10 45	2 27 0	2 27 0	14
16	I 25 33	I 25 33	2 11 16	2 11 16	2 27 31	2 27 31	15
17	I 26 5	I 26 5	2 11 48	2 11 48	2 28 3	2 28 3	16
18	I 26 36	I 26 36	2 12 19	2 12 19	2 28 34	2 28 34	17
19	I 27 7	I 27 7	2 12 50	2 12 50	2 29 5	2 29 5	18
20	I 27 39	I 27 39	2 13 22	2 13 22	2 29 37	2 29 37	19
21	I 28 10	I 28 10	2 13 53	2 13 53	3 0 8	3 0 8	20
22	I 28 42	I 28 42	2 14 25	2 14 25	3 0 40	3 0 40	21
23	I 29 13	I 29 13	2 14 56	2 14 56	3 1 11	3 1 11	22
24	I 29 45	I 29 45	2 15 28	2 15 28	3 1 43	3 1 43	23
25	2 0 16	2 0 16	2 15 59	2 15 59	3 2 14	3 2 14	24
26	2 0 48	2 0 48	2 16 31	2 16 31	3 2 46	3 2 46	25
27	2 1 19	2 1 19	2 17 2	2 17 2	3 3 17	3 3 17	26
28	2 1 50	2 1 50	2 17 33	2 17 33	3 3 48	3 3 48	27
29	2 2 22	2 2 22	2 18 5	2 18 5	3 4 20	3 4 20	28
30	2 2 53	2 2 53	2 18 36	2 18 36	3 4 51	3 4 51	29
31	2 3 24	2 3 24	2 19 8	2 19 8	3 5 23	3 5 23	30

A TABLE of MAR S's Mean Motion.

Com. Years	JULY.		AUGUST.		SEPTEMBER.		Biflexite.
	Longit. δ	Anom. δ	Longit. δ	Anom. δ	Longit. δ	Anom. δ	
	S o '	S o '	S o '	S o '	S o '	S o '	
1	3 5 23	3 5 22	3 21 37	3 21 36	4 7 52	4 7 51	0
2	3 5 54	3 5 53	3 22 9	3 22 8	4 8 24	4 8 23	1
3	3 6 25	3 6 24	3 22 40	3 22 39	4 8 55	4 8 54	2
4	3 6 56	3 6 55	3 23 12	3 23 11	4 9 27	4 9 26	3
5	3 7 28	3 7 27	3 23 43	3 23 42	4 9 58	4 9 57	4
6	3 8 0	3 7 59	3 24 15	3 24 14	4 10 30	4 10 29	5
7	3 8 31	3 8 30	3 24 46	3 24 45	4 11 1	4 11 0	6
8	3 9 2	3 9 1	3 25 17	3 25 16	4 11 32	4 11 31	7
9	3 9 34	3 9 33	3 25 49	3 25 48	4 12 4	4 12 3	8
10	3 10 5	3 10 4	3 26 20	3 26 19	4 12 35	4 12 34	9
11	3 10 37	3 10 36	3 26 52	3 26 51	4 13 7	4 13 6	10
12	3 11 8	3 11 7	3 27 23	3 27 22	4 13 58	4 13 57	11
13	3 11 40	3 11 39	3 27 55	3 27 54	4 14 10	4 14 9	12
14	3 12 11	3 12 10	3 28 26	3 28 25	4 14 41	4 14 40	13
15	3 12 43	3 12 42	3 28 58	3 28 57	4 15 13	4 15 12	14
16	3 13 14	3 13 13	3 29 29	3 29 28	4 15 44	4 15 43	15
17	3 13 46	3 13 45	4 0 1	4 0 0	4 16 16	4 16 15	16
18	3 14 17	3 14 16	4 0 32	4 0 31	4 16 47	4 16 46	17
19	3 14 48	3 14 47	4 1 3	4 1 2	4 17 18	4 17 17	18
20	3 15 20	3 15 19	4 1 35	4 1 34	4 17 50	4 17 49	19
21	3 15 51	3 15 50	4 2 6	4 2 5	4 18 21	4 18 20	20
22	3 16 23	3 16 22	4 2 38	4 2 37	4 18 53	4 18 52	21
23	3 16 54	3 16 53	4 3 9	4 3 8	4 19 24	4 19 23	22
24	3 17 26	3 17 25	4 3 41	4 3 40	4 19 56	4 19 55	23
25	3 17 57	3 17 56	4 4 12	4 4 11	4 20 27	4 20 26	24
26	3 18 29	3 18 28	4 4 44	4 4 43	4 20 59	4 20 58	25
27	3 19 0	3 18 59	4 5 15	4 5 14	4 21 30	4 21 29	26
28	3 19 31	3 19 30	4 5 46	4 5 45	4 22 1	4 22 0	27
29	3 20 3	3 20 2	4 6 18	4 6 17	4 22 33	4 22 32	28
30	3 20 34	3 20 33	4 6 49	4 6 48	4 23 4	4 23 3	29
31	3 21 6	3 21 5	4 7 21	4 7 20	4 23 35	4 23 34	30

A TABLE of MARS'S Mean Motion, in
Hours, Minutes, and Seconds.

H.	Longit. δ	Anom. δ		Longit. δ	Anom. δ
'	o ' "	o ' "	"	o ' "	o ' "
1	o .1 19	o 1 19	31	o 40 37	o 40 37
2	o 2 37	o 2 37	32	o 41 56	o 41 56
3	o 3 56	o 3 56	33	o 43 15	o 43 15
4	o 5 15	o 5 15	34	o 44 33	o 44 33
5	o 6 33	o 6 33	35	o 45 52	o 45 52
6	o 7 52	o 7 52	36	o 47 11	o 47 11
7	o 9 10	o 9 10	37	o 48 30	o 48 30
8	o 10 29	o 10 29	38	o 49 49	o 49 49
9	o 11 48	o 11 48	39	o 51 6	o 51 6
10	o 13 6	o 13 6	40	o 52 25	o 52 25
11	o 14 25	o 14 25	41	o 53 44	o 53 44
12	o 15 43	o 15 43	42	o 55 2	o 55 2
13	o 17 2	o 17 2	43	o 56 21	o 56 21
14	o 18 21	o 18 21	44	o 57 39	o 57 39
15	o 19 39	o 19 39	45	o 58 58	o 58 58
16	o 20 58	o 20 58	46	I 0 16	I 0 16
17	o 22 16	o 22 16	47	I 1 34	I 1 34
18	o 23 35	o 23 35	48	I 2 53	I 2 53
19	o 24 54	o 24 54	49	I 4 12	I 4 12
20	o 26 16	o 26 16	50	I 5 30	I 5 30
21	o 27 31	o 27 31	51	I 6 49	I 6 49
22	o 28 49	o 28 49	52	I 8 8	I 8 8
23	o 30 8	o 30 8	53	I 9 26	I 9 26
24	o 31 27	o 31 27	54	I 10 45	I 10 45
25	o 32 45	o 32 45	55	I 12 4	I 12 4
26	o 34 4	o 34 4	56	I 13 22	I 13 22
27	o 35 22	o 35 22	57	I 14 40	I 14 40
28	o 36 41	o 36 41	58	I 15 59	I 15 59
29	o 38 0	o 38 0	59	I 17 18	I 17 18
30	o 39 18	o 39 18	60	I 18 30	I 18 30
"	iv v	iv v	"	iv v	iv v

A. TABLE of MARS's Equation.

Degrees.	Sig. 0.			Logar. Dist. à ☉ Curt.	Sig. 1.			Logar. Dist. à ☉ Curt.	Sig. 2.			Logar. Dist. à ☉ Curt.	Degrees.
	Equa. Sub.				Equa. Sub.				Equa. Sub.				
	0	1	2		0	1	2		0	1	2		
0	0	0	0	522136	4	49	27	521709	8	39	52	520488	30
1	0	9	59	522135	4	58	25	521680	8	45	53	520436	29
2	0	19	58	522133	5	7	21	521650	8	51	44	520382	28
3	0	29	56	522130	5	16	11	521620	8	57	28	520328	27
4	0	39	53	522126	5	24	57	521590	9	3	3	520272	26
5	0	49	50	522122	5	33	36	521559	9	8	29	520217	25
6	0	59	46	522117	5	42	11	521526	9	13	46	520161	24
7	1	9	42	522112	5	50	42	521492	9	18	56	520104	23
8	1	19	37	522104	5	59	7	521457	9	23	56	520046	22
9	1	29	32	522095	6	7	29	521422	9	28	49	519998	21
10	1	39	24	522082	6	15	45	521385	9	33	33	519929	20
11	1	49	15	522077	6	23	57	521348	9	38	7	519869	19
12	1	59	5	522065	6	32	2	521310	9	42	31	519808	18
13	2	8	54	522053	6	40	3	521272	9	46	48	519747	17
14	2	18	42	522040	6	47	57	521232	9	50	55	519686	16
15	2	28	27	522027	6	55	45	521192	9	54	53	519624	15
16	2	38	10	522012	7	3	27	521151	9	58	39	519561	14
17	2	47	51	521997	7	11	4	521109	10	2	18	519498	13
18	2	57	29	521980	7	18	34	521065	10	5	46	519435	12
19	3	7	5	521963	7	25	59	521021	10	9	5	519371	11
20	3	16	39	521943	7	33	16	520977	10	12	12	519305	10
21	3	26	10	521924	7	40	26	520932	10	15	10	519240	9
22	3	35	38	521904	7	47	29	520884	10	17	57	519175	8
23	3	45	4	521884	7	54	28	520838	10	20	35	519109	7
24	3	54	25	521861	8	1	19	520791	10	23	2	519042	6
25	4	3	45	521838	8	8	3	520743	10	25	18	518975	5
26	4	13	0	521814	8	14	39	520693	10	27	23	518908	4
27	4	22	14	521789	8	21	10	520643	10	29	21	518841	3
28	4	31	21	521763	8	27	32	520593	10	30	57	518772	2
29	4	40	26	521737	8	33	47	520544	10	32	25	518704	1
30	4	49	27	521709	8	39	52	520488	10	33	57	518636	0
	Add.				Add.				Add.				
	Sig. 11.				Sig. 10.				Sig. 9.				

A TABLE of MARS's Equation.

Degrees.	Sig. 3.			Logar. Dist. a ☉ Curt.	Sig. 4.			Logar. Dist. a ☉ Curt.	Sig. 5.			Logar. Dist. a ☉ Curt.	Degrees.
	Equa. Sub.				Equa. Sub.				Equa. Sub.				
	o	'	"		o	'	"		o	'	"		
0	10	33	57	518636	9	42	17	516526	5	53	44	514763	30
1	10	35	8	518566	9	38	27	516457	5	43	25	514720	29
2	10	36	7	518497	9	33	23	516399	5	32	58	514676	28
3	10	36	56	518428	9	28	8	516326	5	22	21	514635	27
4	10	37	32	518358	9	22	40	516254	5	11	36	514595	26
5	10	37	59	518289	9	17	1	516187	5	0	43	514556	25
6	10	38	12	518219	9	11	8	516121	4	49	40	514520	24
7	10	38	12	518148	9	5	4	516056	4	38	34	514484	23
8	10	38	1	518078	8	58	47	515992	4	27	10	514449	22
9	10	37	40	518007	8	52	20	515927	4	15	58	514416	21
10	10	37	6	517936	8	45	40	515863	4	4	31	514383	20
11	10	36	20	517865	8	38	50	515800	3	52	56	514352	19
12	10	35	21	517794	8	31	47	515738	3	41	17	514323	18
13	10	34	13	517722	8	24	31	515675	3	29	31	514295	17
14	10	32	50	517652	8	17	5	515613	3	17	40	514269	16
15	10	31	17	517581	8	9	27	515553	3	5	43	514244	15
16	10	29	30	517510	8	1	37	515495	2	53	42	514221	14
17	10	27	33	517438	7	53	35	515436	2	41	36	514200	13
18	10	25	22	517368	7	45	25	515378	2	29	27	514180	12
19	10	23	0	517297	7	37	3	515321	2	17	14	514162	11
20	10	20	25	517225	7	28	39	515266	2	4	58	514146	10
21	10	17	39	517153	7	19	46	515210	1	52	37	514141	9
22	10	14	39	517083	7	10	52	515156	1	40	14	514117	8
23	10	11	27	517012	7	1	49	515103	1	27	47	514105	7
24	10	8	3	516942	6	52	34	515052	1	15	19	514094	6
25	10	4	27	516872	6	43	11	515001	1	2	48	514085	5
26	10	0	37	516803	6	32	36	514951	0	50	17	514076	4
27	9	56	36	516733	6	23	52	514902	0	37	43	514073	3
28	9	52	22	516664	6	13	51	514855	0	25	10	514070	2
29	9	47	56	516595	6	3	55	514809	0	12	35	514068	1
30	9	43	17	516526	5	53	44	514763	0	0	0	514067	0
	Add.				Add.				Add.				
	Sig. 8.				Sig. 7.				Sig. 6.				

A TABLE of MARS's Inclination from the Plan of the Ecliptic, with the Proportional Scruples of Latitude.

Argument of Latitude.

Degrees.	Sig. 0. North Asc. Sig. 6. South Asc.		Sig. 1. North Asc. Sig. 7. South Asc.		Sig. 2. North Asc. Sig. 8. South Asc.		Degrees.
	Inclinat.		Inclinat.		Inclinat.		
	° ' "	P. Scr.	° ' "	P. Scr.	° ' "	P. Scr.	
0	0 0 0	0 0	0 55 32	30 0	1 36 11	51 57	30
1	0 1 56	1 3	0 57 11	30 54	1 37 8	52 28	29
2	0 3 52	2 5	0 58 50	31 48	1 38 3	52 58	28
3	0 5 48	3 8	1 0 27	32 41	1 38 58	23 27	27
4	0 7 44	4 11	1 2 4	33 33	1 39 50	53 56	26
5	0 9 40	5 14	1 3 40	34 25	1 40 40	54 23	25
6	0 11 36	6 17	1 5 15	35 16	1 41 29	54 49	24
7	0 13 32	7 19	1 6 48	36 6	1 42 15	55 14	23
8	0 15 27	8 21	1 8 21	36 56	1 42 59	55 38	22
9	0 17 22	9 23	1 9 52	37 45	1 43 42	56 1	21
10	0 19 17	10 25	1 11 23	38 34	1 44 22	56 23	20
11	0 21 12	11 27	1 12 52	39 22	1 45 0	56 44	19
12	0 23 6	12 29	1 14 20	40 9	1 45 37	57 4	18
13	0 24 59	13 30	1 15 46	40 55	1 46 13	57 23	17
14	0 26 52	14 31	1 17 10	41 40	1 46 46	57 40	16
15	0 28 45	15 32	1 18 34	42 26	1 47 17	57 57	15
16	0 30 36	16 32	1 19 55	43 10	1 47 46	58 13	14
17	0 32 28	17 32	1 21 14	43 53	1 48 13	58 28	13
18	0 34 19	18 32	1 22 32	44 35	1 48 29	58 42	12
19	0 36 10	19 32	1 23 50	45 16	1 49 2	58 54	11
20	0 37 59	20 31	1 25 5	45 57	1 49 23	59 5	10
21	0 39 48	21 30	1 26 19	46 37	1 49 42	59 16	9
22	0 41 36	22 29	1 27 31	47 16	1 49 59	59 25	8
23	0 43 23	23 27	1 28 42	47 54	1 50 14	59 33	7
24	0 45 10	24 24	1 29 51	48 32	1 50 27	59 40	6
25	0 46 55	25 21	1 30 59	49 9	1 50 38	59 46	5
26	0 48 40	26 18	1 32 4	49 44	1 50 47	59 52	4
27	0 50 25	27 14	1 33 8	50 18	1 50 54	59 56	3
28	0 52 8	28 10	1 34 11	50 52	1 50 59	59 58	2
29	0 53 50	29 5	1 35 11	51 25	1 51 2	59 59	1
30	0 55 32	30 0	1 36 11	51 57	1 51 4	60 0	0
Sig. 11. South Desc. Sig. 5. North Desc.			Sig. 10. South Desc. Sig. 4. North Desc.		Sig. 9. South Desc. Sig. 3. North Desc.		

Argument of Latitude.

A TABLE of VENUS'S Mean Motion.

Epocha, or Radices.									Mean Motion to 20 Years.											
Anni	Longit. ♀			Anom. ♀			Node ♀			Years.	Longit. ♀			Anom. ♀			Node ♀			
Christ	S	°	'	S	°	'	S	°	'	to 20	S	°	'	S	°	'	S	°	'	
1	1	13	23	4	23	37	1	26	55		1	7	14	47	7	14	46	0	0	1
101	8	2	35	11	10	22	1	27	56		2	2	29	35	2	29	32	0	0	1
201	2	21	48	5	27	8	1	28	58		3	10	14	22	10	14	18	0	0	2
301	9	11	0	0	13	53	1	29	59		4	6	0	46	6	0	40	0	0	2
401	4	0	13	7	0	39	2	1	1		5	1	15	34	1	15	27	0	0	3
501	10	19	25	1	17	24	2	2	2		6	9	0	21	9	0	12	0	0	4
601	5	8	37	8	4	8	2	3	4		7	4	15	09	4	14	59	0	0	4
701	11	27	50	2	20	54	2	4	5	B	8	0	1	32	0	1	20	0	0	5
801	6	17	2	9	7	39	2	5	7		9	7	16	20	7	16	7	0	0	6
901	1	6	15	3	24	25	2	6	8		10	3	1	7	3	0	42	0	0	6
1001	7	25	27	10	11	10	2	7	10		11	10	15	55	10	15	39	0	0	7
1101	2	14	39	4	27	55	2	8	11	B	12	6	2	18	6	2	0	0	0	7
1201	9	3	52	11	14	41	2	9	13		13	1	17	6	1	16	47	0	0	8
1301	3	23	4	6	1	26	2	10	14		14	9	1	53	9	1	32	0	0	9
1401	10	12	17	0	18	12	2	11	16		15	4	16	41	4	16	19	0	0	9
1501	5	1	29	7	4	57	2	12	17	B	16	0	3	4	0	2	40	0	0	10
1601	11	20	42	1	21	42	2	13	19		17	7	17	52	7	17	27	0	0	10
1701	6	9	54	8	8	28	2	14	20		18	3	2	39	3	2	13	0	0	11
1801	0	29	6	2	35	13	2	15	21		19	10	17	27	10	16	59	0	0	12
1901	7	18	19	9	11	58	2	16	23	B	20	6	3	50	6	3	21	0	0	12
2001	2	7	31	3	28	44	2	17	25		Years from 1690.									
Venus's Mean Motion exceeding 20 Years.										1690	7	22	24	9	21	13	2	14	14	
20	6	3	50	6	3	21	0	0	12	1691	3	7	11	5	5	59	2	14	15	
40	0	7	41	0	6	42	0	0	25	1692	10	21	59	0	20	45	2	14	15	
60	6	11	31	6	10	3	0	0	37	1693	6	8	22	8	7	7	2	14	16	
80	0	15	22	0	13	24	0	0	49	1694	1	23	10	3	21	53	2	14	16	
100	6	19	12	6	16	45	0	1	1	1695	9	7	58	11	6	40	2	14	17	
1000	6	12	4	5	17	33	0	10	15	1696	4	22	45	6	21	25	2	14	18	
										1697	0	9	9	2	7	48	2	14	18	
										1698	7	23	56	9	22	33	2	14	19	

A TABLE of VENUS's Mean Motion.

Years.	Longit. ♀	Anom. ♀	Node ♀	Years.	Longit. ♀	Anom. ♀	Node ♀
	S O	S O	S O		S O	S O	S O
1699	3 8 44	5 7 20	2 14 19	1729	0 15 17	2 13 9	2 14 38
BI700	10 23 31	0 21 55	2 14 20	1730	8 0 4	9 27 55	2 14 38
1701	6 9 54	8 8 28	2 14 20	1731	3 14 51	5 12 41	2 14 39
1702	1 24 42	3 23 13	2 14 21	BI732	10 29 39	0 27 27	2 14 39
1703	9 9 30	11 8 0	2 14 22	1733	6 16 2	8 13 49	2 14 40
BI704	4 24 17	6 22 45	2 14 23	1734	2 0 50	3 28 35	2 14 40
1705	0 10 41	2 9 8	2 14 23	1735	9 15 38	11 13 22	2 14 41
1706	7 25 28	9 23 53	2 14 24	BI736	5 0 25	6 28 7	2 14 42
1707	3 10 16	5 8 40	2 14 24	1737	0 16 49	2 14 30	2 14 42
BI708	10 25 3	0 23 26	2 14 25	1738	8 1 36	9 29 15	2 14 43
1709	6 11 27	8 9 48	2 14 26	1739	3 16 44	5 14 2	2 14 44
1710	1 26 14	3 24 34	2 14 26	BI740	11 1 11	0 28 37	2 14 44
1711	9 11 1	11 9 20	2 14 27	1741	6 17 35	8 15 10	2 14 45
BI712	4 25 49	6 24 6	2 14 27	1742	2 2 22	3 29 55	2 14 45
1713	0 12 12	2 10 28	2 14 28	1743	9 17 10	11 14 42	2 14 46
1714	7 27 0	9 25 14	2 14 28	BI744	4 1 57	6 29 27	2 14 47
1715	3 11 48	5 10 1	2 14 29	1745	0 18 21	2 15 50	2 14 47
BI716	10 26 35	0 24 46	2 14 30	1746	8 3 8	10 0 35	2 14 48
1717	6 12 59	8 10 9	2 14 30	1747	3 17 56	5 15 22	2 14 48
1718	1 27 46	3 25 54	2 14 31	BI748	11 2 23	1 0 8	2 14 49
1719	9 12 34	11 10 41	2 14 32	1749	6 19 7	8 16 30	2 14 50
BI720	4 27 21	6 25 16	2 14 32	1750	2 3 54	4 1 16	2 14 50
1721	0 13 45	2 11 49	2 14 33	1751	9 18 41	11 16 2	2 14 51
1722	7 28 32	9 26 34	2 14 33	BI752	5 3 29	7 0 48	2 14 51
1723	3 13 20	5 11 21	2 14 34	1753	0 19 52	2 17 10	2 14 52
BI724	10 28 7	0 26 6	2 14 35	1754	8 4 40	10 1 56	2 14 52
1725	6 14 31	8 12 29	2 14 35	1755	3 19 28	5 16 43	2 14 53
1726	1 29 18	3 27 14	2 14 36	BI756	11 4 15	1 1 28	2 14 54
1727	9 14 6	11 12 1	2 14 36	1757	6 20 9	8 17 51	2 14 54
BI728	4 28 53	6 26 47	2 14 37	1758	2 5 26	4 2 36	2 14 55

A TABLE of VENUS's Mean Motion.

Years.	Longit. ♀			Anom. ♀			Node ♀			Years.	Longit. ♀			Anom. ♀			Node ♀		
	S	o		S	o		S	o			S	o		S	o		S	o	
1759	9	20	14	11	17	23	2	14	56	1789	6	26	47	8	23	12	2	15	14
BI760	5	5	1	7	1	48	2	14	56	1790	2	11	34	4	7	58	2	15	14
1761	0	21	25	2	18	31	2	14	57	1791	9	26	22	11	22	44	2	15	15
1762	8	6	12	10	3	16	2	14	57	BI792	5	11	10	7	7	30	2	15	15
1763	3	21	0	5	18	3	2	14	58	1793	0	27	33	2	23	52	2	15	16
BI764	11	5	47	1	2	48	2	14	59	1794	8	12	21	10	8	38	2	15	16
1765	6	21	31	8	19	11	2	14	59	1795	3	27	9	5	23	25	2	15	17
1766	2	6	58	4	3	56	2	15	0	BI796	11	11	56	1	8	10	2	15	18
1767	9	21	46	11	18	43	2	15	0	1797	6	28	20	8	24	33	2	15	18
BI768	5	6	33	7	3	29	2	15	1	1798	2	13	7	4	9	18	2	15	19
1769	0	22	57	2	19	51	2	15	2	1799	9	27	55	11	24	5	2	15	20
1770	8	7	44	10	4	37	2	15	2	BI800	5	12	42	7	8	40	2	15	20
1771	3	22	31	5	19	23	2	15	3	1801	0	29	6	2	25	13	2	15	21
BI772	11	7	19	1	4	9	2	15	3	1802	8	13	53	10	9	58	2	15	21
1773	6	23	42	8	20	31	2	15	4	1803	3	29	40	5	24	45	2	15	22
1774	2	8	30	4	5	17	2	15	4	BI804	11	13	27	1	9	30	2	15	23
1775	9	23	18	11	20	4	2	15	5	1805	6	29	51	8	25	53	2	15	23
BI776	5	8	5	7	4	49	2	15	6	1806	2	14	38	4	10	38	2	15	24
1777	0	24	29	2	21	12	2	15	6	1807	9	29	25	11	25	25	2	15	24
1778	8	9	16	10	5	57	2	15	7	BI808	5	14	13	7	10	11	2	15	25
1779	3	24	4	5	20	44	2	15	8	1809	1	0	37	2	26	33	2	15	26
BI780	11	8	51	1	5	19	2	15	8	1810	8	15	24	10	11	19	2	15	26
1781	6	25	15	8	21	52	2	15	9	1811	4	0	11	5	26	5	2	15	27
1782	2	10	2	4	6	37	2	15	9	BI812	11	14	59	1	10	51	2	15	27
1783	9	24	50	11	21	24	2	15	10	1813	7	1	22	8	27	13	2	15	28
BI784	5	9	37	7	6	9	2	15	11	1814	2	16	10	4	11	59	2	15	28
1785	0	26	1	2	22	32	2	15	11	1815	10	0	58	11	26	46	2	15	29
1786	8	10	48	10	7	17	2	15	12	BI816	5	15	45	7	11	31	2	15	30
1787	3	25	36	5	22	4	2	15	12	1817	1	2	9	2	27	54	2	15	30
BI788	11	10	23	1	6	50	2	15	13	1818	8	16	56	10	12	39	2	15	31

A TABLE of VENUS's Mean Motion.

Com. Years	JANUARY.		FEBRUARY.		MARCH.		Biflexile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o '	S o '	S o '	S o '	S o '	S o '	
1	0 1 36	0 1 36	1 21 16	1 21 16	3 6 8	3 6 8	0
2	0 3 12	0 3 12	1 22 52	1 22 52	3 7 44	3 7 44	1
3	0 4 48	0 4 48	1 24 28	1 24 28	3 9 20	3 9 20	2
4	0 6 25	0 6 25	1 26 5	1 26 5	3 10 57	3 10 57	3
5	0 8 1	0 8 1	1 27 41	1 27 41	3 12 33	3 12 33	4
6	0 9 37	0 9 37	1 29 17	1 29 17	3 14 9	3 14 9	5
7	0 11 13	0 11 13	2 0 53	2 0 53	3 15 45	3 15 45	6
8	0 12 49	0 12 49	2 2 29	2 2 29	3 17 21	3 17 21	7
9	0 14 25	0 14 25	2 4 5	2 4 5	3 18 57	3 18 57	8
10	0 16 1	0 16 1	2 5 41	2 5 41	3 20 33	3 20 33	9
11	0 17 37	0 17 37	2 7 17	2 7 17	3 22 9	3 22 9	10
12	0 19 14	0 19 14	2 8 54	2 8 54	3 23 46	3 23 46	11
13	0 20 50	0 20 50	2 10 30	2 10 30	3 25 22	3 25 22	12
14	0 22 26	0 22 26	2 12 6	2 12 6	3 26 58	3 26 58	13
15	0 24 2	0 24 2	2 13 42	2 13 42	3 28 34	3 28 34	14
16	0 25 38	0 25 38	2 15 18	2 15 18	4 0 15	4 0 15	15
17	0 27 14	0 27 14	2 16 54	2 16 54	4 1 46	4 1 46	16
18	0 28 50	0 28 50	2 18 30	2 18 30	4 3 22	4 3 22	17
19	1 0 26	1 0 26	2 20 6	2 20 6	4 4 58	4 4 58	18
20	1 2 3	1 2 3	2 21 43	2 21 43	4 6 35	4 6 35	19
21	1 3 39	1 3 39	2 23 19	2 23 19	4 8 11	4 8 11	20
22	1 5 15	1 5 15	2 24 55	2 24 55	4 9 47	4 9 47	21
23	1 6 51	1 6 51	2 26 31	2 26 31	4 11 23	4 11 23	22
24	1 8 27	1 8 27	2 28 7	2 28 7	4 12 59	4 12 59	23
25	1 10 3	1 10 3	2 29 43	2 29 43	4 14 35	4 14 35	24
26	1 11 39	1 11 39	3 1 19	3 1 19	4 16 11	4 16 11	25
27	1 13 16	1 13 16	3 2 56	3 2 56	4 17 48	4 17 48	26
28	1 14 52	1 14 52	3 4 32	3 4 32	4 19 24	4 19 24	27
29	1 16 28	1 16 28	3 6 8	3 6 8	4 21 0	4 21 0	28
30	1 18 4	1 18 4	0 0 0	0 0 0	4 22 36	4 22 36	29
31	1 19 40	1 19 40	0 0 0	0 0 0	4 24 12	4 24 12	30

A TABLE of VENUS's Mean Motion.

Com. Years	A P R I L.		M A Y.		J U N E.		Biflexile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Longit. ♀	
	S o	S o	S o	S o	S o	S o	
1	4 25 48	4 25 48	6 13 52	6 13 52	8 3 32	8 3 32	0
2	4 27 24	4 27 24	6 15 28	6 15 28	8 5 8	8 5 8	1
3	4 29 0	4 29 0	6 17 4	6 17 4	8 6 44	8 6 44	2
4	5 0 37	5 0 37	6 18 41	6 18 41	8 8 21	8 8 21	3
5	5 2 13	5 2 13	6 20 17	6 20 17	8 9 57	8 9 57	4
6	5 3 49	5 3 49	6 21 53	6 21 53	8 11 33	8 11 33	5
7	5 5 25	5 5 25	6 23 29	6 23 29	8 13 9	8 13 9	6
8	5 7 1	5 7 1	6 25 5	6 25 5	8 14 45	8 14 45	7
9	5 8 37	5 8 37	6 26 41	6 26 41	8 16 21	8 16 21	8
10	5 10 13	5 10 13	6 28 17	6 28 17	8 17 57	8 17 57	9
11	5 11 49	5 11 49	6 29 53	6 29 53	8 19 33	8 19 33	10
12	5 13 26	5 13 26	7 1 30	7 1 30	8 21 10	8 21 10	11
13	5 15 2	5 15 2	7 3 6	7 3 6	8 22 46	8 22 46	12
14	5 16 28	5 16 28	7 4 42	7 4 42	8 24 22	8 24 22	13
15	5 18 14	5 18 14	7 6 18	7 6 18	8 25 58	8 25 58	14
16	5 19 50	5 19 50	7 7 54	7 7 54	8 27 34	8 27 34	15
17	5 21 26	5 21 26	7 9 30	7 9 30	8 29 10	8 29 10	16
18	5 23 2	5 23 2	7 11 6	7 11 6	9 0 46	9 0 46	17
19	5 24 38	5 24 38	7 12 42	7 12 42	9 2 22	9 2 22	18
20	5 26 15	5 26 15	7 14 19	7 14 19	9 3 59	9 3 59	19
21	5 27 51	5 27 51	7 15 55	7 15 55	9 5 35	9 5 35	20
22	5 29 27	5 29 27	7 17 31	7 17 31	9 7 11	9 7 11	21
23	6 1 3	6 1 3	7 19 7	7 19 7	9 8 47	9 8 47	22
24	6 2 39	6 2 39	7 20 43	7 20 43	9 10 23	9 10 23	23
25	6 4 15	6 4 15	7 22 19	7 22 19	9 11 59	9 11 59	24
26	6 5 51	6 5 51	7 23 55	7 23 55	9 13 35	9 13 35	25
27	6 7 28	6 7 28	7 25 32	7 25 32	9 15 12	9 15 12	26
28	6 9 4	6 9 4	7 27 8	7 27 8	9 16 48	9 16 48	27
29	6 10 40	6 10 40	7 28 44	7 28 44	9 18 24	9 18 24	28
30	6 12 16	6 12 16	8 0 20	8 0 20	9 20 0	9 19 59	29
31	6 13 52	6 13 52	8 1 56	4 1 56	9 21 36	9 21 35	30

A TABLE of VENUS's Mean Motion.

Com. Years	AUGUST.		JULY.		SEPTEMBER.		Biflexile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o ' "	S o ' "	S o ' "	S o ' "	S o ' "	S o ' "	
1	9 21 36	9 21 35	11 11 16	11 11 15	1 0 56	1 0 55	0
2	9 23 12	9 23 11	11 12 52	11 12 51	1 2 32	1 2 31	1
3	9 24 48	9 24 47	11 14 28	11 14 27	1 4 8	1 4 7	2
4	9 26 25	9 26 24	11 16 5	11 16 4	1 5 45	1 5 44	3
5	9 28 1	9 28 0	11 17 41	11 17 40	1 7 21	1 7 20	4
6	9 29 37	9 29 36	11 19 17	11 19 16	1 8 57	1 8 56	5
7	10 1 13	10 1 12	11 20 53	11 20 52	1 10 33	1 10 32	6
8	10 2 49	10 2 48	11 22 29	11 22 28	1 12 9	1 12 8	7
9	10 4 25	10 4 24	11 24 5	11 24 4	1 13 45	1 13 44	8
10	10 6 1	10 6 0	11 25 41	11 25 40	1 15 21	1 15 20	9
11	10 7 37	10 7 36	11 27 17	11 27 16	1 16 57	1 16 56	10
12	10 9 14	10 9 13	11 28 54	11 28 53	1 18 34	1 18 33	11
13	10 10 50	10 10 49	0 0 30	0 0 29	1 20 10	1 20 9	12
14	10 12 26	10 12 25	0 2 6	0 2 5	1 21 46	1 21 45	13
15	10 14 2	10 14 1	0 3 42	0 3 41	1 23 22	1 23 21	14
16	10 15 38	10 15 37	0 5 18	0 5 17	1 24 58	1 24 57	15
17	10 17 14	10 17 13	0 6 54	0 6 53	1 26 34	1 26 33	16
18	10 18 50	10 18 49	0 8 30	0 8 29	1 28 10	1 28 9	17
19	10 20 26	10 20 25	0 10 6	0 10 5	1 29 46	1 29 45	18
20	10 22 3	10 22 2	0 11 43	0 11 42	2 1 23	2 1 22	19
21	10 23 39	10 23 38	0 13 19	0 13 18	2 2 59	2 2 58	20
22	10 25 15	10 25 14	0 14 55	0 14 54	2 4 35	2 4 34	21
23	10 26 51	10 26 50	0 16 31	0 16 30	2 6 11	2 6 10	22
24	10 28 27	10 28 26	0 18 7	0 18 6	2 7 47	2 7 46	23
25	11 0 3	11 0 2	0 19 43	0 19 42	2 9 23	2 9 22	24
26	11 1 39	11 1 38	0 21 19	0 21 18	2 11 59	2 11 58	25
27	11 3 16	11 3 15	0 22 56	0 22 55	2 12 36	2 12 35	26
28	11 4 52	11 4 51	0 24 32	0 24 31	2 14 12	2 14 11	27
29	11 6 28	11 6 27	0 26 8	0 26 7	2 15 48	2 15 47	28
30	11 8 4	11 8 3	0 27 44	0 27 43	2 17 24	2 17 23	29
31	11 9 40	11 9 39	0 29 20	0 29 19	2 19 0	2 18 59	30

For Longit. in the last Page under JUNE 2d. Col. read Anom.

A TABLE of VENUS's Mean Motion.

Com. Years	OCTOBER.		NOVEMB.		DECEMB.		Degrees.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o	S o	S o	S o	S o	S o	
1	2 19 0	2 18 59	4 8 40	4 8 39	5 26 44	5 26 43	0
2	2 20 36	2 20 35	4 10 16	4 10 15	5 28 20	5 28 19	1
3	2 22 12	2 22 11	4 11 52	4 11 51	5 29 56	5 29 55	2
4	2 23 49	2 23 48	4 13 29	4 13 28	6 1 33	6 1 32	3
5	2 25 25	2 25 24	4 15 5	4 15 4	6 3 9	6 3 8	4
6	2 27 1	2 27 0	4 16 41	4 16 40	6 4 45	6 4 44	5
7	2 28 37	2 28 36	4 18 57	4 18 56	6 6 21	6 6 20	6
8	3 0 13	3 0 12	4 19 53	4 19 52	6 7 57	6 7 56	7
9	3 1 49	3 1 48	4 21 29	4 21 28	6 9 33	6 9 32	8
10	3 3 25	3 3 24	4 23 5	4 23 4	6 11 9	6 11 8	9
11	3 5 1	3 5 0	4 24 41	4 24 40	6 12 45	6 12 44	10
12	3 6 38	3 6 37	4 26 18	4 26 17	6 14 22	6 14 21	11
13	3 8 14	3 8 13	4 27 54	4 27 53	6 15 52	6 15 51	12
14	3 9 50	3 9 49	4 29 30	4 29 29	6 17 34	6 17 33	13
15	3 11 26	3 11 25	5 1 6	5 1 5	6 19 10	6 19 9	14
16	3 13 2	3 13 1	5 2 42	5 2 41	6 20 46	6 20 45	15
17	3 14 38	3 14 37	5 4 18	5 4 17	6 22 22	6 22 21	16
18	3 16 14	3 16 13	5 5 54	5 5 53	6 23 58	6 23 57	17
19	3 17 50	3 17 49	5 7 30	5 7 29	6 25 34	6 25 33	18
20	3 19 27	3 19 26	5 9 7	5 9 6	6 27 11	6 27 10	19
21	3 21 3	3 21 2	5 10 43	5 10 42	6 28 47	6 28 46	20
22	3 22 39	3 22 38	5 12 19	5 12 18	7 0 23	7 0 22	21
23	3 24 15	3 24 14	5 13 55	5 13 54	7 1 59	7 1 58	22
24	3 25 51	3 25 50	5 15 31	5 15 30	7 3 35	7 3 34	23
25	3 27 27	3 27 26	5 17 7	5 17 6	7 5 11	7 5 10	24
26	3 29 3	3 29 2	5 18 43	5 18 42	7 6 47	7 6 45	25
27	4 0 40	4 0 39	5 20 20	5 20 19	7 8 24	7 8 22	26
28	4 2 16	4 2 15	5 21 56	5 21 55	7 10 0	7 9 58	27
29	4 3 52	4 3 51	5 23 32	5 23 31	7 11 36	7 11 34	28
30	4 5 28	4 5 27	5 25 8	5 25 7	7 13 12	7 13 10	29
31	4 7 4	4 7 3	5 26 44	5 26 43	7 14 48	7 14 46	30

A TABLE of VENUS's Mean Motion, in Hours, Minutes, and Seconds.

	H.	Longit. ♀			Anom. ♀		Longit. ♀			Anom. ♀		
		°	'	"			°	'	"			
0	1	0	4	0	0	31	2	4	10	2	4	10
1	2	0	8	1	0	32	2	8	11	2	8	11
2	3	0	12	1	0	33	2	12	11	2	12	11
3	4	0	16	1	0	34	2	16	11	2	16	11
4	5	0	20	2	0	35	2	20	12	2	20	12
5	6	0	24	2	0	36	2	24	12	2	24	12
6	7	0	28	2	0	37	2	28	12	2	28	12
7	8	0	32	2	0	38	2	32	13	2	32	13
8	9	0	36	3	0	39	2	36	13	2	36	13
9	10	0	40	3	0	40	2	40	13	2	40	13
10	11	0	44	3	0	41	2	44	14	2	44	14
11	12	0	48	4	0	42	2	48	14	2	48	14
12	13	0	52	4	0	43	2	52	14	2	52	14
13	14	0	56	4	0	44	3	56	15	2	56	15
14	15	1	0	5	1	45	3	0	15	3	0	15
15	16	1	4	5	1	46	3	4	15	3	4	15
16	17	1	8	5	1	47	3	8	16	3	8	16
17	18	1	12	5	1	48	3	12	16	3	12	16
18	19	1	16	6	1	49	3	16	16	3	16	16
19	20	1	20	6	1	50	3	20	17	3	20	17
20	21	1	24	6	1	51	3	24	17	3	24	17
21	22	1	28	7	1	52	3	28	17	3	28	17
22	23	1	32	7	1	53	3	32	18	3	32	18
23	24	1	36	7	1	54	3	36	18	3	36	18
24	25	1	40	8	1	55	3	40	18	3	40	18
25	26	1	44	8	1	56	3	44	19	3	44	19
26	27	1	48	9	1	57	3	48	19	3	48	19
27	28	1	52	9	1	58	3	52	19	3	52	19
28	29	1	56	9	1	59	3	56	20	3	56	20
29	30	2	0	10	2	00	4	0	20	4	0	20
30	31	2	4	10	2	1	4	4	20	4	4	20
31	32	2	8	10	2	2	8	4	20	4	8	20
32	33	2	12	11	2	3	12	4	20	4	12	20
33	34	2	16	11	2	4	16	4	20	4	16	20
34	35	2	20	11	2	5	20	4	20	4	20	20
35	36	2	24	12	2	6	24	4	20	4	24	20
36	37	2	28	12	2	7	28	4	20	4	28	20
37	38	2	32	12	2	8	32	4	20	4	32	20
38	39	2	36	13	2	9	36	4	20	4	36	20
39	40	2	40	13	2	10	40	4	20	4	40	20
40	41	2	44	14	2	11	44	4	20	4	44	20
41	42	2	48	14	2	12	48	4	20	4	48	20
42	43	2	52	14	2	13	52	4	20	4	52	20
43	44	2	56	15	2	14	56	4	20	4	56	20
44	45	2	0	15	2	15	0	4	20	4	0	20
45	46	2	4	15	2	16	4	4	20	4	4	20
46	47	2	8	16	2	17	8	4	20	4	8	20
47	48	2	12	16	2	18	12	4	20	4	12	20
48	49	2	16	16	2	19	16	4	20	4	16	20
49	50	2	20	17	2	20	20	4	20	4	20	20
50	51	2	24	17	2	21	24	4	20	4	24	20
51	52	2	28	17	2	22	28	4	20	4	28	20
52	53	2	32	18	2	23	32	4	20	4	32	20
53	54	2	36	18	2	24	36	4	20	4	36	20
54	55	2	40	18	2	25	40	4	20	4	40	20
55	56	2	44	19	2	26	44	4	20	4	44	20
56	57	2	48	19	2	27	48	4	20	4	48	20
57	58	2	52	19	2	28	52	4	20	4	52	20
58	59	2	56	20	2	29	56	4	20	4	56	20
59	00	2	0	20	2	30	0	4	20	4	0	20
60	01	2	4	20	2	31	4	4	20	4	4	20
61	02	2	8	20	2	32	8	4	20	4	8	20
62	03	2	12	21	2	33	12	4	20	4	12	20
63	04	2	16	21	2	34	16	4	20	4	16	20
64	05	2	20	21	2	35	20	4	20	4	20	20
65	06	2	24	22	2	36	24	4	20	4	24	20
66	07	2	28	22	2	37	28	4	20	4	28	20
67	08	2	32	22	2	38	32	4	20	4	32	20
68	09	2	36	23	2	39	36	4	20	4	36	20
69	10	2	40	23	2	40	40	4	20	4	40	20
70	11	2	44	23	2	41	44	4	20	4	44	20
71	12	2	48	24	2	42	48	4	20	4	48	20
72	13	2	52	24	2	43	52	4	20	4	52	20
73	14	2	56	24	2	44	56	4	20	4	56	20
74	15	2	0	25	2	45	0	4	20	4	0	20
75	16	2	4	25	2	46	4	4	20	4	4	20
76	17	2	8	25	2	47	8	4	20	4	8	20
77	18	2	12	26	2	48	12	4	20	4	12	20
78	19	2	16	26	2	49	16	4	20	4	16	20
79	20	2	20	26	2	50	20	4	20	4	20	20
80	21	2	24	27	2	51	24	4	20	4	24	20
81	22	2	28	27	2	52	28	4	20	4	28	20
82	23	2	32	27	2	53	32	4	20	4	32	20
83	24	2	36	28	2	54	36	4	20	4	36	20
84	25	2	40	28	2	55	40	4	20	4	40	20
85	26	2	44	28	2	56	44	4	20	4	44	20
86	27	2	48	29	2	57	48	4	20	4	48	20
87	28	2	52	29	2	58	52	4	20	4	52	20
88	29	2	56	29	2	59	56	4	20	4	56	20
89	30	2	0	30	2	00	0	4	20	4	0	20
90	31	2	4	30	2	1	4	4	20	4	4	20
91	32	2	8	30	2	2	8	4	20	4	8	20
92	33	2	12	31	2	3	12	4	20	4	12	20
93	34	2	16	31	2	4	16	4	20	4	16	20
94	35	2	20	31	2	5	20	4	20	4	20	20
95	36	2	24	32	2	6	24	4	20	4	24	20
96	37	2	28	32	2	7	28	4	20	4	28	20
97	38	2	32	32	2	8	32	4	20	4	32	20
98	39	2	36	33	2	9	36	4	20	4	36	20
99	40	2	40	33	2	10	40	4	20	4	40	20
00	41	2	44	33	2	11	44	4	20	4	44	20
01	42	2	48	34	2	12	48	4	20	4	48	20
02	43	2	52	34	2	13	52	4	20	4	52	20
03	44	2	56	34	2	14	56	4	20	4	56	20
04	45	2	0	35	2	15	0	4	20	4	0	20
05	46	2	4	35	2	16	4	4	20	4	4	20
06	47	2	8	35	2	17	8	4	20	4	8	20
07	48	2	12	36	2	18	12	4	20	4	12	20
08	49	2	16	36	2	19	16	4	20	4	16	20
09	50	2	20	36	2	20	20	4	20	4	20	20
10	51	2	24	37	2	21	24	4	20	4	24	20
11	52	2	28	37	2	22	28	4	20	4	28	20
12	53	2	32	37	2	23	32	4	20	4	32	20
13	54	2	36	38	2	24	36	4	20	4	36	20
14	55	2	40	38	2	25	40	4	20	4	40	20
15	56	2	44	38	2	26	44	4	20	4	44	20
16	57	2	48	39	2	27	48	4	20	4	48	20
17	58	2	52	39	2	28	52	4	20	4	52	20
18	59	2	56	39	2	29	56	4	20	4	56	20
19	00	2	0	40	2	30	0	4	20	4	0	20
20	01	2	4	40	2	31	4	4	20	4	4	20
21	02	2	8	40	2	32	8	4	20	4	8	20
22	03	2	12	41	2	33	12	4	20	4	12	20
23	04	2	16	41	2	34	16	4	20	4	16	20
24	05	2	20	41	2	35	20	4	20	4	20	20
25	06	2	24	42	2	36	24	4	20	4	24	20
26	07	2	28	42	2	37	28	4	20	4	28	20
27	08	2	32	42	2	38	32	4	20	4	32	20
28	09	2	36	43	2	39	36	4	20	4	36	20
29	10	2	40	43	2	40	40	4	20	4	40	20
30	11	2	44	43	2	41	44	4	20	4	44	20
31	12	2	48	44	2	42	48	4	20	4	48	

A TABLE of VENUS's Equation.

Degrees.	Sig. 0.			Logar. Dist. à ☉ Curt.	Sig. 1.			Logar. Dist. à ☉ Curt.	Sig. 2.			Logar. Dist. à ☉ Curt.	Degrees.
	Equa. Sub.				Equa. Sub.				Equa. Sub.				
0	0	0	0	486293	0	20	24	486227	0	35	4	486088	30
1	0	0	42	486293	0	21	0	486222	0	35	26	486082	29
2	0	1	25	486292	0	21	36	486219	0	35	48	486077	28
3	0	2	8	486290	0	22	12	486215	0	36	8	486071	27
4	0	2	50	486289	0	22	47	486211	0	36	29	486065	26
5	0	3	33	486287	0	23	22	486207	0	36	48	486059	25
6	0	4	15	486286	0	23	56	486204	0	37	6	486054	24
7	0	4	58	486285	0	24	30	486200	0	37	23	486048	23
8	0	5	41	486283	0	25	4	486196	0	37	38	486042	22
9	0	6	24	486281	0	25	38	486192	0	37	54	486036	21
10	0	7	6	486279	0	26	11	486187	0	38	8	486031	20
11	0	7	48	486277	0	26	43	486183	0	38	23	486023	19
12	0	8	31	486276	0	27	14	486179	0	38	36	486018	18
13	0	9	13	486274	0	27	45	486175	0	38	48	486012	17
14	0	9	54	486272	0	28	16	486170	0	38	58	486006	16
15	0	10	36	486270	0	28	47	486165	0	39	7	485999	15
16	0	11	17	486268	0	29	18	486160	0	39	17	485992	14
17	0	11	59	486265	0	29	48	486156	0	39	25	485986	13
18	0	12	41	486264	0	30	17	486152	0	39	33	485980	12
19	0	13	21	486261	0	30	44	486147	0	39	42	485974	11
20	0	14	1	486258	0	31	10	486142	0	39	50	485967	10
21	0	14	41	486255	0	31	35	486136	0	39	58	485961	9
22	0	15	21	486252	0	32	0	486131	0	40	5	485955	8
23	0	16	0	486249	0	32	25	486126	0	40	12	485948	7
24	0	16	39	486247	0	32	49	486121	0	40	18	485943	6
25	0	17	18	486244	0	33	12	486116	0	40	22	485936	5
26	0	17	56	486241	0	33	35	486110	0	40	25	485930	4
27	0	18	34	486237	0	33	58	486105	0	40	27	485924	3
28	0	19	11	486234	0	34	20	486099	0	40	28	485917	2
29	0	19	48	486230	0	34	42	486093	0	40	29	485911	1
30	0	20	24	486227	0	35	4	486088	0	40	30	485905	0
	Add.				Add.				Add.				
	Sig. 11.				Sig. 10.				Sig. 9.				

A TABLE of VENUS's Equation.

Degrees.	Sig. 3.		Degrees.	Sig. 4.		Degrees.	Sig. 5.	
	Equa. Sub.	Logar. Diff. a \odot Curt.		Equa. Sub.	Logar. Diff. a \odot Curt.		Equa. Sub.	Logar. Diff. a \odot Curt.
0	0 40 30	485905	0	34 18	485770	0	20 38	485677
1	0 40 30	485900	1	34 56	485767	1	20 1	485675
2	0 40 30	485896	2	34 34	485763	2	19 24	485674
3	0 40 29	485892	3	34 12	485759	3	18 46	485672
4	0 40 28	485887	4	33 49	485755	4	18 8	485671
5	0 40 25	485882	5	33 26	485751	5	17 29	485669
6	0 40 21	485876	6	33 3	485747	6	16 50	485667
7	0 40 16	485872	7	32 39	485744	7	16 10	485665
8	0 40 10	485868	8	32 14	485741	8	15 30	485664
9	0 40 3	485863	9	31 49	485737	9	14 50	485663
10	0 39 56	485858	10	31 24	485734	10	14 10	485662
11	0 39 48	485854	11	30 58	485730	11	13 29	485661
12	0 39 40	485848	12	30 31	485726	12	12 48	485660
13	0 39 32	485844	13	30 2	485723	13	12 6	485659
14	0 39 24	485839	14	29 32	485720	14	11 24	485659
15	0 39 15	485835	15	29 1	485717	15	10 42	485659
16	0 39 6	485831	16	28 30	485714	16	10 0	485658
17	0 38 56	485827	17	27 59	485711	17	9 18	485658
18	0 38 45	485822	18	27 28	485707	18	8 36	485658
19	0 38 32	485817	19	26 57	485704	19	7 53	485657
20	0 38 18	485813	20	26 25	485701	20	7 10	485657
21	0 38 4	485809	21	25 52	485699	21	6 27	485657
22	0 37 49	485805	22	25 18	485696	22	5 44	485656
23	0 37 34	485801	23	24 44	485693	23	5 1	485656
24	0 37 18	485796	24	24 10	485690	24	4 18	485656
25	0 37 0	485792	25	23 36	485688	25	3 35	485656
26	0 36 41	485787	26	23 1	485686	26	2 52	485655
27	0 36 21	485783	27	22 26	485684	27	2 9	485655
28	0 36 1	485779	28	21 50	485682	28	1 26	485655
29	0 35 40	485775	29	21 14	485680	29	0 43	485655
30	0 35 18	485770	30	20 38	485677	30	0 0	485655
	Add.			Add.			Add.	
	Sig. 8.			Sig. 7.			Sig. 6.	

A TABLE of VENUS's Inclination from the Plan of the Ecliptic, with the Proportional Scruples of Latitude.

Argument of Latitude.

Degrees.	Sig. 0. North Asc. Sig. 6. South Asc.		Sig. 1. North Asc. Sig. 7. South Asc.		Sig. 2. North Asc. Sig. 8. South Asc.		Degrees.
	Inclinat.	P. Scr.	Inclinat.	P. Scr.	Inclinat.	P. Scr.	
0	0 0 0	0 0	1 41 22	30 0	2 55 38	51 57	30
1	0 3 32	1 3	1 44 26	30 54	2 57 23	52 28	29
2	0 7 4	2 5	1 47 27	31 48	2 59 5	52 58	28
3	0 10 36	3 8	1 50 25	32 41	3 0 43	53 27	27
4	0 14 9	4 11	1 53 22	33 33	3 2 17	53 56	26
5	0 17 40	5 14	1 56 18	34 25	3 3 48	54 23	25
6	0 21 11	6 17	1 59 13	35 16	3 5 15	54 49	24
7	0 24 41	7 19	2 2 3	36 6	3 6 38	55 14	23
8	0 28 11	8 21	2 4 52	36 56	3 8 1	55 38	22
9	0 31 41	9 23	2 7 37	37 45	3 9 19	56 1	21
10	0 35 11	10 25	2 10 21	38 34	3 10 34	56 23	20
11	0 38 40	11 27	2 13 2	39 22	3 11 45	56 44	19
12	0 42 9	12 29	2 15 41	40 9	3 12 54	57 4	18
13	0 45 37	13 30	2 18 18	40 55	3 13 57	57 27	17
14	0 49 4	14 31	2 20 25	41 40	3 14 56	57 40	16
15	0 52 28	15 32	2 23 23	42 26	3 15 54	57 57	15
16	0 55 52	16 32	2 25 51	43 10	3 16 47	58 13	14
17	0 59 15	17 32	2 28 18	43 53	3 17 37	58 28	13
18	1 2 37	18 32	2 30 41	44 35	3 18 24	58 42	12
19	1 5 59	19 32	2 33 2	45 16	3 19 6	58 54	11
20	1 9 20	20 31	2 35 20	45 57	3 19 45	59 5	10
21	1 12 40	21 30	2 37 36	46 37	3 20 20	59 16	9
22	1 15 59	22 29	2 39 48	47 16	3 20 52	59 25	8
23	1 19 14	23 27	2 41 37	47 54	3 21 20	59 33	7
24	1 22 28	24 24	2 44 3	48 32	3 21 44	59 40	6
25	1 25 41	25 21	2 46 7	49 9	3 22 4	59 46	5
26	1 28 51	26 18	2 48 7	49 44	3 22 21	59 52	4
27	1 32 5	27 14	2 50 4	50 18	3 22 33	59 56	3
28	1 35 9	28 10	2 51 59	50 52	3 22 42	59 58	2
29	1 38 17	29 5	2 53 49	51 25	3 22 48	50 59	1
30	1 41 22	30 0	2 55 38	51 57	3 22 50	60 0	0
	Sig. 11. South Desc. Sig. 5. North Desc.		Sig. 10. South Desc. Sig. 4. North Desc.		Sig. 9. South Desc. Sig. 3. North Desc.		

Argument of Latitude.

A TABLE of MERCURY'S Mean Motion.

Anni	Longit. ♀	Anom. ♀	Node ♀	Years.	Longit. ♀	Anom. ♀	Node ♀
Christi	S °	S °	S °		S °	S °	S °
101	10 11 53	3 17 14	11 29 48	1	1 23 43	1 23 42	0 0 2
101	0 26 18	5 28 49	0 2 28	2	3 17 27	3 17 24	0 0 3
201	3 10 43	8 10 23	0 5 8	3	5 11 10	5 11 5	0 0 5
301	5 25 8	10 21 58	0 7 48	B 4	7 8 59	7 8 53	0 0 6
401	8 9 33	1 3 33	0 10 28	5	9 2 42	9 2 33	0 0 8
501	10 23 58	3 15 7	0 13 8	6	10 26 25	10 26 15	0 0 10
601	1 8 23	5 26 41	0 15 49	7	0 20 8	0 19 56	0 0 11
701	3 22 49	8 8 17	0 18 29	B 8	2 17 57	2 17 43	0 0 14
801	6 7 14	10 19 52	0 21 9	9	4 11 40	4 11 25	0 0 14
901	8 21 39	1 1 26	0 23 49	10	6 5 24	6 5 7	0 0 16
1001	11 6 4	3 13 1	0 26 29	11	7 29 7	7 28 48	0 0 18
1101	1 20 29	5 24 36	0 29 9	B 12	9 26 56	9 26 36	0 0 19
1201	4 4 54	8 6 10	1 1 49	13	11 20 39	11 20 17	0 0 21
1301	6 19 19	10 17 45	1 4 29	14	1 14 22	1 13 58	0 0 22
1401	9 3 44	0 29 19	1 7 9	15	3 8 6	3 7 39	0 0 24
1501	11 18 9	3 10 54	1 9 49	B 16	5 5 54	5 5 27	0 0 26
1601	2 2 34	5 22 28	1 12 30	17	6 29 38	6 29 9	0 0 27
1701	4 16 59	8 4 2	1 15 10	18	8 23 21	8 22 50	0 0 29
1801	7 1 24	10 15 37	1 17 50	19	10 17 4	10 16 32	0 0 30
1901	9 15 49	0 27 12	1 20 30	B 20	0 14 53	0 14 19	0 0 32
2001	0 0 15	3 8 47	1 23 10	Years from 1690.			
Mercury's Mean Motion exceeding 20 Years.				1690	8 13 46	0 1 9	1 14 52
20	0 14 53	0 14 19	0 0 32	1691	10 7 29	1 24 51	1 14 54
40	0 29 46	0 28 38	0 1 4	B 1692	0 1 13	3 18 33	1 14 55
60	1 14 39	1 12 57	0 1 36	1693	1 29 1	5 16 19	1 14 57
80	1 29 32	1 17 16	0 2 8	1694	3 22 45	7 10 1	1 14 58
100	2 14 25	2 11 35	0 2 40	1695	5 16 28	9 3 42	1 15 0
1000	0 24 11	11 25 47	0 26 41	B 1696	7 10 11	10 27 24	1 15 2
				1697	9 8 0	0 25 11	1 15 3
				1698	11 1 43	2 18 52	1 15 5

A TABLE of MERCURY's Mean Motion.

Years.	Longit. ♄	Anom. ♄	Node ♄	Years.	Longit. ♄	Anom. ♄	Node ♄
	S o	S o	S o		S o	S o	S o
1699	0 25 26	4 12 34	1 15 6	1729	6 19 49	11 6 5	1 16 55
Bi700	2 19 10	6 6 16	1 15 8	1730	9 13 32	0 29 46	1 16 56
1701	4 16 59	8 4 2	1 15 10	1731	11 7 15	2 23 28	1 16 58
1702	6 10 42	9 27 45	1 15 11	Bi732	1 0 59	4 17 10	1 16 59
1703	8 4 25	11 21 26	1 15 13	1733	2 28 47	6 14 57	1 16 1
Bi704	9 28 8	1 15 7	1 15 14	1734	4 20 31	8 8 39	1 16 2
1705	11 25 58	3 12 54	1 15 16	1735	6 16 14	10 2 20	1 15 4
1706	1 29 40	5 6 36	1 15 18	Bi736	8 9 57	11 26 2	1 16 6
1707	3 13 24	7 0 7	1 15 19	1737	10 7 46	1 23 49	1 16 7
Bi708	5 7 7	8 23 59	1 15 21	1738	0 1 29	3 17 30	1 16 9
1709	7 4 56	10 21 47	1 15 22	1739	1 25 12	5 11 12	1 16 10
1710	8 28 39	0 15 28	1 15 24	Bi740	3 18 56	7 4 54	1 16 12
1711	10 22 22	2 9 10	1 15 26	1741	5 16 45	9 2 40	1 16 14
Bi712	0 16 6	4 2 52	1 15 27	1742	7 10 28	10 26 22	1 16 15
1713	2 13 54	6 0 38	1 15 29	1743	9 4 11	0 20 4	1 16 17
1714	4 7 38	7 24 20	1 15 30	Bi744	10 27 54	2 13 45	1 16 18
1715	6 1 21	9 18 1	1 15 32	1745	0 25 44	4 11 32	1 16 20
Bi716	7 25 4	11 11 43	1 15 34	1746	2 19 26	6 5 14	1 16 22
1717	9 22 53	1 9 30	1 15 35	1747	4 13 10	7 28 45	1 16 23
1718	11 16 36	3 3 11	1 15 37	Bi748	6 6 53	9 22 36	1 16 25
1719	1 10 19	4 26 53	1 15 38	1749	8 4 42	11 20 24	1 16 26
Bi720	3 4 3	6 20 35	1 15 40	1750	9 28 25	1 14 5	1 16 28
1721	5 1 51	8 18 21	1 15 42	1751	11 22 9	3 7 47	1 16 30
1722	6 25 31	10 12 4	1 15 43	Bi752	1 15 52	5 1 29	1 16 31
1723	8 19 18	0 5 45	1 15 45	1753	3 13 40	6 29 15	1 16 33
Bi724	10 13 1	1 29 16	1 15 46	1754	5 7 24	8 22 57	1 16 34
1725	0 10 51	3 27 13	1 15 48	1755	7 1 7	10 16 38	1 16 36
1726	2 4 33	5 20 55	1 15 50	Bi756	8 24 50	0 10 20	1 16 38
1727	3 28 17	7 14 26	1 15 51	1757	10 22 39	2 8 7	1 16 39
Bi728	5 22 0	9 8 18	1 15 53	1758	0 16 22	4 1 48	1 16 41

A TABLE of MERCURY's Mean Motion.

Years.	Longit. ♄	Anom. ♄	Node ♄	Years.	Longit. ♄	Anom. ♄	Node ♄
S o	S o	S o	S o	S o	S o	S o	S o
1759	2 10 5	5 25 30	1 16 42	1789	9 4 28	0 19 3	1 17 30
Bi760	4 3 49	7 19 12	1 16 44	1790	10 28 11	2 12 44	1 17 32
1761	6 1 38	9 16 59	1 16 46	1791	0 21 54	4 5 26	1 17 34
1762	7 25 21	11 10 42	1 16 47	Bi792	2 5 38	6 0 8	1 17 35
1763	9 19 4	1 4 23	1 16 49	1793	4 13 26	7 27 54	1 17 37
Bi764	11 12 47	2 28 4	1 16 50	1794	6 7 10	9 21 36	1 17 38
1765	1 10 37	4 25 51	1 16 52	1795	8 0 53	11 15 17	1 17 40
1766	3 4 19	6 19 33	1 16 54	1796	9 24 36	1 8 59	1 17 42
1769	4 28 3	8 13 14	1 16 56	1797	11 22 25	3 6 46	1 17 43
Bi768	6 21 46	10 6 56	1 16 57	1798	1 16 8	5 0 27	1 17 45
1769	8 19 35	0 4 43	1 16 58	1799	3 9 51	6 24 9	1 17 47
1770	10 13 18	1 28 24	1 17 0	Bi800	5 3 35	8 17 51	1 17 48
1771	0 7 1	3 22 6	1 17 2	1801	7 1 24	10 15 37	1 17 50
Bi772	2 0 45	5 15 48	1 17 3	1802	8 25 7	0 9 20	1 17 51
1773	3 28 33	7 13 35	1 17 5	1803	10 18 50	2 3 1	1 17 53
1774	5 22 17	9 17 17	1 17 6	Bi804	0 12 33	3 26 42	1 17 54
1775	7 16 6	11 0 58	1 17 8	1805	2 10 23	5 24 29	1 17 56
1776	9 9 43	0 24 40	1 17 10	1806	4 4 5	7 18 11	1 17 58
1777	11 7 32	2 22 27	1 17 11	1807	5 25 49	9 11 42	1 17 59
1778	1 1 15	4 16 8	1 17 13	Bi808	7 21 32	11 5 34	1 18 1
1779	2 24 58	6 9 50	1 17 14	1809	9 19 21	1 3 22	1 18 2
Bi780	4 18 42	8 3 32	1 17 16	1810	11 13 4	2 27 3	1 18 4
1781	6 16 31	10 1 18	1 17 18	1811	1 6 47	4 20 45	1 18 6
1782	8 10 14	11 25 1	1 17 19	Bi812	3 0 31	6 14 27	1 18 7
1783	10 3 57	1 19 12	1 17 21	1813	4 28 19	8 12 13	1 18 9
Bi784	11 27 40	3 12 23	1 17 22	1814	6 22 3	10 5 55	1 18 10
1785	1 25 30	5 10 10	1 17 24	1815	8 15 46	11 29 36	1 18 12
1786	3 19 12	7 3 52	1 17 26	Bi816	10 9 29	1 23 18	1 18 14
1787	5 12 56	8 27 23	1 17 27	1817	0 7 18	3 21 5	1 18 15
Bi788	7 6 39	10 21 15	1 17 29	1818	2 1 2	5 14 46	1 18 17

A TABLE of MERCURY'S Mean Motion.

Com. Years.	JANUARY.		FEBRUARY.		MARCH.		Biflexile.
	Longit. ♀	Longit.	Anom. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o	S o	S o	S o	S o	S o	
1	0 4 6	0 4 6	4 10 58	4 10 58	8 5 33	8 5 33	0
2	0 8 11	0 8 11	4 15 3	4 15 3	8 9 38	8 9 38	1
3	0 12 17	0 12 17	4 19 9	4 19 9	8 12 44	8 12 44	2
4	0 16 22	0 16 22	4 23 14	4 23 14	8 17 49	8 17 49	3
5	0 20 28	0 20 28	4 27 20	4 27 20	8 21 55	8 21 55	4
6	0 24 33	0 24 33	5 1 25	5 1 25	8 26 0	8 26 0	5
7	0 28 39	0 28 39	5 5 31	5 5 31	9 0 6	9 0 6	6
8	1 2 44	1 2 44	5 9 36	5 9 36	9 4 11	9 4 11	7
9	1 6 50	1 6 50	5 13 42	5 13 42	9 8 17	9 8 17	8
10	1 10 55	1 10 55	5 17 47	5 17 47	9 12 22	9 12 22	9
11	1 15 1	1 15 1	5 21 53	5 21 53	9 16 28	9 16 28	10
12	1 19 7	1 19 7	5 25 59	5 25 59	9 20 34	9 20 34	11
13	1 23 12	1 23 12	6 0 4	6 0 4	9 24 39	9 24 39	12
14	1 27 18	1 27 18	6 4 10	6 4 10	9 28 54	9 28 54	13
15	2 1 23	2 1 23	6 8 15	6 8 15	10 2 50	10 2 50	14
16	2 5 29	2 5 29	6 12 21	6 12 21	10 6 56	10 6 56	15
17	2 9 34	2 9 34	6 16 26	6 16 26	10 11 1	10 11 1	16
18	2 13 40	2 13 40	6 20 32	6 20 32	10 15 7	10 15 7	17
19	2 17 45	2 17 45	6 24 37	6 24 37	10 19 12	10 19 12	18
20	2 21 51	2 21 51	6 28 43	6 28 43	10 23 18	10 23 18	19
21	2 25 56	2 25 56	7 2 48	7 2 48	10 27 23	10 27 23	20
22	3 0 2	3 0 2	7 6 54	7 6 54	11 1 29	11 1 29	21
23	3 4 7	3 4 7	7 10 59	7 10 59	11 5 34	11 5 34	22
24	3 8 13	3 8 13	7 15 5	7 15 5	11 9 40	11 9 40	23
25	3 12 19	3 12 19	7 19 11	7 19 11	11 13 46	11 13 46	24
26	3 16 24	3 16 24	7 23 16	7 23 16	11 17 51	11 17 51	25
27	3 20 30	3 20 30	7 27 2	7 27 2	11 21 57	11 21 57	26
28	3 24 35	3 24 35	8 1 27	8 1 27	11 26 2	11 26 2	27
29	3 28 41	3 28 41	8 5 33	8 5 33	0 0 8	0 0 8	28
30	4 2 46	4 2 46	0 0 0	0 0 0	0 4 13	0 4 13	29
31	4 6 52	4 6 52	0 0 0	0 0 0	0 8 19	0 8 19	30

A TABLE of MERCURY's Mean Motion.

Com. Years	A P R I L.		M A Y.		J U N E.		Biflexile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o	S o	S o	S o	S o	S o	
1	0 12 25	0 12 25	4 15 11	4 15 11	8 22 3	8 22 3	0
2	0 16 30	0 16 30	4 19 16	4 19 16	8 26 8	8 26 8	1
3	0 20 36	0 20 36	4 23 22	4 23 22	9 0 14	9 0 14	2
4	0 24 41	0 24 41	4 27 27	4 27 27	9 4 19	9 4 19	3
5	0 28 47	0 28 47	5 1 33	5 1 33	9 8 25	9 8 25	4
6	1 2 52	1 2 52	5 5 38	5 5 38	9 12 30	9 12 30	5
7	1 6 58	1 6 58	5 9 44	5 9 44	9 16 36	9 16 36	6
8	1 11 3	1 11 3	5 13 49	5 13 49	9 20 41	9 20 41	7
9	1 15 9	1 15 9	5 17 55	5 17 55	9 24 47	9 24 47	8
10	1 19 14	1 19 14	5 22 0	5 22 0	9 28 52	9 28 52	9
11	1 23 20	1 23 20	5 26 6	5 26 6	10 2 58	10 2 58	10
12	1 27 26	1 27 26	6 0 12	6 0 12	10 7 4	10 4 4	11
13	2 1 31	2 1 31	6 4 17	6 4 17	10 11 9	10 11 9	12
14	2 5 37	2 5 37	6 8 23	6 8 23	10 15 15	10 15 15	13
15	2 9 42	2 9 42	6 12 28	6 12 28	10 19 20	10 19 20	14
16	2 13 48	2 13 48	6 16 4	6 16 4	10 23 26	10 23 26	15
17	2 17 53	2 17 53	6 20 39	6 20 39	10 27 31	10 27 30	16
18	2 21 59	2 21 59	6 24 45	6 24 45	11 1 37	11 1 36	17
19	2 26 4	2 26 4	6 28 50	6 28 50	11 5 42	11 5 41	18
20	3 0 10	3 0 10	7 2 56	7 2 56	11 9 48	11 9 47	19
21	3 4 15	3 4 15	7 7 1	7 7 1	11 13 53	11 13 52	20
22	3 8 21	3 8 21	7 11 7	7 11 7	11 17 59	11 17 58	21
23	3 12 26	3 12 26	7 15 12	7 15 12	11 22 4	11 22 3	22
24	3 16 32	3 16 32	7 19 18	7 19 18	11 26 10	11 26 9	23
25	3 20 38	3 20 38	7 23 24	7 23 24	0 0 16	0 0 15	24
26	3 24 43	3 24 43	7 27 29	7 27 29	0 4 21	0 4 20	25
27	3 28 49	3 28 49	8 1 35	8 1 35	0 8 27	0 8 26	26
28	4 2 54	4 2 54	8 5 40	8 5 40	0 12 32	0 12 31	27
29	4 7 0	4 7 0	8 9 45	8 9 45	0 16 38	0 16 37	28
30	4 11 5	4 11 5	8 13 51	8 13 51	0 20 42	0 20 42	29
31	4 15 11	4 15 11	8 17 57	8 17 57	0 24 49	0 24 48	30

In former page, Read Jan. and Feb. Long. Anom. Long. Anom.

A TABLE of MERCURY'S Mean Motion.

Com. Years	JULY.		AUGUST.		SEPTEMB.		Biflexile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S ° ' "	S ° ' "	S ° ' "	S ° ' "	S ° ' "	S ° ' "	
1	0 24 49	0 24 48	5 1 41	5 1 40	9 8 33	9 8 32	0
2	0 28 54	0 28 53	5 5 46	5 5 45	9 12 38	9 12 37	1
3	1 3 0	1 2 59	5 9 52	5 9 51	9 16 44	9 16 43	2
4	1 7 5	1 7 4	5 13 57	5 13 56	9 20 49	9 20 48	3
5	1 11 11	1 11 10	5 18 3	5 18 2	9 24 55	9 24 54	4
6	1 15 16	1 15 15	5 22 8	5 22 7	9 29 0	9 28 59	5
7	1 19 22	1 19 21	5 26 14	5 26 13	10 3 6	10 3 5	6
8	1 23 27	1 23 26	6 0 19	6 0 18	10 7 11	10 7 10	7
9	1 27 33	1 27 32	6 4 25	6 4 24	10 11 17	10 11 16	8
10	2 1 38	2 1 37	6 8 30	6 8 29	10 15 22	10 15 21	9
11	2 5 44	2 5 43	6 12 36	6 12 35	10 19 28	10 19 27	10
12	2 9 50	2 9 49	6 16 42	6 16 41	10 23 34	10 23 33	11
13	2 13 55	2 13 54	6 20 47	6 20 46	10 27 39	10 27 38	12
14	2 18 1	2 18 0	6 24 53	6 24 52	11 1 45	10 1 44	13
15	2 22 6	2 22 5	6 28 58	6 28 57	11 5 50	10 5 49	14
16	2 26 12	2 26 11	7 7 4	7 7 3	11 9 56	11 9 55	15
17	3 0 17	3 0 16	7 3 9	7 3 8	11 14 1	11 14 0	16
18	3 4 23	3 4 22	7 11 15	7 11 14	11 18 7	11 18 6	17
19	3 8 28	3 8 27	7 15 19	7 15 20	11 22 12	11 22 11	18
20	3 12 34	3 12 33	7 19 25	7 19 26	11 26 18	11 26 17	19
21	3 16 37	3 16 36	7 23 30	7 23 31	0 0 23	0 0 22	20
22	3 20 45	3 20 44	7 27 37	7 27 36	0 4 29	0 4 28	21
23	3 24 50	3 24 49	8 1 42	8 1 41	0 8 34	0 8 33	22
24	3 28 56	3 28 55	8 5 48	8 5 47	0 12 40	0 12 39	23
25	4 3 2	4 3 1	8 9 54	8 9 53	0 16 46	0 16 45	24
26	4 7 7	4 7 6	8 13 59	8 13 58	0 20 51	0 20 50	25
27	4 11 13	4 11 12	8 17 5	8 17 4	0 24 57	0 24 56	26
28	4 15 18	4 15 17	8 22 10	8 22 9	0 29 2	0 29 1	27
29	4 19 24	4 19 23	8 26 16	8 26 15	1 3 8	1 3 7	28
30	4 23 29	4 23 28	9 0 21	9 0 20	1 7 13	1 7 12	29
31	4 27 35	4 27 34	9 4 27	9 4 26	1 11 19	1 11 18	30

A TABLE of MERCURY'S Mean Motion.

Com. Years	OCTOBER.		NOVEMB.		DECEMB.		Bissextile.
	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	Longit. ♀	Anom. ♀	
	S o	S o	S o	S o	S o	S o	
1	1 11 19	1 11 18	5 18 11	5 18 10	9 20 57	9 20 56	10
2	1 15 24	1 15 23	5 22 16	5 22 15	9 25 2	9 25 1	11
3	1 19 30	1 19 29	5 26 22	5 26 21	9 29 8	9 29 7	12
4	1 23 35	1 23 34	6 0 27	6 0 26	10 3 13	10 3 12	13
5	1 27 41	1 27 40	6 4 33	6 4 32	10 7 19	10 7 18	14
6	2 1 46	2 1 45	6 8 38	6 8 37	10 10 24	10 10 23	15
7	2 5 52	2 5 51	6 12 44	6 12 43	10 15 30	10 15 29	16
8	2 9 57	2 9 56	6 16 49	6 16 48	10 19 35	10 19 34	17
9	2 14 3	2 14 2	6 20 55	6 20 54	10 23 41	10 23 40	18
10	2 18 8	2 18 7	6 25 0	6 25 7	10 27 46	10 27 45	19
11	2 22 14	2 22 13	6 29 6	6 29 5	11 1 52	11 1 50	20
12	2 26 20	2 26 19	7 3 12	7 3 11	11 5 58	11 5 56	21
13	3 0 25	3 0 24	7 7 17	7 7 16	11 10 3	11 10 1	22
14	3 4 31	3 4 30	7 11 23	7 11 22	11 14 9	11 14 7	23
15	3 8 36	3 8 35	7 15 28	7 15 27	11 18 14	11 18 12	24
16	3 12 42	3 12 41	7 19 34	7 19 33	11 22 20	11 22 18	25
17	3 16 47	3 16 46	7 23 39	7 23 38	11 26 25	11 26 23	26
18	3 20 53	3 20 52	7 27 45	7 27 44	0 0 31	0 0 29	27
19	3 24 58	3 24 57	8 1 50	8 1 49	0 4 36	0 4 34	28
20	3 29 4	3 29 3	8 5 56	8 5 55	0 8 42	0 8 40	29
21	4 3 9	4 3 8	8 10 1	8 10 0	0 12 47	0 12 45	30
22	4 7 15	4 7 14	8 14 7	8 14 6	0 16 53	0 16 51	31
23	4 11 20	4 11 19	8 18 12	8 18 11	0 20 58	0 20 56	32
24	4 15 26	4 15 25	8 22 18	8 22 17	0 25 4	0 25 2	33
25	4 19 32	4 19 31	8 26 24	8 26 23	0 29 10	0 29 8	34
26	4 23 37	4 23 36	9 0 29	9 0 28	1 3 15	1 3 13	35
27	4 27 43	4 27 42	9 4 35	9 4 34	1 7 21	1 7 19	36
28	5 1 48	5 1 47	9 8 40	9 8 39	1 11 26	1 11 24	37
29	5 5 54	5 5 53	9 12 45	9 12 44	1 15 32	1 15 30	38
30	5 9 59	5 9 58	9 16 51	9 16 50	1 19 37	1 19 35	39
31	5 14 5	5 14 4	9 20 57	9 20 56	1 23 43	1 23 41	40

A TABLE of MERCURY'S Mean Motion,
in Hours, Minutes, and Seconds.

H.	Longit. ♀	Anom. ♀		Longit. ♀	Anom. ♀
	° ' "	° ' "		° ' "	° ' "
1	0 10 14	0 10 14	31	5 17 9	5 17 9
2	0 20 28	0 20 28	32	5 27 22	5 27 22
3	0 30 42	0 30 42	33	5 37 56	5 37 36
4	0 40 56	0 40 56	34	5 47 50	5 47 50
5	0 51 9	0 51 9	35	5 58 4	5 58 4
6	1 1 23	1 1 23	36	6 8 18	6 8 18
7	1 11 37	1 11 37	37	6 18 32	6 18 32
8	1 21 51	1 21 51	38	6 28 46	6 28 46
9	1 31 5	1 31 5	39	6 39 0	6 39 0
10	1 42 19	1 42 19	40	6 49 14	6 49 14
11	1 52 32	1 52 32	41	6 59 28	6 59 20
12	2 2 46	2 2 46	42	7 9 42	7 9 42
13	2 13 0	2 13 0	43	7 19 56	7 19 56
14	2 23 14	2 23 14	44	7 30 8	7 30 8
15	2 33 28	2 33 28	45	7 40 22	7 40 22
16	2 43 41	2 43 41	46	7 50 36	7 50 36
17	2 55 55	2 55 55	47	8 0 50	8 0 50
18	3 4 9	3 4 9	48	8 11 4	8 11 4
19	3 14 23	3 14 23	49	8 21 18	8 21 18
20	3 24 37	3 24 37	50	8 31 32	8 31 32
21	3 34 51	3 34 51	51	8 41 46	8 41 46
22	3 45 4	3 45 4	52	8 52 0	8 52 0
23	3 55 18	3 55 18	53	9 2 14	9 2 14
24	4 5 32	4 5 32	54	9 12 28	9 12 28
25	4 15 46	4 15 46	55	9 22 44	9 22 44
26	4 26 0	4 26 0	56	9 32 56	9 32 56
27	4 36 14	4 36 14	57	9 43 10	9 43 10
28	4 46 28	4 46 28	58	9 53 24	9 53 24
29	4 56 42	4 56 42	59	10 3 38	10 3 38
30	5 6 56	5 6 56	60	10 13 52	10 13 52
"	" iv v	" iv v	"	" iv v	" iv v

A TABLE of MERCURY'S Equation.

Degrees.	Sig. 0.			Logar. Diff. Δ Curt.	Sig. 1.			Logar. Diff. Δ Curt.	Sig. 2.			Logar. Diff. Δ Curt.	Degrees.
	Equa. Sub.				Equa. Sub.				Equa. Sub.				
	0	1	2		0	1	2		0	1	2		
0	0	0	0	466948	9	42	58	466144	17	57	28	463896	30
1	0	19	34	466943	10	1	22	466093	18	11	22	463795	29
2	0	39	48	466937	10	19	40	466041	18	25	3	463694	28
3	0	59	42	466929	10	37	52	465987	18	38	31	463591	27
4	1	19	36	466921	10	55	57	465930	18	52	47	463485	26
5	1	39	29	466911	11	13	56	465872	19	4	50	463378	25
6	1	59	19	466900	11	31	49	465812	19	41	70	463270	24
7	2	19	11	466886	11	49	34	465750	19	30	15	463159	23
8	2	39	1	466871	12	7	12	465687	19	42	36	463048	22
9	2	58	50	466855	12	24	42	465623	19	54	43	462935	21
10	3	18	38	466836	12	42	5	465557	20	6	35	462819	20
11	3	38	54	466816	12	59	20	465490	20	18	12	462703	19
12	3	57	36	466793	13	16	26	465422	20	29	35	462585	18
13	4	17	48	466771	13	33	24	465350	20	40	41	462495	17
14	4	37	25	466747	13	50	14	465277	20	51	36	462345	16
15	4	56	59	466722	14	6	56	465204	21	2	14	462223	15
16	5	16	28	466694	14	23	29	465128	21	12	35	462098	14
17	5	25	59	466665	14	39	52	465051	21	22	39	461972	13
18	5	55	25	466625	14	56	8	464972	21	32	28	461844	12
19	6	14	47	466602	15	12	1	464891	21	42	0	461713	11
20	6	34	5	466569	15	28	5	464809	21	51	14	461582	10
21	6	53	19	466534	15	43	50	464725	22	0	12	461450	9
22	7	12	28	466497	15	59	24	464639	22	9	5	461316	8
23	7	31	33	466459	16	14	47	464552	22	17	12	461179	7
24	7	50	34	466419	16	30	1	464464	22	25	15	461042	6
25	8	9	31	466377	16	45	5	464373	22	32	59	460903	5
26	8	28	23	466334	16	59	55	464281	22	40	24	460764	4
27	8	47	10	466289	17	14	35	464187	22	47	30	460623	3
28	9	5	52	466241	17	29	4	463091	22	54	16	460480	2
29	9	24	28	466193	17	43	22	463994	23	0	42	460338	1
30	9	42	58	466144	17	57	28	463896	23	6	48	460191	0
	Add.				Add.				Add.				
	Sig. 11.				Sig. 10.				Sig. 9.				

A TABLE of MERCURY'S Equation.

Degrees.	Sig. 3.			Sig. 4.			Sig. 5.			Degrees.
	Equa. Sub.			Equa. Sub.			Equa. Sub. / Logar.			
	Logar.			Logar.			Logar.			
	o	p	t	o	"	"	o	p	t	
0	23	6	48	23	6	45	15	16	44	30
1	23	12	33	22	59	27	14	52	3	29
2	23	17	59	22	51	35	14	26	49	28
3	23	23	5	22	43	11	14	1	4	27
4	23	27	49	22	34	14	13	32	49	26
5	23	32	12	22	24	44	13	7	59	25
6	23	36	14	22	14	0	12	40	43	24
7	23	39	54	22	4	1	12	12	57	23
8	23	43	11	21	52	47	11	44	43	22
9	23	46	5	21	39	58	11	16	4	21
10	23	48	36	21	27	49	10	46	55	20
11	23	50	44	21	15	41	10	17	26	19
12	23	52	29	21	2	10	9	47	23	18
13	23	53	50	20	48	1	9	17	1	17
14	23	54	47	20	33	15	8	46	19	16
15	23	55	19	20	17	56	8	15	14	15
16	23	55	23	20	2	1	7	43	47	14
17	23	55	2	19	45	27	7	12	1	13
18	23	54	13	19	28	20	6	39	58	12
19	23	52	54	19	10	36	6	7	38	11
20	23	51	13	18	52	17	5	35	3	10
21	23	49	0	18	33	21	5	2	14	9
22	23	46	19	18	13	50	4	29	11	8
23	23	43	51	17	53	44	3	55	50	7
24	23	39	29	17	33	2	3	22	31	6
25	23	35	19	17	11	45	2	48	58	5
26	23	30	38	16	49	52	2	15	21	4
27	23	24	26	16	27	29	1	41	37	3
28	23	19	44	16	4	28	1	7	48	2
29	23	13	30	15	40	54	0	33	55	1
30	23	6	45	15	16	44	0	0	0	0
	Add.			Add.			Add.			
	Sig. 8.			Sig. 7.			Sig. 6.			

A TABLE of MERCURY'S Inclination from the Plan of the Ecliptic, with the Proportional Scruples of Latitude.

Argument of Latitude.

Degrees.	Sig. 0. North Asc. Sig. 6. South Asc.		Sig. 1. North Asc. Sig. 7. South Asc.		Sig. 2. North Asc. Sig. 8. South Asc.		Degrees.
	Inclinat.	P. Scr.	Inclinat.	P. Scr.	Inclinat.	P. Scr.	
0	0 0 0	0 0	3 27 0	30 0	5 58 32	51 57	30
1	0 7 13	1 3	3 33 13	30 54	6 2 6	52 28	29
2	0 14 27	2 5	3 39 22	31 48	6 5 33	52 58	28
3	0 21 40	3 8	3 45 28	32 41	6 8 53	53 27	27
4	0 28 53	4 11	3 51 30	33 33	6 12 6	53 56	26
5	0 36 5	5 14	3 57 28	34 25	6 15 13	54 23	25
6	0 43 16	6 17	4 3 21	35 16	6 18 13	54 49	24
7	0 59 26	7 19	4 9 9	36 6	6 21 6	55 14	23
8	0 57 36	8 21	4 14 59	36 56	6 23 51	55 38	22
9	1 4 45	9 23	4 20 32	37 45	6 26 29	56 1	21
10	1 11 53	10 25	4 26 6	38 34	6 29 0	56 23	20
11	1 18 59	11 27	4 31 36	39 22	6 31 24	56 44	19
12	1 26 4	12 29	4 37 0	40 9	6 33 42	57 4	18
13	1 33 7	13 30	4 42 20	40 55	6 35 53	57 23	17
14	1 40 8	14 31	4 47 35	41 40	6 37 57	57 40	16
15	1 47 8	15 32	4 52 45	42 26	6 39 53	57 57	15
16	1 54 6	16 31	4 57 49	43 10	6 41 42	58 13	14
17	2 1 2	17 32	5 2 19	43 53	6 43 26	58 28	13
18	2 7 56	18 32	5 7 41	44 35	6 44 57	58 42	12
19	2 14 47	19 32	5 12 28	45 16	6 46 24	58 54	11
20	2 21 35	20 31	5 17 9	45 57	6 47 43	59 5	10
21	2 28 21	21 30	5 21 44	46 37	6 48 54	59 16	9
22	2 35 5	22 29	5 26 14	47 16	6 49 58	59 25	8
23	2 41 46	23 27	5 30 37	47 54	6 50 55	59 33	7
24	2 48 24	24 24	5 34 55	48 32	6 51 44	59 40	6
25	2 54 58	25 21	5 39 7	49 0	6 52 25	59 46	5
26	3 1 29	26 18	5 43 13	49 44	6 52 59	59 52	4
27	3 7 57	27 14	5 47 13	50 18	6 53 26	59 56	3
28	3 14 22	28 10	5 51 6	50 52	6 53 45	59 58	2
29	3 20 42	29 5	5 54 52	51 25	6 53 56	59 59	1
30	3 27 0	30 0	5 58 32	51 57	6 54 0	60 0	0
	Sig. 11. South Desc. Sig. 5. North Desc.		Sig. 10. South Desc. Sig. 4. North Desc.		Sig. 9. South Desc. Sig. 3. North Desc.		

Argument of Latitude.

A TABLE of the Refraction of the SUN, MOON, and STARS, with the Parallax of the SUN.

Dist. a Vert.	Refra.	Par. ☉	Dist. a Vert.	Refra.	Par. ☉	Dist. a Vert.	Refra.	Par. ☉
gr.	' "	' "	gr.	' "	' "	gr.	' "	' "
0	0 0	0 0	30	0 29	0 14	60	1 24	0 26
1	0 1	0 1	31	0 30	0 15	61	1 27	0 26
2	0 2	0 1	32	0 31	0 15	62	1 31	0 26
3	0 2	0 2	33	0 32	0 16	63	1 36	0 27
4	0 3	0 2	34	0 33	0 16	64	1 40	0 27
5	0 4	0 3	35	0 34	0 17	65	1 45	0 27
6	0 5	0 3	36	0 35	0 17	66	1 50	0 27
7	0 6	0 4	37	0 36	0 18	67	1 55	0 28
8	0 6	0 4	38	0 37	0 18	68	2 1	0 28
9	0 7	0 5	39	0 39	0 19	69	2 7	0 28
10	0 8	0 5	40	0 41	0 19	70	2 14	0 28
11	0 9	0 6	41	0 42	0 20	71	2 22	0 28
12	0 10	0 6	42	0 44	0 20	72	2 31	0 28
13	0 11	0 7	43	0 46	0 21	73	2 40	0 28
14	0 12	0 7	44	0 47	0 21	74	2 50	0 29
15	0 13	0 8	45	0 49	0 21	75	3 3	0 29
16	0 14	0 8	46	0 51	0 22	76	3 16	0 29
17	0 15	0 9	47	0 53	0 22	77	3 32	0 29
18	0 16	0 9	48	0 55	0 22	78	3 48	0 29
19	0 17	0 10	49	0 57	0 23	79	4 9	0 29
20	0 18	0 10	50	0 59	0 23	80	4 35	0 29
21	0 19	0 10	51	1 0	0 23	81	5 5	0 29
22	0 20	0 11	52	1 2	0 24	82	5 42	0 30
23	0 21	0 11	53	1 5	0 24	83	6 30	0 30
24	0 22	0 12	54	1 8	0 24	84	7 32	0 30
25	0 23	0 12	55	1 10	0 25	85	8 55	0 30
26	0 24	0 13	56	1 12	0 25	86	10 53	0 30
27	0 26	0 13	57	1 15	0 25	87	13 55	0 30
28	0 27	0 14	58	1 18	0 26	88	18 24	0 30
29	0 28	0 14	59	1 21	0 26	89	25 12	0 30
30	0 29	0 14	60	1 24	0 26	90	30 0	0 30

A TABLE of the Declination of the Ecliptic, and Meridian Angles

Degrees.	Declinat.			M. An.		Declinat.	Declinat.			M. An.		Declinat.	Declinat.			M. An.		Degrees.
	°	'	"	°	'		°	'	"	°	'		°	'	"	°	'	
0	0	0	0	66	29	11	29	57	69	20	20	11	52	77	42	30		30
1	0	23	54	66	29	11	51	1	69	31	20	24	25	78	4	29		29
2	0	47	50	66	30	12	11	52	69	43	20	36	36	78	26	28		28
3	1	11	44	66	31	12	32	31	69	55	20	48	23	78	48	27		27
4	1	35	37	66	31	12	52	58	70	8	20	59	49	79	11	26		26
5	1	59	29	66	31	13	13	12	70	21	21	10	51	79	34	25		25
6	2	23	20	66	35	13	33	13	70	35	21	21	28	79	57	24		24
7	2	47	5	66	38	13	53	1	70	49	21	31	41	80	20	23		23
8	3	10	52	66	41	14	12	35	71	3	21	41	33	80	43	22		22
9	3	34	33	66	44	14	31	54	71	18	21	50	58	81	7	21		21
10	3	58	13	66	47	14	50	59	71	13	22	0	0	81	31	20		20
11	4	21	47	66	51	15	9	48	71	48	22	8	35	81	55	19		19
12	4	45	19	66	55	15	28	23	72	4	22	16	47	82	19	18		18
13	5	8	45	67	0	15	46	42	72	20	22	24	32	82	44	17		17
14	5	32	8	67	5	16	4	45	72	36	22	31	53	83	9	16		16
15	5	55	24	67	11	16	22	31	72	53	22	38	46	83	34	15		15
16	6	18	34	67	17	16	40	10	73	10	22	45	16	83	59	14		14
17	6	41	40	67	24	16	57	11	73	27	22	51	17	84	24	13		13
18	7	4	39	67	31	17	14	6	73	45	22	56	54	84	50	12		12
19	7	27	31	67	38	17	30	40	74	3	23	2	4	85	15	11		11
20	7	50	16	67	45	17	46	59	74	21	23	6	47	85	41	10		10
21	8	12	54	67	53	18	2	57	74	40	23	11	3	85	6	9		9
22	8	35	25	68	1	18	18	39	74	59	23	14	53	85	32	8		8
23	8	57	45	68	9	18	33	58	75	18	23	18	15	85	58	7		7
24	9	19	58	68	18	18	49	0	75	38	23	21	12	87	24	6		6
25	9	42	3	68	28	19	3	41	75	58	23	23	40	87	50	5		5
26	10	3	59	68	38	19	18	2	76	18	23	25	42	88	16	4		4
27	10	25	43	68	48	19	32	1	76	39	23	27	16	88	42	3		3
28	10	47	20	68	58	19	45	40	77	0	23	28	23	89	8	2		2
29	11	8	43	69	9	19	58	57	77	21	23	29	3	89	34	1		1
30	11	29	57	69	20	20	11	52	77	42	23	29	15	90	0	0		0
	♈			♎		♊			♏		♍			♐				

A TABLE of Right Ascensions.

Index.	γ	δ	Π	ζ	Ω	μ
	o	o	o	o	o	o
0	0 0	27 54	57 48	90 0	122 12	152 6
1	0 55	28 51	58 51	91 5	123 14	153 4
2	1 50	29 49	59 53	92 11	124 16	154 1
3	2 45	30 46	60 56	93 16	125 19	154 58
4	3 40	31 44	61 59	94 22	126 20	155 55
5	4 35	32 42	63 3	95 27	127 22	156 51
6	5 30	33 40	64 6	96 32	128 24	157 48
7	6 25	34 38	65 9	97 38	129 25	158 44
8	7 21	35 37	66 13	98 43	130 26	159 40
9	8 16	36 36	67 17	99 48	131 27	160 37
10	9 11	37 34	68 21	100 53	132 28	161 33
11	10 6	38 33	69 25	101 58	133 28	162 29
12	11 2	39 33	70 29	103 3	134 29	163 25
13	11 57	40 32	71 34	104 8	135 29	164 20
14	12 53	41 31	72 38	105 13	136 29	165 16
15	13 48	42 31	73 43	106 17	137 29	166 12
16	14 44	43 31	74 47	107 22	138 28	167 7
17	15 40	44 31	75 52	108 26	139 28	168 3
18	16 35	45 31	76 57	109 31	140 27	168 58
19	17 31	46 32	78 2	110 35	141 27	169 54
20	18 27	47 32	79 7	111 39	142 26	170 49
21	19 23	48 33	80 12	112 43	143 24	171 44
22	20 20	49 34	81 17	113 47	144 23	172 39
23	21 16	50 35	82 22	114 51	145 22	173 35
24	22 12	51 36	83 28	115 54	146 20	174 30
25	23 9	52 38	84 33	116 57	147 18	175 25
26	24 6	53 40	85 38	118 1	148 16	176 20
27	25 2	54 42	86 44	119 4	149 14	177 15
28	25 59	55 44	87 49	120 7	150 11	178 10
29	26 57	56 46	88 55	121 9	151 9	179 5
30	27 54	57 48	90 0	122 12	152 6	180 0

A TABLE of Right Ascensions.

Index.	♈	♉	♊	♋	♌	♍
	0	0	0	0	0	0
0	180 0	207 54	237 48	270 0	302 12	332 6
1	180 55	208 51	238 51	271 5	303 14	333 4
2	181 50	209 49	239 53	272 11	304 16	334 1
3	182 45	210 46	240 56	273 16	305 19	334 58
4	183 40	211 44	241 59	274 22	306 20	335 55
5	184 35	212 42	243 3	275 27	307 22	336 51
6	185 30	213 40	244 6	276 32	308 24	337 48
7	186 25	214 48	245 9	277 38	309 25	338 44
8	187 27	215 37	246 13	278 43	310 26	339 40
9	188 16	216 36	247 17	279 48	311 27	340 37
10	189 11	217 34	248 21	280 53	312 28	341 33
11	190 6	218 33	249 25	281 58	313 28	342 29
12	191 2	219 33	250 29	283 3	314 29	343 25
13	191 57	220 32	251 34	284 8	315 29	344 20
14	192 53	221 31	252 38	285 13	316 29	345 16
15	193 48	222 31	253 43	286 17	317 29	346 12
16	194 44	223 31	254 47	287 22	318 29	347 7
17	195 40	224 31	255 52	288 26	319 28	348 3
18	196 35	225 31	256 57	289 31	320 28	348 58
19	197 31	226 32	258 2	290 35	321 27	349 54
20	198 27	227 32	259 7	291 39	322 26	350 49
21	199 23	228 33	260 12	292 43	323 24	351 44
22	200 20	229 34	261 17	293 47	324 23	352 39
23	201 16	330 35	262 22	294 51	325 22	353 35
24	202 12	231 36	263 28	295 54	326 20	354 30
25	203 9	232 38	264 33	296 57	327 18	355 25
26	204 6	233 40	265 38	298 1	328 16	356 20
27	205 2	234 41	266 44	299 4	329 14	357 15
28	205 59	235 43	267 49	300 7	330 11	358 10
29	206 57	236 46	268 50	301 9	331 9	359 5
30	207 54	237 48	270 0	302 12	332 6	360 0

A TABLE converting Hours and Min. into Degrees and Minutes of the Equator, and the contrary.

D.	Time.	D.	Time.	D.	Time.
°	H ' "	°	H ' "	°	H ' "
"	" "	"	" "	"	" "
1	0 4	31	2 4	70	4 40
2	0 8	32	2 8	80	5 20
3	0 12	33	2 12	90	6 0
4	0 16	34	2 16	100	6 40
5	0 20	35	2 20	110	7 20
6	0 24	36	2 24	120	8 0
7	0 28	37	2 28	130	8 40
8	0 32	38	2 32	140	9 20
9	0 36	39	2 36	150	10 0
10	0 40	40	2 40	160	10 40
11	0 44	41	2 44	170	11 20
12	0 48	42	2 48	180	12 0
13	0 52	43	2 52	190	12 40
14	0 56	44	2 56	200	13 20
15	1 0	45	3 0	210	14 0
16	1 4	46	3 4	220	14 40
17	1 8	47	3 8	230	15 20
18	1 12	48	3 12	240	16 0
19	1 16	49	3 16	250	16 40
20	1 20	50	3 20	260	17 20
21	1 24	51	3 24	270	18 0
22	1 28	52	3 28	280	18 40
23	1 32	53	3 32	290	19 20
24	1 36	54	3 36	300	20 0
25	1 40	55	3 40	301	20 40
26	1 44	56	3 44	302	21 20
27	1 48	57	3 48	303	22 0
28	1 52	58	3 52	304	22 40
29	1 56	59	3 56	305	23 20
30	2 0	60	4 0	306	24 0

A TABLE of the Equation of Natural Days.

Degrees.	γ		δ		Π		Degrees.
	Add.		Add.		Add.		
	'	"	'	"	'	"	
0	0	0	8	25	8	47	30
1	0	20	8	36	8	37	29
2	0	40	8	45	8	26	28
3	0	59	8	55	8	15	27
4	1	19	9	4	8	3	26
5	1	39	9	12	7	50	25
6	1	59	9	19	7	36	24
7	2	18	9	26	7	22	23
8	2	38	9	32	7	7	22
9	2	57	9	37	6	52	21
10	3	16	9	42	6	36	20
11	3	35	9	46	6	20	19
12	3	51	9	50	6	3	18
13	4	12	9	52	5	46	17
14	4	30	9	54	5	28	16
15	4	47	9	56	5	10	15
16	5	5	9	56	4	51	14
17	5	22	9	56	4	32	13
18	5	38	9	55	4	12	12
19	5	55	9	53	3	53	11
20	6	11	9	51	3	33	10
21	6	26	9	48	3	12	9
22	6	41	9	44	2	51	8
23	6	56	9	40	2	31	7
24	7	10	9	34	2	9	6
25	7	24	9	28	1	48	5
26	7	37	9	21	1	27	4
27	7	50	9	14	1	5	3
28	8	2	9	6	0	43	2
29	8	14	8	57	0	22	1
30	8	25	8	47	0	0	0
	Substr.		Substr.		Substr.		
	κ	η	π	Ω	ν	ξ	

A CATALOGUE of several Fixed Stars of Note, according to the Observations of *Tycho Brahe*, and by him Rectified to the beginning of the Year, 1601.

<i>Names of the Stars.</i>	Longitude S. gr. ' "			Latitude gr. ' "			Mag.
SO. * R. Horn <i>Aries</i> call'd the 1st.	γ	27	37	7	8	N	4
North following in same Horn.	γ	28	23	8	29	N	4
Bright * in the Head of <i>Aries</i> .	δ	2	6	9	57	N	3
Southern Jaw of <i>Aries</i> .	δ	3	20	5	42	N	6
First of 3 in the tail of <i>Aries</i> .	δ	15	15	1	46	N	4
Middle and Brightest of the <i>Pleiades</i> .	δ	24	24	4	0	N	3
Nostril of <i>Taurus</i> .	π	0	12	5	46	S	3
North eye of <i>Taurus</i> .	π	2	53	2	36	S	3
South eye of <i>Taurus</i> <i>Aldebaran</i> .	π	4	12	5	31	S	1
End N. Horn δ or foot of <i>Auriga</i> .	π	16	59	5	20	N	2
<i>Propus</i> foremost in the foot of <i>Gemini</i> .	π	25	22	0	13	S	4
Hindmost Heel Higher Foot <i>Gemini</i> .	π	29	44	0	53	S	3
Bright Foot of <i>Gemini</i> .	σ	3	31	6	48	S	2
Head of <i>Hercules</i> <i>Pollux</i> .	σ	13	43	6	38	N	2
North <i>Affellus</i> .	Ω	1	57	3	8	N	4
South <i>Affellus</i> .	Ω	3	8	0	4	N	4
Heart of <i>Leo</i> .	Ω	24	17	0	26	N	1
Second in the left Wing of <i>Virgo</i> .	π	4	35	2	50	N	3
<i>Spica Virginis</i> <i>Arista</i> .	π	18	16	1	59	S	1
South Ballance.	μ	9	31	0	26	N	2
Higher * in the Forehead of <i>Scorpio</i> .	μ	27	36	1	5	N	2
Heart of <i>Scorpio</i> <i>Antares</i> .	τ	4	13	4	27	S	1
Southmost N. part Bow of <i>Sagittary</i> .	υ	0	47	2	0	S	3
Southern Horn of the Goat <i>Australis</i> .	υ	28	31	4	41	N	3
Bright * Doubling tail of <i>Capricorn</i> .	♊	16	14	2	26	S	3
Following * on the Goat's Back.	♊	18	0	2	29	S	3
So. of 2 in hinder part of the Head.	κ	15	50	7	17	N	4
In the Tail of <i>Pisces</i> .	κ	27	2	6	23	N	5
Head of <i>Andromeda</i> .	ν	8	47	25	42	N	2
Girdle of <i>Andromeda</i> .	γ	24	49	25	59	N	2
In following N. Horn of <i>Aries</i> .	γ	28	23	8	29	N	4
Bright * in the Chair <i>Cassiopeia</i> .	γ	29	35	51	14	N	3
Brest of <i>Cassiopeia</i> — <i>Schedir</i> .	δ	2	17	46	35	N	3
Left or South foot of the <i>Whale</i> .	δ	8	39	27	46	N	2
Bright * in the Jaw of the <i>Whale</i> .	δ	8	47	12	37	S	2
Left knee of <i>Cassiopeia</i> .	δ	12	20	46	22	N	3
Head of <i>Algol</i> .	δ	20	37	22	22	N	3
Bright * Right side of <i>Perseus</i> .	δ	27	17	30	5	N	2
Left foot of <i>Orion</i> — <i>Rigel</i> .	π	11	17	31	11	S	1
Paunch or Belly of the <i>Hare</i> .	π	14	6	43	57	S	3
First * in the Belt of <i>Orion</i> .	π	17	50	23	38	S	2
Middlemost * in <i>Orion's</i> belt.	π	17	54	24	33	S	2
Hindmost * in <i>Orion's</i> belt.	π	19	6	25	21	S	2
Pole Star.	π	23	2	66	2	N	2
Right shoulder of <i>Orion</i> .	π	23	12	16	6	S	2

A CATALOGUE of Stars, &c.

Names of the Stars.	Longitude		Latitude		Mag.
	S.	gr.	gr.		
Right shoulder of <i>Auriga</i> .	II	25 52	21 27 N		2
Great Dog <i>Sirius</i> .	S	8 35	39 30 S		1
Higher head of <i>Gemini</i> <i>Castor Apollo</i> .	S	14 41	10 2 N		2
Lesser Dog <i>Procyon</i> .	S	20 18	15 57 S		2
Breast of the Crab <i>Precepe</i> .	Ω	1 46	1 14 N	Neb.	
Shoulder of great Bear 4th Wheel.	Ω	9 34	49 40 N		2
Flank of the Bear 3d Wheel.	Ω	13 43	45 3 N		2
Heart of <i>Hydra</i> .	Ω	21 45	22 24 S		1
Northmost * in <i>Leo's</i> Neck.	Ω	21 57	11 50 N		3
Midmost * in <i>Leo's</i> Neck.	Ω	23 59	8 47 N		2
Left Thigh of the Bear 1st Wheel.	Ω	25 25	51 37 N		2
Brightest * in <i>Leo's</i> Back.	☾	5 41	14 20 N		2
Middle * Tail of <i>Helice</i> 2d Horse.	☾	9 56	56 22 N		2
Tail of <i>Leo</i> .	☾	16 3	12 18 N		1
First Horse of the Chariot Bear's tail.	☾	21 12	54 25 N		2
Right Wing of <i>Virgo</i> <i>Vindemiatrix</i> .	♏	4 23	16 15 N		3
Left Shoulder of <i>Bootes</i> .	♏	13 5	49 33 N		3
<i>Arcturus</i> in the Constellation <i>Bootes</i> .	♏	18 39	31 2 N		1
Bright * of the Crown <i>Lucida Corona</i> .	♐	6 38	44 23 N		2
Bright * of the North Ballance.	♐	13 48	8 35 N		2
Bright * middle of the Serpent's neck.	♐	16 30	25 35 N		2
Right Shoulder of <i>Hercules</i> .	♐	25 27	42 48 N		3
Left Hand of <i>Ophincus</i> .	♐	26 44	17 19 N		3
Knee of <i>Ophincus</i> .	♐	3 39	11 30 N		3
Left Shoulder of <i>Hercules</i> .	♐	9 10	47 47 N		3
Head of <i>Hercules</i> .	♐	10 31	37 23 N		3
Head of the Serpent of <i>Ophincus</i> .	♐	16 50	35 57 N		3
Right Shoulder of <i>Ophincus</i> .	♐	19 45	28 1 N		3
Head of the Dragon.	♐	22 24	75 3 N		3
Shining Harp.	♐	9 43	61 47 N		1
Tail of the Vulture.	♐	14 15	36 16 N		3
Mouth of the Swan.	♐	25 44	49 2 N		3
Eagle or flying Vulture.	♐	26 9	29 21 N		2
North Horn of the Goat.	♐	28 18	7 2 N		3
Pinion Right Wing of the Swan.	♐	10 53	64 28 N		3
Left Shoulder of <i>Aquarius</i> .	♐	17 51	8 42 N		3
Breast of the Swan.	♐	19 25	57 9 N		3
Lower Wing of the Swan.	♐	22 9	49 26 N		3
Mouth of <i>Pegasus</i> .	♐	26 22	22 27 N		3
In the Mouth of the Fish <i>Fomahant</i> .	♐	28 11	21 0 S		1
Tail of the Swan.	♐	29 53	59 56 N		2
Wing of <i>Pegasus</i> <i>Merchab</i> .	♐	17 56	19 26 N		2
Right Shoulder of <i>Pegasus</i> <i>Scheat</i> .	♐	23 49	31 7 N		2
Southmost * of the Whale's tail.	♐	26 56	20 47 S		2

FINIS.

